

CCE RR

ಕರ್ನಾಟಕ ಪ್ರೌಢ ಶಿಕ್ಷಣ ಪರೀಕ್ಷಾ ಮಂಡಳಿ, ಮಲ್ಲೇಶ್ವರಂ, ಬೆಂಗಳೂರು – 560 003

**KARNATAKA SECONDARY EDUCATION EXAMINATION BOARD, MALLESWARAM,
BANGALORE – 560 003**

ಎಸ್.ಎಸ್.ಎಲ್.ಸಿ. ಪರೀಕ್ಷೆ, ಜೂನ್ — 2015

S. S. L. C. EXAMINATION, JUNE, 2015

ಮಾದರಿ ಉತ್ತರಗಳು
MODEL ANSWERS

ದಿನಾಂಕ : 15. 06. 2015]

ಸಂಕೇತ ಸಂಖ್ಯೆ : **81-E**

Date : 15. 06. 2015]

CODE No. : **81-E**

ವಿಷಯ : ಗಣಿತ

Subject : MATHEMATICS

(ಹೊಸ ಪಠ್ಯಕ್ರಮ / New Syllabus)

(ಪುನರಾವರ್ತಿತ ಶಾಲಾ ಅಭ್ಯರ್ಥಿ / Regular Repeater)

(ಇಂಗ್ಲಿಷ್ ಭಾಷಾಂತರ / English Version)

[ಪರಮಾವಧಿ ಅಂಕಗಳು : 80

[Max. Marks : 80

Qn. Nos.	Ans. Key	Value Points	Marks allotted
I. 1.	B	$72 = (28 \times 2) + 16$	1
2.	B	10	1
3.	C	1	1
4.	C	Mutually exclusive event	1
5.	D	2.56.	1
6.	D	12	1
7.	A	4 cm	1
8.	A	10 m	1



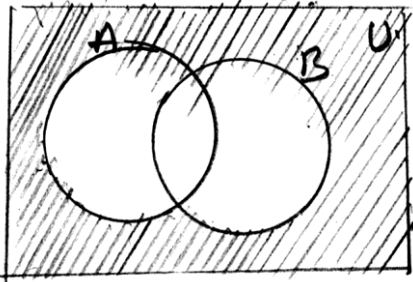
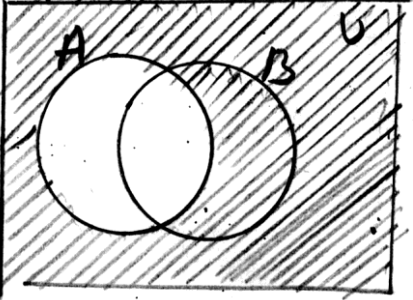
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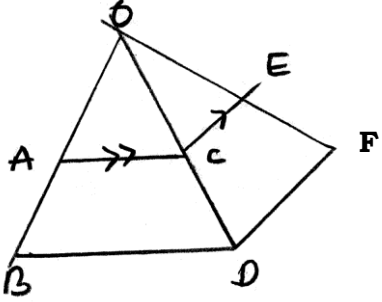
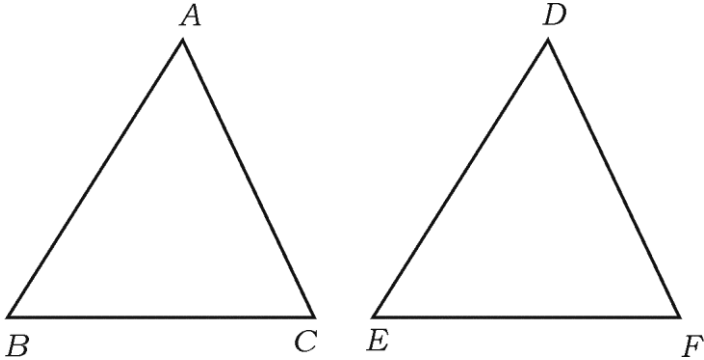
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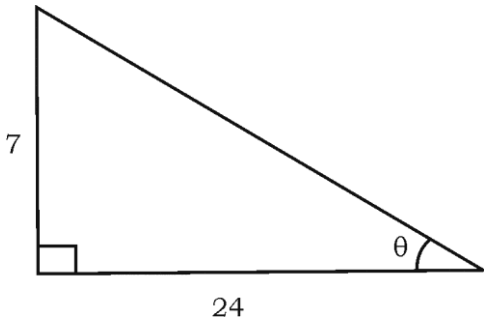
Qn. Nos.	Value Points	Marks allotted
II.		
9.	$T_n = 2n^2 + 5$ $T_3 = 2(3)^2 + 5 \quad \left. \vphantom{T_3} \right\}$ $= 2(9) + 5 \quad \left. \vphantom{T_3} \right\}$ $= 18 + 5 \quad \left. \vphantom{T_3} \right\}$ $= 23. \quad \left. \vphantom{T_3} \right\}$	 $\frac{1}{2}$ $\frac{1}{2}$ 1
10.	Degree of the polynomial is 3.	1
11.	$(\sqrt{5} + \sqrt{2})(\sqrt{5} - \sqrt{2})$ $= (\sqrt{5})^2 - (\sqrt{2})^2$ $= 5 - 2 = 3$	$\frac{1}{2}$ $\frac{1}{2}$ 1
12.	<p>PQOR is a square</p> <p>\therefore Radius = 8 cm</p>	$\frac{1}{2}$ $\frac{1}{2}$ 1
13.	$b^2 - 4ac$ <p>OR</p> $\Delta = b^2 - 4ac.$	1
14.	<p>T.S.A. = $2\pi r(r + h)$ Square units</p> <p>OR</p> <p>T.S.A. = $(2\pi r^2 + 2\pi rh)$ Square units</p>	1
III. 15.	<p>If possible, let us suppose</p> <p>$3 + \sqrt{5}$ be a rational number</p> <p>$\Rightarrow 3 + \sqrt{5} = \frac{p}{q}$, where $p, q \in \mathbb{Z}$, $q \neq 0$</p> <p>$\Rightarrow \sqrt{5} = \frac{p}{q} - 3$</p> <p>$\sqrt{5} = \frac{p - 3q}{q}$ which is rational</p> <p>This leads to a contradiction because $\sqrt{5}$ is irrational</p> <p>$\therefore 3 + \sqrt{5}$ is an irrational number.</p>	$\frac{1}{2}$ $\frac{1}{2}$ 2



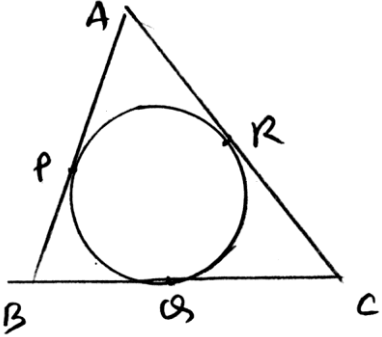
Qn. Nos.	Value Points	Marks allotted
16.	<p>(i) </p> <p style="text-align: center;">$(A \cup B)'$</p> <p>(ii) </p> <p style="text-align: center;">$A' \cap B$</p>	<p>Diagram $\frac{1}{2}$</p> <p>Shading $\frac{1}{2}$</p> <p>Diagram $\frac{1}{2}$</p> <p>Shading $\frac{1}{2}$</p> <p style="text-align: right;">2</p>
17.	<p>$T_n = \frac{1}{a + (n-1)d}$</p> <p>Common difference $(d) = \frac{T_{11} - T_5}{11 - 5} \quad \frac{1}{2}$</p> <p style="text-align: center;">$d = \frac{15 - 12}{6}$</p> <p style="text-align: center;">$d = \frac{3}{6} \quad \frac{1}{2}$</p> <p style="text-align: center;">$d = \frac{1}{2}$</p> <p>$T_5 = \frac{1}{12} \quad \frac{1}{2}$</p> <p>$a + 4d = 12$</p> <p>$a + 4 \times \left(\frac{1}{2}\right) = 12$</p> <p>$a = 12 - 2$</p> <p>$a = 10$</p> <p>$T_1 = \frac{1}{a} = \frac{1}{10} \quad \frac{1}{2}$</p>	<p style="text-align: right;">2</p>



Qn. Nos.	Value Points	Marks allotted
23.	 <p>In $\triangle OBD$</p> $AC \parallel BD$ $\therefore \frac{OA}{AB} = \frac{OC}{CD}$ $\frac{12}{9} = \frac{8}{CD}$ $\frac{4}{3} = \frac{8}{CD} \quad CD = 6 \text{ cm}$ <p>In $\triangle ODF$, $CE \parallel DF$</p> $\therefore \frac{OC}{CD} = \frac{OE}{EF}$ $\frac{8}{6} = \frac{OE}{4.5}$ $\frac{4}{3} = \frac{OE}{4.5} \quad \frac{4 \times 4.5}{3} = OE$ $\therefore OE = 4 \times 1.5 = 6 \text{ cm}$ <p>OR</p>  <p>Data : $\triangle ABC \parallel \triangle DEF$</p> <p>To prove : $\triangle ABC \cong \triangle DEF$</p> <p>Proof : $\frac{\text{Area of triangle } ABC}{\text{Area of triangle } DEF} = \frac{AB^2}{DE^2} = \frac{BC^2}{EF^2} = \frac{CA^2}{DF^2}$</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p> <p>$\frac{1}{2} + \frac{1}{2}$</p> <p>$\frac{1}{2}$</p>

Qn. Nos.	Value Points	Marks allotted
24.	$1 = \frac{AB^2}{DE^2}$ $AB^2 = DE^2$ $AB = DE$ $BC^2 = EF^2$ $BC = EF$ $CA^2 = DF^2$ $CA = DF.$  $24 \tan \theta = 7$ $\tan \theta = \frac{7}{24} = \frac{\text{Opp}}{\text{Adj}}$ $\text{Hyp} = \sqrt{7^2 + 24^2}$ $= \sqrt{49 + 576}$ $= \sqrt{625}$ $= 25$ $\therefore \text{(i) } \sin \theta = \frac{\text{Opp}}{\text{Hyp}} = \frac{7}{25}$ $\text{(ii) } \cos \theta = \frac{\text{Adj}}{\text{Hyp}} = \frac{24}{25}$	<p style="text-align: right;">1/2 2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2 2</p>
25.	<p>Let $m = \text{Slope of the line} = \tan \theta$</p> $= \tan 60^\circ$ $= \sqrt{3}$ <p>Equation of a line $y = mx + c$</p> $y = \sqrt{3} \cdot x + 2$ $y = \sqrt{3}x + 2.$	<p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2 2</p>



Qn. Nos.	Value Points	Marks allotted
26.	<p> $(3, 1)$ $(0, x)$ $x_1 \ y_1$ $x_2 \ y_2$ </p> <p>By distance formula</p> $\text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $5 = \sqrt{(0 - 3)^2 + (x - 1)^2}$ $5 = \sqrt{9 + (x - 1)^2}$ $25 = 9 + (x - 1)^2$ $16 = (x - 1)^2$ $x - 1 = 4 \quad \therefore x = 5.$	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p>
27.	 <p>Given $AB = AC$</p> $AP + BP = AR + RC$ $AP + BQ = AP + QC. \quad [\because BP = BQ, AR = AP]$ $BQ = QC$ <p>\therefore Q is the mid-point of BC.</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p>
28.	<p>Let $r_1 = 15$ cm, $r_2 = 8$ cm and $h = 63$ cm.</p> <p>Volume of the dustbin (frustum)</p> $= \frac{1}{3} \pi h (r_1^2 + r_2^2 + r_1 r_2)$ $= \frac{1}{3} \times \frac{22}{7} \times 63 (15^2 + 8^2 + 120)$ $= 66 (225 + 64 + 120)$ $= 26,994 \text{ cubic cm}$	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p>

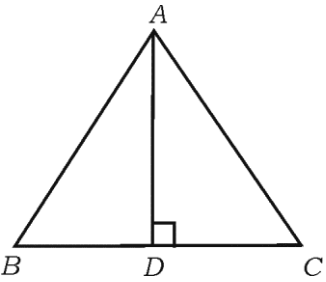


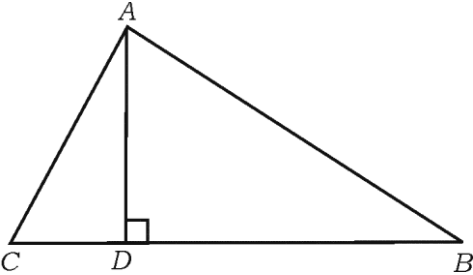
Qn. Nos.	Value Points	Marks allotted
IV. 31.	$\frac{{}^nC_r}{{}^{(n-1)}C_{r-1}} = \frac{\frac{ n }{ n-r \cdot r }}{\frac{ n-1 }{ (n-1)-(r-1) \cdot r-1 }}$ $= \frac{ n }{ n-r \cdot r } \times \frac{ (n-1)-(r-1) \cdot r-1 }{ n-1 }$ $= \frac{ n }{ n-r \cdot r } \times \frac{ n-1-r+1 \cdot r-1 }{ n-1 }$ $= \frac{ n }{ n-r \cdot r } \times \frac{ n-r \cdot r-1 }{ n-1 }$ $= \frac{n n-1 }{ n-r \cdot r \cdot r-1 } \times \frac{ n-r \cdot r-1 }{ n-1 }$ $= \frac{n}{r}.$	<p>1</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>3</p>
	OR	
	Diagonals of a polygon of n sides = $\frac{n(n-3)}{2}$	1/2
	$44 = \frac{n(n-3)}{2}$	1/2
	$88 = n^2 - 3n$ $n^2 - 3n - 88 = 0$ $n^2 - 11n + 8n - 88 = 0$	1
	$n(n-11) + 8(n-11) = 0$	
	$n = 11 \quad n = -8$	1/2
	$\therefore n = 11$ Number of sides = 11.	1/2



Qn. Nos.	Value Points						Marks allotted
32.	$A = 25$						
	<i>C.I.</i>	<i>f</i>	<i>Mid-point x</i>	$d = x - A$	d^2	fd	fd^2
	0 – 10	7	5	– 20	400	– 140	2800
	10 – 20	10	15	– 10	100	– 100	1000
	20 – 30	15	25	0	0	0	0
	30 – 40	8	35	+ 10	100	80	800
	40 – 50	10	45	+ 20	400	200	4000
	$N = 50$			$\Sigma fd = 40$			$\Sigma fd^2 = 8600$
							$1\frac{1}{2}$
	Standard deviation $\sigma = \sqrt{\frac{\Sigma fd^2}{N} - \left(\frac{\Sigma fd}{N}\right)^2}$						$\frac{1}{2}$
	$= \sqrt{\frac{8600}{50} - \left(\frac{40}{50}\right)^2}$						$\frac{1}{2}$
	$= \sqrt{172 - 0.64}$						
	$= \sqrt{171.36}$						
	$= 13.1.$						$\frac{1}{2}$
							3
33.	$P(x) = ax^3 + 3x^2 - 13$						
	Put $x = 3$						
	$P(3) = a(3)^3 + 3(3)^2 - 13$						
	$= 27a + 27 - 13$						
	$= 27a + 14$ (i)						1
	$g(x) = 2x^3 - 4x + a$						
	Put $x = 3$						
	$g(3) = 2(3)^3 - 4(3) + a$						
	$= 54 - 12 + a$						1
	$= 42 + a.$ (ii)						



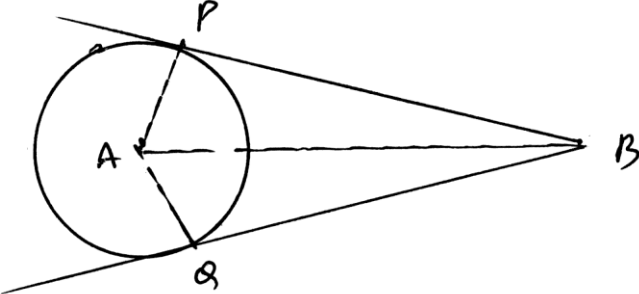
Qn. Nos.	Value Points	Marks allotted																					
	<p>Remainders of $P(x)$ and $g(x)$ are same</p> <p>$\therefore 27a + 14 = 42 + a$ from (i) and (ii)</p> $26a = 28 \quad \frac{1}{2}$ $a = \frac{28}{26}$ $a = \frac{14}{13} \quad \frac{1}{2}$ <p style="text-align: center;">OR</p> <p>Put $x = -4$</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding-right: 10px;">-4</td> <td style="border-right: 1px solid black; padding: 0 10px;">1</td> <td style="padding: 0 10px;">10</td> <td style="padding: 0 10px;">35</td> <td style="padding: 0 10px;">50</td> <td style="padding: 0 10px;">29</td> <td></td> </tr> <tr> <td></td> <td style="border-right: 1px solid black; padding: 0 10px;">0</td> <td style="padding: 0 10px;">-4</td> <td style="padding: 0 10px;">-24</td> <td style="padding: 0 10px;">-44</td> <td style="padding: 0 10px;">-24</td> <td style="text-align: right;">1½</td> </tr> <tr> <td></td> <td style="border-right: 1px solid black; padding: 0 10px;">1</td> <td style="padding: 0 10px;">6</td> <td style="padding: 0 10px;">11</td> <td style="padding: 0 10px;">6</td> <td style="padding: 0 10px;">5</td> <td></td> </tr> </table> <p>\therefore Quotient = $x^3 + 6x^2 + 11x + 6$</p> <p>Given :</p> $x^3 + 6x^2 + 11x + 6 = x^3 - ax^2 + bx + 6$ <p>$\therefore -a = 6 \quad b = 11 \quad \frac{1}{2} + \frac{1}{2}$</p> $a = -6 \quad \frac{1}{2}$ <p>Remainder = 5.</p>	-4	1	10	35	50	29			0	-4	-24	-44	-24	1½		1	6	11	6	5		3
-4	1	10	35	50	29																		
	0	-4	-24	-44	-24	1½																	
	1	6	11	6	5																		
34.	 <p style="text-align: right;">Figure — ½</p> <p>In $\triangle ADB$</p> $AB^2 = AD^2 + BD^2 \quad \dots (i)$ <p>In $\triangle ADC$</p> $AC^2 = AD^2 + CD^2 \quad \dots (ii) \quad \frac{1}{2}$ <p>Subtract (ii) from (i)</p> $AB^2 - AC^2 = BD^2 - CD^2 \quad \frac{1}{2}$ $AB^2 + CD^2 = BD^2 + AC^2$	3																					

Qn. Nos.	Value Points	Marks allotted
	$AB^2 + CD^2 = \left(\frac{1}{2} BC\right)^2 + AC^2 \quad \because BD = \frac{1}{2} BC$	1/2
	$AB^2 + CD^2 = \frac{BC^2}{4} + AC^2$	1/2
	$AB^2 + CD^2 = \frac{AC^2}{4} + AC^2 \quad [\because BC = AC]$	
	$= \frac{5AC^2}{4}$	1/2
	OR	
		
	Figure — 1/2	
	$BC = CD + BD$	
	$BC = CD + 3CD$	
	$BC = 4CD$	
	$CD = \frac{BC}{4}$	1/2
	In $\triangle ABD$,	
	$AB^2 = AD^2 + BD^2 \quad \dots (i)$	
	In $\triangle ACD$,	
	$AC^2 = AD^2 + CD^2 \quad \dots (ii)$	1/2
	Subtract (ii) from (i)	
	$AB^2 - AC^2 = BD^2 - CD^2$	
	$AB^2 - AC^2 = (3CD)^2 - CD^2 \quad \left[\because \frac{BD}{CD} = \frac{3}{1} \right]$	1/2
	$= 9CD^2 - CD^2$	
	$= 8CD^2$	
	$= 8 \left(\frac{BC}{4}\right)^2$	



Qn. Nos.	Value Points	Marks allotted
	$AB^2 - AC^2 = 8 \left(\frac{BC^2}{16} \right)$ $AB^2 - AC^2 = \frac{BC^2}{2}$ $\therefore 2 (AB^2 - AC^2) = BC^2$	$\frac{1}{2}$ $\frac{1}{2}$ 3
35.	LHS : $(\sin \theta + \operatorname{cosec} \theta)^2 + (\cos \theta + \sec \theta)^2$ $= \sin^2 \theta + \operatorname{cosec}^2 \theta + 2 \sin \theta \cdot \operatorname{cosec} \theta + \cos^2 \theta + \sec^2 \theta + 2 \cos \theta \cdot \sec \theta$ $= \sin^2 \theta + \operatorname{cosec}^2 \theta + 2 (1) + \cos^2 \theta + \sec^2 \theta + 2 (1)$ $= \sin^2 \theta + \cos^2 \theta + \operatorname{cosec}^2 \theta + \sec^2 \theta + 4$ $= 1 + \operatorname{cosec}^2 \theta + \sec^2 \theta + 4$ $= 5 + 1 + \cot^2 \theta + 1 + \tan^2 \theta$ $= 7 + \tan^2 \theta + \cot^2 \theta = \text{RHS.}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ 3
	OR $\text{LHS} = \sqrt{\frac{1 + \cos \theta}{1 - \cos \theta}}$ $= \sqrt{\frac{1 + \cos \theta}{1 - \cos \theta} \times \frac{1 + \cos \theta}{1 + \cos \theta}}$ $= \sqrt{\frac{(1 + \cos \theta)^2}{1 - \cos^2 \theta}}$ $= \sqrt{\frac{(1 + \cos \theta)^2}{1 - \cos^2 \theta}}$ $= \frac{1 + \cos \theta}{\sin \theta}$ $= \frac{1}{\sin \theta} + \frac{\cos \theta}{\sin \theta}$ $= \operatorname{cosec} \theta + \cot \theta = \text{RHS.}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ 3



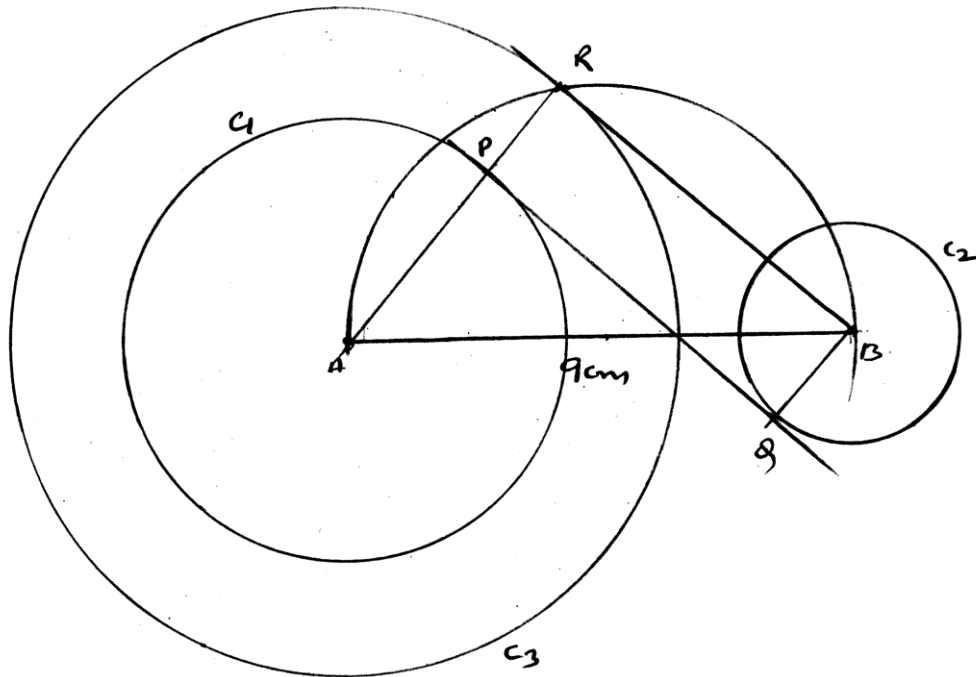
Qn. Nos.	Value Points	Marks allotted
36.	<div style="text-align: center;">  </div> <p style="text-align: right;">Figure — $\frac{1}{2}$</p> <p><i>Data :</i> A is the centre of the circle B is the external point BP and BQ are the tangents. $\frac{1}{2}$</p> <p><i>To prove :</i> $BP = BQ$</p> <p><i>Construction :</i> AP, AQ and AB are joined. $\frac{1}{2}$</p> <p><i>Proof :</i> In $\triangle APB$ and $\triangle AQB$ $\frac{1}{2}$ $AP = AQ$ (radii of the same circle) (radius drawn at the point of contact of the tangent) $\angle APB = \angle AQB = 90^\circ$ $\frac{1}{2}$ $AB = AB$ $\therefore \triangle APB \cong \triangle AQB$ [RHS theorem] $\frac{1}{2}$ $\therefore BP = BQ.$</p>	3
V. 37.	<p>Let the terms be $\frac{a}{r}$, a, ar $\frac{1}{2}$</p> <p>Given : Product = 216</p> $\frac{a}{r} \cdot a \cdot ar = 216$ $\frac{1}{2}$ $a^3 = 216$ $a = 6.$ $\frac{1}{2}$ <p>And</p> $\left(\frac{a}{r} \times a \right) + (a \times ar) + \left(\frac{a}{r} \times ar \right) = 156$ $\frac{1}{2}$ $\frac{a^2}{r} + a^2r + a^2 = 156$ $\frac{36}{r} + 36r + 36 = 156$ $\frac{36}{r} + 36r = 156 - 36$ $\frac{1}{2}$	

Qn. Nos.	Value Points	Marks allotted
	$\frac{36 + 36r^2}{r} = 120$ $36r^2 + 36 = 120r$ $36r^2 - 120r + 36 = 0$ $3r^2 - 10r + 3 = 0$ $3r^2 - 9r - 1r + 3 = 0$ $3r(r - 3) - 1(r - 3) = 0$ $(r - 3)(3r - 1) = 0$ $r = 3 \text{ or } r = \frac{1}{3}$	1/2
	<p>The terms of the progression are</p> $2, 6, 18 \text{ or } 18, 6, 2.$	1/2
	OR	
	<p>Let the terms be $a - d, a, a + d$.</p> <p>Given : $a - d + a + a + d = 18$</p> $3a = 18 \quad \therefore a = 6$	1/2
	<p>And</p> $(a - d)^2 + a^2 + (a + d)^2 = 140$ $(6 - d)^2 + 36 + (6 + d)^2 = 140$ $(6 - d)^2 + (6 + d)^2 = 140 - 36$ $36 + d^2 - 12d + 36 + d^2 + 12d = 104$ $2d^2 + 72 = 104$ $2d^2 = 104 - 72$ $2d^2 = 32$ $d^2 = 16$	1/2
	$\therefore d = \pm 4.$	
	<p>If $d = 4$ then terms are</p> $6 - 4, 6, 6 + 4$ <p style="text-align: center;"><i>i.e.</i> 2, 6, 10</p>	1/2
	<p>If $d = -4$, then terms are</p> $6 - (-4), 6, 6 - 4$ $10, 6, 2.$	1/2



Qn. Nos.	Value Points	Marks allotted
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38.



By measuring $PQ = 6.7 \text{ cm}$

To draw C_1, C_2 and C_3 circles — $1\frac{1}{2}$

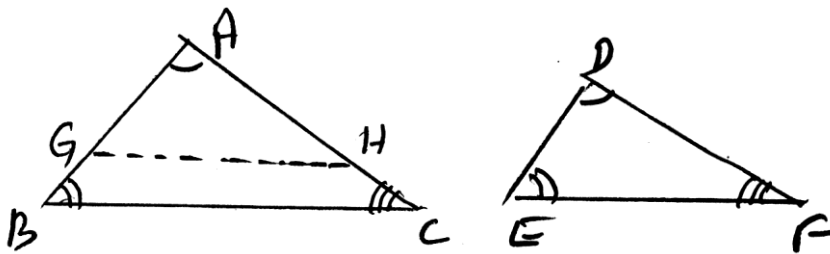
To bisect AB and to draw semicircle — 1

Joining AR, BR and PQ — 1

Measuring $PQ = 6.7 \text{ cm}$ — $\frac{1}{2}$

4

39.



$\frac{1}{2}$

Data : In $\triangle ABC$ and $\triangle DEF$

$$\angle BAC = \angle EDF$$

$$\angle ABC = \angle DEF$$

$\frac{1}{2}$



Qn. Nos.	Value Points	Marks allotted
	To prove that : $\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$	1/2
	Construction : Mark points G and H on AB and AC such that	
	$AG = DE$ and $AH = DF$. Join G and H .	1/2
	Proof : Compare $\triangle AGH$ and $\triangle DEF$	
	$AG = DE$ [\because construction]	
	$\angle GAH = \angle EDF$ [\because data]	
	$AH = DF$ [\because construction]	1/2
	$\therefore \triangle AGH \cong \triangle DEF$ [\because SAS]	
	$\angle AGH = \angle DEF$ [CPCT]	
	But $\angle ABC = \angle DEF$ [\because data]	1/2
	$\Rightarrow \angle AGH = \angle ABC$ [\because Axiom 1]	
	$GH \parallel BC$	
	(If corresponding angles are equal then lines are parallel)	1/2
	\therefore In $\triangle ABC$, $\frac{AB}{AG} = \frac{BC}{GH} = \frac{CA}{HA}$ (Corollary to Thales)	
	Hence $\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$ [$\because \triangle AGH \cong \triangle DEF$]	1/2

4

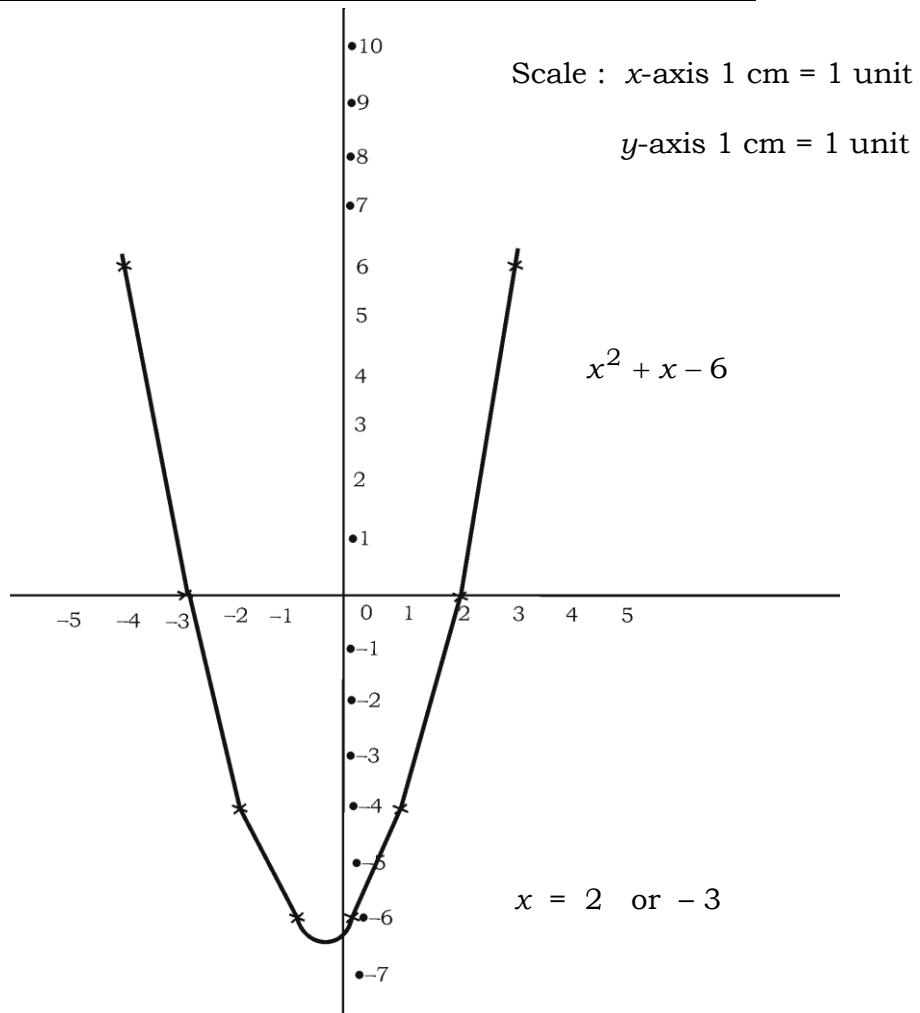


Qn. Nos.	Value Points	Marks allotted
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40.

$$y = x^2 + x - 6$$

x	0	1	-1	2	-2	3	-3	-4
y	-6	-4	-6	0	-4	6	0	6



4

