01. $\int_0^{\pi/2} \frac{\sqrt{\sin x}}{\sqrt{\sin x}+\sqrt{\cos x}} dx$ is equal to

(A) 0 (B) $-\pi$ (C) $3\pi/2$ (D) $\pi/2$ (E) $\pi/4$

Ans : E

02. If (x, y) is equidistant from (a + b, b – a) and (a – b, a + b), then

(A) x + y = 0 (B) bx – ay = 0 (C) ax – by = 0 (D) bx + ay = 0 (E) ax + by = 0

Ans : B

03. If the points (1, 0), (0, 1) and (x, 8) are collinear, then the value of x is equal to

(A) 5 (B) – 6 (C) 6 (D) 7 (E) – 7

Ans : E

04. The minimum value of the function max $\{x, x^2\}$ is equal to

(A) 0 (B) 1 (C) 2 (D) 1/2 (E) 3/2

Ans : A

05. Let f(x + y) = f(x) f(y) for all x and y. If f(0) = 1, f(3) = 3 and $f'(0) = 11$, then $f'(3)$ is equal to

(A) 11 (B) 22 (C) 33 (D) 44 (E) 55

Ans : C

06. If f(9) = $f'(9) = 0$, then $\lim_{x\to 9} \frac{\sqrt{f(x)}-3}{\sqrt{x}-3}$ is equal to

(A) 0 (B) f(0) (C) $f'(3)$ (D) f(9) (E) 1

Ans : A

07. The value of $\cos(\pi/4+x)+\cos(\pi/4-x)$ is

(A) $\sqrt{2}\sin^2 x$ (B) $\sqrt{2}\sin x$ (C) $\sqrt{2}\cos^2 x$ (D) $\sqrt{3}\cos x$ (E) $\sqrt{2}\cos x$

Ans : E

08. Area of the triangle with vertices (– 2, 2), (1, 5) and (6, – 1) is

(A) 15 (B) 3/5 (C) 29/2 (D) 33/2 (E) 35/2

Ans : D

09. The equation of the line passing through (– 3, 5) and perpendicular to the line through the points (1, 0) and (– 4, 1) is

(A) 5x + y + 10 = 0 (B) 5x – y + 20 = 0 (C) 5x – y – 10 = 0
(D) 5x + y + 20 = 0 (E) 5y – x – 10 = 0

Ans : B

10. The coefficient of x^5 in the expansion of $(1 + x^2)^5(1 + x)^4$ is

(A) 30 (B) 60 (C) 40 (D) 10 (E) 45

Ans : B

11. The coefficient of x^4 in the expansion of $(1 – 2x)^5$ is equal to

(A) 40 (B) 320 (C) – 320 (D) – 32 (E) 80

Ans : E

12. The equation $5x^2 + y^2 + y = 8$ represents
(A) an ellipse (B) a parabola (C) a hyperbola (D) a circle (E) a straight line
Ans : A

13. The centre of the ellipse $4x^2 + y^2 - 8x + 4y - 8 = 0$ is
(A) (0, 2) (B) (2, – 1) (C) (2, 1) (D) (1, 2) (E) (1, – 2)
Ans : E

14. The area bounded by the curves $y = -x^2 + 3$ and $y = 0$ is
(A) $\sqrt{3}+1$ (B) $\sqrt{3}$ (C) $4\sqrt{3}$ (D) $5\sqrt{3}$ (E) $6\sqrt{3}$
Ans : C

15. The order of the differential equation $\left(\frac{d^3y}{dx^3}\right)^2 + \left(\frac{d^2y}{dx}\right)^2 + \left(\frac{dy}{dx}\right)^5 = 0$ is
(A) 3 (B) 4 (C) 1 (D) 5 (E) 6
Ans : A

16. If $f(x) = \sqrt{2x} + \frac{4}{\sqrt{2x}}$, then $f'(2)$ is equal to
(A) 0 (B) – 1 (C) 1 (D) 2 (E) – 2
Ans : A

17. The area of the circle $x^2 - 2x + y^2 - 10y + k = 0$ is 25π. The value of k is equal to
(A) – 1 (B) 1 (C) 0 (D) 2 (E) 3
Ans :B

18. $\int_{2016}^{2017} \frac{\sqrt{x}}{\sqrt{x}+\sqrt{4033-x}} dx$ is equal to
(A) 1/4 (B) 3/2 (C) 2017/2 (D) 1/2 (E) 508
Ans :D

19. The solution of $dy/dx + y \tan x = \sec x$, $y(0) = 0$ is
(A) $y \sec x = \tan x$ (B) $y \tan x = \sec x$ (C) $\tan x = y \tan x$
(D) $x \sec x = \tan y$ (E) $y \cot x = \sec x$
Ans :A

20. If the vectors $2\hat{i}+2\hat{j}+6\hat{k}$, $2\hat{i}+\lambda\hat{j}+6\hat{k}$, $2\hat{i}-3\hat{j}+\hat{k}$ are coplanar, then the value of λ is
(A) – 10 (B) 1 (C) 0 (D) 10 (E) 2
Ans :E

21. The distance between (2, 1, 0) and $2x + y + 2z + 5 = 0$ is
(A) 10 (B) 10/3 (C) 10/9 (D) 5 (E) 1
Ans :B

22. The equation of the hyperbola with vertices $(0,\pm15)$ and foci $(0,\pm20)$ is

(A) $\frac{x^2}{175}-\frac{y^2}{225}=1$ (B) $\frac{x^2}{625}-\frac{y^2}{125}=1$ (C) $\frac{y^2}{225}-\frac{x^2}{125}=1$

(D) $\frac{y^2}{65}-\frac{x^2}{65}=1$ (E) $\frac{y^2}{225}-\frac{x^2}{175}=1$

Ans : E

23. The value of $\frac{15^3+6^3+3.6.15.21}{1+4(6)+6(36)+4(216)+1296}$ is equal to

(A) 29/7 (B) 7/19 (C) 6/17 (D) 21/19 (E) 27/7

Ans : E

24. The equation of the plane that passes through the points (1, 0, 2), (– 1, 1, 2), (5, 0, 3) is

(A) x + 2y – 4z + 7 = 0 (B) x + 2y – 3z + 7 = 0

(C) x – 2y + 4z + 7 = 0 (D) 2y – 4z – 7 + x = 0

(E) x + 2y + 3z + 7 = 0

Ans : A

25. The vertex of the parabola $y^2 – 4y – x + 3 = 0$ is

(A) (– 1, 3) (B) (– 1, 2) (C) (2, – 1) (D) (3, – 1) (E) (1, 2)

Ans : B

26. If $\vec{a},\vec{b},\vec{c}$ are vectors such that $\vec{a}+\vec{b}+\vec{c}=0$ and $|\vec{a}|=7,|\vec{b}|=5,|\vec{c}|=3$, then the angle between $\vec{c}$ and $\vec{b}$ is

(A) $\pi/3$ (B) $\pi/6$ (C) $\pi/4$ (D) π (E) 0

Ans : A

27. Let $f(x) = 2x^3 – 9ax^2 + 12a^2x + 1$, where $a > 0$. The minimum of f is attained at a point q and the maximum is attained at a point p. If $p^3 = q$, then a is equal to

(A) 1 (B) 3 (C) 2 (D) $\sqrt{2}$ (E) 1/2

Ans :D

28. For all rest numbers x and y, it is known as the real valued function f satisfies f(x) + f(y) = f(x + y). If f(1) = 7, then $\sum_{r=1}^{100} f(r)$ is equal to

(A) $7\times51\times102$ (B) $6\times50\times102$ (C) $7\times50\times102$

(D) $6\times25\times102$ (E) $7\times50\times101$

Ans :E

29. The eccentricity of the ellipse $\frac{(x-1)^2}{2}+\left(y+\frac{3}{4}\right)^2=\frac{1}{16}$ is

(A) $1/\sqrt{2}$ (B) $1/2\sqrt{2}$ (C) 1/2 (D) 1/4 (E) $1/4\sqrt{2}$

Ans : A

30. $\int_{-1}^{1}\max\{x,x^3\}dx$ is equal to

(A) 3/4 (B) 1/4 (C) 1/2 (D) 1 (E) 0

Ans :B

31. If $x \in [0, \pi/2], y \in [0, \pi/2]$ and sin x + cos y = 2, then the value of x + y is equal to
(A) 2π (B) π (C) $\pi/4$ (D) $\pi/2$ (E) 0
Ans :D

32. Let a, a + r and a + 2r be positive real numbers such that their product is 64. Then the minimum value of a + 2r is equal to
(A) 4 (B) 3 (C) 2 (D) 1/2 (E) 1
Ans : A

33. The sum S = 1/9! + 1/3!7! + 1/5!5! + 1/7!3! + 1/9! is equal to
(A) $2^{10}/8!$ (B) $2^9/10!$ (C) $2^7/10!$ (D) $2^6/10!$ (E) $2^5/8!$
Ans :B

34. If $f(x) = \begin{vmatrix} x & x^2 & x^3 \\ 1 & 2x & 3x^2 \\ 0 & 2 & 6x \end{vmatrix}$, then $f'(x)$ is equal to
(A) $x^3 + 6x^2$ (B) $6x^3$ (C) 3x (D) $6x^2$ (E) 0
Ans : D

35. $\int \frac{x^2}{1+(x^3)^2} dx$ is equal to
(A) $\tan^{-1} x^2 + c$ (B) $2/3 \tan^{-1} x^3 + c$ (C) $1/3 \tan^{-1} (x^3) + c$
(D) $1/2 \tan^{-1} x^2 + c$ (E) $\tan^{-1} x^3 + c$
Ans : C

36. Let $f_n(x)$ be the nth derivative of f(x). The least value of n so that $f_n = f_{n+1}$ where $f(x) = x^2 + e^x$ is
(A) 4 (B) 5 (C) 2 (D) 3 (E) 6
Ans :D

37. sin 765^o is equal to
(A) 1 (B) 0 (C) $\sqrt{3}/2$ (D) 1/2 (D) $1/\sqrt{2}$
Ans : E

38. The distance of the point (3, – 5) from the line 3x – 4y – 26 = 0 is
(A) 3/7 (B) 2/5 (C) 7/5 (D) 3/5 (E) 1
Ans :D

39. The difference between the maximum and minimum value of the function $f(x) = \int_0^x (t^2 + t + 1) dt$ on [2, 3] is
(A) 39/6 (B) 49/6 (C) 59/6 (D) 69/6 (E) 79/6
Ans : C

40. If a and b are the non zero distinct roots of $x^2 + ax + b = 0$, then the minimum value of $x^2 + ax + b$ is
(A) 2/3 (B) 9/4 (C) – 9/4 (D) – 2/3 (E) 1
Ans : C

41. If the straight line y = 4x + c touches the ellipse $\frac{x^2}{4}+y^2=1$ then c is equal to

(A) 0 (B) $\pm\sqrt{65}$ (C) $\pm\sqrt{62}$ (D) $\pm\sqrt{2}$ (E) ± 13

Ans:B

42. The equations $\lambda x - y = 2$, $2x - 3y = -\lambda$ and $3x - 2y = -1$ are consistent for

(A) $\lambda = -4$ (B) $\lambda = 1, 4$ (C) $\lambda = 1, -4$ (D) $\lambda = -1, 4$ (E) $\lambda = -1$

Ans:D

43. The set $\{(x,y):|x|+|y|=1\}$ in the xy plane represents

(A) a square (B) A circle (C) An ellipse
(D) A rectangle which is not a square (E) A rhombus which is not a square

Ans:A

44. The value of $\cos\left(\tan^{-1}\left(\frac{3}{4}\right)\right)$ is

(A) $\frac{4}{5}$ (B) $\frac{3}{5}$ (C) $\frac{3}{4}$ (D) $\frac{2}{5}$ (E) 0

Ans: A

45. Let A (6, -1), B (1, 3) and C (x, 8) be three points such that AB = BC. The values of x are

(A) 3, 5 (B) -3, 5 (C) 3, -5 (D) 4, 5 (E) -3, -5

Ans:B

46. In an experiment with 15 observations on x, the following results were available

$\sum x^2 = 2830$ $\sum x = 170$

One observation that was 20, was found to be wrong and was replaced by the correct value 30. Then the corrected variance is

(A) 9.3 (B) 8.3 (C) 188.6 (D) 177.3 (E) 78

Ans:E

47. The angle between the pair of lines $\frac{x-2}{2}=\frac{y-1}{5}=\frac{z+3}{-3}$ and $\frac{x+2}{-1}=\frac{y-4}{8}=\frac{z-5}{4}$ is

(A) $\cos^{-1}\left(\frac{21}{9\sqrt{38}}\right)$ (B) $\cos^{-1}\left(\frac{23}{9\sqrt{38}}\right)$ (C) $\cos^{-1}\left(\frac{24}{9\sqrt{38}}\right)$
(D) $\cos^{-1}\left(\frac{25}{9\sqrt{38}}\right)$ (E) $\cos^{-1}\left(\frac{26}{9\sqrt{38}}\right)$

Ans:E

48. Let $\vec{a}$ be a unit vector. If $(\vec{x}-\vec{a}).(\vec{x}+\vec{a})=12$, then the magnitude of $\vec{x}$ is

(A) $\sqrt{8}$ (B) $\sqrt{9}$ (C) $\sqrt{10}$ (D) $\sqrt{13}$ (E) $\sqrt{12}$

Ans:D

49. The area of the triangular region whose sides are y = 2x + 1, y = 3x + 1 and x = 4 is

(A) 5 (B) 6 (C) 7 (D) 8 (E) 9

Ans:D

50. If $nC_{r-1} = 36$, $nC_r = 84$ and $nC_{r+1} = 126$, then the value of r is
(A) 9 (B) 3 (C) 4 (D) 5 (E) 6
Ans:B

51. Let $f(x + y) = f(x)\, f(y)$ and $f(x) = 1 + \sin(3x)\, g(x)$, where g is differentiable. The $f'(x)$ is equal to
(A) 3f(x) (B) g(0) (C) f(x) g(0) (D) 3g(x) (E) 3f(x) g(0)
Ans:E

52. The roots of the equation $\begin{vmatrix} x-1 & 1 & 1 \\ 1 & x-1 & 1 \\ 1 & 1 & x-1 \end{vmatrix} = 0$ are
(A) 1, 2 (B) -1, 2 (C) -1, -2 (D) 1, -2 (E) 1, 1
Ans:B

53. If the 7^{th} and 8^{th} term of the binomial expansion $(2a - 3b)^n$ are equal, then $\frac{2a+3b}{2a-3b}$ is equal to
(A) $\frac{13-n}{n+1}$ (B) $\frac{n+1}{13-n}$ (C) $\frac{6-n}{13-n}$ (D) $\frac{n-1}{13-n}$ (E) $\frac{2n-1}{13-n}$
Ans: A

54. Standard deviation of first *n* odd natural numbers is
(A) $\sqrt{n}$ (B) $\sqrt{\frac{(n+2)(n+1)}{3}}$ (C) $\sqrt{\frac{n^2-1}{3}}$ (D) n (E) 2n
Ans:C

55. Let S = {1, 2, 3, ……10}. The number of subsets of S containing only odd numbers is
(A) 15 (B) 31 (C) 63 (D) 7 (E) 5
Ans:B

56. The area of the parallelogram with vertices (0, 0), (7, 2), (5, 9) and (12, 11) is
(A) 50 (B) 54 (C) 51 (D) 52 (E) 53
Ans:E

57. $\begin{vmatrix} 1 & 1 & 1 \\ p & q & r \\ p & q & r+1 \end{vmatrix}$ is equal to
(A) q – p (B) q + p (C) q (D) p (E) 0
Ans: A

58. Let $A = \begin{bmatrix} 5 & 0 \\ 1 & 0 \end{bmatrix}$ and $B = \begin{bmatrix} 20 & 5 \\ -1 & 0 \end{bmatrix}$. If 4A + 5B – C = 0, then C is
(A) $\begin{bmatrix} 5 & 25 \\ -1 & 0 \end{bmatrix}$ (B) $\begin{bmatrix} 20 & 5 \\ -1 & 0 \end{bmatrix}$ (C) $\begin{bmatrix} 5 & -1 \\ 0 & 25 \end{bmatrix}$ (D) $\begin{bmatrix} 5 & 25 \\ -1 & 5 \end{bmatrix}$ (E) $\begin{bmatrix} 0 & 5 \\ 5 & 25 \end{bmatrix}$
Ans:B

59. If $U = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{-1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$, then U^{-1} is

(A) U^T (B) U (C) I (D) 0 (E) U^2

Ans: A

60. If $A = \begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$, then A^{-1} is

(A) A^T (B) A^2 (C) A (D) I (E) 0

Ans: A

61. If $\begin{pmatrix} x+y & x-y \\ 2x+z & x+z \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 1 & 1 \end{pmatrix}$, then the values of x, y and z are respectively

(A) 0, 0, 1 (B) 1, 1, 0 (C) -1, 0, 0 (D) 0, 0, 0 (E) 1, 1, 1

Ans: A

62. $\begin{pmatrix} 7 & 1 & 5 \\ 8 & 0 & 0 \end{pmatrix}\begin{pmatrix} 2 \\ 3 \\ 1 \end{pmatrix} + 5\begin{pmatrix} 1 \\ 0 \end{pmatrix}$ is equal to

(A) $\begin{pmatrix} 16 \\ 27 \end{pmatrix}$ (B) $\begin{pmatrix} 27 \\ 16 \end{pmatrix}$ (C) $\begin{pmatrix} 15 \\ 16 \end{pmatrix}$ (D) $\begin{pmatrix} 16 \\ 15 \end{pmatrix}$ (E) $\begin{pmatrix} 16 \\ 16 \end{pmatrix}$

Ans:B

63. If $\begin{pmatrix} 1 & 2 & 4 \\ 1 & 3 & 5 \\ 1 & 4 & a \end{pmatrix}$ is singular, then the value of a is

(A) a = -6 (B) a = 5 (C) a = -5 (D) a = 6 (E) a = 0

Ans:D

64. If $\begin{pmatrix} 1 & 2 & -3 \\ 0 & 4 & 5 \\ 0 & 0 & 1 \end{pmatrix}\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$, then (x, y, z) is equal to

(A) (1, 6, 6) (B) (1, -6, 1) (C) (1, 1, 6) (D) (6, -1, 1) (E) (-1, 6, 1)

Ans:D

65. If $A = \begin{pmatrix} 1 & 5 \\ 0 & 2 \end{pmatrix}$, then

(A) $A^2 - 2A + 2I = 0$ (B) $A^2 - 3A + 2I = 0$ (C) $A^2 - 5A + 2I = 0$
(D) $2A^2 - A + I = 0$ (E) $A^2 + 3A + 2I = 0$

Ans:B

66. If $\begin{pmatrix} 2x+y & x+y \\ p-q & p+q \end{pmatrix} = \begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix}$, then (x, y, p, q) equals

(A) 0, 1, 0, 0 (B) 0, -1, 0, 0 (C) 1, 0, 0, 0 (D) 0, 1, 0, 1 (E) 1, 0, 1, 0

Ans: A

67. The value of $\left|\sqrt{4+2\sqrt{3}}\right| - \left|\sqrt{4-2\sqrt{3}}\right|$ is

(A) 1 (B) 2 (C) 4 (D) 3 (E) 5

Ans:B

68. The value of $8^{2/3} - 16^{1/4} - 9^{1/2}$ is

(A) -1 (B) -2 (C) -3 (D) -4 (E) -5

Ans: A

69. Let x = 2 be a root of $y = 4x^2 - 14x + q = 0$. Then y is equal to

(A) (x – 2) (4x – 6) (B) (x – 2) (4x + 6) (C) (x – 2) (-4x – 6)
(D) (x – 2) (-4x + 6) (D) (x – 2) (4x + 3)

Ans: A

70. If x_1 and x+2+ are the roots of $3x^2 - 2x - 6 = 0$, then $x_1^2 + x_2^2$ is equal to

(A) $\frac{50}{9}$ (B) $\frac{40}{9}$ (C) $\frac{30}{9}$ (D) $\frac{20}{9}$ (E) $\frac{10}{9}$

Ans:B

71. Let x_1 and x_2 be the roots of the equation $x^2 - px - 3 = 0$. If $x_1^2 + x_2^2 = 10$, then the value of p is equal to

(A) -4 or 4 (B) -3 or 3 (C) -2 or 2 (D) -1 or 1 (E) 0

Ans:C

72. If the product of roots of the equation $mx^2 + 6x + (2m - 1) = 0$ is -1, then the value of m is

(A) 1/3 (B) 1 (C) 3 (D) -1 (E) -3

Ans: A

73. If $f(x) = \frac{1}{x^2+4x+4} - \frac{4}{x^4+4x^3+4x^2} + \frac{4}{x^3+2x^2}$, then $f\left(\frac{1}{2}\right)$ is equal to

(A) 1 (B) 2 (C) -1 (D) 3 (E) 4

Ans:E

74. If x and y are the roots of the equation $x^2 + bx + 1 = 0$, then the value of $\frac{1}{x+b} + \frac{1}{y+b}$ is

(A) 1/b (B) b (C) 1/2b (D) 2b (E) 1

Ans:B

75. The equations $x^5 + ax + 1 = 0$ and $x^6 + ax^2 + 1 = 0$ have a common root. Then a is equal to

(A) -4 (B) -2 (C) -3 (D) -1 (E) 0

Ans:B

76. The roots of $ax^2 + x + 1 = 0$, where $a \neq 0$, are in the ratio 1 : 1. Then a is equal to
(A) 1/4 (B) 1/2 (C) 3/4 (D) 1 (E) 0
Ans: A

77. If $z^2 + z + 1 = 0$ where z is a complex number, then the value of $\left(z+\frac{1}{z}\right)^2+\left(z^2+\frac{1}{z^2}\right)^2+\left(z^3+\frac{1}{z^3}\right)^2$ equals
(A) 4 (B) 5 (C) 6 (D) 7 (E) 8
Ans:C

78. Let $\Delta=\begin{vmatrix}1 & 1 & 1\\ 1 & -1-w^2 & w^2\\ 1 & w & w^4\end{vmatrix}$, where $w \neq 1$ is a complex number such that $w^3 = 1$. Then Δ equals
(A) $3w + w^2$ (B) $3w^2$ (C) $3(w = w^2)$ (D) $-3w^2$ (E) $3w^2 + 1$
Ans:B

79. If $\begin{vmatrix}3i & -9i & 1\\ 2 & 9i & -1\\ 10 & 9 & i\end{vmatrix} = x + iy$, then
(A) x = 1, y = 1 (B) x = 0, y = 1 (C) x = 1, y = 0 (D) x = 0, y = 0
(E) x = -1, y = 0
Ans:D

80. If $z = \cos\left(\frac{\pi}{3}\right) - i\sin\left(\frac{\pi}{3}\right)$, the $z^2 - z + 1$ is equal to
(A) 0 (B) 1 (C) -1 (D) $\frac{\pi}{2}$ (E) π
Ans: A

81. $\left(\frac{1+\cos\left(\frac{\pi}{12}\right)+i\sin\left(\frac{\pi}{12}\right)}{1+\cos\left(\frac{\pi}{12}\right)-i\sin\left(\frac{\pi}{12}\right)}\right)^{72}$ is equal to
(A) 0 (B) – 1 (C) 1 (D) 1/2 (E) – 1/2
Ans :C

82. If $A=\begin{vmatrix}4 & k & k\\ 0 & k & k\\ 0 & 0 & k\end{vmatrix}$ and det (A) = 256, then |k| equals
(A) 4 (B) 5 (C) 6 (D) 7 (E) 8
Ans : E

83. If $A=\begin{pmatrix}1 & 0\\ 1 & 1\end{pmatrix}$, then $A^n + nI$ is equal to
(A) I (B) nA (C) 1+nA (D) I – nA (E) nA – I
Ans :C

84. If $|z| = 5$ and $w = \frac{z-5}{z+5}$, then Re(w) is equal to
(A) 0 (B) 1/25 (C) 25 (D) 1 (E) – 1
Ans :A

85. If $A = \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix}$, then A^{2017} is equal to
(A) $2^{2015}A$ (B) $2^{2016}A$ (C) $2^{2014}A$ (D) $2^{2017}A$ (E) $2^{2020}A$
Ans : B

86. If $a = e^{i\theta}$, then $\frac{1+a}{1-a}$ is equal to
(A) $\cot\frac{\theta}{2}$ (B) $\tan\theta$ (C) $i\cot\frac{\theta}{2}$ (D) $i\tan\frac{\theta}{2}$ (E) $2\tan\theta$
Ans :C

87. Three numbers x, y, and z are in arithmetic progression. If $x + y + z = -3$ and $xyz = 8$, then $x^2 + y^2 + z^2$ is equal to
(A) 9 (B) 10 (C) 21 (D) 20 (E) 1
Ans :C

88. The 30^{th} term of the arithmetic progression 10, 7, 4 is
(A) – 97 (B) – 87 (C) – 77 (D) – 67 (E) – 57
Ans :C

89. The arithmetic mean of two numbers x and y is 3 and geometric mean is 1. Then $x^2 + y^2$ is equal to
(A) 30 (B) 31 (C) 32 (D) 33 (E) 34
Ans :E

90. The solution of $3^{2x-1} = 81^{1-x}$ is
(A) 2/3 (B) 1/6 (C) 7/6 (D) 5/6 (E) 1/3
Ans :D

91. The sixth term in the sequence is 3,1, $\frac{1}{3}$,… is
(A) 1/27 (B) 1/9 (C) 1/81 (D) 1/17 (E) 1/7
Ans :C

92. Three numbers are in arithmetic progression. Their sum is 21 and the product of the first number and the third number is 45. Then the product of these three number is
(A) 315 (B) 90 (C) 180 (D) 270 (E) 450
Ans :A

93. If a + 1, 2a + 1, 4a – 1 are in arithmetic progression, then the value of a is
(A) 1 (B) 2 (C) 3 (D) 4 (E) 5
Ans : B

94. Two numbers x and y have arithmetic mean 9 and geometric mean 4. Then x and y are the roots of
(A) $x^2 - 18x - 16 = 0$ (B) $x^2 - 18x + 16 = 0$ (C) $x^2 + 18x - 16 = 0$
(D) $x^2 + 18x + 16 = 0$ (E) $x^2 - 17x + 16 = 0$
Ans : B

95. Three unbiased coins are tossed. The probability of getting at least 2 tails is
(A) 3/4 (B) 1/4 (C) 1/2 (C) 1/3 (D) 2/3
Ans :C

96. A single letter is selected from the word TRICKS. The probability that it is either T or R is
(A) 1/36 (B) 1/4 (C) 1/2 (D) 2/3 (E) 1/3
Ans :E

97. From 4 red balls, 2 white balls and 4 black balls, four balls are selected. The probability of getting 2 red balls is
(A) 7/21 (B) 8/21 (C) 9/21 (C) 10/21 (E) 11/21
Ans : C

98. In a class, 60% of the students know lesion I, 40% know lesion II and 20% know lesson I and II. A student is selected at random. The probability that the student does not know lesson I and lesson II is
(A) 0 (B) 4/5 (C) 3/5 (D) 1/5 (E) 2/5
Ans :D

99. Two distinct numbers x and y are chosen from 1,2,3,4,5. The probability that the arithmetic mean of x and y is an inter is
(A) 0 (B) 1/5 (C) 3/5 (D) 2/5 (E) 4/5
Ans :D

100. The number of 3×3 matrices with entries – 1 or +1 is
(A) 2^{-4} (B)2^5 (C)2^6 (D)2^7 (E)2^9
Ans :E

101. Let S be the set of all 2×2 symmetric matrices whose entries are either zero or one. A matrix X is chosen from S. The probability that the determinant of X is not zero is
(A) 1/3 (B) 1/2 (C) 3/4 (D) 1/4 (E) 2/9
Ans :B

102. The number of words that can be formed by using all the letters of the word PROBLEM only one is
(A)5 ! (B) 6! (C) 7! (D) 8! (E) 9!
Ans :C

103. The number of diagonals in a hexagon is
(A) 8 (B) 9 (C) 10 (D) 11 (E) 12
Ans : B

104. The sum of odd integers from 1 to 2001 is
(A) 1001^2 (B) 1000^2 (C) 1002^2 (D) 1003^2 (E)999^2
Ans :A

105. Two balls are selected from two black and two red balls. The probability that the two balls will have no black balls is
(A) 1/7 (B) 1/5 (C) 1/4 (D) 1/3 (E) 1/6
Ans :E

106. If $z = i^9 + i^{19}$, then z is equal to
(A) 0+0i (B) 1+0i (C) 0+i (D)1 +2i (E) 1+ 3i
Ans :A

107. The mean for the data 6, 7, 10, 12, 13, 4, 8, 12 is
(A) 9 (B) 8 (C) 7 (D) 6 (E) 5
Ans :A

108. The set of all real numbers satisfying the inequality x – 2 < 1 is
(A)$(3, \infty)$ (B)$[3, \infty)$ (C) $[-3, \infty)$ (D) $(-\infty, -3)$ (E) $(-\infty, 3)$
Ans :E

109. If $\frac{|x-3|}{x-3} >$, then
(A) $x \in (-3, \infty)$ (B) $x \in (3, \infty)$ (C) $x \in (2, \infty)$ (D) $x \in (1, \infty)$ (E) $x \in (-\infty, 3)$
Ans : B

110. The mode of the data 8, 11, 9 , 8, 11, 9, 7, 8 , 7, 3, 2 is
(A) 11 (B) 9 (C) 8 (D) 3 (E) 7
Ans :C

111. If the mean of six numbers is 41, then the sum of these numbers is
(A) 246 (B) 236 (C) 226 (D) 216 (E) 206
Ans :A

112. If $\int_0^x f(t)dt = x^2 + e^x (x > 0)$, then f(1) is equal to
(A) 1+ e (B) 2+ e (C) 3 + e (D) e (E) 0
Ans :A

113. $\int \frac{x+1}{x^{1/2}} dx =$
(A) $-x^{3/2} + x^{1/2} + c$ (B) $x^{1/2}$ (C) $x^{3/2} + 2x^{1/2} + c$ (D) $x^{3/2} + x^{1/2} + c$ (E) $x^{3/2}$ \
Ans :C

114. In a flight 50 people speak Hindi, 20 speak English and 10 speak both English and Hindi. The number of people who speak at least one of the two languages is
(A) 40 (B) 50 (C) 20 (D) 80 (E) 60
Ans :E

115. If $f(x) = \frac{x+1}{x-1}$, then the value of f(f(x) is equal to
(A) x (B) 0 (C) – x (D) 1 (E) 2
Ans : A

116. Two dice are thrown simultaneously. What is the probability of getting two numbers whose product is even?
(A) 3/4 (B)1/4 (C) 1/2 (D) 2/3 (E) 1/16
Ans :A

117. $\lim_{x \to 0} \frac{\sqrt{2+x} - \sqrt{2-x}}{x}$ is equal to
(A) $\frac{1}{\sqrt{2}}$ (B) $\sqrt{2}$ (C) 0 (D) Does not exist (E) $\frac{1}{2\sqrt{2}}$
Ans : A

118. $\int \frac{dx}{e^x + e^{-x} + 2}$ is equal to

(A) $\frac{1}{e^x + 1} + c$ (B) $\frac{-1}{e^x + 1} + c$ (C) $\frac{1}{1 + e^{-x}} + c$ (D) $\frac{1}{e^{-x} - 1} + c$ (E) $\frac{1}{e^x - 1} + c$

Ans : B

119. $\tan\left(\frac{\pi}{4} + \frac{\theta}{2}\right) + \tan\left(\frac{\pi}{4} - \frac{\theta}{2}\right)$ is equal to

(A) sec θ (B) 2sec θ (C) sec θ /2 (D) sin θ (E) cos θ

Ans : B

120. $\int_{-1}^{0} \frac{dx}{x^2 + x + 2}$ is equal to

(A) $\pi/4$ (B) $\pi/2$ (C) π (D) 0 (E) $-\pi$

Ans : NA