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**2008 SRM UNIVERSITY**  
**B.TECH II SEMESTER DEGREE EXAMINATIONS**  
**NUMERICAL METHODS**

**DECEMBER 2008**

**TIME:3 HOUR**  
**MARK:100**

**ANSWER ALL QUESTIONS**

**PART-A(10\*2=20 MARKS)**

- 1.State principle of least squares.
- 2.Write down Newton Raphson formula.
- 3.Define the operators :(i)d (ii) $\mu$ .
- 4.Give the Newton's divided difference interpolation formula..
- 5.Write the numerical integration formula using trapezoidal method.
- 6.Evaluate  $\int_0^1 e^x dx$ , using simpson's 1/3rd rule.  
 $e^0 = 1, e^1 = 2.72, e^2 = 7.39, e^3 = 20.09, e^4 = 54.6$ .
- 7.State Taylor's algorithm for the first order differential equation.
- 8.How many prior values are required to predict the next value in milne's method?
- 9.Classify the PDE  $xU_{xx} + yY_{yy} = 0, x > 0, y > 0$ .
- 10.Write the crank-nicholson difference scheme to solve  $U_{xx} = aU_t$  with  $u(0,t) = t, u(1,t) = t^2, u(x,0) = f(x)$ .

**PART-B(5\*16 = 80MARKS)**

- 11.a.Fit a parabola to the following data:  
x 1 2 3 4 5  
y 2 3 5 8 10  
(OR)  
b.Solve by Gauss jacobi method  
 $12x + 4y - z = 32$   
 $x + 3y + 10z = 24$   
 $2x + 17y + 4z = 35$
- 12.a. Apply Newton's backward difference formula to the data below to obtain a polynomial of degree 4.  
x 1 2 3 4 5  
y 1 -1 1 -1 1  
(OR)  
b. Use Lagrange's formula to find x when y = 85 from the following:  
x 2 5 8 14  
y 94.8 87.9 81.3 68.7
- 13.a.Find  $f'(x)$  and  $f''(x)$  at  $x = 1.1$ . Given  
x 1 1.1 1.2 1.3 1.4 1.5 1.6  
y 7.9 8.4 8.7 9.1 9.4 9.7 10.1  
(OR)

b. Evaluate  $\int dx/(1+x^2)$  using (i) Simpson's 1/3 rule (ii) Simpson's 3/8 rule and compare the result with the exact integration.

14. a. Solve the equation  $dy/dx = 1 - y$  with  $x=0, y=0$  using modified Euler method. Find  $y(0.1)$ ,  $y(0.2)$ .

(OR)

b. Using Milne's predictor and corrector formula, find  $y(4.4)$  given  $5xy' + y^2 = 2, y(4) = 1, y(4.1) = 1.0049, y(4.2) = 1.0097$  and  $y(4.3) = 1.0143$ .

15. a. Solve  $U_{xx} + U_{yy} = 0$  over the square mesh of side 4 units, satisfying the following boundary conditions.

(i)  $u(0, y) = 0$  for  $0 \leq y \leq 4$

(ii)  $u(4, y) = 12 + y$  for  $0 \leq y \leq 4$

(iii)  $u(x, 0) = 3x$  for  $0 \leq x \leq 4$

(iv)  $u(x, 4) = x^2$  for  $0 \leq x \leq 4$

(OR)

b. Solve the equation  $U_t = U_{xx}$  subject to the conditions  $u(x, 0) = \sin px, 0 \leq x \leq 1, u(0, t) = u(1, t) = 0$  using Crank-Nicholson method

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