

SSLC EXAMINATION MARCH 2013
MATHEMATICS – ANSWER KEY

1. $f+2d=19$

$d=4$

2nd term=15, 4th term=23

2. $p(x)=3x^3-2x^2+kx-6$

if $(x-2)$ is a factor

$p(2)=0$

$k=-5$

3.

OA=OB(tangents)

B(0,4)

OACB is a square

C(4,4)

4.

$P(B)=1/3$

$P(B)=1*6/(3*6)$

$=6/18$

Black beads=6

total=18

$P(B)=1/4$

number of white balls to be added=6

$6/(18+6)=1/4$

5.

Mean=4430/100=44.3

6. if O is center

$\angle A=1/2\angle DOC$

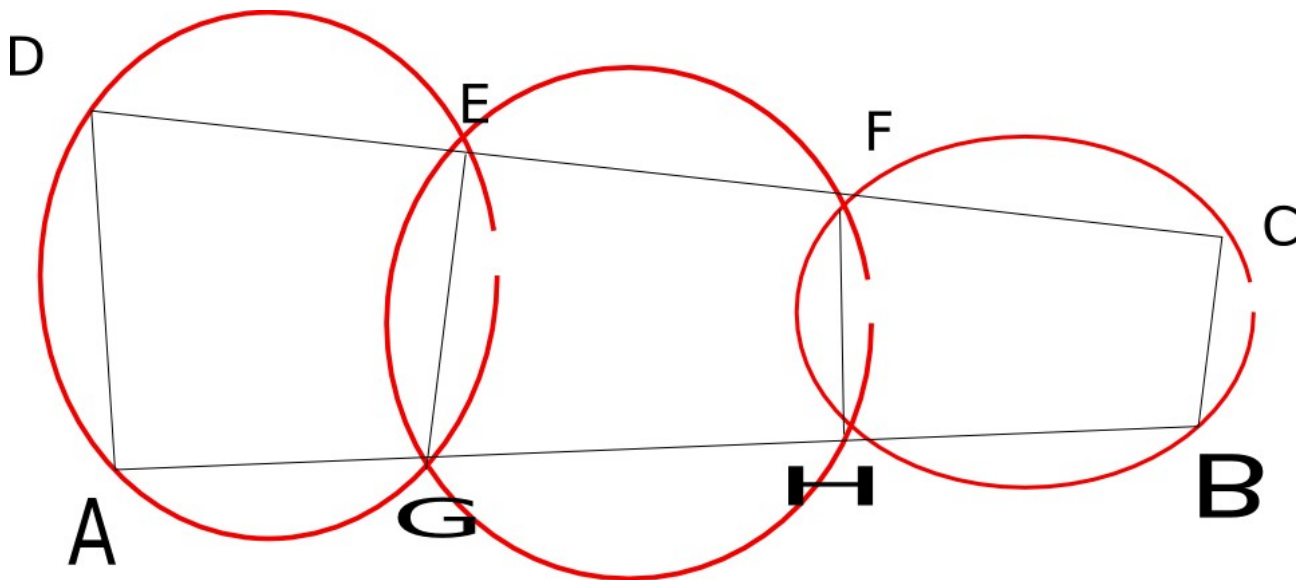
$\angle B=1/2\angle EOD$

$\angle C=1/2\angle EOA$

$\angle D=1/2\angle AOB$

$\angle E=1/2\angle BOC$

$\angle A+\angle B+\angle C+\angle D+\angle E=1/2*360=180$



Let $\angle A = x, \angle D = y$
 $\angle AGE = 180 - x, \angle DEG = 180 - y$
 $\angle EGH = x, \angle FEG = y$
 $\angle GHF = 180 - x, \angle EFH = 180 - y$
 $\angle BHF = x, \angle CFH = y$
 $\angle B = 180 - x, \angle C = 180 - y$
 $\angle A + \angle C = 180, \angle D + \angle B = 180$

7. distance between (2,4) (2,0) is not equal to radius
ie circle **do not** pass through (2,0)

8.

if O is centre

$\angle AOB = 140$
 $\angle P = 70 (1/2 * 140)$
 $\angle A = \angle B = 55 (PA = PB)$

9. $S_n = 5n^2 + 2n$
 $S_1 = 7$ (first term = 7)
 $S_2 = 5 * 4 + 2 * 2 = 24$
 $X_2 = 24 - 7 = 17$
terms 7, 17

10. $b = x$
 $h = x + 6$

Area = 36
 $x(x + 6) = 72$
 $x^2 + 6x + \dots = 72$
 completing square
 $x^2 + 6x + 9 = 72 + 9$
 $(x + 3)^2 = 81$
 $x + 3 = 9$
 $x = 6$ sides 6, 12

11.
 $\angle A, \angle C, \angle B = 45, 45, 90$

$$AB, BC, AC = 1:1:\sqrt{2}$$

$$BC = 4$$

$$AC = 4\sqrt{2}$$

$$AD = 2\sqrt{2}$$

$$BD = 2\sqrt{2} \text{ (in a right angled triangle circum center is mid point of Hypotenuse)}$$

$$12. b = 12 (e = 12)$$

$$\begin{aligned} \text{Area of one Lateral face} &= \sqrt{3} * 12 / 2 \\ &= 36\sqrt{3} \end{aligned}$$

$$LSA = 144\sqrt{3}$$

$$\begin{aligned} TSA &= 144 + 144\sqrt{3} \\ &= 144 * (1 + \sqrt{3}) \end{aligned}$$

if edges are doubled

$$TSA = \text{becomes 4 times } (576 * (1 + \sqrt{3}))$$

13.

$$100 - 1 = 99$$

99 is a multiple of d(3)

Yes 100 is a term

$$\text{nth term} = 1 + (n-1)3$$

$$= 1 + 3n - 3$$

$$= 3n - 2$$

$$(3n-2)^2 = 9n^2 - 12n + 4$$

$$= 3(3n^2 - 4n + 1) + 1$$

$$= d * N + 1$$

$$(3n-2)^2 - \text{first term} = \text{common difference} * N$$

14. Draw the triangle and its incircle

$$15. p(x) = 6x^3 + 3x^2$$

$$p(-1) = 6 * -1 + 3 * 1 < 0$$

ie, (x+1) is not a factor.

Let ax+b added

$$6x^3 + 3x^2 + ax + b = p(x)$$

$$p(1) = a + b = -9$$

$$p(-1) = -a + b = 3$$

$$\text{Solving } a = -6, b = -3$$

ie, -6x - 3 to be added

OR

$$q(a) = k$$

$$r(a) = -k$$

$$q(a) + r(a) = k + (-k) = 0$$

ie (x-a) is a factor of q(x)+r(x)

$$16. N = 130, N/2 = 65$$

$$x - 600 = 65 - 41$$

$$800-600 = 101-41$$

$$x-600/200=24/60$$

Median= 680

17. Draw the figure

$$18. x + 1/x = 25/12$$

solving $12x^2 - 25x + 12 = 0$

number = $4/3$ or $3/4$

$$x + 1/x \geq 2$$

$b^2 - 4ac \geq 0$ otherwise $b^2 - 4ac$ is negative

OR

let Abu complete the job in x days

Abu's work in 1 day = $1/x$

Babus work in 1 day = $1/x+6$

$$1/x + 1/x+6 = 1/4$$

$$x^2 - 2x - 24 = 0$$

$$(x-6)(x+4) = 0$$

$$x = 6$$

Abu in 6 days

Babu alone in 12 days

19. Draw Perpendicular from A to BC meets BC at D

in triangle ABD

$$\cos 50 = BD/10 \quad (BD = 6.4)$$

$$BC = 12.8$$

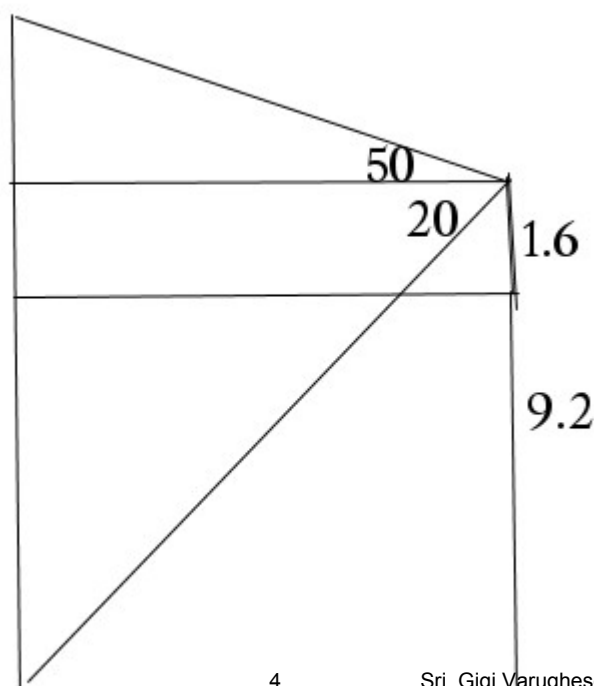
Draw diameter as angle in the same segment

$$\sin 50 = 10/d$$

$$d = 12.8$$

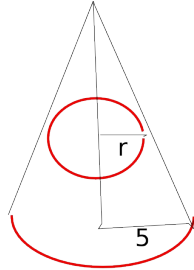
OR

$$d = 25.5$$



$$\text{height} = 9.2 + 1.6 + 30.345 = 41.12\text{m}$$

20. $l=10, r=5, h=5\sqrt{3}$
 $V = \frac{1}{3} \cdot 3.14 \cdot 5 \cdot 5 \cdot 5\sqrt{3}$
 from similar triangles



5

$$\frac{5}{r} = \frac{10}{5\sqrt{3} - r}$$

Solving $r = 5/\sqrt{3}$
 Volume of the sphere $= \frac{4}{3} \cdot \pi \cdot 5/\sqrt{3} \cdot 5/\sqrt{3} \cdot 5/\sqrt{3}$
 $= 500 \pi / 9\sqrt{3} \text{ cc}$

21. Height = $8 - 2 = 6$

Area = 15

$$\frac{1}{2} \cdot BC \cdot 6 = 15$$

$$BC = 5$$

$$C = (3 + 5, 2)$$

$$C = (8, 2)$$

22. $(4, 2)$ is point on $4x - 3y - 10 = 0$ ($4 \cdot 4 - 3 \cdot 2 - 10 = 0$)

$$x = 1 (y = -2)$$

$$(1, -2)$$

$$\text{slope} = 4/3$$

eqn. Of line with slope $4/3$ and passing through $(3, 5)$ is $4x - 3y + 3 = 0$