

FIITJEE Solutions to

IIT - JEE – 2008

(Paper – 2, Code–4)

Time: 3 hours

M. Marks: 243

Note: (i) The question paper consists of 3 parts (Part I : Mathematics, Part II : Physics, Part III : Chemistry). Each part has 4 sections.

(ii) **Section I** contains 9 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D), out of which **only one** is correct.

(iii) **Section II** contains 4 questions. Each question contains STATEMENT–1 and STATEMENT–2.

Bubble (A) if both the statements are TRUE and STATEMENT-2 is the correct explanation of STATEMENT-1

Bubble (B) if both the statements are TRUE but STATEMENT-2 is NOT the correct explanation of STATEMENT- 1

Bubble (C) if STATEMENT-1 is TRUE and STATEMENT-2 is FALSE.

Bubble (D) if STATEMENT-1 is FALSE and STATEMENT-2 is TRUE.

(iv) **Section III** contains 3 sets of Linked Comprehension type questions. Each set consists of a paragraph followed by 3 questions. Each question has 4 choices (A), (B), (C) and (D), out of which **only one** is correct.

(v) **Section IV** contains 3 questions. Each question contains statements given in 2 columns. Statements in the first column have to be matched with statements in the second column. The answers to these questions have to be appropriately bubbled in the ORS as per the instructions given at the beginning of the section.

Marking Scheme:

(i) For each question in **Section I**, you will be awarded **3 Marks** if you have darkened only the bubble corresponding to the correct answer and **zero mark** if no bubble is darkened. In all other cases, **minus one (– 1) mark** will be awarded.

(ii) For each question in **Section II**, you will be awarded **3 Marks** if you darken only the bubble corresponding to the correct answer and **zero mark** if no bubble is darkened. In all other cases, **minus one (–1) mark** will be awarded.

(iii) For each question in **Section III**, you will be awarded **4 Marks** if you darken only the bubble corresponding to the correct answer and **zero mark** if no bubble is darkened. In all other cases, **minus one (– 1) mark** will be awarded.

(iv) For each question in **Section IV**, you will be awarded **6 Marks** if you have darken ALL the bubble corresponding ONLY to the correct answer or **awarded 1 mark each** for correct bubbling of answer in any row. **No negative mark will be awarded for an incorrectly bubbled answer.**

Mathematics

PART – I

SECTION – I

Straight Objective Type

This section contains 9 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

- An experiment has 10 equally likely outcomes. Let A and B be two non-empty events of the experiment. If A consists of 4 outcomes, the number of outcomes that B must have so that A and B are independent, is
(A) 2, 4 or 8 (B) 3, 6 or 9

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(C) 4 or 8

(D) 5 or 10

Sol. (D)

$$P(A \cap B) = \frac{4}{10} \times \frac{p}{10} = \frac{2p}{5}$$

$$\Rightarrow \frac{2p}{5} \text{ is an integer}$$

$$\Rightarrow p = 5 \text{ or } 10.$$

2. The area of the region between the curves $y = \sqrt{\frac{1+\sin x}{\cos x}}$ and $y = \sqrt{\frac{1-\sin x}{\cos x}}$ bounded by the lines $x = 0$ and $x = \frac{\pi}{4}$ is

$$(A) \int_0^{\sqrt{2}-1} \frac{t}{(1+t^2)\sqrt{1-t^2}} dt$$

$$(B) \int_0^{\sqrt{2}-1} \frac{4t}{(1+t^2)\sqrt{1-t^2}} dt$$

$$(C) \int_0^{\sqrt{2}+1} \frac{4t}{(1+t^2)\sqrt{1-t^2}} dt$$

$$(D) \int_0^{\sqrt{2}+1} \frac{t}{(1+t^2)\sqrt{1-t^2}} dt$$

Sol. (B)

$$\begin{aligned} & \int_0^{\pi/4} \left(\sqrt{\frac{1+\sin x}{\cos x}} - \sqrt{\frac{1-\sin x}{\cos x}} \right) dx \\ &= \int_0^{\pi/4} \left(\sqrt{\frac{1+\tan \frac{x}{2}}{1-\tan \frac{x}{2}}} - \sqrt{\frac{1-\tan \frac{x}{2}}{1+\tan \frac{x}{2}}} \right) dx = \int \frac{\left(1+\tan \frac{x}{2}\right) - \left(1-\tan \frac{x}{2}\right)}{\sqrt{1-\tan^2 \frac{x}{2}}} dx \\ &= \int_0^{\pi/4} \frac{2 \tan \frac{x}{2}}{\sqrt{1-\tan^2 \frac{x}{2}}} dx = \int_0^{\sqrt{2}-1} \frac{4t}{(1+t^2)\sqrt{1-t^2}} dt \text{ as } \tan \frac{x}{2} = t. \end{aligned}$$

3. Consider three points $P = (-\sin(\beta - \alpha), -\cos\beta)$, $Q = (\cos(\beta - \alpha), \sin\beta)$ and $R = (\cos(\beta - \alpha + \theta), \sin(\beta - \theta))$, where $0 < \alpha, \beta, \theta < \frac{\pi}{4}$. Then

(A) P lies on the line segment RQ
(C) R lies on the line segment QP

(B) Q lies on the line segment PR
(D) P, Q, R are non-collinear

Sol. (D)

$$P \equiv (-\sin(\beta - \alpha), -\cos\beta) \equiv (x_1, y_1)$$

$$Q \equiv (\cos(\beta - \alpha), \sin\beta) \equiv (x_2, y_2)$$

$$\text{and } R \equiv (x_2 \cos\theta + x_1 \sin\theta, y_2 \cos\theta + y_1 \sin\theta)$$

$$\text{We see that } T \equiv \left(\frac{x_2 \cos\theta + x_1 \sin\theta}{\cos\theta + \sin\theta}, \frac{y_2 \cos\theta + y_1 \sin\theta}{\cos\theta + \sin\theta} \right)$$

and P, Q, T are collinear

\Rightarrow P, Q, R are non-collinear.

4. Let $I = \int \frac{e^x}{e^{4x} + e^{2x} + 1} dx$, $J = \int \frac{e^{-x}}{e^{-4x} + e^{-2x} + 1} dx$. Then, for an arbitrary constant C, the value of $J - I$ equals

$$(A) \frac{1}{2} \log \left(\frac{e^{4x} - e^{2x} + 1}{e^{4x} + e^{2x} + 1} \right) + C$$

$$(B) \frac{1}{2} \log \left(\frac{e^{2x} + e^x + 1}{e^{2x} - e^x + 1} \right) + C$$

$$(C) \frac{1}{2} \log \left(\frac{e^{2x} - e^x + 1}{e^{2x} + e^x + 1} \right) + C$$

$$(D) \frac{1}{2} \log \left(\frac{e^{4x} + e^{2x} + 1}{e^{4x} - e^{2x} + 1} \right) + C$$

Sol. (C)

$$J - I = \int \frac{e^x (e^{2x} - 1)}{e^{4x} + e^{2x} + 1} dx = \int \frac{(z^2 - 1)}{z^4 + z^2 + 1} dz \quad \text{where } z = e^x$$

$$= \int \frac{\left(1 - \frac{1}{z^2}\right) dz}{\left(z + \frac{1}{z}\right)^2 - 1} = \frac{1}{2} \ln \left(\frac{e^x + e^{-x} - 1}{e^x + e^{-x} + 1} \right) + c$$

$$\therefore J - I = \frac{1}{2} \ln \left(\frac{e^{2x} - e^x + 1}{e^{2x} + e^x + 1} \right) + c.$$

5. Let $g(x) = \log(f(x))$ where $f(x)$ is a twice differentiable positive function on $(0, \infty)$ such that $f(x+1) = x f(x)$. Then, for $N = 1, 2, 3, \dots$,

$$g''\left(N + \frac{1}{2}\right) - g''\left(\frac{1}{2}\right) =$$

$$(A) -4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2} \right\}$$

$$(B) 4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2} \right\}$$

$$(C) -4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$$

$$(D) 4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$$

Sol.

$$(A) \quad g(x+1) = \log(f(x+1)) = \log x + \log(f(x))$$

$$= \log x + g(x)$$

$$\Rightarrow g(x+1) - g(x) = \log x$$

$$\Rightarrow g''(x+1) - g''(x) = -\frac{1}{x^2}$$

$$g''\left(1 + \frac{1}{2}\right) - g''\left(\frac{1}{2}\right) = -4$$

$$g''\left(2 + \frac{1}{2}\right) - g''\left(1 + \frac{1}{2}\right) = -\frac{4}{9}$$

....

$$g''\left(N + \frac{1}{2}\right) - g''\left(N - \frac{1}{2}\right) = -\frac{4}{(2N-1)^2}$$

Summing up all terms

$$\text{Hence, } g''\left(N + \frac{1}{2}\right) - g''\left(\frac{1}{2}\right) = -4 \left(1 + \frac{1}{9} + \dots + \frac{1}{(2N-1)^2} \right).$$

6. Let two non-collinear unit vectors \hat{a} and \hat{b} form an acute angle. A point P moves so that at any time t the position vector \overline{OP} (where O is the origin) is given by $\hat{a} \cos t + \hat{b} \sin t$. When P is farthest from origin O, let M be the length of \overline{OP} and \hat{u} be the unit vector along \overline{OP} . Then,

$$(A) \quad \hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{1/2}$$

$$(B) \quad \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{1/2}$$

$$(C) \quad \hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{1/2}$$

$$(D) \quad \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{1/2}$$

Sol.

(A)

$$|\overline{OP}| = |\hat{a} \cos t + \hat{b} \sin t|$$

$$= (\cos^2 t + \sin^2 t + 2 \cos t \sin t \hat{a} \cdot \hat{b})^{1/2}$$

$$= (1 + 2 \cos t \sin t \hat{a} \cdot \hat{b})^{1/2}$$

$$= (1 + \sin 2t \hat{a} \cdot \hat{b})^{1/2}$$

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$$\therefore |\overline{OP}|_{\max} = (1 + \hat{a} \cdot \hat{b})^{1/2} \text{ when, } t = \frac{\pi}{4}$$

$$\hat{u} = \frac{\hat{a} + \hat{b}}{\sqrt{2} \frac{|\hat{a} + \hat{b}|}{\sqrt{2}}}$$

$$\Rightarrow \hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|}$$

7. Let the function $g: (-\infty, \infty) \rightarrow \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ be given by $g(u) = 2 \tan^{-1}(e^u) - \frac{\pi}{2}$. Then, g is

- (A) even and is strictly increasing in $(0, \infty)$
 (B) odd and is strictly decreasing in $(-\infty, \infty)$
 (C) odd and is strictly increasing in $(-\infty, \infty)$
 (D) neither even nor odd, but is strictly increasing in $(-\infty, \infty)$

Sol. (C)

$$g(u) = 2 \tan^{-1}(e^u) - \frac{\pi}{2}$$

$$= 2 \tan^{-1} e^u - \tan^{-1} e^u - \cot^{-1} e^u = \tan^{-1} e^u - \cot^{-1} e^u$$

$$g(-x) = -g(x)$$

$$\Rightarrow g(x) \text{ is odd}$$

$$\text{and } g'(x) > 0 \Rightarrow \text{increasing.}$$

8. Consider a branch of the hyperbola $x^2 - 2y^2 - 2\sqrt{2}x - 4\sqrt{2}y - 6 = 0$ with vertex at the point A. Let B be one of the end points of its latus rectum. If C is the focus of the hyperbola nearest to the point A, then the area of the triangle ABC is

- (A) $1 - \sqrt{\frac{2}{3}}$ (B) $\sqrt{\frac{3}{2}} - 1$
 (C) $1 + \sqrt{\frac{2}{3}}$ (D) $\sqrt{\frac{3}{2}} + 1$

Sol. (B)

$$\text{Hyperbola is } \frac{(x - \sqrt{2})^2}{4} - \frac{(y + \sqrt{2})^2}{2} = 1$$

$$a = 2, b = \sqrt{2}$$

$$e = \sqrt{\frac{3}{2}}$$

$$\text{Area} = \frac{1}{2} a(e-1) \times \frac{b^2}{a} = \frac{1}{2} \frac{(\sqrt{3} - \sqrt{2}) \times 2}{\sqrt{2}} = \frac{(\sqrt{3} - \sqrt{2})}{\sqrt{2}}$$

$$\Rightarrow \text{Area} = \left(\sqrt{\frac{3}{2}} - 1 \right)$$

9. A particle P starts from the point $z_0 = 1 + 2i$, where $i = \sqrt{-1}$. It moves first horizontally away from origin by 5 units and then vertically away from origin by 3 units to reach a point z_1 . From z_1 the particle moves $\sqrt{2}$ units in the direction of the vector $\hat{i} + \hat{j}$ and then it moves through an angle $\frac{\pi}{2}$ in anticlockwise direction on a circle with centre at origin, to

reach a point z_2 . The point z_2 is given by

- (A) $6 + 7i$ (B) $-7 + 6i$
 (C) $7 + 6i$ (D) $-6 + 7i$

Sol. (D)

$$z_0 \equiv (1 + 2i)$$

$$z_1 \equiv (6 + 5i)$$

$$z_2 \equiv (-6 + 7i)$$

SECTION – II

Reasoning Type

This section contains 4 reasoning type questions. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

10. Consider
 $L_1 : 2x + 3y + p - 3 = 0$
 $L_2 : 2x + 3y + p + 3 = 0$,
 where p is a real number, and $C : x^2 + y^2 + 6x - 10y + 30 = 0$.
 STATEMENT-1 : If line L_1 is a chord of circle C , then line L_2 is not always a diameter of circle C .
and
 STATEMENT-2 : If line L_1 is a diameter of circle C , then line L_2 is not a chord of circle C .
- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1.
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

Sol. (C)
 Circle $\equiv (x + 3)^2 + (y - 5)^2 = 4$
 Distance between L_1 and L_2
 $\Rightarrow \frac{6}{\sqrt{13}} < \text{radius}$
 \Rightarrow statement (2) is false
 But statement (1) is correct.

11. Let a, b, c, p, q be real numbers. Suppose α, β are the roots of the equation $x^2 + 2px + q = 0$ and $\alpha, \frac{1}{\beta}$ are the roots of the equation $ax^2 + 2bx + c = 0$, where $\beta^2 \notin \{-1, 0, 1\}$.
- STATEMENT-1 : $(p^2 - q)(b^2 - ac) \geq 0$
and
 STATEMENT-2 : $b \neq pa$ or $c \neq qa$
- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1.
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

Sol. (B)
 Suppose roots are imaginary then $\beta = \bar{\alpha}$
 and $\frac{1}{\beta} = \bar{\alpha} \Rightarrow \beta = \frac{1}{\bar{\alpha}}$ not possible
 \Rightarrow roots are real $\Rightarrow (p^2 - q)(b^2 - ac) \geq 0$
 \Rightarrow statement (1) is correct.
 $\frac{-2b}{a} = \alpha + \frac{1}{\beta}$ and $\frac{\alpha}{\beta} = \frac{c}{a}$, $\alpha + \beta = -2p$, $\alpha\beta = q$
 If $\beta = 1$, then $\alpha = q \Rightarrow c = qa$ (not possible)
 also $\alpha + 1 = \frac{-2b}{a} \Rightarrow -2p = \frac{-2b}{a} \Rightarrow b = ap$ (not possible)
 \Rightarrow statement (2) is correct but it is not the correct explanation.

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12. Suppose four distinct positive numbers a_1, a_2, a_3, a_4 are in G.P. Let $b_1 = a_1, b_2 = b_1 + a_2, b_3 = b_2 + a_3$ and $b_4 = b_3 + a_4$.

STATEMENT-1 : The numbers b_1, b_2, b_3, b_4 are neither in A.P. nor in G.P.

and

STATEMENT-2 : The numbers b_1, b_2, b_3, b_4 are in H.P.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1.
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

Sol.

(C)

$$b_1 = a_1, b_2 = a_1 + a_2, b_3 = a_1 + a_2 + a_3, b_4 = a_1 + a_2 + a_3 + a_4$$

Hence b_1, b_2, b_3, b_4 are neither in A.P. nor in G.P. nor in H.P.

13. Let a solution $y = y(x)$ of the differential equation

$$x\sqrt{x^2-1} dy - y\sqrt{y^2-1} dx = 0 \quad \text{satisfy } y(2) = \frac{2}{\sqrt{3}}.$$

$$\text{STATEMENT-1 : } y(x) = \sec\left(\sec^{-1}x - \frac{\pi}{6}\right)$$

and

$$\text{STATEMENT-2 : } y(x) \text{ is given by } \frac{1}{y} = \frac{2\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}}$$

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1.
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

Sol.

(C)

$$\int \frac{dx}{x\sqrt{x^2-1}} = \int \frac{dy}{y\sqrt{y^2-1}}$$

$$\sec^{-1}x = \sec^{-1}y + c$$

$$\sec^{-1}2 = \sec^{-1}\left(\frac{2}{\sqrt{3}}\right) + c$$

$$c = \frac{\pi}{3} - \frac{\pi}{6} = \frac{\pi}{6}$$

$$\sec^{-1}x = \sec^{-1}y + \frac{\pi}{6}$$

$$y = \sec\left(\sec^{-1}x - \frac{\pi}{6}\right)$$

$$\cos^{-1}\frac{1}{x} = \cos^{-1}\frac{1}{y} + \frac{\pi}{6}$$

$$\cos^{-1}\frac{1}{y} = \cos^{-1}\frac{1}{x} - \cos^{-1}\left(\frac{\sqrt{3}}{2}\right)$$

$$\frac{1}{y} = \frac{\sqrt{3}}{2x} - \sqrt{1 - \frac{1}{x^2}} \left(\frac{1}{2}\right)$$

$$\frac{2}{y} = \frac{\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}}.$$

SECTION – III

Linked Comprehension Type

This section contains 2 paragraphs. Based upon each paragraph, 3 multiple choice questions have to be answered. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

Paragraph for Question Nos. 14 to 16

Consider the function $f : (-\infty, \infty) \rightarrow (-\infty, \infty)$ defined by $f(x) = \frac{x^2 - ax + 1}{x^2 + ax + 1}$, $0 < a < 2$.

14. Which of the following is true?

(A) $(2 + a)^2 f'(1) + (2 - a)^2 f'(-1) = 0$

(B) $(2 - a)^2 f'(1) - (2 + a)^2 f'(-1) = 0$

(C) $f(1) f'(-1) = (2 - a)^2$

(D) $f(1) f'(-1) = -(2 + a)^2$

Sol. (A)

$$f''(x) = \frac{4ax(x^2 + ax + 1)^2 - 4ax(x^2 - 1)(2x + a)(x^2 + ax + 1)}{(x^2 + ax + 1)^4}$$

$$f''(1) = \frac{4a}{(2 + a)^2} \quad f''(-1) = \frac{-4a}{(2 - a)^2}$$

$$(2 + a)^2 f''(1) + (2 - a)^2 f''(-1) = 0.$$

15. Which of the following is true?

(A) $f(x)$ is decreasing on $(-1, 1)$ and has a local minimum at $x = 1$

(B) $f(x)$ is increasing on $(-1, 1)$ and has a local maximum at $x = 1$

(C) $f(x)$ is increasing on $(-1, 1)$ but has neither a local maximum nor a local minimum at $x = 1$

(D) $f(x)$ is decreasing on $(-1, 1)$ but has neither a local maximum nor a local minimum at $x = 1$

Sol. (A)

$$f'(x) = \frac{2a(x^2 - 1)}{(x^2 + ax + 1)^2}$$

Decreasing $(-1, 1)$ and minima at $x = 1$

16. Let $g(x) = \int_0^{e^x} \frac{f'(t)}{1+t^2} dt$

which of the following is true?

(A) $g'(x)$ is positive on $(-\infty, 0)$ and negative on $(0, \infty)$

(B) $g'(x)$ is negative on $(-\infty, 0)$ and positive on $(0, \infty)$

(C) $g'(x)$ changes sign on both $(-\infty, 0)$ and $(0, \infty)$

(D) $g'(x)$ does not change sign on $(-\infty, \infty)$

Sol. (B)

$$g'(x) = \frac{f'(e^x)e^x}{1 + e^{2x}}$$

Hence positive for $(0, \infty)$ and negative for $(-\infty, 0)$.

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Paragraph for Question Nos. 17 to 19

Consider the line

$$L_1: \frac{x+1}{3} = \frac{y+2}{1} = \frac{z+1}{2}, L_2: \frac{x-2}{1} = \frac{y+2}{2} = \frac{z-3}{3}$$

17. The unit vector perpendicular to both L_1 and L_2 is

- (A) $\frac{-\hat{i}+7\hat{j}+7\hat{k}}{\sqrt{99}}$ (B) $\frac{-\hat{i}-7\hat{j}+5\hat{k}}{5\sqrt{3}}$
 (C) $\frac{-\hat{i}+7\hat{j}+5\hat{k}}{5\sqrt{3}}$ (D) $\frac{7\hat{i}-7\hat{j}-\hat{k}}{\sqrt{99}}$

Sol. (B)

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix} = -\hat{i} - 7\hat{j} + 5\hat{k}$$

Hence unit vector will be $\frac{-\hat{i}-7\hat{j}+5\hat{k}}{5\sqrt{3}}$.18. The shortest distance between L_1 and L_2 is

- (A) 0 (B) $\frac{17}{\sqrt{3}}$
 (C) $\frac{41}{5\sqrt{3}}$ (D) $\frac{17}{5\sqrt{3}}$

Sol. (D)

$$S. D = \frac{(1+2)(-1) + (2-2)(-7) + (1+3)(5)}{5\sqrt{3}} = \frac{17}{5\sqrt{3}}$$

19. The distance of the point (1, 1, 1) from the plane passing through the point (-1, -2, -1) and whose normal is perpendicular to both the lines L_1 and L_2 is

- (A) $\frac{2}{\sqrt{75}}$ (B) $\frac{7}{\sqrt{75}}$
 (C) $\frac{13}{\sqrt{75}}$ (D) $\frac{23}{\sqrt{75}}$

Sol. (C)

$$\text{Plane is given by } -(x+1) - 7(y+2) + 5(z+1) = 0$$

$$\Rightarrow x + 7y - 5z + 10 = 0$$

$$\Rightarrow \text{distance} = \frac{1+7-5+10}{\sqrt{75}} = \frac{13}{\sqrt{75}}$$

SECTION – IV

Matrix-Match Type

This contains 3 questions. Each question contains statements given in two columns which have to be matched. Statements (A, B, C, D) in column I have to be matched with statements (p, q, r, s) in column II. The answers to these questions have to be appropriately bubbled as illustrated in the following example.

If the correct match are A-p, A-s, B-r, C-p, C-q and D-s, then the correctly bubbled 4×4 matrix should be as follows:

	p	q	r	s
A	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

20. Consider the lines given by

$$L_1 : x + 3y - 5 = 0$$

$$L_2 : 3x - ky - 1 = 0$$

$$L_3 : 5x + 2y - 12 = 0$$

Match the Statements / Expressions in **Column I** with the Statements / Expressions in **Column II** and indicate your answer by darkening the appropriate bubbles in the 4×4 matrix given in the ORS.

	Column I	Column II
(A)	L_1, L_2, L_3 are concurrent, if	(p) $k = -9$
(B)	One of L_1, L_2, L_3 is parallel to at least one of the other two, if	(q) $k = -\frac{6}{5}$
(C)	L_1, L_2, L_3 form a triangle, if	(r) $k = \frac{5}{6}$
(D)	L_1, L_2, L_3 do not form a triangle, if	(s) $k = 5$

Sol. (A) \rightarrow (s); (B) \rightarrow (p, q); (C) \rightarrow (r); (D) \rightarrow (p, q, s)
 $x + 3y - 5 = 0$ and $5x + 2y - 12 = 0$ intersect at (2, 1)

$$\text{Hence } 6 - k - 1 = 0 \quad k = 5$$

for L_1, L_2 to be parallel

$$\frac{1}{3} = \frac{3}{-k} \Rightarrow k = -9$$

for L_2, L_3 to be parallel

$$\frac{3}{5} = \frac{-k}{2} \Rightarrow k = -\frac{6}{5}$$

for $k \neq 5, -9, -\frac{6}{5}$ they will form triangle

for $k = 5$ $k = -9, -\frac{6}{5}$ they will not form triangle

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21. Consider all possible permutations of the letters of the word ENDEANOEL.
Match the Statements / Expressions in **Column I** with the Statements / Expressions in **Column II** and indicate your answer by darkening the appropriate bubbles in the 4×4 matrix given in the ORS.

Column I	Column II
(A) The number of permutations containing the word ENDEA is	(p) $5!$
(B) The number of permutations in which the letter E occurs in the first and the last positions is	(q) $2 \times 5!$
(C) The number of permutations in which none of the letters D, L, N occurs in the last five positions is	(r) $7 \times 5!$
(D) The number of permutations in which the letters A, E, O occur only in odd positions is	(s) $21 \times 5!$

Sol.**(A) \rightarrow (p); (B) \rightarrow (s); (C) \rightarrow (q); (D) \rightarrow (q)**(A) ENDEA, N, O, E, L are five different letter, then permutation = $5!$ (B) If E is in the first and last position then $\frac{(9-2)!}{2!} = 7 \times 3 \times 5! = 21 \times 5!$ (C) for first four letters = $\frac{4!}{2!}$ for last five letters = $5!/3!$ Hence $\frac{4!}{2!} \times \frac{5!}{3!} = 2 \times 5!$ (D) For A, E and O $5!/3!$ and for others $4!/2!$ hence $\frac{5!}{3!} \times \frac{4!}{2!} = 2 \times 5!$.

22. Match the Statements / Expressions in **Column I** with the Statements / Expressions in **Column II** and indicate your answer by darkening the appropriate bubbles in the 4×4 matrix given in the ORS.

Column I	Column II
(A) The minimum value of $\frac{x^2 + 2x + 4}{x + 2}$ is	(p) 0
(B) Let A and B be 3×3 matrices of real numbers, where A is symmetric, B is skew-symmetric, and $(A + B)(A - B) = (A - B)(A + B)$. If $(AB)^t = (-1)^k AB$, where $(AB)^t$ is the transpose of the matrix AB, then the possible values of k are	(q) 1
(C) Let $a = \log_3 \log_3 2$. An integer k satisfying $1 < 2^{(-k+3^{-a})} < 2$, must be less than	(r) 2
(D) If $\sin\theta = \cos\phi$, then the possible values of $\frac{1}{\pi} \left(\theta \pm \phi - \frac{\pi}{2} \right)$ are	(s) 3

Sol.**(A) \rightarrow (r); (B) \rightarrow (q, s); (C) \rightarrow (r, s); (D) \rightarrow (p, r)**(A) $y = \frac{x^2 + 2x + 4}{x + 2}$ $\Rightarrow x^2 + (2 - y)x + 4 - 2y = 0$ $\Rightarrow y^2 + 4y - 12 \geq 0$ $y \leq -6$ or $y \geq 2$

minimum value is 2.

(B) $(A + B)(A - B) = (A - B)(A + B)$ $\Rightarrow AB = BA$

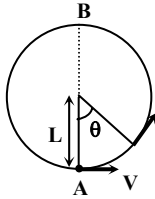
as A is symmetric and B is skew symmetric

 $\Rightarrow (AB)^t = -AB$ $\Rightarrow k = 1$ and $k = 3$ (C) $a = \log_3 \log_3 2 \Rightarrow 3^{-a} = \log_2 3$ Now $1 < 2^{-k + \log_2 3} < 2$ $\Rightarrow 1 < 3 \cdot 2^{-k} < 2$ $\Rightarrow \log_2 \left(\frac{3}{2} \right) < k < \log_2(3)$ $\Rightarrow k = 1$ or $k < 2$ and $k < 3$.

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25. A bob of mass M is suspended by a massless string of length L . The horizontal velocity V at position A is just sufficient to make it reach the point B . The angle θ at which the speed of the bob is half of that at A , satisfies

Figure:



- (A) $\theta = \frac{\pi}{4}$ (B) $\frac{\pi}{4} < \theta < \frac{\pi}{2}$
 (C) $\frac{\pi}{2} < \theta < \frac{3\pi}{4}$ (D) $\frac{3\pi}{4} < \theta < \pi$

Sol. (D)

$$\frac{1}{2} 5mg\ell = \frac{1}{2} m \frac{5g\ell}{4} + mg\ell(1 - \cos \theta)$$

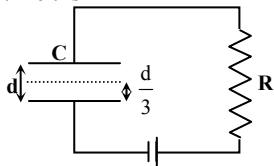
$$\cos \theta = -\frac{7}{8}$$

Hence, $3\pi/4 < \theta < \pi$

26. A parallel plate capacitor C with plates of unit area and separation d is filled with a liquid of dielectric constant $K = 2$. The level of liquid is $\frac{d}{3}$ initially. Suppose the liquid level decreases at a constant speed V , the time constant as a

function of time t is

Figure:



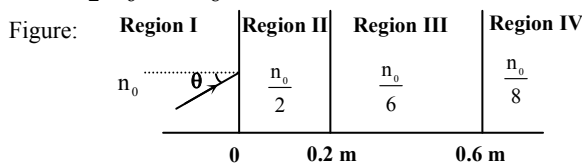
- (A) $\frac{6\epsilon_0 R}{5d + 3Vt}$ (B) $\frac{(15d + 9Vt)\epsilon_0 R}{2d^2 - 3dVt - 9V^2t^2}$
 (C) $\frac{6\epsilon_0 R}{5d - 3Vt}$ (D) $\frac{(15d - 9Vt)\epsilon_0 R}{2d^2 + 3dVt - 9V^2t^2}$

Sol. (A)

$$C_{\text{equivalent}} = \frac{\frac{2\epsilon_0}{\frac{d}{3} - vt} + \frac{\epsilon_0}{\frac{2d}{3} + vt}}{\frac{2\epsilon_0}{\frac{d}{3} - vt} + \frac{\epsilon_0}{\frac{2d}{3} + vt}}$$

$$\therefore \tau = C_{\text{equivalent}} R$$

27. A light beam is travelling from Region I to Region IV (Refer Figure). The refractive index in Regions I, II, III and IV are n_0 , $\frac{n_0}{2}$, $\frac{n_0}{6}$ and $\frac{n_0}{8}$, respectively. The angle of incidence θ for which the beam just misses entering Region IV is



- (A) $\sin^{-1}\left(\frac{3}{4}\right)$ (B) $\sin^{-1}\left(\frac{1}{8}\right)$ (C) $\sin^{-1}\left(\frac{1}{4}\right)$ (D) $\sin^{-1}\left(\frac{1}{3}\right)$

Sol. (B)

Total internal reflection occurs at the interface of region III and IV.

Because mediums are parallel

$$n_0 \sin \theta = \frac{n_0}{8} \sin\left(\frac{\pi}{2}\right)$$

$$\sin \theta = 1/8$$

28. A vibrating string of certain length ℓ under a tension T resonates with a mode corresponding to the first overtone (third harmonic) of an air column of length 75 cm inside a tube closed at one end. The string also generates 4 beats per second when excited along with a tuning fork of frequency n . Now when the tension of the string is slightly increased the number of beats reduces 2 per second. Assuming the velocity of sound in air to be 340 m/s, the frequency n of the tuning fork in Hz is

- (A) 344 (B) 336 (C) 117.3 (D) 109.3

Sol. (A)

$$n_s = \frac{3}{4} \left(\frac{340}{0.75} \right) = n - 4$$

$$\therefore n = 344 \text{ Hz}$$

29. A radioactive sample S1 having an activity $5\mu\text{Ci}$ has twice the number of nuclei as another sample S2 which has an activity of $10\mu\text{Ci}$. The half lives of S1 and S2 can be

- (A) 20 years and 5 years, respectively
 (B) 20 years and 10 years, respectively
 (C) 10 years each
 (D) 5 years each

Sol. (A)

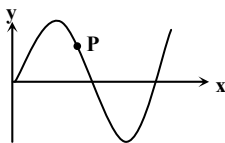
$$5\mu\text{Ci} = \frac{\ln 2}{T_1} (2N_0)$$

$$10\mu\text{Ci} = \frac{\ln 2}{T_2} (N_0)$$

Dividing we get $T_1 = 4T_2$

30. A transverse sinusoidal wave moves along a string in the positive x -direction at a speed of 10 cm/s. The wavelength of the wave is 0.5 m and its amplitude is 10 cm. At a particular time t , the snap-shot of the wave is shown in figure. The velocity of point P when its displacement is 5 cm is

Figure:



(A) $\frac{\sqrt{3}\pi}{50} \hat{j}$ m/s

(B) $-\frac{\sqrt{3}\pi}{50} \hat{j}$ m/s

(C) $\frac{\sqrt{3}\pi}{50} \hat{i}$ m/s

(D) $-\frac{\sqrt{3}\pi}{50} \hat{i}$ m/s

Sol. (A) $y = 5$ cm and $V = +ve$

$$y = A \sin(\omega t \pm \phi) \quad V = A\omega \cos(\omega t \pm \phi)$$

We get $\omega t \pm \phi = 30^\circ$

$$\omega = 2\pi \frac{v}{\lambda} = \frac{2\pi}{5}$$

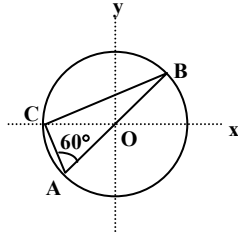
$$v = A\omega \cos(\omega t + \phi) = \left(\frac{10}{100}\right) \times \left(\frac{2\pi}{5}\right) \left(\frac{\sqrt{3}}{2}\right) = \frac{\pi\sqrt{3}}{50} \text{ m/s}$$

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31. Consider a system of three charges $\frac{q}{3}$, $\frac{q}{3}$ and $-\frac{2q}{3}$ placed at points A, B and C, respectively, as shown in the figure.

Take O to be the centre of the circle of radius R and angle CAB = 60°

Figure:



- (A) The electric field at point O is $\frac{q}{8\pi\epsilon_0 R^2}$ directed along the negative x-axis
 (B) The potential energy of the system is zero
 (C) The magnitude of the force between the charges at C and B is $\frac{q^2}{54\pi\epsilon_0 R^2}$
 (D) The potential at point O is $\frac{q}{12\pi\epsilon_0 R}$

Sol. (C)

$$F_{BC} = \frac{1}{4\pi\epsilon_0} \frac{\left(\frac{q}{3}\right)\left(\frac{2q}{3}\right)}{\left(R\sqrt{3}\right)^2} = \frac{q^2}{54\pi\epsilon_0 R^2}$$

SECTION – II

Reasoning Type

This section contains 4 reasoning type questions. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

32. STATEMENT-1

For practical purposes, the earth is used as a reference at zero potential in electrical circuits.

and

STATEMENT-2

The electrical potential of a sphere of radius R with charge Q uniformly distributed on the surface is given by $\frac{Q}{4\pi\epsilon_0 R}$.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 **is** a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 **is NOT** a correct explanation for STATEMENT-1
 (C) STATEMENT -1 is True, STATEMENT-2 is False
 (D) STATEMENT -1 is False, STATEMENT-2 is True

Sol. (B)

33. STATEMENT-1

It is easier to pull a heavy object than to push it on a level ground.

and

STATEMENT-2

The magnitude of frictional force depends on the nature of the two surfaces in contact.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 **is** a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 **is NOT** a correct explanation for STATEMENT-1
 (C) STATEMENT -1 is True, STATEMENT-2 is False
 (D) STATEMENT -1 is False, STATEMENT-2 is True

Sol. (B)
In pushing Normal contact force is greater than in pulling.

34 STATEMENT-1
For an observer looking out through the window of a fast moving train, the nearby objects appear to move in the opposite direction to the train, while the distant objects appear to be stationary.

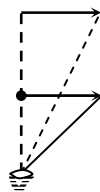
and

STATEMENT-2

If the observer and the object are moving at velocities \vec{V}_1 and \vec{V}_2 respectively with reference to a laboratory frame, the velocity of the object with respect to the observer is $\vec{V}_2 - \vec{V}_1$.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1
 (C) STATEMENT -1 is True, STATEMENT-2 is False
 (D) STATEMENT -1 is False, STATEMENT-2 is True

Sol. (B)
Distance appeared to move depends upon angle subtended on eye.



35 STATEMENT-1
The sensitivity of a moving coil galvanometer is increased by placing a suitable magnetic material as a core inside the coil.

and

STATEMENT-2

Soft iron has a high magnetic permeability and cannot be easily magnetized or demagnetized.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1
 (C) STATEMENT -1 is True, STATEMENT-2 is False
 (D) STATEMENT -1 is False, STATEMENT-2 is True

Sol. (C)

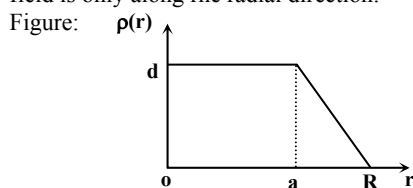
SECTION – III

Linked Comprehension Type

This section contains 2 paragraphs. Based upon each paragraph, 3 multiple choice questions have to be answered. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

Paragraph for Question Nos. 36 to 38

The nuclear charge (Ze) is non-uniformly distributed within a nucleus of radius R . The charge density $\rho(r)$ [charge per unit volume] is dependent only on the radial distance r from the centre of the nucleus as shown in figure. The electric field is only along the radial direction.



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36. The electric field at $r = R$ is
 (A) independent of a (B) directly proportional to a
 (C) directly proportional to a^2 (D) inversely proportional to a

Sol. (A)

37. For $a = 0$, the value of d (maximum value of ρ as shown in the figure) is
 (A) $\frac{3Ze}{4\pi R^3}$ (B) $\frac{3Ze}{\pi R^3}$ (C) $\frac{4Ze}{3\pi R^3}$ (D) $\frac{Ze}{3\pi R^3}$

Sol. (B)

$$q = \int_0^R \frac{d}{R} (R - x) 4\pi x^2 dx = Ze$$

$$d = \frac{3Ze}{\pi R^3}$$

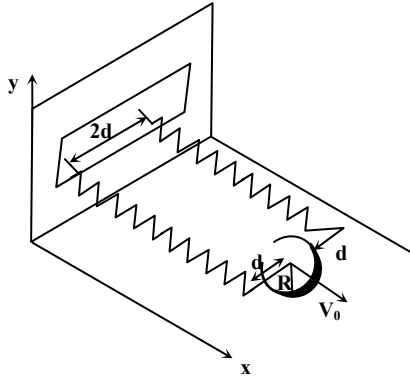
38. The electric field within the nucleus is generally observed to be linearly dependent on r . This implies.
 (A) $a = 0$ (B) $a = \frac{R}{2}$ (C) $a = R$ (D) $a = \frac{2R}{3}$

Sol. (C)

If within a sphere ρ is constant $E \propto r$

Paragraph for Question Nos. 39 to 41

A uniform thin cylindrical disk of mass M and radius R is attached to two identical massless springs of spring constant k which are fixed to the wall as shown in the figure. The springs are attached to the axle of the disk symmetrically on either side at a distance d from its centre. The axle is massless and both the springs and the axle are in horizontal plane. The unstretched length of each spring is L . The disk is initially at its equilibrium position with its centre of mass (CM) at a distance L from the wall. The disk rolls without slipping with velocity $\vec{V}_0 = V_0 \hat{i}$. The coefficient of friction is μ .
 Figure:



39. The net external force acting on the disk when its centre of mass is at displacement x with respect to its equilibrium position is
 (A) $-kx$ (B) $-2kx$ (C) $-\frac{2kx}{3}$ (D) $-\frac{4kx}{3}$

Sol. (D)

$$\begin{aligned} 2kx - f &= ma \\ \Rightarrow f.R &= I\alpha \\ a &= R\alpha \\ \Rightarrow ma &= \frac{4kx}{3} \end{aligned}$$

40. The centre of mass of the disk undergoes simple harmonic motion with angular frequency ω equal to
 (A) $\sqrt{\frac{k}{M}}$ (B) $\sqrt{\frac{2k}{M}}$ (C) $\sqrt{\frac{2k}{3M}}$ (D) $\sqrt{\frac{4k}{3M}}$

Sol.

(D)

$$-(2kx)R = I_p \alpha$$

$$\alpha = -\frac{4kR}{3mR^2}(R\theta) = -\frac{4k}{3m}\theta$$

41. The maximum value of V_0 for which the disk will roll without slipping is

(A) $\mu g \sqrt{\frac{M}{k}}$

(B) $\mu g \sqrt{\frac{M}{2k}}$

(C) $\mu g \sqrt{\frac{3M}{k}}$

(D) $\mu g \sqrt{\frac{5M}{2k}}$

Sol.

(C)

$$2kx - f_{\max} = ma$$

$$2kx \cdot r = I_p \alpha$$

$$f_{\max} = \mu mg$$

$$\Rightarrow x = \frac{3 \mu mg}{2k}$$

$$\Rightarrow \frac{1}{2}(2k)x^2 = \frac{1}{2}I_p \omega^2$$

$$\Rightarrow \gamma = \mu g \sqrt{\frac{3m}{k}}$$

SECTION – IV

Matrix-Match Type

This section contains 3 questions. Each question contains statements given in two columns which have to be matched. Statements in **Column I** are labelled as A, B, C and D whereas statements in **Column II** are labelled as p, q, r and s. The answers to these questions have to be appropriately bubbled as illustrated in the following example.

If the correct matches are A-p, A-r, B-p, B-s, C-r, C-s and D-q, then the correctly bubbled matrix will be look like the following:

	p	q	r	s
A	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
B	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>

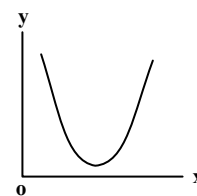
42.

Column I gives a list of possible set of parameters measured in some experiments. The variations of the parameters in the form of graphs are shown in **Column II**. Match the set of parameters given in **Column I** with the graph given in **Column II**. Indicate your answer by darkening the appropriate bubbles of the 4 × 4 matrix given in the ORS.

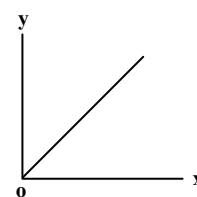
Column I

(A) Potential energy of a simple pendulum (y axis) as a function of displacement (x axis) (p)

Column II

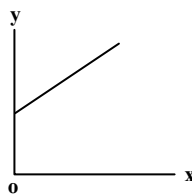


(B) Displacement (y axis) as a function of time (x axis) for a one dimensional motion at zero or constant acceleration when the body is moving along the positive x-direction (q)

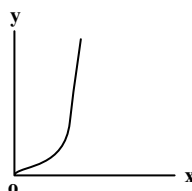


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- (C) Range of a projectile (y axis) as a function of its velocity (x axis) when projected at a fixed angle



- (D) The square of the time period (y axis) of a simple pendulum as a function of its length (x axis)

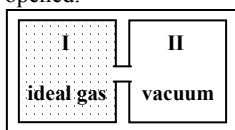


Sol. (A) → s, (B) → q & s, (C) → s, (D) → q

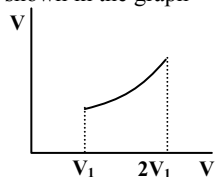
43. **Column I** Contains a list of processes involving expansion of an ideal gas. Match this with **Column II** describing the thermodynamic change during this process. Indicate your answer by darkening the appropriate bubbles of the 4 × 4 matrix given in the ORS.

Column I

- (A) An insulated container has two chambers separated by a valve. Chamber I contains an ideal gas and the Chamber II has vacuum. The valve is opened.

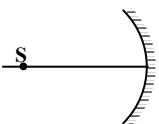
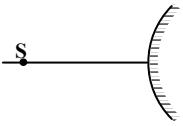
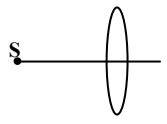
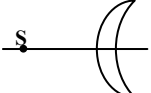
**Column II**

- (p) The temperature of the gas decreases
- (q) The temperature of the gas increases or remains constant
- (r) The gas loses heat
- (s) The gas gains heat
- (B) An ideal monoatomic gas expands to twice its original volume such that its pressure $P \propto \frac{1}{V^2}$, where V is the volume of the gas
- (C) An ideal monoatomic gas expands to twice its original volume such that its pressure $P \propto \frac{1}{V^{4/3}}$, where V is its volume
- (D) An ideal monoatomic gas expands such that its pressure P and volume V follows the behaviour shown in the graph



Sol. (A) → q, (B) → p & r, (C) → p & s, (D) → q & s

44. An optical component and an object S placed along its optic axis are given in **Column I**. The distance between the object and the component can be varied. The properties of images are given in **Column II**. Match all the properties of images from **Column II** with the appropriate components given in **Column I**. Indicate your answer by darkening the appropriate bubbles of the 4×4 matrix given in the ORS.

Column I	Column II
(A) 	(p) Real image
(B) 	(q) Virtual image
(C) 	(r) Magnified image
(D) 	(s) Image at infinity

Sol. (A) \rightarrow p, q, r & s, (B) \rightarrow q, (C) \rightarrow p, q, r & s, (D) \rightarrow p, q, r & s

Chemistry

PART – III SECTION – I

Straight Objective Type

This section contains 9 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

45. The IUPAC name of $[\text{Ni}(\text{NH}_3)_4][\text{NiCl}_4]$ is
 (A) Tetrachloronickel (II) – tetraamminenickel (II)
 (B) Tetraamminenickel (II) – tetrachloronickel (II)
 (C) Tetraamminenickel (II) – tetrachloronickelate (II)
 (D) Tetrachloronickel (II) – tetraamminenickelate (0)

Sol. (C)
IUPAC name is tetraamminenickel (II) – tetrachloronickelate (II)

46. Among the following the coloured compound is
 (A) CuCl (B) $\text{K}_3[\text{Cu}(\text{CN})_4]$
 (C) CuF_2 (D) $[\text{Cu}(\text{CH}_3\text{CN})_4]\text{BF}_4$

Sol. (C)
In the crystalline form CuF_2 is blue coloured.

47. Both $[\text{Ni}(\text{CO})_4]$ and $[\text{Ni}(\text{CN})_4]^{2-}$ are diamagnetic. The hybridization of nickel in these complexes, respectively, are
 (A) sp^3, sp^3 (B) $\text{sp}^3, \text{dsp}^2$
 (C) $\text{dsp}^2, \text{sp}^3$ (D) $\text{dsp}^2, \text{dsp}^2$

Sol. (B)
 $\text{Ni}(\text{CO})_4 = \text{sp}^3$
 $[\text{Ni}(\text{CN})_4]^{2-} = \text{dsp}^2$

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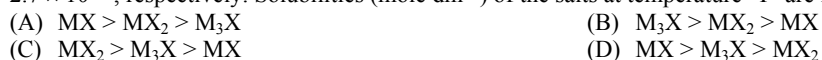
48. Among the following, the surfactant that will form micelles in aqueous solution at the lowest molar concentration at ambient conditions is



Sol. (A)

Critical concentration for micelle formation decreases as the molecular weight of hydrocarbon chain of surfactant grows because in this case true solubility diminishes and the tendency of surfactant molecule to associate increases.

49. Solubility product constant (K_{sp}) of salts of types MX, MX_2 and M_3X at temperature 'T' are 4.0×10^{-8} , 3.2×10^{-14} and 2.7×10^{-15} , respectively. Solubilities (mole dm^{-3}) of the salts at temperature 'T' are in the order



Sol. (D)

$$\text{Solubility of (MX)} = \sqrt{4 \times 10^{-8}} = 2 \times 10^{-4}$$

$$\text{Solubility of (MX}_2) = 8 \times 10^{-5}$$

$$\text{Solubility of (M}_3\text{X)} = 1 \times 10^{-4}$$

$$\therefore \text{MX} > \text{M}_3\text{X} > \text{MX}_2$$

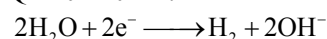
50. Electrolysis of dilute aqueous NaCl solution was carried out by passing 10 milli ampere current. The time required to liberate 0.01 mol of H_2 gas at the cathode is (1 Faraday = 96500 C mol^{-1})



Sol. (B)

$$Q = i \times t$$

$$Q = 10 \times 10^{-3} \times t$$



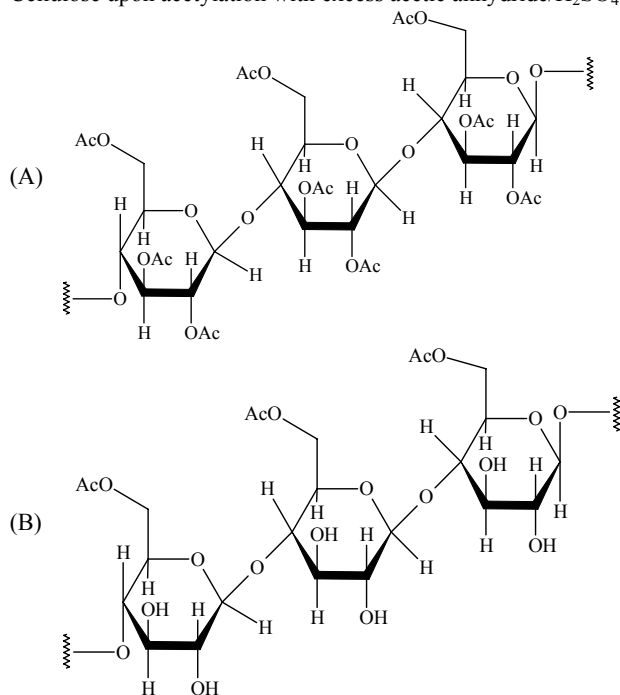
To liberate 0.01 mole of H_2 , 0.02 Faraday charge is required

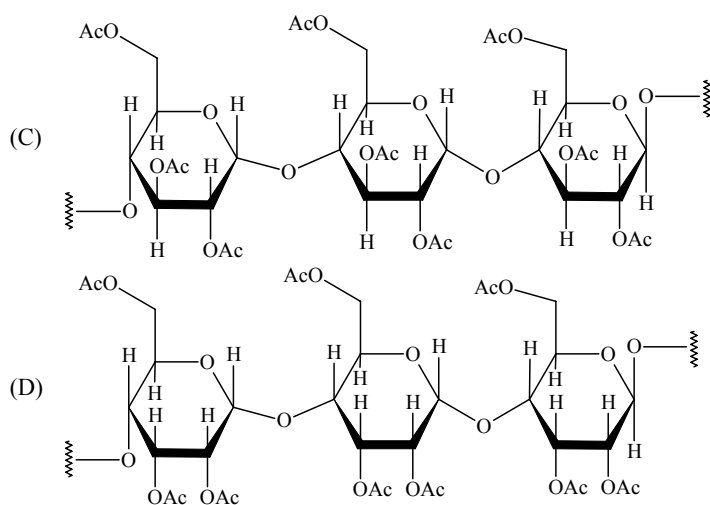
$$Q = 0.02 \times 96500 \text{ C}$$

$$\therefore 0.02 \times 96500 = 10^{-2} \times t$$

$$t = 19.30 \times 10^4 \text{ sec}$$

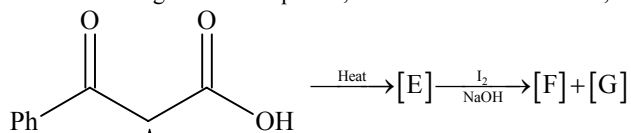
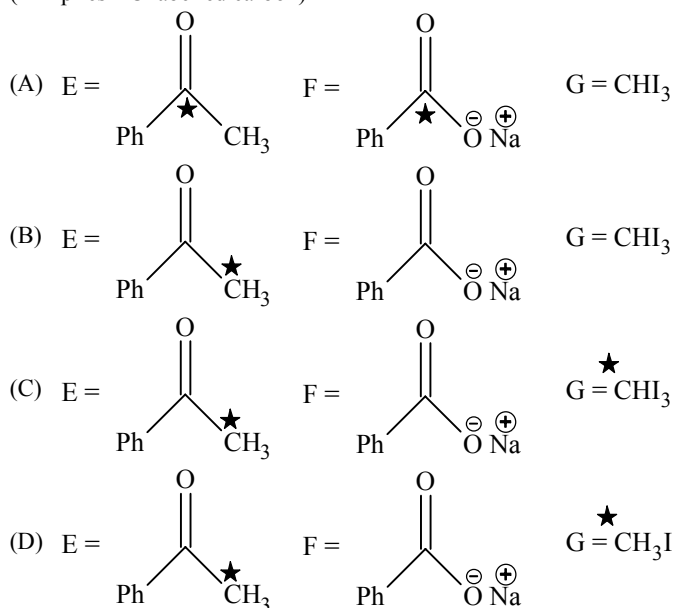
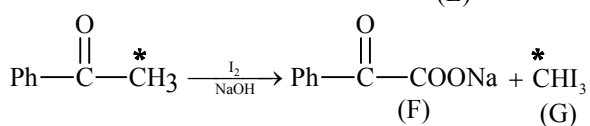
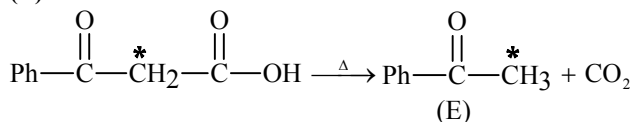
51. Cellulose upon acetylation with excess acetic anhydride/ H_2SO_4 (catalytic) gives cellulose triacetate whose structure is



**Sol.****(A)**As in cellulose β 1-4 glycosidic linkage is present.

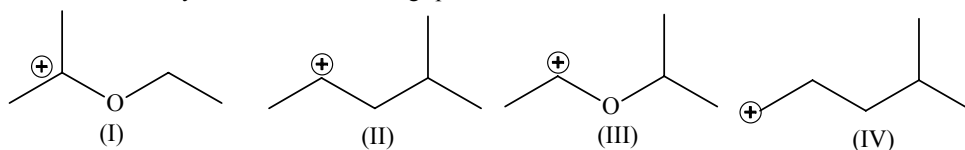
52.

In the following reaction sequence, the correct structures of E, F and G are

(* implies ^{13}C labelled carbon)**Sol.****(C)**

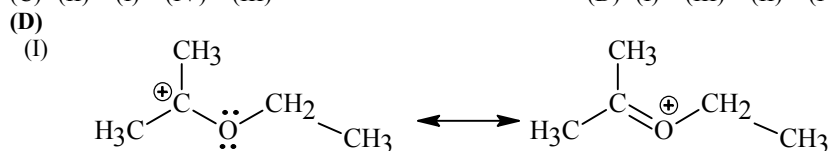
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53. The correct stability order for the following species is

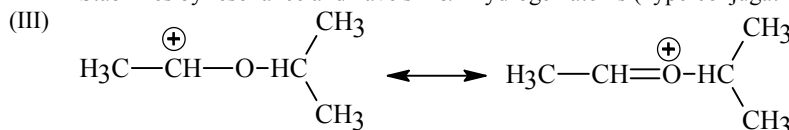


- (A) (II) > (IV) > (I) > (III)
 (B) (I) > (II) > (III) > (IV)
 (C) (II) > (I) > (IV) > (III)
 (D) (I) > (III) > (II) > (IV)

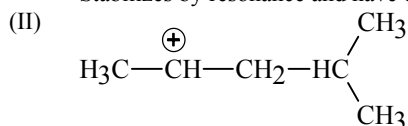
Sol.



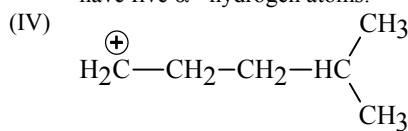
Stabilizes by resonance and have six α - hydrogen atoms (hyperconjugation)



Stabilizes by resonance and have only three α - hydrogen atoms.



have five α - hydrogen atoms.



have only two α - hydrogen atoms.

\therefore I > III > II > IV

SECTION – II

Reasoning Type

This section contains 4 reasoning type questions. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

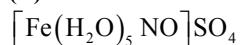
54. STATEMENT-1: The geometrical isomers of the complex $[M(NH_3)_4Cl_2]$ are optically inactive.
and
 STATEMENT-2: Both geometrical isomers of the complex $[M(NH_3)_4Cl_2]$ possess axis of symmetry.
 (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is NOT a correct explanation for STATEMENT-1
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

Sol.

(B)
 The molecule should not possess alternate axis of symmetry to be optically active.

55. STATEMENT-1: $[Fe(H_2O)_5NO]SO_4$ is paramagnetic.
and
 STATEMENT-2: The Fe in $[Fe(H_2O)_5NO]SO_4$ has three unpaired electrons.
 (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is NOT a correct explanation for STATEMENT-1
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

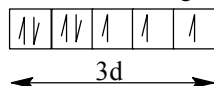
Sol. (A)



Here Fe has +1 oxidation state.

$\text{Fe}^+ = 3d^6 4s^1$ in presence of NO^+ 4s¹ electron are paired in 3d sub shell.

So electronic configuration of Fe^+ is



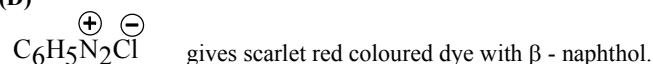
56. STATEMENT-1: Aniline on reaction with NaNO_2/HCl at 0°C followed by coupling with β -naphthol gives a dark blue coloured precipitate.

and

STATEMENT-2: The colour of the compound formed in the reaction of aniline with NaNO_2/HCl at 0°C followed by coupling with β -naphthol is due to the extended conjugation.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is NOT a correct explanation for STATEMENT-1
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

Sol. (D)



57. STATEMENT-1: There is a natural asymmetry between converting work to heat and converting heat to work.

and

STATEMENT-2: No process is possible in which the sole result is the absorption of heat from a reservoir and its complete conversion into work.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is correct explanation for STATEMENT-1
 (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is NOT a correct explanation for STATEMENT-1
 (C) STATEMENT-1 is True, STATEMENT-2 is False
 (D) STATEMENT-1 is False, STATEMENT-2 is True

Sol. (B)

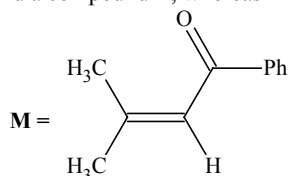
SECTION – III

Linked Comprehension Type

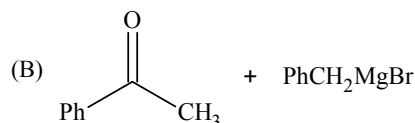
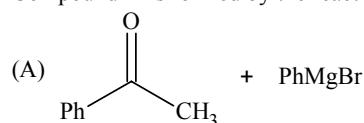
This section contains 2 paragraphs. Based upon each paragraph, 3 multiple choice questions have to be answered. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

Paragraph for Question Nos. 58 to 60

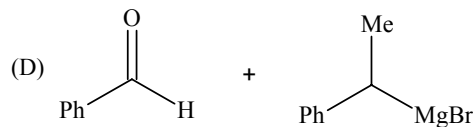
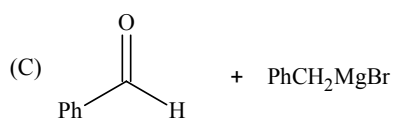
A tertiary alcohol **H** upon acid catalysed dehydration gives a product **I**. Ozonolysis of **I** leads to compounds **J** and **K**. Compound **J** upon reaction with KOH gives benzyl alcohol and a compound **L**, whereas **K** on reaction with KOH gives only **M**,



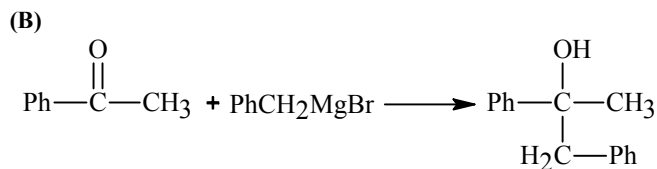
58. Compound **H** is formed by the reaction of



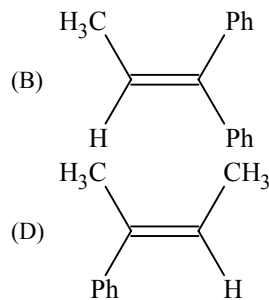
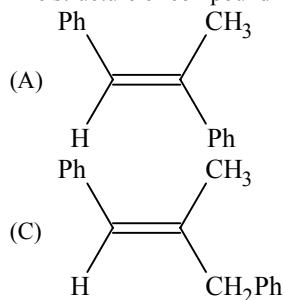
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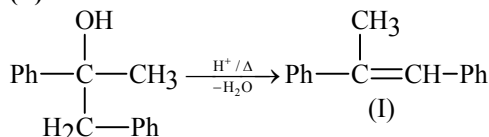
Sol.



59. The structure of compound I is



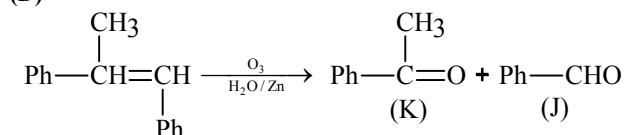
Sol.



60. The structures of compounds J, K and L, respectively, are

- (A) PhCOCH_3 , $\text{PhCH}_2\text{COCH}_3$ and $\text{PhCH}_2\text{COO}^-\text{K}^+$ (B) PhCHO , PhCH_2CHO and PhCOO^-K^+
 (C) PhCOCH_3 , PhCH_2CHO and $\text{CH}_3\text{COO}^-\text{K}^+$ (D) PhCHO , PhCOCH_3 and PhCOO^-K^+

Sol.



Hence, (D) is the correct answer.

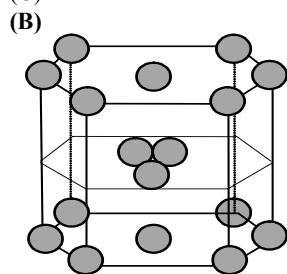
Paragraph for Question Nos. 61 to 63

In hexagonal systems of crystals, a frequently encountered arrangement of atoms is described as a hexagonal prism. Here, the top and bottom of the cell are regular hexagons and three atoms are sandwiched in between them. A space-filling model of this structure, called hexagonal close-packed (HCP), is constituted of a sphere on a flat surface surrounded in the same plane by six identical spheres as closely as possible. Three spheres are then placed over the first layer so that they touch each other and represent the second layer. Each one of these three spheres touches three spheres of the bottom layer. Finally, the second layer is covered with a third layer that is identical to the bottom layer in relative position. Assumer radius of every sphere to be 'r'.

61. The number of atoms on this HCP unit cell is

- (A) 4 (B) 6
 (C) 12 (D) 17

Sol.



$$\text{Total effective number of atoms} = 12 \times \frac{1}{6} + 2 \times \frac{1}{2} + 3 = 6$$

62. The volume of this HCP unit cell is

- (A) $24\sqrt{2}r^3$ (B) $16\sqrt{2}r^3$
 (C) $12\sqrt{2}r^3$ (D) $\frac{64r^3}{3\sqrt{3}}$

Sol. (A)

$$\text{Height of unit cell} = 4r\sqrt{\frac{2}{3}}$$

$$\text{Base area} = 6 \times \frac{\sqrt{3}}{4} (2r)^2$$

$$\begin{aligned} \text{Volume} &= \text{height} \times \text{base area} \\ &= 24\sqrt{2}r^3 \end{aligned}$$

63. The empty space in this HCP unit cell is

- (A) 74% (B) 47.6%
 (C) 32% (D) 26%

Sol. (D)

$$\text{Packing fraction} = 74\%$$

$$\text{Empty space} = 26\%$$

SECTION – IV

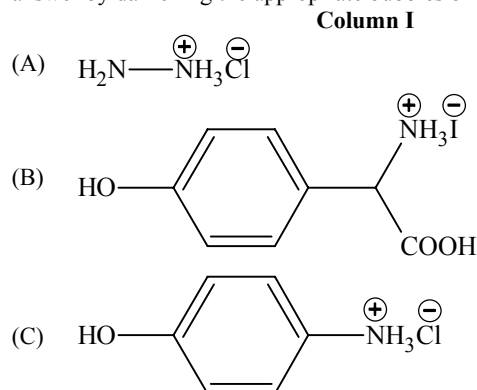
Matrix-Match Type

This contains 3 questions. Each question contains statements given in two columns which have to be matched. Statements (A, B, C, D) in column I have to be matched with statements (p, q, r, s) in column II. The answers to these questions have to be appropriately bubbled as illustrated in the following example.

If the correct match are A-p, A-s, B-r, C-p, C-q and D-s, then the correctly bubbled 4×4 matrix should be as follows:

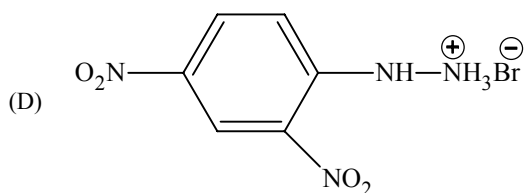
	p	q	r	s
A	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>

64. Match the compounds in **Column I** with their characteristic test(s)/ reaction(s) given in **Column II**. Indicate your answer by darkening the appropriate bubbles of the 4×4 matrix gives in the ORS.



- Column II**
- (p) sodium fusion extract of the compound gives Prussian blue colour with FeSO_4
- (q) gives positive FeCl_3 test
- (r) gives white precipitate with AgNO_3

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(s) reacts with aldehydes to form the corresponding hydrazone derivative

Sol.
 A – r, s
 B – p, q
 C – p, q, r
 D – p, s

65. Match the entries in **Column I** with the correctly related quantum number(s) in **Column II**. Indicate your answer by darkening the appropriate bubbles of the 4×4 matrix given in the ORS.

Column I	Column II
(A) Orbital angular momentum of the electron in a hydrogen-like atomic orbital	(p) Principal quantum number
(B) A hydrogen-like one-electron wave function obeying Pauli principle	(q) Azimuthal quantum number
(C) Shape, size and orientation of hydrogen-like atomic orbitals	(r) Magnetic quantum number
(D) Probability density of electron at the nucleus in hydrogen-like atom	(s) Electron spin quantum number

Sol.
 A – q
 B – s
 C – p, q, r
 D – p, q, r

66. Match the conversions in **Column I** with the type(s) of reaction(s) given in **Column II**. Indicate your answer by darkening the appropriate bubbles of the 4×4 matrix given in the ORS.

Column I	Column II
(A) $\text{PbS} \rightarrow \text{PbO}$	(p) roasting
(B) $\text{CaCO}_3 \rightarrow \text{CaO}$	(q) calcination
(C) $\text{ZnS} \rightarrow \text{Zn}$	(r) Carbon reduction
(D) $\text{Cu}_2\text{S} \rightarrow \text{Cu}$	(s) self reduction

Sol.
 A – p
 B – q
 C – p, r
 D – p, s