

# VECTORS

QNo1: If  $\vec{a}, \vec{b}, \vec{c}$  are the position vectors of the vertices of an equilateral triangle whose orthocenter is at the origin, then :

- (a)  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$       (b)  $\vec{a}^2 = \vec{b}^2 + \vec{c}^2$       (c)  $\vec{a} + \vec{b} = \vec{c}$       (d) none of these



QNo2: If  $\vec{a}, \vec{b}, \vec{c}$  are three vectors such that  $\vec{a} + \vec{b} = \vec{c}$ , then  $\vec{b}$  is called

- (a) a projection of  $\vec{c}$       (b) a component of  $\vec{c}$       (c) a complement  $\vec{c}$       (d) none of these

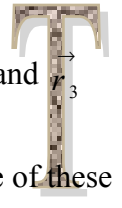


QNo3: If  $\vec{a} = (1, -1)$  and  $\vec{b} = (-2, m)$  are collinear vectors, then  $m =$

- (a) 4      (b) 3      (c) 2      (d) 0

QNo4: If  $\vec{c}$  is one unit vector  $\perp$  to  $\vec{a}, \vec{b}$ , then the second unit vector  $\perp$  to  $\vec{a}, \vec{b}$  will be

- (a)  $\vec{a}$       (b)  $\vec{a} \times \vec{b}$       (c)  $-\vec{c}$       (d) none of these

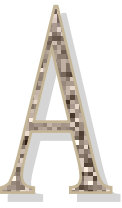


QNo5: The position vectors of three consecutive vertices A, B and C of a parallelogram ABCD are  $\vec{r}_1, \vec{r}_2$  and  $\vec{r}_3$  respectively. Then the position vector of the formula vertex D is :

- (a)  $\vec{r}_1 + \vec{r}_2 - \vec{r}_3$       (b)  $\vec{r}_2 + \vec{r}_3 - \vec{r}_1$       (c)  $\vec{r}_3 + \vec{r}_1 - \vec{r}_2$       (d) none of these

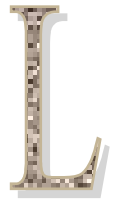
QNo6: Projection of the vector  $\vec{a} = 2\vec{i} + 3\vec{j} - 2\vec{k}$  on the vector  $\vec{b} = \vec{i} + 2\vec{j} + 3\vec{k}$  is

- (a)  $\frac{2}{\sqrt{14}}$       (b)  $\frac{1}{\sqrt{14}}$       (c)  $\frac{3}{\sqrt{14}}$       (d) none of these



QNo7: The value of  $|\vec{a} \times \vec{i}|^2 + |\vec{a} \times \vec{j}|^2 + |\vec{a} \times \vec{k}|^2$  is :

- (a)  $|\vec{a}|^2$       (b)  $2|\vec{a}|^2$       (c)  $3|\vec{a}|^2$       (d)  $4|\vec{a}|^2$



QNo8:  $\vec{i} \times (\vec{x} \times \vec{i}) + \vec{j} \times (\vec{x} \times \vec{j}) + \vec{k} \times (\vec{x} \times \vec{k})$  is equal to

- (a)  $\vec{0}$       (b)  $\vec{x}$       (c)  $2\vec{x}$       (d) 0

QNo9:  $(\vec{a} \times \vec{b})^2$  is equal to

- (a)  $\vec{a} \cdot \vec{b} - (\vec{a} \cdot \vec{b})^2$       (b)  $\vec{a}^2 \cdot \vec{b}^2 + (\vec{a} \cdot \vec{b})^2$       (c)  $(\vec{a} \cdot \vec{b})^2$       (d)  $\vec{a}^2 \cdot \vec{b}^2$

QNo10: The vector  $\frac{2}{7}\vec{i} + \frac{3}{7}\vec{j} - \frac{6}{7}\vec{k}$  is

- (a) a null vector      (b) a unit vector      (c) a vector whose components are (2, 3, -6)  
(d) a vector which is equally inclined to the axes



QNo11:  $\vec{a} \cdot (\vec{a} \times \vec{b}) =$

- (a)  $\vec{a} \cdot \vec{b}$       (b)  $ab$       (c) 0      (d)  $a^2 + ab$

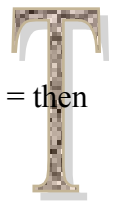


QNo12:  $\vec{a} \times (\vec{b} \times \vec{c}) + \vec{b} \times (\vec{c} \times \vec{a}) + \vec{c} \times (\vec{a} \times \vec{b})$  is :

- (a)  $2(\vec{a} \cdot \vec{b} \cdot \vec{c})$       (b)  $\vec{0}$       (c)  $\vec{a} + \vec{b} + \vec{c}$       (d) 0

QNo13: If the vectors  $3\vec{i} + \lambda\vec{j} + \vec{k}$  and  $2\vec{i} + \vec{j} + 8\vec{k}$  are  $\perp$ , then  $\lambda$  is equal to :

- (a) -4      (b) 1      (c) 14      (d) 1/7



QNo14:  $\vec{e}_1, \vec{e}_2, \vec{e}_3$  are vectors reciprocals to the non-coplanar vectors  $\vec{e}_1, \vec{e}_2, \vec{e}_3$ , then  $[\vec{e}_1, \vec{e}_2, \vec{e}_3] [\vec{e}_1, \vec{e}_2, \vec{e}_3] =$  then

$[\vec{e}_1, \vec{e}_2, \vec{e}_3], [\vec{e}_1, \vec{e}_2, \vec{e}_3] =$

QNo15: 
$$\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \end{vmatrix}$$
 is equal to :

- (a)  $[\vec{a}, \vec{b}, \vec{c}]^2$  (b)  $[\vec{a}, \vec{b}, \vec{c}]$  (c)  $[\vec{a}, \vec{b}, \vec{c}]^3$  (d) none of these

QNo16: If  $\vec{a}, \vec{b}, \vec{c}$  are vectors such that  $\vec{c} = \vec{a} + \vec{b}$  and  $\vec{a} \cdot \vec{b} = 0$ , then

- (a)  $a^2 + b^2 + c^2 = 0$  (b)  $a^2 - b^2 = 0$  (c)  $c^2 = a^2 + b^2$  (d)  $c^2 = \vec{a} \times \vec{b}$

QNo17: If  $|\vec{a}| = 6, |\vec{b}| = 8, |\vec{a} - \vec{b}| = 10$ , then  $|\vec{a} + \vec{b}|$  is equal to :

- (a) 10 (b) 24 (c) 40 (d) 36

QNo18: If  $\vec{a}, \vec{b}, \vec{c}$  are coplanar, then  $[\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}] =$

- (a) a (b) 0 (c) b (d) a + b

QNo19: If  $\vec{a}, \vec{b}, \vec{c}$  are coplanar, then  $[\vec{a} \times \vec{b}, \vec{b} \times \vec{c}, \vec{c} \times \vec{a}] =$

- (a) abc (b) ab (c) bc (d) 0

QNo20: The value of  $(\vec{a} - \vec{b})[(\vec{b} - \vec{c}) \times (\vec{c} \times \vec{a})]$  is

- (a) 0 (b)  $2[\vec{a} \vec{b} \vec{c}]$  (c)  $3[\vec{a} \vec{b} \vec{c}]$  (d) none of these

QNo21: The value of  $(\vec{r} \cdot \vec{i})\vec{i} + (\vec{r} \cdot \vec{j})\vec{j} + (\vec{r} \cdot \vec{k})\vec{k}$  is equal to :

- (a)  $\vec{i}$  (b)  $\vec{j}$  (c)  $\vec{k}$  (d)  $\vec{r}$

QNo22: Let  $\vec{A}$  and  $\vec{B}$  be two non-parallel unit vectors in a plane. If the vectors  $(\alpha \vec{A} + \vec{B})$  bisects the internal angle between  $\vec{A}$  and  $\vec{B}$ , then  $\alpha$  is :

- (a) 1/2 (b) 1 (c) 2 (d) 4

QNo23: Let  $\vec{a}$  be a non-zero vector then  $\frac{\vec{a}}{|\vec{a}|}$  is a

- (a) null vectors (b) scalar (c) unit vector parallel to  $\vec{a}$  (d) unit vector perpendicular to  $\vec{a}$

QNo24: If  $\vec{a}$  is a non-zero vector and K is a scalar such that  $|K \vec{a}| = 1$ , then K is equal to

- (a)  $|\vec{a}|$  (b) 1 (c)  $\frac{1}{|\vec{a}|}$  (d)  $+\frac{1}{|\vec{a}|}$

QNo25: Let  $\vec{a} = -\vec{i} + 2\vec{j} = (-1, 2)$

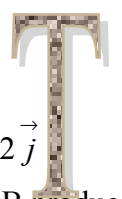
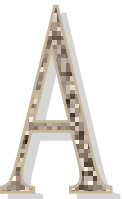
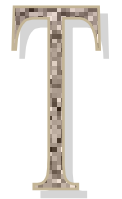
$$\vec{b} = 3\vec{i} - 2\vec{j} = (3, -2)$$

$$\vec{c} = 5\vec{j} = (0, 5)$$

Then  $\vec{a} + \vec{b} = -2\vec{c}$  is :

- (a)  $2\vec{i} + 10\vec{j}$  (b)  $-2\vec{i} + 10\vec{j}$  (c)  $2\vec{i} - 10\vec{j}$  (d)  $3\vec{i} + 2\vec{j}$

QNo26: If  $\vec{a}$  and  $\vec{b}$  are position vector of A and B respectively, then the position vector of a point C in AB produced



such that  $\vec{AC} = 3 \vec{AB}$  is :

(a)  $3 \vec{a} - \vec{b}$

(b)  $3 \vec{b} - \vec{a}$

(c)  $3 \vec{a} - 2 \vec{b}$

(d)  $3 \vec{b} - 2 \vec{a}$

QNo27: Let  $\vec{a}$  and  $\vec{b}$  be unit vectors inclined at an angle  $\alpha$  to each other, then  $|\vec{a} + \vec{b}| < 1$  if

(a)  $\alpha = \frac{\pi}{2}$

(b)  $\alpha < \frac{\pi}{3}$

(c)  $\alpha > \frac{2\pi}{3}$

(d)  $\frac{\pi}{3} < \alpha < \frac{2\pi}{3}$

QNo28:  $[\vec{i} \vec{j} \vec{k}]$  is equal to :

(a) 0

(b) 1

(c) -1

(d) 3

QNo29: Given two vectors  $\vec{a} = 2\vec{i} - 3\vec{j} + 6\vec{k}$ ,  $\vec{b} = -2\vec{i} + 2\vec{j} - \vec{k}$  and  $\lambda = \frac{\text{the projection of } \vec{a} \text{ on } \vec{b}}{\text{the projection of } \vec{b} \text{ on } \vec{a}}$  then the value of

$\lambda$  is :

(a) 3/7

(b) 7

(c) 3

(d) 7/3

QNo30: Let  $\vec{a}$  and  $\vec{b}$  proper vectors. Then  $\vec{a}$  and  $\vec{b}$  are at right angles iff  $\vec{a} \cdot \vec{b}$  is equal to :

(a) 1

(b) 0

(c) -1

(d) none of these

QNo31:  $(1, 0, 0) \times (0, 1, 0)$  is equal to :

(a) (1, 1, 0)

(b) 0

(c) (0, 0, 1)

(d) 2

QNo32: If cross product of two non-zero vectors is zero, then the vectors are :

(a) collinear

(b) co-directional

(c) co-initial

(d) co-terminus

QNo33:  $\vec{i} \cdot (\vec{j} \times \vec{k}) + \vec{j} \cdot (\vec{k} \times \vec{i}) + \vec{k} \cdot (\vec{i} \times \vec{j})$  is equal to :

(a) 0

(b) -3

(c) -1

(d) 3

QNo34: If  $\vec{a} = \vec{i} - 3\vec{j} + \vec{k}$  and  $\vec{b} = \vec{i} + \vec{j} + \vec{k}$ , then  $|\vec{a} \times \vec{b}|$  is equal to :

(a)  $4\sqrt{2}$

(b)  $3\sqrt{2}$

(c)  $2\sqrt{5}$

(d)  $2\sqrt{3}$

QNo35: If  $\vec{a}, \vec{b}, \vec{c}$  are any three mutually  $\perp$  unit vectors, then  $|\vec{a} + \vec{b} + \vec{c}|$  is equal to :

(a) 1

(b)  $\sqrt{2}$

(c)  $\sqrt{3}$

(d) 2

QNo36: A unit vector parallel to the sum of the vectors  $\vec{a} = 2\vec{i} + 4\vec{j} - 5\vec{k}$  and  $\vec{b} = \vec{i} + 2\vec{j} + 3\vec{k}$  is given by

(a)  $3\vec{i} + 6\vec{j} - 2\vec{k}$

(b)  $-\frac{1}{7}(3\vec{i} + 6\vec{j} - 2\vec{k})$

(c)  $\frac{1}{7}(3\vec{i} + 6\vec{j} - 2\vec{k})$

(d) none of these

QNo37: If  $\vec{a} = \vec{i} + \vec{j} - \vec{k}$ ,  $\vec{b} = \vec{i} - \vec{j} + \vec{k}$  and  $\vec{c}$  is a unit vector perpendicular to the vector  $\vec{a}$  and coplanar with  $\vec{a}$  and  $\vec{b}$ , then a unit vector  $\vec{d}$  perpendicular, to both  $\vec{a}$  and  $\vec{c}$  is :

(a)  $\frac{1}{\sqrt{6}}(2\vec{i} - \vec{j} + \vec{k})$

(b)  $\frac{1}{\sqrt{2}}(\vec{i} + \vec{j})$

(c)  $\frac{1}{\sqrt{2}}(\vec{j} + \vec{k})$

(d)  $\frac{1}{\sqrt{2}}(\vec{i} + \vec{k})$

QNo38: The unit vector perpendicular to each of the vectors  $\vec{i} + 2\vec{j} + 3\vec{k}$  and  $-3\vec{i} - 2\vec{j} + \vec{k}$  is

(a)  $\frac{1}{6\sqrt{5}}(8\vec{i} - 10\vec{j} + 4\vec{k})$

(b)  $8\vec{i} - 10\vec{j} + 4\vec{k}$

(c)  $8\vec{i} + 10\vec{j} + 4\vec{k}$

(d) none of these

QNo39: A unit vector perpendicular to each of the vectors  $-6\vec{i} + 8\vec{k}$ ,  $8\vec{i} + 6\vec{k}$  forming a right handed system is :

(a)  $-\vec{j}$

(b)  $\vec{j}$

(c)  $\frac{1}{10}(6\vec{i} + 8\vec{k})$

(d)  $\frac{1}{10}(-6\vec{i} + 8\vec{k})$

QNo40: If  $\vec{a}, \vec{b}, \vec{c}$  are unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ , then the value of  $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} =$

- (a)  $2/3$  (b)  $-2/3$  (c)  $-(3/2)$  (d)  $3/2$

QNo41: If  $\vec{x}$  and  $\vec{y}$  are two unit vectors and  $\theta$  is the angle between them, then  $\frac{1}{2}|\vec{x} - \vec{y}|$  is equal to :

- (a) 0 (b)  $x/2$  (c)  $\cos \frac{\theta}{2}$  (d)  $\sin \frac{\theta}{2}$

QNo42:  $[\vec{a} \vec{b} \vec{c}]$  is the scalar product of three vectors  $\vec{a}, \vec{b}$  and  $\vec{c}$ . Then  $[\vec{a} \vec{b} \vec{c}]$  is equal to

- (a)  $[\vec{b} \vec{a} \vec{c}]$  (b)  $[\vec{c} \vec{b} \vec{a}]$  (c)  $[\vec{b} \vec{c} \vec{a}]$  (d)  $[\vec{a} \vec{c} \vec{b}]$

QNo43: If  $\theta$  is the angle between vectors  $\vec{a}$  and  $\vec{b}$ , then  $\vec{a} \cdot \vec{b} > 0$  only if

- (a)  $0 \leq \theta \leq \pi$  (b)  $\frac{\pi}{2} \leq \theta \leq \pi$  (c)  $0 \leq \theta \leq \frac{\pi}{2}$  (d)  $0 < \theta < \frac{\pi}{2}$

QNo44: If  $\theta$  is the angle between vectors  $\vec{a}, \vec{b}$ , and  $|\vec{a} \times \vec{b}| = \sqrt{3}|\vec{a} \cdot \vec{b}|$ , then  $\theta$  is equal to :

- (a)  $\pi/6$  (b)  $\pi/4$  (c)  $\pi/2$  (d)  $\pi/3$

QNo45: If  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a} = 0$ , then  $\vec{a} \cdot (\vec{b} \times \vec{c})$  is equal to :

- (a) a non-zero vector (b) 1 (c) -1 (d)  $|\vec{a}| |\vec{b}| |\vec{c}|$

QNo46: Let  $\vec{a}, \vec{b}, \vec{c}$  be the position vectors of three vertices A, B, C of a triangle respectively. Then the area of this triangle is given by :

- (a)  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$  (b)  $\frac{1}{2}(\vec{a} \times \vec{b}) \cdot \vec{c}$  (c)  $\frac{1}{2}|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}|$  (d) none of these

QNo47: The sine of the angle between the vectors  $\vec{i} - 2\vec{j} + 3\vec{k}$  and  $2\vec{i} + \vec{j} + \vec{k}$  is :

- (a)  $\frac{5}{2\sqrt{7}}$  (b)  $\frac{5}{\sqrt{7}}$  (c)  $\frac{3}{\sqrt{14}}$  (d)  $\frac{5}{21}$

QNo48: The value of  $[\vec{a} - \vec{b}, \vec{b} - \vec{c}, \vec{c} - \vec{a}]$  where  $|\vec{a}| = 1, |\vec{b}| = 2$  and  $|\vec{c}| = 3$  is

- (a) 1 (b) 6 (c) 0 (d) 3.

QNo49:  $[\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}]$  is equal to

- (a) 0 (b)  $\vec{a} \times \vec{b} \cdot \vec{c}$  (c)  $2|[\vec{a} \vec{b} \vec{c}]|$  (d) none of these

QNo50: The sine of the angle between the vectors  $\vec{a} = 3\vec{i} + \vec{j} + \vec{k}, \vec{b} = 2\vec{i} - 2\vec{j} + \vec{k}$  is :

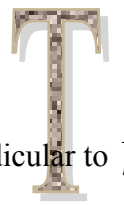
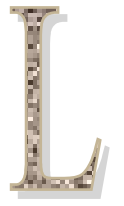
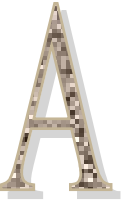
- (a)  $\sqrt{\frac{74}{99}}$  (b)  $\sqrt{\frac{25}{99}}$  (c)  $\sqrt{\frac{37}{99}}$  (d)  $\frac{5}{\sqrt{41}}$

QNo51: If  $\theta$  is the angle between two vectors  $\vec{a}$  and  $\vec{b}$ , then  $\frac{|\vec{a} \times \vec{b}|}{|\vec{a} \cdot \vec{b}|}$  equals :

- (a)  $\cot \theta$  (b)  $-\cot \theta$  (c)  $\tan \theta$  (d)  $-\tan \theta$

QNo52: The vector  $\vec{a} \times (\vec{b} \times \vec{a})$  is :

- (a) a null vector (b) perpendicular to both  $\vec{a}$  and  $\vec{b}$  (c) perpendicular to  $\vec{a}$  (d) perpendicular to  $\vec{b}$



QNo53: If  $\vec{a}$  and  $\vec{b}$  are any two vectors, then

- (a)  $|\vec{a} \times \vec{b}| \leq |\vec{a}| |\vec{b}|$       (b)  $|\vec{a} \times \vec{b}| \geq |\vec{a}| |\vec{b}|$       (c)  $|\vec{a} \times \vec{b}| > |\vec{a}| |\vec{b}|$       (d)  $|\vec{a} \times \vec{b}| < |\vec{a}| |\vec{b}|$

QNo54: If  $\vec{a}$  and  $\vec{b}$  are any two vectors, then

- (a)  $|\vec{a} \cdot \vec{b}| > |\vec{a}| |\vec{b}|$       (b)  $|\vec{a} \cdot \vec{b}| < |\vec{a}| |\vec{b}|$       (c)  $|\vec{a} \cdot \vec{b}| \geq |\vec{a}| |\vec{b}|$       (d)  $|\vec{a} \cdot \vec{b}| \leq |\vec{a}| |\vec{b}|$

QNo55: Let the vectors  $\vec{u}, \vec{v}$  and  $\vec{w}$  be coplanar. Then  $\vec{u} \cdot (\vec{v} \times \vec{w})$  is :

- (a) 0      (b)  $\vec{0}$       (c) a unit vector      (d) none of these

QNo56: The vector  $2\vec{i} + \vec{j} + \vec{k}$  is perpendicular to  $\vec{i} - 4\vec{j} + \lambda\vec{k}$  if  $\lambda$  is equal to :

- (a) 0      (b) -1      (c) 2      (d) -3

QNo57: The angle between the vectors  $2\vec{i} + 3\vec{j} + \vec{k}$  and  $2\vec{i} - \vec{j} - \vec{k}$  is :

- (a)  $\frac{\pi}{2}$       (b)  $\frac{\pi}{4}$       (c)  $\frac{\pi}{3}$       (d) 0

QNo58: If  $\vec{a} = 4\vec{i} + 6\vec{j}$  and  $\vec{b} = 3\vec{j} + 4\vec{k}$ , then the vector form of the component of  $\vec{a}$  along  $\vec{b}$  is :

- (a)  $\frac{18}{10\sqrt{3}}(3\vec{j} + 4\vec{k})$       (b)  $\frac{18}{5}(3\vec{j} + 4\vec{k})$       (c)  $\frac{18}{\sqrt{13}}(3\vec{j} + 4\vec{k})$       (d)  $3\vec{j} + 4\vec{k}$

QNo59: Area of the parallelogram whose diagonals are  $\vec{a}$  and  $\vec{b}$  is :

- (a)  $\vec{a} \cdot \vec{b}$       (b)  $|\vec{a} \times \vec{b}|$       (c)  $\vec{a} + \vec{b}$       (d)  $\frac{1}{2} |\vec{a} + \vec{b}|$

QNo60: The area of the parallelogram whose diagonals are given by the vectors

$$3\vec{i} + \vec{j} - 2\vec{k} \text{ and } \vec{i} - 3\vec{j} + 4\vec{k} \text{ is}$$

- (a)  $10\sqrt{3}$       (b)  $5\sqrt{3}$       (c) 8      (d) 4

QNo61: Let G be the centroid of a triangle ABC. If  $\vec{AB} = \vec{a}$ ,  $\vec{AC} = \vec{b}$ , then the bisector  $\vec{AG}$ , in terms of vectors  $\vec{a}$  and  $\vec{b}$  is :

- (a)  $\frac{2}{3}(\vec{a} + \vec{b})$       (b)  $\frac{1}{6}(\vec{a} + \vec{b})$       (c)  $\frac{1}{3}(\vec{a} + \vec{b})$       (d)  $\frac{1}{2}(\vec{a} + \vec{b})$

QNo62: If A, B, C, D, E are five coplanar points then  $\vec{DA} + \vec{DB} + \vec{DC} + \vec{AE} + \vec{BE} + \vec{CE}$  is equal to

- (a)  $\vec{DE}$       (b)  $3\vec{DE}$       (c)  $2\vec{DE}$       (d)  $4\vec{ED}$

QNo63: If three points A, B, C whose position vectors are respectively  $\vec{i} - 2\vec{j} - 8\vec{k}$  and  $5\vec{i} - 2\vec{k}$  and  $11\vec{i} + 3\vec{j} + 7\vec{k}$  are collinear, then the ratios in which B, divides AC is :

- (a) 1 : 2      (b) 2 : 3      (c) 2 : 1      (d) none of these

QNo64: In a  $\Delta$  ABC,  $|\vec{AB}| = a$ ,  $|\vec{AD}| = b$  and  $|\vec{AC}| = c$ , then  $\vec{DB} \cdot \vec{AB}$  has the value

- (a)  $\frac{3a^2 + b^2 - c^2}{2}$       (b)  $\frac{a^2 + 3b^2 - c^2}{2}$       (c)  $\frac{a^2 - b^2 + 3c^2}{2}$       (d)  $\frac{a^2 + 3b^2 + c^2}{2}$

QNo65: The position vectors of four points P, Q, R, S are  $2\vec{a} + 4\vec{c}$ ,  $5\vec{a} + 3\sqrt{3}\vec{b} + 4\vec{c}$ ,  $-2\sqrt{3}\vec{b} + \vec{c}$  and  $2\vec{a} + \vec{c}$  respectively. Then

- (a)  $PQ \parallel RS$       (b) PQ is not parallel to RS      (c)  $PQ = RS$       (d)  $PQ \parallel RS$  and  $PQ = RS$

QNo66: Let  $\vec{OA} = \vec{i} + 3\vec{j} - 2\vec{k}$  and  $\vec{OB} = 3\vec{i} + \vec{j} - 2\vec{k}$ .

The vector  $\vec{OC}$  bisecting the angle AOB and C being a point on the line AB is

- (a)  $4(\vec{i} + \vec{j} - \vec{k})$  (b)  $2(\vec{i} + \vec{j} - \vec{k})$  (c)  $(\vec{i} + \vec{j} - \vec{k})$  (d) none of these

QNo67: Let  $\alpha, \beta, \lambda$  be three distinct real numbers. The points with position vectors  $\alpha\vec{i} + \beta\vec{j} - \lambda\vec{k}$ ,  $\beta\vec{i} + \lambda\vec{j} + \alpha\vec{k}$ ,  $\lambda\vec{i} + \alpha\vec{j} + \beta\vec{k}$

- (a) are collinear (b) form an equilateral triangle (c) form a scalene triangle (d) form a right angled triangle

QNo68: Let  $\vec{p}$  and  $\vec{q}$  be the position vectors of P and Q respectively, with respect to O and  $|\vec{p}| = p, |\vec{q}| = q$ . The points R and S divide PQ internally and externally in the ratio 2 : 3 respectively. If  $\vec{OR}$  and  $\vec{OS}$  are perpendicular, then :

- (a)  $9p^2 = 4q^2$  (b)  $4p^2 = 9q^2$  (c)  $9p = 4q$  (d)  $4p = 9q$

QNo69: A unit vector perpendicular to the vectors  $4\vec{i} - \vec{j} + 3\vec{k}$  and  $-2\vec{i} + \vec{j} - 2\vec{k}$  is

- (a)  $\frac{1}{3}(\vec{i} - 2\vec{j} + 2\vec{k})$  (b)  $\frac{1}{3}(-\vec{i} + 2\vec{j} + 2\vec{k})$  (c)  $\frac{1}{3}(2\vec{i} + \vec{j} + 2\vec{k})$  (d)  $\frac{1}{3}(2\vec{i} - 2\vec{j} + 2\vec{k})$

QNo70: Given  $\vec{a} = \vec{i} + \vec{j} - \vec{k}$ ,  $\vec{b} = -\vec{i} + \vec{j} + \vec{k}$  and  $\vec{c} = -\vec{i} + 2\vec{j} - \vec{k}$ . A unit vector perpendicular to both  $\vec{a} + \vec{b}$  and  $\vec{b} + \vec{c}$  is :

- (a)  $\vec{i}$  (b)  $\vec{k}$  (c)  $\vec{j}$  (d)  $\frac{\vec{i} + \vec{j} + \vec{k}}{\sqrt{3}}$

QNo71: For a non-zero vector  $\vec{a}$ , which of the following statement is true :

- (a)  $\vec{a} \cdot \vec{a} \geq 0$  (b)  $\vec{a} \cdot \vec{a} > 0$  (c)  $\vec{a} \cdot \vec{a} = 0$  (d)  $\vec{a} \cdot \vec{a} \leq 0$

QNo72: For a non-zero vector  $\vec{a}$ , the set of real numbers satisfying the inequality  $|(5-x)\vec{a}| < |2\vec{a}|$  consists of all x such that :

- (a)  $0 < x < 3$  (b)  $3 < x < 7$  (c)  $-7 < x < -3$  (d)  $-7 < x < 3$

QNo73: A vector  $\vec{a}$  has magnitude 5 units and points north east and another vector  $\vec{b}$  has magnitude 5 units and point north west. Then the magnitude of the vector  $(\vec{a} - \vec{b})$  is :

- (a) 0 (b)  $5\sqrt{2}$  (c) 10 (d) 25

QNo74: The position vectors of three consecutive vertices A, B and C of a parallelogram ABCD are  $\vec{r}_1, \vec{r}_2$  and  $\vec{r}_3$  respectively. Then the position vector of the fourth vertex D is :

- (a)  $\vec{r}_1 + \vec{r}_2 - \vec{r}_3$  (b)  $\vec{r}_2 + \vec{r}_3 - \vec{r}_1$  (c)  $\vec{r}_3 + \vec{r}_1 - \vec{r}_2$  (d) none of these

QNo75: If vectors  $\vec{AB} = 3\vec{i} - 3\vec{k}$  and  $\vec{AC} = \vec{i} - 2\vec{j} + \vec{k}$  are the sides of a triangle ABC, then the length of the median AM, is

- (a)  $\sqrt{3}$  (b)  $\sqrt{6}$  (c)  $2\sqrt{3}$  (d)  $3\sqrt{2}$

QNo76: If the points A, B, C and D have position vectors  $\vec{a}, 2\vec{a} + \vec{b}, 4\vec{a} + 2\vec{b}$  and  $5\vec{a} + 4\vec{b}$  respectively. Then the three collinear points are :

- (a) A, B and C (b) A, C and D (c) A, B and D (d) B, C and D

QNo77: For non-zero vectors  $\vec{a}$  and  $\vec{b}$ , if  $|\vec{a} + \vec{b}| < |\vec{a} - \vec{b}|$ , then  $\vec{a}$  and  $\vec{b}$  are

- (a) collinear (b) perpendicular to each other (c) inclined at an acute angle (d) inclined at an obtuse angle

QNo78: For the vectors  $\vec{a} = \vec{i} + 2\vec{j} + \vec{k}$ ,  $\vec{b} = 2\vec{i} + \vec{j}$ ,  $\vec{c} = 3\vec{i} - 4\vec{j} - 5\vec{k}$ , If  $\vec{a} + t\vec{b}$  is perpendicular to  $\vec{c}$ , the value of t, is :

- (a) 1 (b) -4 (c) 4 (d) 5

QNo79: If the difference of two unit vectors is again a unit vector, then the angle between them is :

- (a)  $30^\circ$  (b)  $45^\circ$  (c)  $60^\circ$  (d)  $90^\circ$

QNo80: If  $\vec{x} \times \vec{b} = \vec{c} \times \vec{b}$  and  $\vec{x} \perp \vec{a}$ , then  $\vec{x}$  is equal to

- (a)  $\frac{(\vec{b} \times \vec{c}) \times \vec{a}}{\vec{b} \cdot \vec{a}}$  (b)  $\frac{\vec{b} \times (\vec{a} \times \vec{c})}{\vec{b} \cdot \vec{c}}$  (c)  $\frac{(\vec{c} \times \vec{b}) \times \vec{a}}{\vec{a} \cdot \vec{b}}$  (d) none of these

QNo81: The adjacent sides of a parallelogram are  $\vec{a} = \vec{i} + 2\vec{j}$  and  $\vec{b} = 2\vec{i} + \vec{j}$ , where  $\vec{i}$  and  $\vec{j}$  are the usual unit-vectors along the positive directions of x and y axes respectively. Then the angle between the diagonals is :

- (a)  $30^\circ$  and  $150^\circ$  (b)  $45^\circ$  and  $135^\circ$  (c)  $60^\circ$  and  $120^\circ$  (d)  $90^\circ$  and  $90^\circ$

QNo82: If  $\vec{a}$  and  $\vec{b}$  are two vectors such that  $\vec{a} \cdot \vec{b} = 0$  and  $\vec{a} \times \vec{b} = \vec{0}$ , then the correct statement is ;

- (a)  $\vec{a}$  is parallel to  $\vec{b}$  (b)  $\vec{a}$  is perpendicular to  $\vec{b}$  (c) either  $\vec{a} = \vec{0}$  or  $\vec{b} = \vec{0}$  (d) none of these

QNo83: If  $\vec{c} = \vec{a} \times \vec{b}$  and  $\vec{b} = \vec{c} \times \vec{a}$ , then

- (a)  $\vec{a} \cdot \vec{b} = \vec{c}^2$  (b)  $\vec{c} \cdot \vec{a} = \vec{b}^2$  (c)  $\vec{b} \cdot \vec{c} = \vec{a}^2$  (d)  $\vec{a} \perp \vec{b}$  or  $a \parallel b \times c$

QNo84: If  $\vec{v}$  and  $\vec{w}$  are two mutually perpendicular unit vector and  $\vec{u} = a\vec{v} + b\vec{w}$ , where a and b are non-zero real numbers, then the angle between  $\vec{u}$  and  $\vec{w}$  is :

- (a)  $\cos^{-1}(a)$  (b)  $\cos^{-1}(b)$  (c)  $\cos^{-1}\left(\frac{a}{\sqrt{a^2 + b^2}}\right)$  (d)  $\cos^{-1}\left(\frac{b}{\sqrt{a^2 + b^2}}\right)$

QNo85: If  $\vec{a}$  and  $\vec{b}$  are two non-zero vectors, then a vector perpendicular to the vector  $(\vec{b} \cdot \vec{b})\vec{a} - (\vec{a} \cdot \vec{b})\vec{b}$  is

- (a)  $\vec{a}$  (b)  $\vec{b}$  (c)  $\vec{a} - \vec{b}$  (d)  $\vec{a} + \vec{b}$

QNo86: The vector  $\frac{1}{3}(2\vec{i} - 2\vec{j} + \vec{k})$  is

- (a) a unit vector (b) makes an angle  $\frac{\pi}{3}$  with the vector  $2\vec{i} - 4\vec{j} + 3\vec{k}$   
 (c) parallel to the vector  $-\vec{i} + \vec{j} + \frac{1}{3}\vec{k}$  (d)  $\perp$  to the vector  $3\vec{i} + 2\vec{j} + 2\vec{k}$

QNo87: Given that  $(\vec{a} + \vec{b})$  is perpendicular to  $\vec{b}$  and  $\vec{a}$  is perpendicular to  $2\vec{b} + \vec{a}$ . This implies

- (a)  $a = \sqrt{2}b$  (b)  $a = 2b$  (c)  $a = b$  (d)  $2a = b$

QNo88: Let  $|\vec{a}| = 3$  and  $|\vec{b}| = 4$ . The value of  $\lambda$  for which  $\vec{a} + \lambda\vec{b}$  and  $\vec{a} - \lambda\vec{b}$  are perpendicular is given by :

- (a)  $\pm \frac{3}{4}$  (b)  $-\frac{2}{3}$  (c)  $\frac{2}{3}$  (d)  $-\frac{3}{5}$

QNo89: The vectors  $\vec{a} = \vec{i} + \vec{j}$ ,  $\vec{b} = \vec{j} + \vec{k}$  and  $\vec{c}$  are of same length and taken pairwise, form equal angles. Then  $\vec{c}$  is equal to :

- (a)  $\vec{i} + 2\vec{j} + \vec{k}$  (b)  $-\frac{1}{3}\vec{i} + \frac{4}{3}\vec{j} - \frac{1}{3}\vec{k}$  (c)  $\vec{i} - \vec{j} + \vec{k}$  (d) none of these

QNo90: Let  $\vec{a}$  be a vector of magnitude  $\sqrt{75}$  which is perpendicular to both  $2\vec{i} - \vec{j} + \vec{k}$  and  $3\vec{i} + 2\vec{j} - \vec{k}$ . Then  $\vec{a}$  is equal to :

- (a)  $-\vec{i} + 5\vec{j} + 7\vec{k}$       (b)  $7\vec{i} + 5\vec{j} + \vec{k}$       (c)  $\vec{i} + 5\vec{j} - 7\vec{k}$       (d)  $-7\vec{i} - 5\vec{j} - \vec{k}$

QNo91: A tetrahedron has vertices at O (0, 0,0), A (1, 2, 1), B (2, 1, 3) and C (-1, 1, 2). Then the angle between the faces OAB and ABC will be :

- (a)  $\cos^{-1} \left( \frac{19}{35} \right)$       (b)  $\cos^{-1} \left( \frac{71}{31} \right)$       (c)  $30^\circ$       (d)  $90^\circ$

QNo92: Given the vectors  $\vec{a} = (3, -1, 5)$  and  $\vec{b} = (1, 2, -3)$ . A vector  $\vec{c}$  is such that it is perpendicular to the z-axis and satisfies the conditions  $\vec{c} \cdot \vec{a} = 9$  and  $\vec{c} \cdot \vec{b} = -4$ . Then  $\vec{c}$  is equal to :

- (a) (-2, 3, 0)      (b) (2, -3, 1)      (c) (2, -3, 0)      (d) none of these

QNo93: Projection of the vector  $2\vec{i} + 3\vec{j} - 2\vec{k}$  on the vector  $\vec{i} + 2\vec{j} + 3\vec{k}$  is :

- (a)  $\frac{2}{\sqrt{14}}$       (b)  $\frac{1}{\sqrt{14}}$       (c)  $\frac{3}{\sqrt{14}}$       (d) none of these

QNo94: Direction of zero vector

- (a) does not exist      (b) is towards origin      (c) is indeterminate      (d) none of these

QNo95: If  $a\vec{i} + \vec{j} + \vec{k}$ ,  $\vec{i} - b\vec{j} + \vec{k}$ ,  $\vec{i} + \vec{j} - c\vec{k}$  are coplanar, then  $abc + 2$  is equal to

- (a)  $a + b + c$       (b)  $a - b - c$       (c)  $a + b + c$       (d)  $a - b + c$

QNo96: The Points D, E, F divide BC, CA, AB of triangle ABC in the ratio 1 : 4, 3 : 2 and 3 : 7 respectively and the point K divides AB in the ratio 1 : 3. Let  $\vec{R}_1$  be the resultant of the vectors  $\vec{AD}$ ,  $\vec{BE}$ ,  $\vec{CF}$  and let the vector CK be denoted by  $\vec{R}_2$ . Then

- (a)  $\vec{R}_1 = \vec{R}_2$       (b)  $5\vec{R}_1 = 2\vec{R}_2$       (c)  $2\vec{R}_1 = 5\vec{R}_2$       (d) none of these

QNo97: If  $\vec{AB} = 3\vec{i} + \vec{j} - \vec{k}$  and  $\vec{AC} = \vec{i} - \vec{j} + 3\vec{k}$ . If the point P on the line segment BC is equidistant from AB and AC, then  $\vec{AP}$  is :

- (a)  $2\vec{i} - \vec{k}$       (b)  $\vec{i} - 2\vec{k}$       (c)  $2\vec{i} + \vec{k}$       (d) none of these

QNo98: P is a point on the line through the point A whose position vector is  $\vec{a}$  and the line is parallel to the vector  $\vec{b}$ . If PA = 6, then the position vector of P is :

- (a)  $\vec{a} + 6\vec{b}$       (b)  $\vec{a} \pm \frac{6}{|\vec{b}|} \vec{b}$       (c)  $\vec{a} - 6\vec{b}$       (d)  $\vec{b} + \frac{6}{|\vec{a}|} \vec{a}$

QNo99: The position vectors of the vertices A, B, C of a triangle are  $\vec{i} - \vec{j} - 3\vec{k}$ ,  $2\vec{i} + \vec{j} - 2\vec{k}$  and  $-5\vec{i} + 2\vec{j} - 6\vec{k}$  respectively. The length of the bisector AD of the angle BAC where D is on the line segment is :

- (a)  $15/2$       (b)  $1/4$       (c)  $11/2$       (d) none of these

QNo100: If the position vectors of points A, B, C are respectively  $\vec{r}, \vec{j}, \vec{k}$  and  $\vec{AB} = \vec{CX}$ , then the position vector of point X is :

- (a)  $-\vec{i} + \vec{j} + \vec{k}$       (b)  $\vec{i} - \vec{j} + \vec{k}$       (c)  $\vec{i} + \vec{j} - \vec{k}$       (d)  $\vec{i} + \vec{j} + \vec{k}$

QNo101: A and B are two points. The position vector of A is  $6\vec{b} - 2\vec{a}$ . A point P divides the line AB in the ratio 1 : 2. If  $\vec{a} - \vec{b}$  is the position vector of B is given by :



(a)  $7\vec{a}-15\vec{b}$

(b)  $7\vec{a}+15\vec{b}$

(c)  $15\vec{a}-7\vec{b}$

(d)  $15\vec{a}+7\vec{b}$

QNo102: The perimeter of the triangle whose vertices have the position vectors  $(\vec{i} + \vec{j} + \vec{k})$ ,  $(5\vec{i} + 3\vec{j} - 3\vec{k})$  and  $(2\vec{i} + 5\vec{j} + 9\vec{k})$ , is given by :

(a)  $15 + \sqrt{157}$

(b)  $15 - \sqrt{157}$

(c)  $\sqrt{15} - \sqrt{157}$

(d)  $\sqrt{15} + \sqrt{157}$

QNo103: If  $\vec{a} = 2\vec{i} - \vec{j} + 3\vec{k}$ ,  $\vec{b} = \vec{i} + 2\vec{j} + \vec{k}$ ,  $\vec{c} = 3\vec{i} + \vec{j} + 2\vec{k}$ , then the value of  $\vec{a} \cdot (\vec{b} \times \vec{c})$  is :

(a) 0

(b) -10

(c) 1

(d) 10

QNo104: ABCDEF is a regular hexagon and  $\vec{AB} = \vec{a}$ ,  $\vec{BC} = \vec{b}$  and  $\vec{CD} = \vec{c}$ , then  $\vec{AE}$  is :

(a)  $\vec{a} + \vec{b} + \vec{c}$

(b)  $\vec{a} + \vec{b}$

(c)  $\vec{b} + \vec{c}$

(d)  $\vec{c} + \vec{a}$

QNo105: Let  $\vec{a}, \vec{b}, \vec{c}$  be three non-coplanar vectors and  $\vec{p}, \vec{q}, \vec{r}$  are vectors defined by the relation

$$\vec{p} = \frac{\vec{b} \times \vec{c}}{(\vec{a} \vec{b} \vec{c})}; \vec{q} = \frac{\vec{c} \times \vec{a}}{(\vec{a} \vec{b} \vec{c})}; \vec{r} = \frac{\vec{a} \times \vec{b}}{(\vec{a} \vec{b} \vec{c})}$$
 then the value of the expression

$$\vec{a} + \vec{b} \cdot \vec{p} + (\vec{b} + \vec{c}) \cdot \vec{q} + (\vec{c} + \vec{a}) \cdot \vec{r}$$
 is equal to :

(a) 0

(b) 1

(c) 2

(d) 3

QNo106: The unit vector perpendicular to each of the vectors  $2\vec{i} - \vec{j} + \vec{k}$  and  $3\vec{i} + 4\vec{j}$  is :

(a)  $\frac{1}{\sqrt{146}}(4\vec{i} - 3\vec{j} + 11\vec{k})$

(b)  $\frac{1}{\sqrt{146}}(-4\vec{i} + 3\vec{j} + 11\vec{k})$

(c)  $\frac{1}{\sqrt{146}}(4\vec{i} + 3\vec{j} + 11\vec{k})$

(d)  $\frac{1}{146}(-4\vec{i} + 3\vec{j} + 11\vec{k})$

QNo107: Let  $\vec{a}, \vec{b}, \vec{c}$  be three vectors such that  $\vec{a} \cdot (\vec{b} + \vec{c}) + \vec{b} \cdot (\vec{c} + \vec{a}) + \vec{c} \cdot (\vec{a} + \vec{b}) = 0$  and  $|\vec{a}| = 1, |\vec{b}| = 4, |\vec{c}| = 8$ , then  $|\vec{a} + \vec{b} + \vec{c}|$  equals :

(a) 13

(b) 81

(c) 9

(d) 5

QNo108: The sum of two unit vector is a unit vector. The magnitude of their difference is :

(a) 2

(b)  $\sqrt{3}$

(c)  $\sqrt{2}$

(d) 1

QNo109: If  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  are the position vectors of points A, B, C and D such that no three of them are collinear and  $\vec{a} + \vec{c} = \vec{b} + \vec{d}$ , then ABCD is :

(a) a parallelogram

(b) a rhombus

(c) a rectangle

(d) a square

QNo110: The vector  $2\vec{i} - m\vec{j} + m\vec{k}$  and  $(1+m)\vec{i} - 2m\vec{j} + \vec{k}$  include an acute angle for

(a) all values of m

(b)  $m < -2$  or  $m > -\frac{1}{2}$

(c)  $m = -\frac{1}{2}$

(d)  $m \in \left[-2, -\frac{1}{2}\right]$

QNo111: If for vector  $\vec{a}$  and  $\vec{b}, \vec{a} + \vec{b} \neq \vec{0}$  and  $\vec{c}$  is a non-zero vector, then  $(\vec{a} + \vec{b}) \times [\vec{c} - (\vec{a} + \vec{b})]$  is :

(a)  $\vec{a} + \vec{b}$

(b)  $(\vec{a} + \vec{b}) \times \vec{c}$

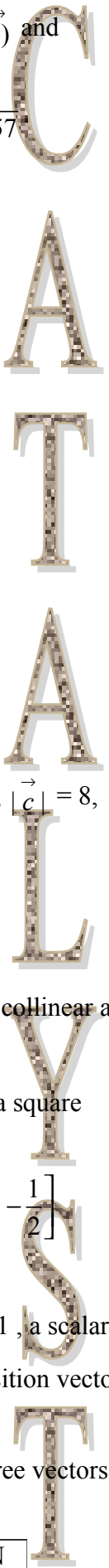
(c)  $\lambda \vec{c}$ , where  $\lambda$  is a non-zero scalar

(d)  $\lambda (\vec{a} + \vec{b})$ ,  $\lambda \neq 0, 1$ , a scalar

QNo112: If a, b, c are different real numbers,  $a\vec{i} + b\vec{j} + c\vec{k}$ ,  $b\vec{i} + c\vec{j} + a\vec{k}$  and  $c\vec{i} + a\vec{j} + b\vec{k}$  are position vectors of three non-collinear points A, B, C, then

(a) centroid of  $\Delta ABC$  is  $\frac{a+b+c}{3}(\vec{i} + \vec{j} + \vec{k})$

(b)  $(\vec{i} + \vec{j} + \vec{k})$  is not equally inclined to three vectors



(c) triangle ABC is a scalene triangle

(d) perpendicular from the origin to the plane of the triangle does not meet it at the centroid

QNo113: If  $\vec{a}$  and  $\vec{b}$  are two perpendicular vectors, then out of the following three statements

- (i)  $(\vec{a} + \vec{b})^2 = (\vec{a})^2 + (\vec{b})^2$     (b)  $(\vec{a} - \vec{b})^2 = (\vec{a})^2 - (\vec{b})^2$     (c)  $(\vec{a} - \vec{b})^2 = (\vec{a})^2 + (\vec{b})^2$     (d)  $(\vec{a} + \vec{b})^2 = (\vec{a} - \vec{b})^2$   
(a) only one is correct    (b) only two are correct    (c) only three are correct    (d) all the four are correct

QNo114: Any line passing thro' two points whose position vectors are  $\vec{a} + \vec{b}$  and  $\vec{a} - \vec{b}$  is  $\vec{r} =$

- (a)  $\vec{a} + (1 - 2t)\vec{b}$     (b)  $\vec{a} - (1 - 2t)\vec{b}$     (c)  $\vec{a} + (1 + 2t)\vec{b}$     (d)  $\vec{a} + (2t - 1)\vec{b}$

QNo115: If  $\vec{x} \cdot \vec{a} = 0$ ,  $\vec{x} \cdot \vec{b} = 0$ ,  $\vec{x} \cdot \vec{c} = 0$  for some non-zero vectors  $\vec{x}$ , then  $[\vec{a} + \vec{b} + \vec{c}] \cdot \vec{x} = 0$ , is

- (a) true    (b) false    (c) cannot say anything    (d) none of these

QNo116: Let  $\vec{A}, \vec{B}, \vec{C}$  be unit vectors. Suppose  $\vec{A} \cdot \vec{B} = \vec{A} \cdot \vec{C} = 0$  and the angle between  $\vec{B}$  and  $\vec{C}$  is  $\frac{\pi}{6}$ . Then  $\vec{A} \cdot (\vec{B} \times \vec{C})$

Equals:

- (a)  $\vec{B} \times \vec{C}$     (b)  $2(\vec{B} \times \vec{C})$     (c)  $-2(\vec{B} \times \vec{C})$     (d)  $\pm 2(\vec{B} \times \vec{C})$

QNo117: If  $\vec{A}, \vec{B}, \vec{C}$  are three non-coplanar vectors, then  $\frac{\vec{A} \cdot (\vec{B} \times \vec{C})}{\vec{C} \cdot (\vec{A} \times \vec{B})} + \frac{\vec{B} \cdot (\vec{A} \times \vec{C})}{\vec{C} \cdot (\vec{A} \times \vec{B})}$  is equal to

- (a) -1    (b) 0    (c) 1    (d) none of these

QNo118:  $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$  iff

- (a)  $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{0}$     (b)  $\vec{c} \times \vec{a} = \vec{b}$     (c)  $\vec{a} \times \vec{c} \times \vec{b} = \vec{0}$     (d) none of these

QNo119: If  $\vec{a} = 2\vec{i} - 3\vec{j} - \vec{k}$  and  $\vec{b} = \vec{i} + 4\vec{j} - 2\vec{k}$ , then  $(\vec{a} + \vec{b}) \times (\vec{a} - \vec{b})$  is given by

- (a)  $20\vec{i} + 6\vec{j} - 22\vec{k}$     (b)  $-(20\vec{i} + 6\vec{j} - 22\vec{k})$     (c)  $6\vec{i} + 20\vec{j} + 22\vec{k}$     (d)  $20\vec{i} + 22\vec{j} + 6\vec{k}$

QNo120: If  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$  and  $|\vec{a}| = 3$ ,  $|\vec{b}| = 5$ ,  $|\vec{c}| = 7$ , then the angle between  $\vec{a}$  and  $\vec{b}$  is :

- (a)  $\frac{\pi}{3}$     (b)  $\frac{\pi}{2}$     (c)  $\frac{\pi}{4}$     (d)  $\frac{\pi}{6}$

QNo121: If P and Q be two given points on the curve  $y = x + \frac{1}{x}$  such that  $\frac{\vec{OP} \cdot \vec{i}}{OP} = 1$  and  $\frac{\vec{OQ} \cdot \vec{i}}{OQ} = -1$  where  $\vec{i}$  is a unit vector along the x-axis, then the length of vector  $2\vec{OP} + 3\vec{OQ}$  is :

- (a)  $5\sqrt{5}$     (b)  $3\sqrt{5}$     (c)  $2\sqrt{5}$     (d)  $\sqrt{5}$

QNo122: a, b, c are the pth, qth, rth terms of an H.P. and  $\vec{u} = (q - r)\vec{i} + (r - p)\vec{j} + (p - q)\vec{k}$

$\vec{v} = \frac{\vec{i}}{a} + \frac{\vec{j}}{b} + \frac{\vec{k}}{c}$ , then

- (a)  $\vec{u}, \vec{v}$  are parallel vectors    (b)  $\vec{u}, \vec{v}$  are orthogonal vectors    (c)  $\vec{u} \cdot \vec{v} = 1$     (d)  $\vec{u} \times \vec{v} = \vec{i} + \vec{j} + \vec{k}$

QNo123: If  $\vec{a} + \vec{b} \perp \vec{a}$  and  $|\vec{b}| = \sqrt{2} |\vec{a}|$ , then

- (a)  $(2\vec{a} + \vec{b})$  is parallel to  $\vec{b}$     (b)  $(2\vec{a} + \vec{b}) \perp \vec{b}$     (c)  $(2\vec{a} - \vec{b}) \perp \vec{b}$     (d)  $(2\vec{a} - \vec{b}) \perp \vec{a}$

QNo124: Let  $\vec{\lambda} = \vec{a} \times (\vec{b} + \vec{c}), \vec{\mu} = \vec{b} \times (\vec{c} + \vec{a}), \vec{v} = \vec{c} \times (\vec{a} + \vec{b})$ . Then

- (a)  $\vec{\lambda} + \vec{u} = \vec{v}$     (b)  $\vec{\lambda}, \vec{u}, \vec{v}$  are coplanar    (c)  $\vec{\lambda} + \vec{v} = 2\vec{u}$     (d) none of these

QNo125: If  $\vec{a} = \vec{i} + \vec{j}, \vec{b} = 2\vec{j} - \vec{k}$  and  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}, \vec{r} \times \vec{b} = \vec{a} \times \vec{b}$ , then  $\frac{\vec{r}}{|\vec{r}|}$  is equal to

- (a)  $\frac{1}{\sqrt{11}}(\vec{i} + 3\vec{j} - \vec{k})$  (b)  $\frac{1}{\sqrt{11}}(\vec{i} - 3\vec{j} + \vec{k})$  (c)  $\frac{1}{\sqrt{3}}(\vec{i} - \vec{j} + \vec{k})$  (d) none of these

QNo126: If  $\vec{a}, \vec{b}, \vec{c}$  are three vectors such that  $(\vec{a} + \vec{b}) \cdot \vec{c} = (\vec{a} - \vec{b}) \cdot \vec{c} = 0$ , then  $(\vec{a} \times \vec{b}) \times \vec{c}$  is :

- (a)  $\vec{0}$  (b)  $\vec{a}$  (c)  $\vec{b}$  (d) none of these

QNo127: If  $\vec{a}, \vec{b}, \vec{c}$  are three non-coplanar non-zero vectors, then  $(\vec{a} \cdot \vec{a})\vec{b} \times \vec{c} + (\vec{a} \cdot \vec{b})\vec{c} \times \vec{a} + (\vec{a} \cdot \vec{c})\vec{a} \times \vec{b}$  is equal to :

- (a)  $[\vec{b} \vec{c} \vec{a}]\vec{a}$  (b)  $[\vec{c} \vec{a} \vec{b}]\vec{b}$  (c)  $[\vec{a} \vec{b} \vec{c}]\vec{c}$  (d) none of these

QNo128: The three concurrent edges of a parallelepiped represents the vectors  $\vec{a}, \vec{b}, \vec{c}$  such that  $[\vec{a} \vec{b} \vec{c}] = \lambda$

Then the volume of the parallelepiped whose three concurrent edges are the three concurrent diagonals of three faces of the given parallelepiped is :

- (a)  $2\lambda$  (b)  $3\lambda$  (c)  $\lambda$  (d) none of these

QNo129: If  $\vec{a}, \vec{b}, \vec{c}$  are three non-coplanar non-zero vectors and  $\vec{r}$  is any vector in space, then

$(\vec{a} \times \vec{b}) \times (\vec{r} \times \vec{c}) + (\vec{b} \times \vec{c}) \times (\vec{r} \times \vec{a}) + (\vec{c} \times \vec{a}) \times (\vec{r} \times \vec{b})$  is equal to :

- (a)  $2[\vec{a} \vec{b} \vec{c}]\vec{r}$  (b)  $3[\vec{a} \vec{b} \vec{c}]\vec{r}$  (c)  $[\vec{a} \vec{b} \vec{c}]\vec{r}$  (d) none of these

QNo130:  $\vec{AB} = \vec{b}$  and  $\vec{AC} = \vec{c}$ , then the length of the perpendicular from A to the line BC is :

- (a)  $\frac{|\vec{b} \times \vec{c}|}{|\vec{b} + \vec{c}|}$  (b)  $\frac{|\vec{b} \times \vec{c}|}{|\vec{b} - \vec{c}|}$  (c)  $\frac{1}{2} \frac{|\vec{b} \times \vec{c}|}{|\vec{b} - \vec{c}|}$  (d) none of these

QNo131: The projection of the vector  $\vec{i} + \vec{j} + \vec{k}$  on the line whose vector equation is  $\vec{r} = (3+t)\vec{i} + (2t-1)\vec{j} + 3t\vec{k}, t$  being a scalar, is :

- (a)  $\frac{1}{\sqrt{14}}$  (b) 6 (c)  $\frac{6}{\sqrt{14}}$  (d) none of these

QNo132: A vector  $\vec{r}$  satisfies the equations  $\vec{r} \times \vec{a} = \vec{b}$  and  $\vec{r} \cdot \vec{a} = 0$ . Then

- (a)  $\vec{r} = \frac{\vec{a} \times \vec{b}}{\vec{a} \cdot \vec{b}}$  (b)  $\vec{r} = \frac{\vec{a} \times \vec{b}}{\vec{a} \cdot \vec{a}}$  (c)  $\vec{r} = \frac{\vec{a} \times \vec{b}}{\vec{b} \cdot \vec{b}}$  (d) none of these

QNo133: If the vectors  $\vec{a}, \vec{b}, \vec{c}$  are non-coplanar and l, m, n are distinct scalars, then

$[l\vec{a} + m\vec{b} + n\vec{c}, i\vec{b} + m\vec{c} + n\vec{a}, i\vec{c} + m\vec{a} + n\vec{b}] = 0$

- (a)  $lm + nm + nl = 0$  (b)  $l + m + n = 0$  (c)  $l^2 + m^2 + n^2 = 0$  (d)  $l^3 + m^3 + n^3 = 0$

QNo134: The vector  $\vec{x}$  is perpendicular to the vectors  $\vec{a} = 2\vec{i} + 3\vec{j} - \vec{k}$  and  $\vec{b} = \vec{i} - 2\vec{j} + 3\vec{k}$ . If  $\vec{x} \cdot (2\vec{i} - \vec{j} + \vec{k}) = -6$ , then  $\vec{x} =$

- (a)  $-3\vec{i} + 3\vec{j} + 3\vec{k}$  (b)  $3\vec{i} - 3\vec{j} + 3\vec{k}$  (c)  $3\vec{i} + 3\vec{j} - 3\vec{k}$  (d) none of these

QNo135: If  $\vec{d}$  is a unit vector such that  $\vec{d} = \lambda\vec{b} \times \vec{c} + \mu\vec{c} \times \vec{a} + \nu\vec{a} \times \vec{b}$ , then

$|(\vec{d} \cdot \vec{a})(\vec{b} \times \vec{c}) + (\vec{d} \cdot \vec{b})(\vec{c} \times \vec{a}) + (\vec{d} \cdot \vec{c})(\vec{a} \times \vec{b})|$  is equal to :

- (a)  $|[\vec{a} \vec{b} \vec{c}]|$  (b) 1 (c)  $3|[\vec{a} \vec{b} \vec{c}]|$  (d) none of these

- QNo136: If  $\vec{a}, \vec{b}$  and  $\vec{c}$  be three non-zero and non-coplanar vectors and  $\vec{p}, \vec{q}$  and  $\vec{r}$  be three vectors given by  $\vec{p} = \vec{a} + \vec{b} - 2\vec{c}$ ,  $\vec{q} = 3\vec{a} - 2\vec{b} + \vec{c}$  and  $\vec{r} = \vec{a} - 4\vec{b} + 2\vec{c}$ . If the volume of the parallelepiped determined by  $\vec{a}, \vec{b}$  and  $\vec{c}$  is  $V_1$  and that of the parallelepiped determined by  $\vec{p}, \vec{q}$  and  $\vec{r}$  is  $V_2$  then  $V_2 : V_1$  is :  
 (a) 1 : 15 (b) 15 : 1 (c) 4 : 5 (d) 5 : 4
- QNo137: If  $\vec{a}, \vec{b}, \vec{c}$  are three vectors of which every pair is non-collinear. If the vector  $\vec{a} + \vec{b}$  and  $\vec{b} + \vec{c}$  are collinear with  $\vec{c}$  and  $\vec{a}$  respectively, then  $\vec{a} + \vec{b} + \vec{c}$  is :  
 (a) a unit vector (b) the null vector (c) equally inclined to  $\vec{a}, \vec{b}, \vec{c}$  (d) none of these
- QNo138: If  $\vec{r} = 3\vec{i} + 2\vec{j} - 5\vec{k}$ ,  $\vec{a} = 2\vec{i} - \vec{j} + \vec{k}$ ,  $\vec{b} = \vec{i} + 3\vec{j} - 2\vec{k}$  and  $\vec{c} = -2\vec{i} + \vec{j} - 3\vec{k}$  such that  $\vec{r} = \lambda\vec{a} + \mu\vec{b} + \nu\vec{c}$ , then  
 (a)  $\mu, \frac{\lambda}{2}, \nu$  are in A.P. (b)  $\lambda, \mu, \nu$  are in A.P. (c)  $\lambda, \mu, \nu$  are in H.P. (d)  $\mu, \lambda, \nu$  are in G.P.
- QNo139: If  $\vec{a}$  is perpendicular to  $\vec{b}$  and  $\vec{p}$  is a non-zero vector such that  $\vec{p} \cdot \vec{r} + (\vec{r} \cdot \vec{b})\vec{a} = \vec{c}$ , then  $\vec{r} =$   
 (a)  $\frac{\vec{c}}{p} - \frac{(\vec{b} \cdot \vec{c})\vec{a}}{p^2}$  (b)  $\frac{\vec{a}}{p} - \frac{(\vec{c} \cdot \vec{a})\vec{b}}{p^2}$  (c)  $\frac{\vec{b}}{p} - \frac{(\vec{a} \cdot \vec{b})\vec{c}}{p^2}$  (d)  $\frac{\vec{c}}{p^2} - \frac{(\vec{b} \cdot \vec{c})\vec{a}}{p}$
- QNo140: A particle is acted upon by the force  $\vec{F}_1 = 3\vec{i} + 2\vec{j} + 5\vec{k}$  and  $\vec{F}_2 = 2\vec{i} + \vec{j} - 3\vec{k}$  and is displaced from the point P ( $2\vec{i} - \vec{j} - 3\vec{k}$ ) to the point Q ( $4\vec{i} - 3\vec{j} + 7\vec{k}$ ). The work done by the force is :  
 (a) 17 units (b) 24 units (c) 32 units (d) none of these
- QNo141: Vector moment of the force  $\vec{F} = 3\vec{i} + 2\vec{j} - 4\vec{k}$  acting at the point (1, -1, 2) about the point (2, -1, 3) is :  
 (a)  $2\vec{i} - 7\vec{j} - 2\vec{k}$  (b)  $-2\vec{i} - \vec{j} + 2\vec{k}$  (c)  $2\vec{i} + 7\vec{j} - 2\vec{k}$  (d)  $-2\vec{i} - 7\vec{j} + 2\vec{k}$
- QNo142: Angle between vectors  $\vec{i} - \vec{j} + \vec{k}$  and  $\vec{i} + 2\vec{j} + \vec{k}$  is :  
 (a)  $\cos^{-1} \frac{1}{\sqrt{15}}$  (b)  $\cos^{-1} \frac{4}{\sqrt{15}}$  (c)  $\cos^{-1} \frac{4}{15}$  (d)  $\frac{\pi}{2}$
- QNo143: The area of the parallelogram of which  $\vec{i}$  and  $\vec{i} + \vec{j}$  are adjacent is :  
 (a) 2 (b)  $\frac{1}{2}$  (c) 1 (d)  $\sqrt{2}$
- QNo144: The unit vector perpendicular to vectors  $\vec{i} - \vec{j}$  and  $\vec{i} + \vec{j}$  forming a right handed system is :  
 (a)  $\vec{k}$  (b)  $-\vec{k}$  (c)  $\frac{1}{\sqrt{2}}(\vec{i} - \vec{j})$  (d)  $\frac{1}{2}(\vec{i} + \vec{j})$
- QNo145: Value of a for which  $2\vec{i} - \vec{j} + \vec{k}, \vec{i} + 2\vec{j} - 3\vec{k}$  and  $3\vec{i} + a\vec{j} + 5\vec{k}$  are coplanar is :  
 (a) 2 (b) 4 (c) -4 (d) 3
- QNo146: If  $\vec{a}, \vec{b}, \vec{c}, \vec{d}$  are the vertices of a square, then  
 (a)  $(\vec{b} - \vec{a}) = (\vec{c} - \vec{b})$  (b)  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$  (c)  $(\vec{c} - \vec{a}) \cdot (\vec{d} - \vec{b}) = 0$  (d) none of these
- QNo147: The vectors  $2\vec{i} + 3\vec{j}, 5\vec{i} + 6\vec{j}$  and  $8\vec{i} + \lambda\vec{j}$  have their initial points at (1, 1). The value of  $\lambda$  so that the vectors terminate on one straight line is :  
 (a) 0 (b) 3 (c) 6 (d) 9

QNo148: If  $|\vec{a}| = \sqrt{5}$  and  $|\vec{b}| = \sqrt{6}$ , then  $[(\vec{a} \times \vec{b}) \times \vec{b}] \times \vec{b}$  is

- (a)  $6(\vec{b} \times \vec{a})$                       (b)  $6(\vec{a} \times \vec{b})$                       (c)  $5(\vec{a} \times \vec{b})$                       (d)  $5(\vec{b} \times \vec{a})$

QNo149: If  $\vec{a} + \vec{b}$  is orthogonal to  $\vec{b}$  and  $\vec{a} + 2\vec{b}$  is orthogonal to  $\vec{a}$ , then

- (a)  $|\vec{a}| = \sqrt{2}|\vec{b}|$                       (b)  $|\vec{a}| = 2|\vec{b}|$                       (c)  $|\vec{a}| = |\vec{b}|$                       (d)  $|\vec{b}| = 2|\vec{a}|$

QNo150: If  $4\vec{i} + 7\vec{j} + 8\vec{k}$ ,  $2\vec{i} + 3\vec{j} + 4\vec{k}$  and  $2\vec{i} + 5\vec{j} + 7\vec{k}$  are the position vectors of the vertices A, B and C respectively of triangle ABC. The position vector of the point where the bisector of angle A meets

- (a)  $\frac{2}{3}(-6\vec{i} - 8\vec{j} - 6\vec{k})$                       (b)  $\frac{2}{3}(6\vec{i} + 8\vec{j} + 6\vec{k})$                       (c)  $\frac{1}{3}(6\vec{i} + 13\vec{j} + 18\vec{k})$                       (d)  $\frac{1}{3}(5\vec{j} + 12\vec{k})$

ANSWERS:

1	A	11	21	31	41	51	61	71	81	91	101	111	121	131	141
		C	D	C	D	C	C	B	D	A	A	B	D	C	A
2	B	12	22	32	42	52	62	72	82	92	102	112	122	132	142
		B	B	A	C	C	B	B	C	C	A	A	B	B	D
3	C	13	23	33	43	53	63	73	83	93	102	113	123	133	143
		C	C	D	D	A	B	B	D	A	B	C	B	B	C
4	C	14	24	34	44	54	64	74	84	94	104	114	124	134	144
		B	D	A	D	D	A	C	D	C	C	A	B	A	A
5	C	15	25	35	45	55	65	75	85	95	105	115	125	135	145
		A	C	C	D	A	A	B	B	B	D	A	A	A	C
6	A	16	26	36	46	56	66	76	86	96	106	116	126	136	146
		C	D	C	C	C	B	C	A	B	D	D	A	B	C
7	B	17	27	37	47	57	67	77	87	97	107	117	127	137	147
		A	D	C	A	A	B	D	A	C	C	B	A	B	D
8	C	18	28	38	48	58	68	78	88	98	108	118	128	138	148
		B	B	A	C	B	A	D	A	B	B	C	A	A	A
9	A	19	29	39	49	59	69	79	89	99	109	119	129	139	149
		D	D	B	C	B	B	C	B	A	A	B	A	A	A
10		20	30	40	50	60	70	80	90	100	110	120	130	140	150
	B	A	B	C	A	B	B	A	A	A	A	A	B	B	C

