



# Rao IIT Academy

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## XII CBSE - BOARD - MARCH - 2017

CODE (55/1) SET -1

Date: 15.03.2017

PHYSICS - SOLUTIONS

### SECTION - A

1. Nichrome, since its resistance is high. [1 M]

*Topic:Current Electricity; Sub-Topic:Resistance\_ L-1\_ Target-2017\_ XII-CBSE Board Exam\_\_Physics*

2. Yes [1 M]

*Topic:Electromagnetic waves; Sub-Topic:Properties\_ L-1\_ Target-2017\_ XII-CBSE Board Exam\_\_Physics*

3. 
$$\mu = \frac{\sin\left(\frac{\delta m + A}{2}\right)}{\sin\frac{A}{2}}$$

for red light  $\mu =$  least;  $\delta_m \rightarrow$  will reduce [1 M]

*Topic:Ray optics; Sub-Topic:Refractive through prism\_ L-3\_ \_Target-2017\_ XII-CBSE Board Exam\_\_Physics*

4. Photo electric effect. [1 M]

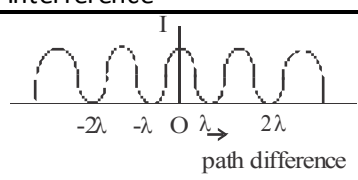
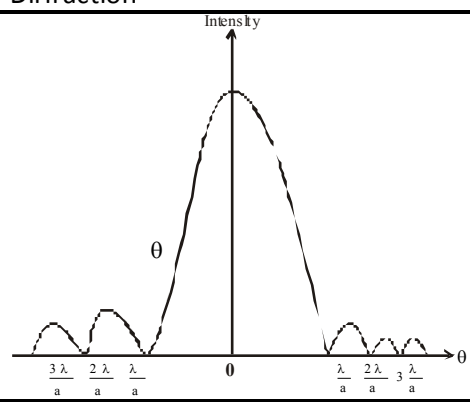
*Topic:Dual nature of radiation & matters; Sub-Topic:Properties\_ L-1\_ \_Target-2017\_ XII-CBSE Board Exam\_\_Physics*

5. The polarity of plate 'A' will be positive with respect to plate 'B' in the capacitor. [1 M]

*Topic:EMI; Sub-Topic:Lenz's law\_ L-2\_ Target-2017\_ XII-CBSE Board Exam\_\_Physics*

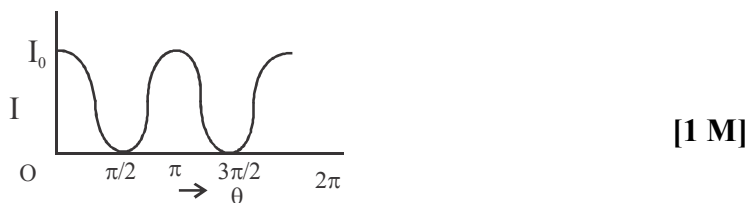
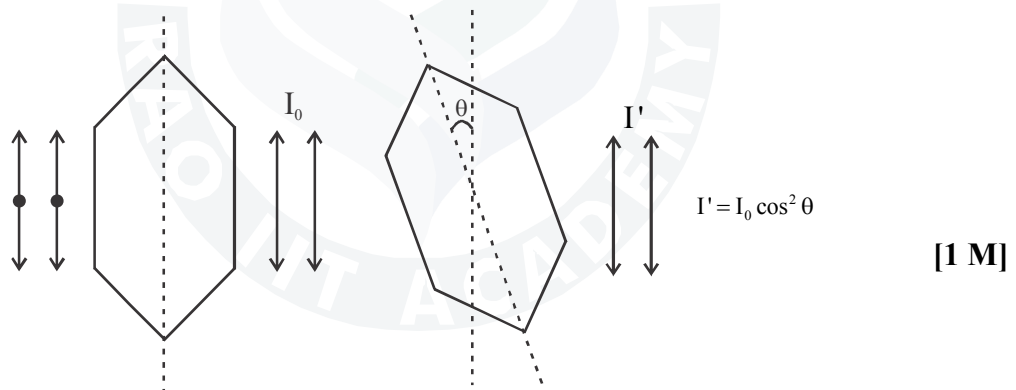
**SECTION - B**

6.

Interference	Diffraction
	
Fringe widths are same	Fringe widths are different
Generally fringe pattern is hyperbolic e.g. in YDSE or Biprism	Generally fringe pattern is circular. [1 M]

*Topic: Wave optics; Sub-Topic: Difference between interference & diffraction\_L-1\_Target-2017\_XII-CBSE Board Exam\_Physics*

(OR)



*Topic: Wave optics; Sub-Topic: Polarization\_L-2\_Target-2017\_XII-CBSE Board Exam\_Physics*

7. (a) X - rays  
 Uses - Use to study atomic structure. [1 M]
- (b) Microwaves  
 Uses : Used in radar application. [1 M]

*Topic: Electromagnetic waves; Sub-Topic: Spectrum \_L-1\_Target-2017\_XII-CBSE Board Exam\_Physics*

8. Magnetic force = Electrostatic force

$$qvB = qE \quad [1 \text{ M}]$$

$$\Rightarrow v = \frac{E}{B} \quad [1 \text{ M}]$$

*Topic: Moving charges & Magnetism; Sub-Topic: Velocity selector \_ L-1\_ Target-2017\_ XII-CBSE Board Exam \_ Physics*

9.  $P = \sqrt{2mE}$  [1 M]

$$P = \sqrt{2 \times 9.1 \times 10^{-31} \times 12.5 \times 1.6 \times 10^{-19}}$$

$$\frac{h}{\lambda} = \sqrt{2 \times 9.1 \times 12.5 \times 1.6 \times 10^{-50}}$$

$$\lambda = \frac{h}{\sqrt{364 \times 10^{-50}}} = \frac{6.6 \times 10^{-34}}{19.07 \times 10^{-25}} = 0.34 \times 10^{-9} \text{ m}$$

$3.4 \times 10^{-10} \text{ m}$  ultraviolet. [1 M]

*Topic: Atoms ; Sub-Topic: Debroglie wave length \_ L-3 \_\_ Target-2017\_ XII-CBSE Board Exam \_ Physics*

10. For permanent magnet

a - Magnetically hard

b - Retentivity & coercivity should be large [1 M]

For electromagnet

a - Magnetically soft

b - coercivity should be low. [1 M]

*Topic: Magnetism & matter; Sub-Topic: \_\_ Hysteresis loop \_ L-3\_ Target-2017\_ XII-CBSE Board Exam \_ Physics*

### SECTION - C

11. (a) Heat increased 9 factor, so current increased by 3 factor, so potential increased by 3 factor.

$$\text{also } H = \frac{V^2}{R} t$$

$$H \propto V^2$$

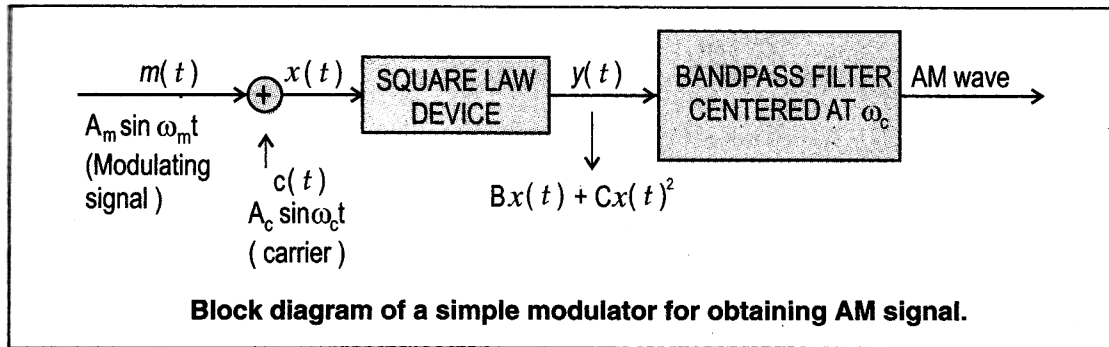
H increased by factor 9, so  $V$  increased by factor 3 [2 M]

(b)  $I = \frac{12}{6} = 2 \text{ A}$

$$V = E - ir = 12 - 2 \times 2 = 8 \text{ V} \quad [1 \text{ M}]$$

*Topic: Current Electricity ; Sub-Topic: \_ Potential difference \_ L-3 \_\_ Target-2017\_ XII-CBSE Board Exam \_ Physics*

12 (a) Production and Direction of Amplitude Modulated Wave



[1 M]

Here modulation signal  $A_m \sin \omega_m t$  is added to carrier signal  $A_c \sin \omega_c t$  to produce the signal  $x(t)$ .

$$x(t) = A_c \sin \omega_c t + A_m \sin \omega_m t$$

After, passing through square law devices

$$y(t) = Bx(t) + Cx^2(t)$$

$$y(t) = BA_m \sin \omega_m t + BA_c \sin \omega_c t + C A_m^2 \sin^2 \omega_m t + C A_c^2 \sin^2 \omega_c t + C.2 A_m A_c \sin \omega_m t. \sin \omega_c t$$

$$y(t) = BA_m \sin \omega_m t + BA_c \sin \omega_c t + \frac{C}{2} (A_m^2 + A_c^2) + C A_m A_c \cos (\omega_c - \omega_m)t - C A_m A_c \cos (\omega_c + \omega_m)t$$

Where,  $\frac{C}{2} (A_m^2 + A_c^2)$  is a D.C. term.

The bandpass filter rejects D.C. term and allows sinusoidal functions.

[1 M]

(b)  $W_c + W_m = 660 \dots (i)$

$W_c - W_m = 640 \dots (ii)$

On solving (i) and (ii)

$W_c = 650 \text{ KHz}$

$W_m = 10 \text{ KHz}$

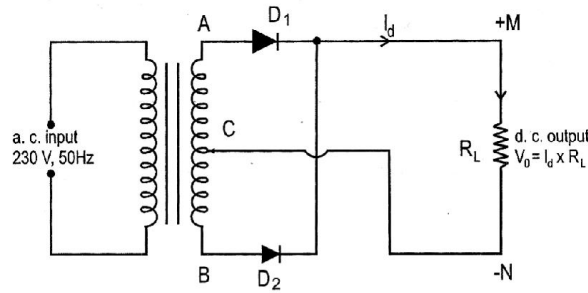
[1 M]

*Topic: Communication system; Sub-Topic: Amplitude modulation \_ L-2 \_ Target-2017 \_ XII-CBSE Board Exam \_ Physics*

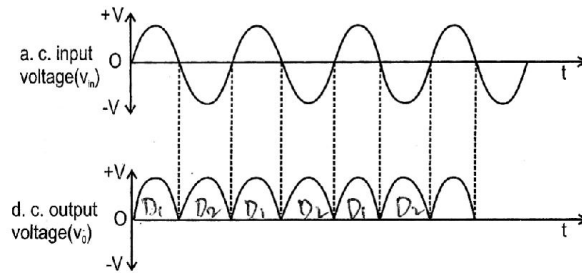
13. (a) Reverse Bias

[1 M]

(b)



Circuit diagram for full wave rectifier



Input and output waveforms for full wave rectifier

[1 M]

During positive half cycle of the A.C. input point A is + ve w.r.t. point C, (and point B is – ve w.r.t. point C), therefore the diode  $D_1$  is forward biased and  $D_2$  is reverse biased.

The current flows through diode  $D_1$ ,  $R_L$  and upper half winding (AC).

During every negative half cycle of A.C. input, point B is + ve w.r.t point C (and point A is – ve w.r.t. point C), therefore diode  $D_2$  is forward biased and diode  $D_1$  is reverse biased.

Current flows through  $R_L$ , from point M to point N (unidirectional).

[1 M]

**Topic:** *Semiconductors Electronics materials devices and simple circuit* ; **Sub-Topic:** *Diode applicaiton* \_  
\_L-3\_ \_Target-2017\_ XII-CBSE Board Exam \_Physics

14. According to photon picture of light, in photoelectric effect, electron absorbs a quantum of energy ( $h\nu$ ) of radiation. If this quantum of energy absorbed exceeds the minimum energy needed for the electron to escape from the metal surface, the electron is emitted with some kinetic energy, the maximum value of which can be given by

$$K_{\max} = h\nu - \phi_0$$

[1 M]

This is know as Einstein's photoelectric equation.  $\phi_0$  is the work function of metal, which is the minimum energy needed by a surface electron to come out.

[1 M]

The two features of photoelectric effect which cannot be explained by wave theory, are

- (i) Instantaneous emission      (ii) Existance of threshold frequency

[1 M]

**Topic:** *Dual natrue of radition & matter*; **Sub-Topic:** *Einstein's photoelectric equation* \_L-1\_ Target-2017\_ XII-CBSE Board Exam \_Physics

15. (a) **Given:** [0.5 M]

wavelength in air,  $\lambda_a = 589 \text{ nm} = 5.89 \times 10^{-7} \text{ m}$

refractive index of water,  $\mu_w = 1.33$

$\therefore$  speed of light in vacuum,  $c = 3 \times 10^8 \text{ m/s}$

$\therefore$  frequency,  $\nu = \frac{c}{\lambda_a}$

( $\therefore$  speed in air  $\approx c$ )  $= \frac{3 \times 10^8 \text{ m/s}}{5.89 \times 10^{-7} \text{ m}} = 5.093 \times 10^{14} \text{ Hz}$

Now, speed of light in water,  $\nu = \frac{c}{\mu_w}$

$= \frac{3 \times 10^8 \text{ m/s}}{1.33} \approx 2.2605 \times 10^8 \text{ m/s}$  [0.5 M]

$\therefore$  wavelength in water,  $\lambda_w = \frac{\nu}{\nu}$

( $\therefore$  frequency remains the same in all media)

$= \frac{c/\mu_w}{c/\lambda_a} = \frac{\lambda_a}{\mu_w} = \frac{5.89 \times 10^{-7} \text{ m}}{1.33}$

$\approx 4.43 \times 10^{-7} \text{ m}$

Thus, for the refracted light,

wavelength  $\lambda_w \approx 4.43 \times 10^{-7} \text{ m}$

frequency  $\nu \approx 5.09 \times 10^{14} \text{ Hz}$  and

speed  $\nu \approx 2.26 \times 10^8 \text{ m/s}$ . [0.5 M]

**Topic: Ray optics ; Sub-Topic: Refraction\_L-1\_Target-2017\_XII-CBSE Board Exam\_Physics**

(b) **Given:**  $\mu = 1.55, f = 20 \text{ cm}$  [0.5 M]

$|R_1| = |R_2| = R$  (let)

$\therefore$  for double convex lens as  $R_1 > 0$  and  $R_2 < 0$

So,  $R_1 = R$  and  $R_2 = -R$

Using Lens Maker's Equation

$\frac{1}{f} = (\mu - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$ , we get [0.5 M]

$\frac{1}{20} = (1.55 - 1) \cdot \left( \frac{1}{R} + \frac{1}{R} \right)$

$$\Rightarrow \frac{1}{20} = 0.55 \times \frac{2}{R}$$

$$\Rightarrow R = 0.55 \times 2 \times 20 \text{ cm} = 22 \text{ cm}$$

∴ The radius of curvature is 22 cm.

[0.5 M]

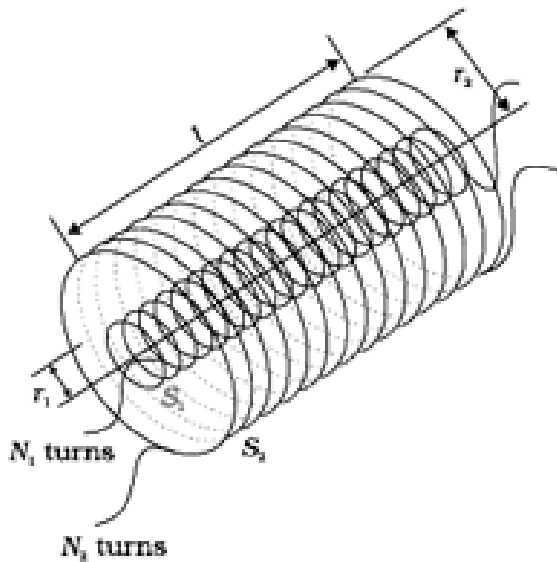
**Topic: Ray optics; Sub-Topic: lens maker's equation \_ L-2 \_ Target-2017 \_ XII-CBSE Board Exam \_ Physics**

16. If we consider two coaxial coils  $S_1$  and  $S_2$ , when a current  $I_2$  is set up through  $S_2$ , it in turn sets up a magnetic flux through  $S_1$ . Let us denote it by  $\phi_1$ . The corresponding flux linkage with solenoid  $S_1$  is

$$N_1 \phi_1 = M_{12} I_2 \quad \dots\dots(1) \quad [0.5 \text{ M}]$$

$M_{12}$  is called the mutual inductance of solenoid  $S_1$  with respect to solenoid  $S_2$ .

The magnetic field due to the current  $I_2$  in  $S_2$  is  $\mu_0 n_2 I_2$ . the resulting flux linkage with coil  $S_1$  is,



[0.5 M]

$$N_1 \phi_1 = (n_1 l) (\pi r_1^2) (\mu_0 n_2 I_2)$$

$$= \mu_0 n_1 n_2 \pi r_1^2 l I_2 \quad \dots\dots(2)$$

where  $n_1 l$  is the total number of turns in solenoid  $S_1$ . Thus, from equation (1) and equation (2).

$$M_{12} = \mu_0 n_1 n_2 \pi r_1^2 l \quad \dots\dots(3)$$

We now consider the reverse case. A current  $I_1$  is passed through the solenoid  $S_1$  and the flux linkage with coil  $S_2$  is,

$$N_2 \phi_2 = M_{21} I_1 \quad \dots\dots(4) \quad [1 \text{ M}]$$

$M_{21}$  is called the mutual inductance of solenoid  $S_2$  with respect to solenoid  $S_1$ .

The flux due to the current  $I_1$  in  $S_1$  can be assumed to be confined solely inside  $S_1$  since the solenoids are very long. Thus, flux linkage with solenoid  $S_2$  is

$$N_2 \phi_2 = (n_2 l) (\pi r_1^2) (\mu_0 n_1 I_1)$$

where  $n_2 l$  is the total number of turns of  $S_2$ . From equation (4).

$$M_{21} = \mu_0 n_1 n_2 \pi r_1^2 l \quad \dots\dots\dots(5)$$

Using Equation (3) and Equation (5), we get

$$M_{12} = M_{21} = M \text{ (say)}$$

$$\therefore M = \mu_r \mu_0 n_1 n_2 \pi r_1^2 l \quad [1 \text{ M}]$$

**Topic: EMI; Sub-Topic: Mutual induction \_ L-1 \_ Target-2017 \_ XII-CBSE Board Exam \_ Physics**

**(OR)**

The flux linkage through a coil of N turns is proportional to the current through the coil and is expressed as

$$N \cdot \phi_B \propto I$$

or  $N \cdot \phi_B = LI$

where the constant of proportionality L is called self inductance of the coil. [1 M]

Energy stored in an inductor:

For the current I at an instant in a circuit containing an inductor, the rate of work done is

$$\frac{dW}{dt} = |\varepsilon| \cdot I, \text{ where } \varepsilon \text{ is self induced emf.}$$

If we ignore the resistive losses and consider only the inductive effect, then using

$$\varepsilon = -L \frac{dI}{dt}, \text{ we get}$$

$$\frac{dW}{dt} = LI \cdot \frac{dI}{dt}$$

or,  $dW = LI \cdot dI$

$\therefore$  Total amount of work done in establishing the current I is

$$W = \int dW = \int_0^I LI dI = \frac{1}{2} LI^2$$

Thus, the energy required to build up the current I is

$$W = \frac{1}{2} LI^2$$

This energy is stored as magnetic potential energy in the Inductor.

Thus, energy stored,  $U = \frac{1}{2} LI^2$  [2 M]

**Topic: EMI; Sub-Topic: Self induction \_ L-1 \_ Target-2017 \_ XII-CBSE Board Exam \_ Physics**



17. (a) The metre bridge works on the principle of balanced condition of wheatstone bridge. [1 M]

(B) According to the problem;  $\frac{R}{S} = \frac{l_1}{100-l_1}$  .....(i) [0.5 M]

Now, when X is connected in parallel with S, the effective resistance of this pair becomes  $\frac{S.X}{S+X}$

$\therefore$  we get  $\left(\frac{S.X}{S+X}\right) = \frac{l_2}{100-l_2}$  .....(ii) [0.5 M]

$\therefore$  Dividing eq. (i) by (ii) we, get

$$\frac{X}{S+X} = \frac{l_1}{l_2} \left( \frac{100-l_2}{100-l_1} \right)$$

or  $l_2(100-l_1)X = l_1(100-l_2)(S+X)$

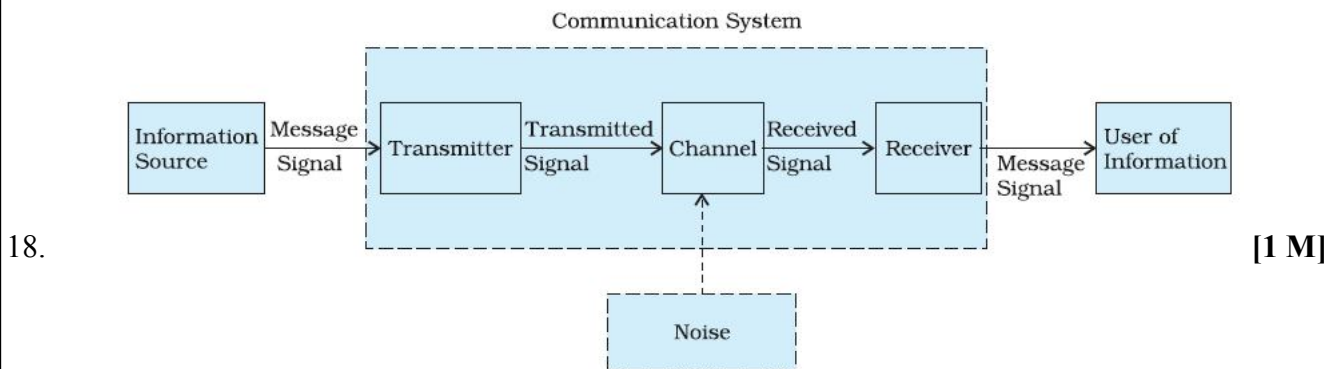
or  $\{l_2(100-l_1)-l_1(100-l_2)\}X = l_1(100-l_2)S$  [0.5 M]

or  $(l_2-l_1) \times (100X) = l_1(100-l_2)S$

or  $X = \frac{l_1(100-l_2)}{100(l_2-l_1)}S$

where  $l_1$  and  $l_2$  are in centimetres [0.5 M]

Topic:Current electricity; Sub-Topic:Meter bredge L-2 Target-2017 XII-CBSE Board Exam Physics

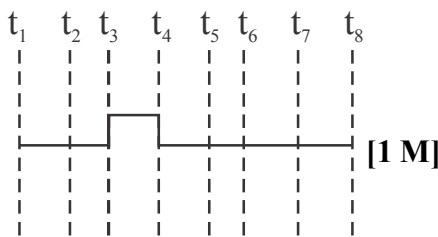


- (a) **Transmitter** : A transmitter processes the incoming message signal so as to make it suitable for transmission through a channel and subsequent reception.
- (b) **Channel** : The function of channel is to provide a physical medium for the transmitted signal to move from transmitter to receiver. Thus, a channel connects the transmitter to a receiver.
- (c) **Receiver**: A receiver extracts the desired message signals from the recived signals at the channel output. [2 M]

Topic:Communication system; Sub-Topic:Basic communication system L-1 Target-2017 XII-CBSE Board Exam Physics

19. (a) **Emitter** : It supplies a large number of majority carriers for the current flow through the transistor.  
**Base** : The thin base allows most of the majority charge carriers coming from emitter to appear in the base-collector junction.  
**Collector** : This segment collects major portion of the majority carriers supplied by the emitter. [1 M]

(b) Output waveform will be as follows :

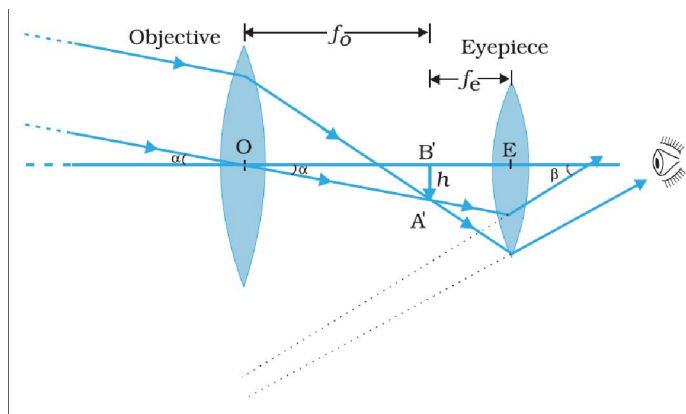


A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

Truth table of AND gate [1 M]

*Topic: Semi conductor electronics; Sub-Topic: Logic gates\_L-1\_Target-2017\_ XII-CBSE Board Exam\_Physics*

20. (a)



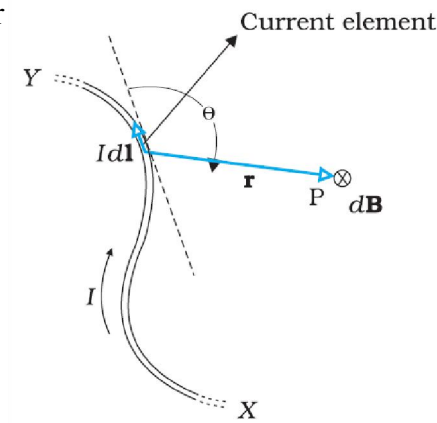
[1 M]

*Topic: Ray optics; Sub-Topic: Telescope\_L-1\_Target-2017\_ XII-CBSE Board Exam\_Physics*

- (b) For a telescope, lens  $L_1$  is chosen as objective, as its aperture and focal length are largest. [1 M]  
 The lens  $L_3$  is chosen as eyepiece as its focal length is smallest. [1 M]

*Topic: Ray optics; Sub-Topic: Telescope\_L-2\_Target-2017\_ XII-CBSE Board Exam\_Physics*

21. (a) According to Biot-Savart's law, the magnitude of the magnetic field  $d\vec{B}$  due to a small element of length 'dl' of a current carrying wire at a point P, is proportional to the current I, the element length dl and is inversely proportional to the square of the distance r. It is also proportional to  $\sin \theta$  where  $\theta$  is angle between  $\vec{dl}$  and  $\vec{r}$



Its direction is perpendicular to the plane containing  $\vec{dl}$  and  $\vec{r}$ .

In vector form

$$d\vec{B} \propto \frac{I \vec{dl} \times \vec{r}}{r^3}$$

$$\text{or, } d\vec{B} = \frac{\mu_0}{4\pi} \cdot \frac{I \vec{dl} \times \vec{r}}{r^3}$$

( $\vec{dl}$  is directed along the length of the wire in the direction of current and  $\vec{r}$  is the vector joining the centre of current element to the point P) [1 M]

**Topic: Moving charges and magnetism; Sub-Topic: Biot-Savart law \_L-1\_ Target-2017\_ XII-CBSE Board Exam \_Physics**

(b) Field due to current in coil P, is

$$\vec{B}_2 = \frac{\mu_0 I_1}{2R} \cdot \hat{k}$$

(Assuming current to be anticlockwise as seen from +ve z-axis)

and that due to current in coil Q is

$$\vec{B}_2 = \frac{\mu_0 I_2}{2R} \hat{i}$$

(Assuming current to be anticlockwise as seen from positive  $x$ -axis.)

$$\therefore \text{ net field } \vec{B} = \vec{B}_1 + \vec{B}_2$$

$$\therefore \vec{B} = \left( \frac{\mu_0 I_1}{2R} \right) \hat{k} + \left( \frac{\mu_0 I_2}{2R} \right) \hat{i}$$

$$\because I_1 = 1A \text{ and } I_2 = \sqrt{3} A$$

$$= \left( \frac{\mu_0}{2R} \right) \hat{k} + \left( \frac{\sqrt{3} \mu_0}{2R} \right) \hat{i}$$

[1 M]

{all units are in S.I.}

$$\therefore |\vec{B}| = \sqrt{\left( \frac{\mu_0}{2R} \right)^2 + \left( \frac{\sqrt{3} \mu_0}{2R} \right)^2}$$

$$= \frac{\mu_0}{2R} \sqrt{1+3}$$

$$= \frac{\mu_0}{2R} \times 2$$

$$\therefore |\vec{B}| = \frac{\mu_0}{R}$$

[0.5 M]

The field is directed in XZ plane. Let  $\theta$  be the angle of  $\vec{B}$  with positive  $x$ -axis.

$$\text{than } \tan \theta = \left( \frac{\mu_0}{2R} \right) / \left( \sqrt{3} \frac{\mu_0}{2R} \right)$$

$$\text{or, } \tan \theta = \frac{1}{\sqrt{3}}$$

$$\Rightarrow \theta = 30^\circ$$

Thus  $\vec{B}$  is directed in XZ -plane making an angle of  $30^\circ$  with x-axis. [0.5 M]

*Topic: Moving charges and magnetism; Sub-Topic: Application of Biot-Savart law \_L-2\_ Target-2017\_ XII-CBSE Board Exam \_Physics*

22. Let C be the capacitance of each capacitor.  
With switch S closed, the two capacitors are in parallel.  
 $\therefore$  equivalent capacitance is  $2C$ .

$$\therefore \text{Energy stored} = \frac{1}{2}(2C)V^2$$

$$\text{or } U_1 = CV^2 \dots (i) \quad \text{[0.5 M]}$$



Now, when switch is opened and then free space of capacitors are filled with dielectric, the capacitance of each capacitor will be  $KC$ . For capacitor B, the charge will remain same as before and for A, the potential difference will remain same.

Charge on each capacitor in the previous case will be  $CV$

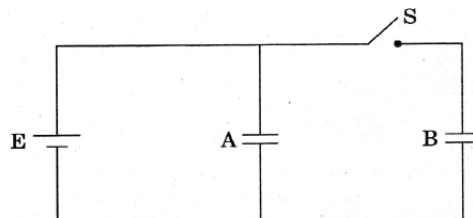
$$\therefore \text{Energy stored in capacitor A in current case is } U_A = \frac{1}{2}(KC)V^2 = \frac{1}{2}KCV^2 \text{ and that in capacitor B, is}$$

$$U_B = \frac{Q^2}{2KC} = \frac{(CV)^2}{2KC} = \frac{1}{2K}CV^2 \quad \text{[1 M]}$$

$\therefore$  Total energy stored,

$$U_2 = U_A + U_B$$

$$\text{or, } U_2 = \frac{1}{2}KCV^2 + \frac{1}{2K}CV^2$$



$$\text{or, } U_2 = \frac{1}{2} \left( K + \frac{1}{K} \right) CV^2$$

$$\text{or, } U_2 = \left( \frac{K^2 + 1}{2K} \right) CV^2 \dots (ii) \quad [1 \text{ M}]$$

$$\therefore \frac{U_1}{U_2} = \frac{CV^2}{\left( \frac{K^2 + 1}{2K} \right) CV^2} \quad \{ \text{Using eq. (i) and (ii)} \}$$

$$\text{or, } \frac{U_1}{U_2} = \frac{2K}{K^2 + 1} \quad [0.5 \text{ M}]$$

**Topic: Electrostatic potential & capacitance ; Sub-Topic: Energy stored in capacitors\_L-2\_Target-2017\_XII-CBSE Board Exam\_Physics**

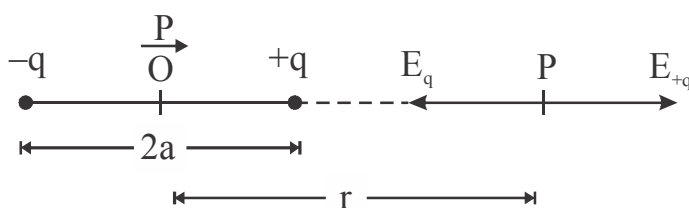
**SECTION - D**

23. (a) It was a nuclear reactor. The cause of disaster was human error which bypassed the safety procedure. [1 M]
- (b) Energy released due to uncontrolled chain reaction which led to production of excessive heat due to which water converted into pressurised steam and blast occurred. [1.5 M]
- (c) Asha had in depth knowledge of nuclear reaction. She was aware about the accident her mom was very compassionate and caring lady. [1.5 M]

**Topic: Nuclei; Sub-Topic: Nuclear reactor\_L-1\_Target-2017\_XII-CBSE Board Exam\_Physics**

**SECTION - E**

24. (a) Electric field at an axial point of an electric dipole.  
As shown in figure, consider an electric dipole consisting of charges +q and -q, separated by distance 2a and placed in vacuum. Let P be a point on the axial line at distance r from the centre O of the dipole on the side of the charge +q.



[1 M]

Electric Field at an axial point of dipole

Electric field at an axial point of dipole

$$\vec{E}_{-q} = \frac{-q}{4\pi\epsilon_0 (r + a)^2} \hat{p} \quad (\text{towards left})$$

where  $\hat{p}$  is a unit vector along the dipole axis from -q to +q.

Electric field due to charge +q at point P is

$$\vec{E}_{+q} = \frac{q}{4\pi\epsilon_0 (r - a)^2} \hat{p} \quad (\text{towards right})$$

Hence the resultant electric field at point P is

$$\begin{aligned}\vec{E}_{axial} &= \vec{E}_{+q} + \vec{E}_{-q} \\ &= \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{(r-a)^2} - \frac{1}{(r+a)^2} \right] \hat{p} \\ &= \frac{q}{4\pi\epsilon_0} \cdot \frac{4ar}{(r^2 - a^2)^2} \hat{p}\end{aligned}$$

or 
$$\vec{E}_{axial} = \frac{1}{4\pi\epsilon_0} \cdot \frac{2ar}{(r^2 - a^2)^2} \hat{p}$$

Here  $p = q \times 2a =$  dipole moment

For  $r \gg a$ ,  $a^2$  can be neglected compared to  $r^2$ .

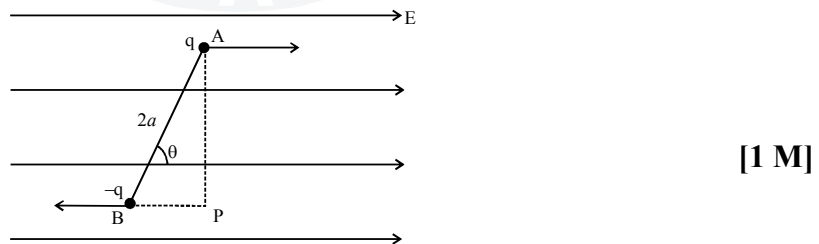
$$\vec{E}_{axial} = \frac{1}{4\pi\epsilon_0} \cdot \frac{2p}{r^3} \hat{p} \quad (\text{towards right}) \quad [1 \text{ M}]$$

Topic:Electrostatic charges; Sub-Topic:Dipole\_L-1\_Target-2017\_XII-CBSE Board Exam\_Physics



Topic:Electrostatic charges; Sub-Topic:Dipole\_L-1\_Target-2017\_XII-CBSE Board Exam\_Physics

(c) Expression for Torque for a Dipole Placed in a Uniform Electric Field:



Consider a dipole AB placed in a uniform electric field of intensity E.

$\therefore$  The force on A is  $+q\vec{E}$  and on B is  $-q\vec{E}$ . These two forces are separated by distance  $2a \sin \theta$ . This constitute a couple,

According to definition of torque of a couple,

$$\tau = qE \times 2a \sin \theta$$

$\therefore$   $\tau = pE \sin \theta$  In vector form  $\vec{\tau} = \vec{p} \times \vec{E}$

**Case - I:** For stable equilibrium  $\theta$  should be  $= 0^\circ$  in that case  $\tau$  is zero

**Case - II:** For unstable equilibrium  $\theta$  should be  $= 180^\circ$  in that case  $\tau$  is  $-pE$  [1 M]

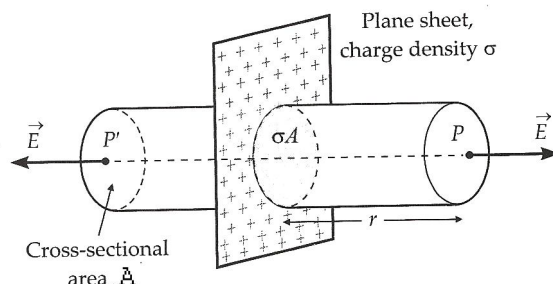
Topic:Electrostatic charges; Sub-Topic:Torque acting on dipole\_L-1\_Target-2017\_XII-CBSE Board Exam\_Physics

(OR)

(a) **Electric field due to uniformly charged infinite plane sheet**

Apply Gauss's theorem to calculate electric field due to an infinite plane sheet of charge.

Electric field due to a uniformly charged infinite plane sheet. As shown in figure, consider a thin, infinite plane sheet of charge with uniform surface charge density  $\sigma$ . We wish to calculate its electric field at a point P at distance r from it. [1 M]



[0.5 M]

Gaussian surface for a uniformly charged infinite plane sheet.

By symmetry, electric field E points outwards normal to the sheet. Also, it must have same magnitude and opposite direction at two points P and P' equidistant from the sheet and on opposite sides. We choose cylindrical Gaussian surface of cross-sectional area A and length 2r with its axis perpendicular to the sheet.

As the lines of force are parallel to the curved surface of the cylinder, the flux through the curved surface is zero. The flux through the plane-end faces of the cylinder is

$$\phi_E = EA + EA = 2EA$$

Charge enclosed by the Gaussian surface,

$$q = \sigma A$$

According to Gauss's theorem,

$$\phi_E = \frac{q}{\epsilon_0}$$

$$\therefore 2EA = \frac{\sigma A}{\epsilon_0} \text{ or } E = \frac{\sigma}{2\epsilon_0}$$

[1.5 M]

**Topic: Electrostatic charges; Sub-Topic: Application of Gauss's theorem\_L-2\_Target-2017\_XII-CBSE Board Exam\_Physics**

(b) Let P be a point at distance r from the sheet.

The required work done to bring point charge 'q' from infinity to P, is

$$W = q \cdot (V_P - V_\infty) \quad \dots\dots(i)$$

$$\text{Now, } V_P - V_\infty = -\int_\infty^r \vec{E} \cdot \vec{dr} = -\int_\infty^r E dr = -\int_\infty^r \left( \frac{\sigma}{2\epsilon_0} \right) \cdot dr \quad [1.5 M]$$

$\left\{ \begin{array}{l} \therefore \text{Field in front of an infinitely large plane sheet} \\ \text{of charge is uniform and is given by } \frac{\sigma}{2\epsilon_0} \end{array} \right\}$

$$-\frac{\sigma}{2\epsilon_0} \int_{\infty}^r dr = -\frac{\sigma}{2\epsilon_0} \cdot [r]_{\infty}^r$$

$$-\frac{\sigma}{2\epsilon_0} (r - \infty) = \infty$$

$$\text{or, } V_p - V_{\infty} = \infty$$

$$\therefore \text{ from eq. (i), } W = \infty$$

[1 M]

**Topic:Electrostatic potential & capacitance; Sub-Topic:Electric potential\_L-3\_Target-2017\_XII-CBSE Board Exam\_Physics**

25. (a) Device is capacitor [0.5 M]

(b)  $B \rightarrow$  Voltage (Because it is sine wave)

$C \rightarrow$  Current (Because current leads voltage by  $\pi/2$ )

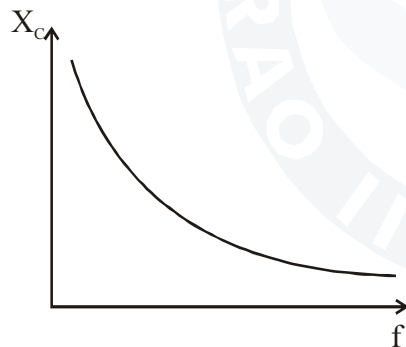
$A \rightarrow$  Power (Average power over one cycle is zero)

[1 M]

(c)  $X_C = \frac{1}{\omega C}$

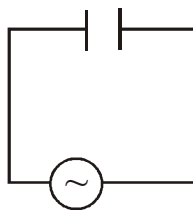
$$X_C = \frac{1}{2\pi fC}$$

[1 M]



[1 M]

(d)



$$V = v_0 \sin \omega t$$

[1 M]

$$C = \frac{q}{v}$$

$$q = Cv_0 \sin \omega t$$

$$i = \frac{dq}{dt} = \frac{d}{dt}(Cv_0 \sin \omega t)$$

$$= \omega Cv_0 \sin \omega t$$



$$= \frac{v_0}{\frac{1}{\omega C}} \cos \omega t$$

$$i = \frac{v_0}{X_C} \sin \left( \omega t + \frac{\pi}{2} \right)$$

$$i = i_0 \sin \left( \omega t + \frac{\pi}{2} \right)$$

In pure capacitive circuit current leads voltage by  $\frac{\pi}{2}$  [1.5 M]

*Topic:AC; Sub-Topic:AC applied to capacitor\_L-2\_Target-2017\_XII-CBSE Board Exam\_Physics*

(OR)

- (a) An ac generator converts mechanical energy into electrical energy. It consists of a coil mounted on a rotar shaft. The axis of rotation of coil is perpendicular to magnetic field and the coil (armature) is mechanically rotated in magnetic field. Rotation causes magnetic flux hence an emf is induced in coil. Let  $\omega$  be angular velocity and  $\theta$  be the angle between magnetic field and area vector, then  $\theta = \omega t$ , hence flux is,

$$\Phi_B = BA \cos \theta \quad [1 M]$$

$$= -NAB \frac{d}{dt} (\cos \omega t)$$

Thus instantaneous emf is,

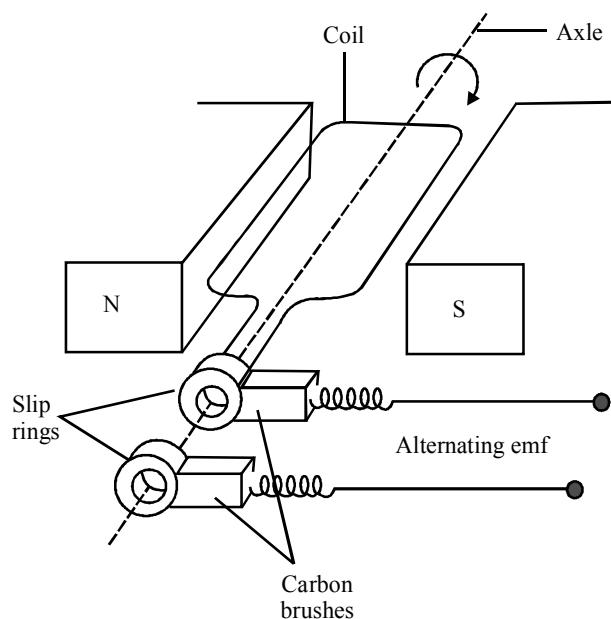
$$\varepsilon = NBA\omega \sin \omega t$$

If  $NAB\omega = \varepsilon_0$  then

$$\varepsilon = \varepsilon_0 \sin \omega t$$

Sine function varies between  $\pm 1$  and emf for  $\theta = 0^\circ$  to  $\theta = 270^\circ$

The direction of current changes periodically hence called alternating current.



[1.5 M]

*Topic:EMI; Sub-Topic:AC Generator\_L-2\_Target-2017\_XII-CBSE Board Exam\_Physics*

(b)  $e = Blv \sin \theta$

**Given:**  $B = 0.3 \times 10^{-4} \text{ wb/m}^2$  [0.5 M]

$v = 5 \text{ m/s}$

$l = 10 \text{ m}$

$\theta = 90^\circ$

$e = Blv \sin \theta$

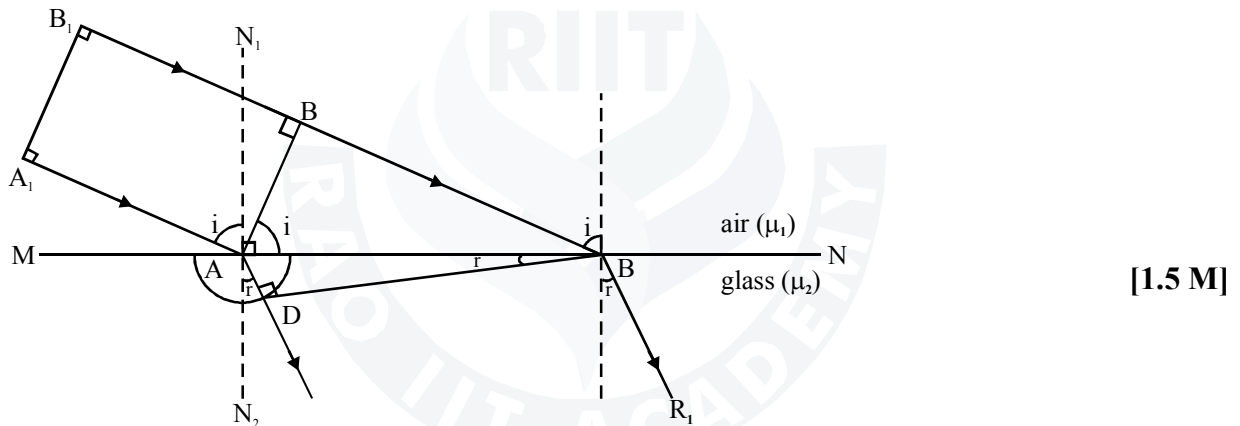
$= 0.3 \times 10^{-4} \times 10 \times 5 \times \sin 90^\circ$  [1.5 M]

$e = 15 \times 10^{-4} \text{ V}$

$e = 1.5 \times 10^{-3} \text{ V} = 1.5 \text{ mV}$  [0.5 M]

**Topic:EMI; Sub-Topic:Faraday's law of emi\_L-2\_Target-2017\_XII-CBSE Board Exam\_Physics**

26. (a) **Wave front:-** Wave front is locus of all the points where reaches at same time in same phase. [0.5 M]



Suppose that a plane wavefront of light is incident at a plane refracting surface MN separating two media. Let  $A_1B_1$  and  $AB$  be the successive positions of the incident wavefront.  $A_1A$  and  $B_1B$  the corresponding rays. When the wavefront reaches the point A, it becomes a secondary source and emits secondary waves in the second medium. Let  $V_1$  and  $V_2$  be the speed of light in the medium one (say a rarer medium of R.I.  $\mu_1$ ) and the medium two (a denser medium of R.I.  $\mu_2$ ) respectively. If  $t$  is the time taken by the incident ray to cover the distance  $BC$ , then  $BC = V_1 t$ . During this time, the secondary waves originating at A cover a distance  $V_2 t$  in the denser medium. Therefore, the secondary spherical wavelet has radius  $V_2 t$  in the denser medium two (a denser medium) respectively. If  $t$  is the time taken by the incident ray to cover the distance  $BC$ , then  $BC = V_1 t$ . During this time, the secondary waves originating at A cover a distance  $V_2 t$  in the denser medium. Therefore, the secondary spherical wavelet has a radius  $V_2 t$ . With A as the centre, draw a hemisphere of radius  $V_2 t$  in the denser medium. It represents the secondary wavelet. According to Huygens's principle locus of tangent to all secondary wavelets represent new wave front. Draw a tangent  $CD$  to the secondary wavelet. As the points C & D are in the same phase of wave motion,  $CD$  represents the refracted wavefront in denser medium. It moves parallel to itself taking successive positions  $C_1D_1, C_2D_2$ , etc.  $AD_2$  and  $CC_2$  represents the corresponding refracted rays. Draw  $PAQ$  normal to  $MN$ .

Now,  $\angle A_1AP = i =$  angle of incidence &  $\angle QAD = r =$  angle of refraction

Also, from the figure,  $\angle BAC = i$  and  $\angle ACD = r$

From the triangles  $\triangle BAC$  &  $\triangle ACD$

$$\sin i = \frac{BC}{AC} \text{ \& \ } \sin r = \frac{AD}{AC}, \quad \text{Let } \mu = \frac{\mu_2}{\mu_1} \therefore \text{Refractive index } \mu = \frac{\sin i}{\sin r} = \frac{BC/AC}{AD/AC} = \frac{BC}{AD} \quad \dots(1)$$

$$\therefore \text{Refractive index } \mu = \frac{V_1 t}{V_2 t}$$

$$\therefore \mu = \frac{V_1}{V_2} \quad \dots\dots\dots(2)$$

$$\therefore \text{Refractive index of medium 2 w.r.t. 1} = \frac{\text{speed of light in medium 1}}{\text{speed of light in medium 2}}$$

= constant for given pair of media & given frequency.

From equation (1) and (2)

$$\frac{\sin i}{\sin r} = \frac{\mu_2}{\mu_1}$$

Thus Snell's law can be proved using Huygens' principle.

[2 M]

**Topic:Wave optics; Sub-Topic:Refraction of plane wave from L-1 Target-2017 XII-CBSE Board Exam Physics**

(b) According to Brewster's Law

$$\tan i_p = \mu$$

$$i_p = \tan^{-1}(\mu)$$

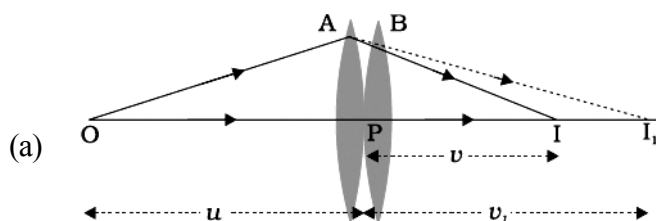
$$i_p = \tan^{-1}(1.5)$$

$$\boxed{i_p = 56.30^\circ}$$

[1 M]

**Topic:Wave optics; Sub-Topic:Polarisation L-1 Target-2017 XII-CBSE Board Exam Physics**

(OR)



[1 M]

Consider two lenses placed close to each other. The focal lengths of lens 1 and 2 is  $f_1$  and  $f_2$  respectively.

For Lens 1

$$\frac{1}{v'} - \frac{1}{u} = \frac{1}{f_1} \quad \dots(i)$$

For Lens 2

$$\frac{1}{v} - \frac{1}{v'} = \frac{1}{f_2} \quad \dots(\text{ii})$$

Adding (i) and (ii)

$$\frac{1}{v'} - \frac{1}{u} + \frac{1}{v} - \frac{1}{v'} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f_1} + \frac{1}{f_2}$$

Since,  $\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$  [1 M]

then,  $\frac{1}{f_T} = \frac{1}{f_1} + \frac{1}{f_2}$

$P = P_1 + P_2 + P_3 + \dots$  total power

$f_T \rightarrow$  Total new focal length of the combination.

**Power of Lens**

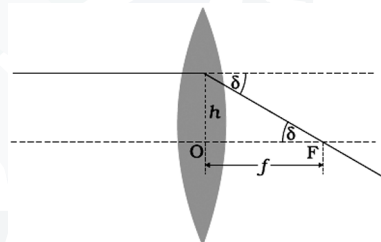
Power of lens is defined as the total tangent of the angle by which it converges or diverges a beam of light falling at unit distance from the optical centre.

$$\tan \delta = \frac{h}{f}$$

If,  $h = 1$ , then

$$\tan \delta = \frac{1}{f} \quad (\text{or}) \quad P = \frac{1}{f}$$

SI unit of power is Dioptre.



[1 M]

*Topic: Ray optics; Sub-Topic: Combination of lens \_ L-1 \_ Target-2017 \_ XII-CBSE Board Exam \_ Physics*

- (b) For equilateral prism  $A = 60^\circ$   
for minimum angle of deviation

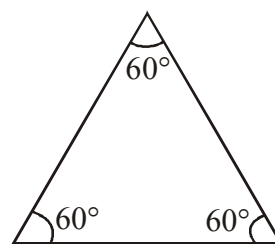
$$i + e = A + \delta_m$$

$$2i = A + \delta_m$$

$$\frac{2 \times 3 A}{4} = A + \delta_m$$

$$\delta_m = \frac{3 A}{2} - A$$

$$\delta_m = \frac{A}{2}$$



$$\mu = \frac{\sin\left(\frac{A + \frac{A}{2}}{2}\right)}{\sin\left(\frac{A}{2}\right)} \quad [1 \text{ M}]$$

$$\mu = \frac{\sin\frac{3A}{4}}{\sin\frac{A}{2}} = \frac{\sin 45^\circ}{\sin 30^\circ} = \frac{0.7071}{0.5}$$

$$= 1.414$$

$$\boxed{\mu = 1.414}$$

$$V = \frac{c}{\mu}$$

$$= \frac{3 \times 10^8}{1.414} = 2.1216 \times 10^8 \text{ m/s} \quad [1 \text{ M}]$$

*Topic: Ray optics; Sub-Topic: Prism\_L-2\_Target-2017\_XII-CBSE Board Exam\_Physics*