ICSE Paper 2008

MATHEMATICS

SECTION A [40 MARKS]

(Answer all questions from this Section.)

Question 1.

а<u>с</u>

- (a) The simple interest on a sum of money for 2 years at 4% per annum is ₹ 340.
 Find :
 - (i) the sum of money and
 - (ii) the compound interest on this sum for one year payable half yearly at the same rate.
 [3]

(b) If
$$\frac{8a-5b}{8c-5d} = \frac{8a+5b}{8c+5d}$$
, prove that $\frac{a}{b} = \frac{c}{d}$ [3]

(c) If
$$(x-2)$$
 is a factor of $2x^3 - x^2 - px - 2$

(i) find the value of p.

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(ii) with the value of p, factorize the above expression completely. [4] Solution.

(a) (i) Given : S.I. = ₹340, T = 2Years, R = 4%, P = ?

S.I. =
$$\frac{P \times R \times T}{100}$$

P = $\frac{S.I. \times 100}{R \times T} = \frac{340 \times 100}{4 \times 2}$
= ₹4250

Ans.

(ii) Given : T = 1 Years = $1 \times 2 = 2$ times, R = 4%, $\Rightarrow R = 2\%$ (for half yearly.)

C.I. = P
$$\left[\left(1 + \frac{R}{100} \right)^{T} - 1 \right]$$

= 4250 $\left[\left(1 + \frac{2}{100} \right)^{2} - 1 \right]$
= 4250 $\left[\frac{101}{2500} \right] = ₹ 171.70$ Ans.

(b) Given:

⇒

$$\frac{8a+5b}{8c+5d} = \frac{8a-5b}{8c-5d}$$

$$\frac{8a+5d}{8a-5b} = \frac{8c+5d}{8c-5d}$$
(Apply alternendo)
$$\frac{8a+5b+8a-5b}{8a+5b-8a+5b} = \frac{8c+5d+8c-5d}{8c+5d-8c+5d}$$
(Apply componendo and dividendo rule)
$$\frac{169}{10b} = \frac{16}{10}\frac{c}{d}$$

 $\frac{a}{b} = \frac{c}{d}$

Proved

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(c) (x-2) is a factor of $2x^3 - x^2 - px - 2$ (i) $\Rightarrow x = 2$ will satisfy this equation. $2 \cdot 2^3 - 2^2 - 2p - 2 = 0$ ⇒ 16 - 4 - 2p - 2 = 0 \Rightarrow 10-2p = 0 $2x^2 + 3x + 1$ 2p = 10⇒ $(x-2)(2x^3-x^2-5x-2)$ $2x^3 - 4x^2$ ⇒ p = 5Ans. + (ii) On dividing $2x^3 - x^2 - 5x - 2$ by x - 2, $3x^2 - 5x - 2$ we get $3x^2 - 6x$ $(x-2)(2x^2+3x+1)$ \Rightarrow x-2 $(x-2)(2x^2+2x+x+1)$ ⇒ x-2(x-2)(2x(x+1)+1(x+1))⇒ (x-2)(x+1)(2x+1) \Rightarrow Ans.

Question 2.

(a) Solve the given inequation and graph the solution on the number line.

$$y - 3 < y + 1 \le 4y + 7; y \in R.$$
 [3]

(b) In the given figure, find the area of the unshaded portion within the rectangle.

(Take $\pi = 3.14$) [3]



- (c) A shopkeeper buys a camera at a discount of 20% from the wholesaler, the printed price of the camera being ₹ 1600 and the rate of sales tax is 6%. The shopkeeper sells it to the buyer at the printed price and charges tax at the same rate. Find :
 - (i) The price at which the camera can be bought.

(ii) The VAT (Value Added Tax) paid by the shopkeeper.

[4]

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Solution.

(a) Given :
$$2y-3 < y+1 \le 4y+7, y \in \mathbb{R}$$

 $2y-3 < y+1$
 $\Rightarrow 2y-y < 3+1$
 $\Rightarrow y < 4$
solution set : $\{y \mid y \in \mathbb{R}, -2 \le y < 4\}$
 $-3 -2 -1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5$
(b) Length of rectangle = 15 cm
Breadth of rectangle = 15 × 6
 $= 90 \text{ cm}^2$

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Area of circle =
$$\pi r^2$$

= $3 \cdot 14 \times 9$
= $28 \cdot 26 \text{ cm}^2$.
Area of shaded portion = Area of $2\frac{1}{2}$ circle
= $28 \cdot 26 + 28 \cdot 26 + 14 \cdot 13$
= $70 \cdot 65 \text{ cm}^2$.
Area of unshaded portion in the rectangle = Area of the rectangle
- Area of shaded portion
= $90 - 70 \cdot 65$
= $19 \cdot 35 \text{ cm}^2$ Ans.
(c) (i) Cost of camera for buyer = Printed Price + Sales tax on it
= $1600 + \frac{6}{100} \times 1600$
= $\overline{1696}$ Ans.
(ii) Discount on printed price = $\frac{20}{100} \times 1600 = \overline{1280}$.
Sales tax = $\frac{6}{100} \times 1280 = \overline{1280}$.
Sales tax = $\frac{6}{100} \times 1600 = \overline{196}$.
VAT paid by shopkeeper = $\frac{6}{100} \times 1600 = \overline{1920}$ Ans.

Question 3.

(a) David opened a Recurring Deposit Account in a bank and deposited ₹ 300 per month for two years. If he received ₹ 7725 at the time of maturity, find the rate of interest per annum [3] ~7

(b) If
$$\begin{bmatrix} 1 & 4 \\ -2 & 3 \end{bmatrix} + 2M = 3 \begin{bmatrix} 3 & 2 \\ 0 & -3 \end{bmatrix}$$
, find the Matrix M. [3]

- (c) Use a graph paper for this question. (Take 1 cm = 1 unit on both the axes). Plot the points A (-2, 0), B (4, 0), C (1, 4) and D (-2, 4).
 - Draw the line of symmetry of \triangle ABC. Name it L_1 . (i)
 - Point D is reflected about the Line L_1 to get the image E. Write the (ii) coordinates of E.
 - (iii) Name the figure ABED.
- (iv) Draw all the lines of symmetry of the figure ABED. [4] Solution.

(a) Given : Deposited per month (P) = $\mathbf{\overline{x}}$ 300, n = 2 Year = 24 months, Amount = ₹7725, R = ?

Principal equivalent to 1 month =
$$P \times \frac{n(n+1)}{2} = \frac{300 \times 24 \times 25}{2}$$

= $300 \times 12 \times 25 = ₹ 90,000$
A = P + SI
 \Rightarrow 7725 = $24 \times 300 + \frac{90000 \times R \times 1}{12 \times 100}$



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Date	Particulars	Withdrawals (in ₹)	Deposits (in ₹)	Balance (in ₹)	
Jan 3, 07	B/F		5.04 <u>8-0</u> 70-3 3 0	2642.00	
Jan 16	To Self	640.00		2002.00	
March 5	By Cash	1 <u> </u>	850.00	2852.00	
April 10	To Self	1130.00		1722.00	
April 25	By Cheque	—	650.00	2372.00	
June 15	By Cash	577.00		1795.00	

Calculate the interest from January 2007 to June 2007 at the rate of 4% per annum. [4]

Solution.

sin 25° cos 25° (a) Given : sec 65° + cosec 65° $= \sin 25^{\circ} \cos 65^{\circ} + \cos 25^{\circ} \sin 65^{\circ}$ $= \sin 25^{\circ} \cos (90^{\circ} - 25^{\circ}) + \cos 25^{\circ} \sin (90^{\circ} - 25^{\circ})$ = sin 25° sin 25° + cos 25° cos 25° $= \sin^2 25^\circ + \cos^2 25^\circ = 1$ $(: \sin^2 \theta + \cos^2 \theta \approx 1)$ Ans. (b) (i) $\angle BCE = \angle BAD = 80^{\circ}$ ('.' ext. of cyclic quad. is equal to opp. int. angle.) $\angle CAD = \angle BAD - \angle BAC = 80^\circ - 25^\circ = 55^\circ$ \Rightarrow Ans. (ii) $\angle CBD = \angle CAD$ (. Angle of the same segment are equal.) ≂ 55° Ans. (iii) AB || DC (given) $\angle BAD + \angle ADC = 180^{\circ}$ $(25 + 55) + \angle ADC = 180^{\circ}$ ⇒ $= 180 - 80 = 100^{\circ}$ (... ABCD is cyclic quad.) Ans. (c) Minimum Balance for January = ₹ 2,002 Minimum Balance for February = **₹** 2,002 Minimum Balance for March $= \mathbf{Z}$ 2,852 含 Minimum Balance for April = **₹** 1,722 Minimum Balance for May = ₹ 2,372 Minimum Balance for June = ₹ 1,795 Total = 🕇 12,745 S.I. = $\frac{P \times R \times T}{100}$ $=\frac{12745\times4\times1}{100\times12}$ = ₹42·48 Ans.

SECTION B [40 Marks]

Answer any Four Questions in this Section.

Question 5.

(a) A function in x is defined as : *

$$f(x) = \frac{x+2}{2x-1}; x \in R \text{ and } x \neq \frac{1}{2},$$

Find: (i) $f(-3),$
(ii) $f(x-1),$
(iii) $x \text{ if } f(x) = 1.$ [3]

(b) Prove the identity:
$$\frac{\sin A}{1 + \cos A} = \csc A - \cot A.$$
 [3]

(ii) In what ratio is the line joining AB, divided by the x-axis? [4] Solution.

(b)

L.H.S. =
$$\frac{\sin A}{1 + \cos A}$$

= $\frac{\sin A}{1 + \cos A} \times \frac{1 - \cos A}{1 - \cos A}$
= $\frac{\sin A (1 - \cos A)}{1 - \cos^2 A}$
= $\frac{\sin A (1 - \cos A)}{\sin^2 A}$
= $\frac{1}{\sin A} - \frac{\cos A}{\sin A}$
= $\csc A - \cot A = R.H.S.$

1

 \Rightarrow

Proved

Ans.

(c) (i) Given : A = (-4, 3), B = (8, -6)

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

= $\sqrt{(8 + 4)^2 + (-6 - 3)^2}$
= $\sqrt{144 + 81}$
= $\sqrt{225} = 15.$

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(ii) Let any point on x-axis will be P(x, 0).

$$x = \frac{mx_1 + nx_2}{m + n},$$

$$y = \frac{my_1 + ny_2}{m + n},$$

$$0 = \frac{m \cdot 3 + n \cdot (-6)}{m + n},$$

$$\Rightarrow \quad 3m = 6n,$$

$$\Rightarrow \qquad \frac{m}{n} = \frac{6}{3} = \frac{2}{1},$$

The ratio will be 2 : 1.

Ans.

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Question 6.

(a) Solve the following quadratic equation for x and give your answer correct to two decimal places :

$$5x(x+2) = 3$$

(b) In the figure given alongside PQ = QR, \angle

 $RQP = 68^\circ$, PC and CQ are tangents to the

circle with centre O. Calculate the values of :

- (i) $\angle QOP$,
- ∠QCP.
- (ii) [3] (c) A company with 4000 shares of nominal value of ₹ 110 each declares an annual dividend of 15%. Calculate :
 - The total amount of dividend paid by the company. (i)
 - (ii) The annual income of Shah Rukh who holds 88 shares in the company.
 - (iii) If he received only 10% on his investment, find the price Shah Rukh paid for each share. [4]

Solution.

(a) Given :

Hence

$$5x (x + 2) = 3$$

$$5x^2 + 10x - 3 = 0$$

Camparing with $ax^2 + bx + c = 0$, we get a = 5, b = 10 and c = -3.

We know that

$$= \frac{2a}{10 \pm \sqrt{(10)^2 - 4 \times 5 \times (-3)}}{2 \times 5}$$

$$= \frac{-10 \pm \sqrt{100 + 60}}{10}$$

$$= \frac{-10 \pm 4\sqrt{10}}{10} = \frac{-5 \pm 2\sqrt{10}}{5}$$

$$= \frac{-5 \pm 2 \times 3 \cdot 16}{5} = \frac{-5 \pm 6 \cdot 32}{5}$$
Hence
$$x = 0.26 \text{ or } -2.26.$$
(b) Given : PQ = QR, \angle RQP = 68°

 $-b \pm \sqrt{b^2 - 4ac}$

(i) In
$$\triangle$$
 PQR, PQ = RQ
 $\therefore \qquad \angle PRQ = \angle QPR$
 $\Rightarrow \qquad \angle PRQ + \angle QPR + 68^\circ = 180^\circ \quad [sum of the angle of a $\triangle is 180^\circ]$
 $\Rightarrow \qquad 2 \angle PRQ = 180 - 68 = 112^\circ$
 $\Rightarrow \qquad \angle PRQ = 56^\circ$
 $\therefore \qquad \angle QOP = 2 \times \angle PRQ$
[angle at centre of the circle is twice the
angle of at the remaining circumference]
 $= 2 \times 56 = 112^\circ$ Ans.$



Ans.

· (ii)	0yearsquestion	2 <u>1</u>	" Mathematics, 2	008 563
(ii)		22 O 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		1 000
		$PQC = \angle PRG$	•	
A.)		$PC = \angle PRG$	No.	
		$PQC = \angle QPC$	C = 56°	
<u></u>	A success of Constants of the	24 7 .2		
1		STATES STATES		
=	, Zi	$QCP = 180^\circ -$	56° – 56°	G
60 - 61 <u>11</u> 1		= 68°	1 1 150	Ans.
(c) Given	No. of shares = 4000, N			
(i)	Dividend on	$1 \text{ share } = \frac{16}{10}$	$\frac{5}{0} \times 110$	
		= ₹1	16-50	
	Total	lividend = 40	00×16.50	
		= ₹6	56000 ·	Ans.
(ii)	Income on 8	8 shares = 88	× 16·50	
		= ₹1	1,452	
	Annual income of Sha	ih Rukh 😑 🖣 🛛	1,452.	Ans.
(iii)	Let his inv	estment = x		13
		$\frac{10}{100} \times x = ₹1$	1459	
		100		
		$x = \mathbf{R}$		12
	Price for ea	$h \text{ share } = \frac{14}{3}$	<u>1520</u> = ₹ 165.	Ans.
			88	
Question '		c.11. **	د	80
	come of Mr. Bachhan was		00 000 non month	
	nic Salary Arness Allowance		20,000 per month 12,000 per month	
	erest from Bank		16,000 for the whole ye	ar.
Saving	26.5	9394 SU20	20,000 /07 0.00 0.000 /07	
	tribution towards Provid	ent Fund : 15	5% of Basic salary	
	tional Savings Certificate		40,000	
• Cor	atribution towards LIC pr	emium : 🕄	30,000 per year	
Donat				-1.00 m
	National Defence Fund			
	um of 🖣 3,000 was deduc			
김 씨는 아이가 아이가 있는 것이 같아.	for the first 11 months o		ulate the tax Mr. Bach	
21 - 10 10 10 - 10 - 11 - 10 - 11	the last month of the find	ncial year :		[6]
Tax sl			to.	
	1,00,000	: No tax.		
	₹ 1,00,001 to ₹ 1,50,000	· · · · · · · · · · · · · · · · · · ·	ie income exceeding 🖣 1	10-10-10 (10-10-10-10-10-10-10-10-10-10-10-10-10-1
From	₹ 1,50,001 to ₹ 2,50,000	: ₹ 5,000+ ₹ 1,50,00	- 20% of the income 10	exceeding
Above	₹2,50,000	: ₹25,000 ₹2,50,00	+ 30% of the income	exceeding
Dodui	tions against savings		aximum amount of ₹1	.00.000
-	5 0. 3 500	(3)		,,
	tion Cess	. 2% of the	e tax payable.	

**. Solution has not given due to out of present syllabus.

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- (b) A vertical pole and a vertical tower are on the same level ground. From the top of the pole the angle of elevation of the top of the tower is 60° and the angle of depression of the foot of the tower is 30°. Find the height of the tower if the height of the pole is 20 m.

Solution.

(b) Let h be the height of tower and x be the distance between tower and pole.



Question 8.

(a) Find the H.C.F. of the given polynomials : **

$$x^2 - \frac{1}{a^2}$$
 and $x^2 + \frac{2x}{a} + \frac{1}{a^2}$ [3]

- (b) Using a ruler and a pair of compasses only, construct :
 - (i) A triangle ABC, given AB = 4 cm, BC = 6 cm and $\angle ABC = 90^\circ$.
 - (ii) A circle which passes through the points A, B and C and mark its centre as
 O.
- (c) Points A and B have coordinates (7, -3) and (1, 9) respectively. Find :
 - (i) The slope of AB.
 - (ii) The equation of the perpendicular bisector of the line segment AB.
 - (iii) The value of 'p' if (-2, p) lies on it.

Solution.

(b) Steps of Construction :

- (1) Draw side BAC, 6 cm.
- (2) Draw a $\angle B = 90^\circ$, and cut AB = 4 cm.

(3) Meet AC.

- (4) Draw Bisector of BC and AB. Which meet at point 'O'.
- (5) Now draw a circle as centre 'O'.
- (6) This circle passes through the point A, B, and 'C'.



^{**} Solution has not given due to out of present syllabus.

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(c) (i) Slope of AB
$$(m_1) = \frac{y_2 - y_1}{x_2 - x_1}$$

 $= \frac{9 + 3}{1 - 7} = \frac{12}{-6} = -2$ Ans. A $\begin{pmatrix} 7, -3 \\ -2, 0 \end{pmatrix}$ B $(1, 9)$
(ii) The mid point of line AB = $\begin{pmatrix} x_1 + x_2 & y_1 + y_2 \\ 2 & 2 & 2 \end{pmatrix}$
 $= \begin{pmatrix} 7 \pm 1 & -3 + 9 \\ 2 & 2 & 2 \end{pmatrix}$ (i) The mid point of line AB = $\begin{pmatrix} x_1 + x_2 & y_1 + y_2 \\ 2 & 2 & 2 \end{pmatrix}$
 $= \begin{pmatrix} 7 \pm 1 & -3 + 9 \\ 2 & 2 & 2 \end{pmatrix}$ (ii) The mid point of line AB = $\begin{pmatrix} x_1 + x_2 & y_1 + y_2 \\ 2 & 2 & 2 \end{pmatrix}$
Equation of perpendicular bisector of AB
 $m_2 = \frac{-1}{m_1} = \frac{-1}{-2} = \frac{1}{2}$
Equation of perpendicular bisector
 $y - y_1 = m(x - x_1)$
 $\Rightarrow y - 3 = \frac{1}{2}(x - 4)$
 $\Rightarrow 2y - 6 = x - 4$
 $\Rightarrow x - 2y + 2 = 0$ Ans.
(iii) Given point (-2, p) lies on the equation $x - 2y + 2 = 0$
 $-2 - 2p + 2 = 0$
 $\Rightarrow -2p = 0$
 $\Rightarrow p = 0$ Ans.
Question 9.
(a) Given $A = \begin{bmatrix} p & 0 \\ 2 \end{bmatrix}, B = \begin{bmatrix} 0 & -q \\ 1 & 0 \end{bmatrix}, C = \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix}$ and $BA = C^2$.
Find the values of p and q.
(b) In $A ABC, AP : PB = 2 : 3. PO$ is parallel to
BC and is extended to Q so that CQ is
parallel to BA. Find :
(i) Area $AAPO$ area $AABC$.
(ii) Area $AAPO$ area the floor.
(ii) Radius of the floor.
(ii) Height of the tent.
(iii) Length of the canvas required to cover this conical tent if its width is 2 m.
(4)
Solution.
(a) Given: $A = \begin{bmatrix} p & 0 \\ 0 & 2 \end{bmatrix}, B = \begin{bmatrix} 0 & -q \\ 1 & 0 \end{bmatrix}, C = \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix}$
 $BA = C^2$.

566 | ICSE Last 10 Years Solved Papers $\begin{bmatrix} 0 & -q \\ 1 & 0 \end{bmatrix} \begin{bmatrix} p & 0 \\ 0 & 2 \end{bmatrix} = \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix}$ - $\begin{bmatrix} 0 \times p + (-q) \times 0 & 0 \times 0 + (-q) \times 2 \\ 1 \times p + 0 \times 0 & 1 \times 0 + 0 \times 2 \end{bmatrix} = \begin{bmatrix} 2 \times 2 + (-2) \times 2 & 2 \times (-2) + (-2) \times 2 \\ 2 \times 2 + & 2 \times 2 & 2 \times (-2) + & 2 \times 2 \end{bmatrix}$ $\begin{bmatrix} 0 & -2q \\ p & 0 \end{bmatrix} = \begin{bmatrix} 0 & -8 \\ 8 & 0 \end{bmatrix}.$ \Rightarrow \Rightarrow p = 8, q = 4 $\frac{\text{AP}}{\text{PB}} = \frac{2}{3} = \frac{\text{AO}}{\text{OC}}$ Ans. \Rightarrow **(b)** (i) $\frac{AP}{AP + PB} = \frac{2}{2+3}$ $\frac{AP}{AB} = \frac{2}{5}$...(1) ⇒ PO is parallel to BC and CQ is parallel to BA. So, PBCQ is a parallelogram. PB = CQ⇒ $\frac{AP}{PB} = \frac{2}{3} = \frac{AP}{CQ}$ ⇒ In \triangle APO and \triangle ABC, $\angle APO = \angle ABC$ (∵ PO || BC) $\angle A = \angle A$ $\triangle APO \sim \triangle ABC$ $\frac{AO}{AB} = \frac{AO}{AC} =$ 2 5 area of \triangle APO AP² $\frac{1}{\text{area of } \Delta \text{ ABC}} = \frac{1}{\text{AB}^2}$ 1 ⇒ [Ratio between the areas of two similar Δ 's is equal to the ratio between the squares of their corresponding sides] $=\left(\frac{2}{5}\right)^{2}=\frac{4}{25}$ Ans. (vertically opp.) (ii) In \triangle APO and \triangle CQO, $\angle AOP = \angle COQ$ $\angle OAP = \angle OCQ$ $\triangle AOP \sim \triangle COQ$ (By A.A axiom) \Rightarrow $\frac{\text{area of } \Delta \text{ APO}}{\text{area of } \Delta \text{ CQO}} = \frac{\text{AP}^2}{\text{CQ}^2} = \left(\frac{2}{3}\right)^2 = \frac{4}{9}$ Ans. So (c) Given : Volume (V) = 1232 m, Area of base = 154 m^2 Let r be the radius and h be the height. Area = $\pi r^2 = 154$ (i) $\frac{22}{7}r^2 = 154$ $r^2 = 49$ $r = 7 \,\mathrm{m}$ Ans. Volume (V) = $\frac{1}{3}\pi r^2 h = 1232$ (ii) $\frac{1}{3} \times \frac{22}{7} \times (7)^2 \times h = 1232$

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$$h = \frac{1232 \times 3}{22 \times 7} = 24 \text{ m.}$$
 Ans.

(iii) Let l be the slant height of the conical tent, then

$$l = \sqrt{h^2 + r^2} = \sqrt{24^2 + 7^2} = 25m$$
Area of canvas required = Curved surface area of the tent
$$\Rightarrow \text{ Length x width of canvas} = \pi r l \text{ (for tent)}$$

$$\Rightarrow \text{ Length of canvas} \times 2 = \frac{22}{7} \times 7 \times 25$$
Length of canvas = $\frac{550}{2} = 275 \text{ m}$. Ans

Question 10.

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(a) In the given figure, AE and BC intersect each other at point D. If $\angle CDE = 90^{\circ}$, [3] AB = 5 cm, BD = 4 cm and CD = 9 cm, find DE.



- (b) A straight line AB is 8 cm long. Locate by construction the locus of a point. which is :
 - (i) Equidistant from A and B.
 - (ii) Always 4 cm from the line AB.
 - (iii) Mark two points X and Y, which are 4 cm from AB and equidistant from A [8] and B, Name the figure AXBY.
- (c) Some students planned a picnic. The budget for the food was ₹ 480. As eight of
 - them failed to join the party, the cost of the food for each member increased by $extsf{R}$ [4] 10. Find how many students went for the picnic.

Solution.

⇒

(a) Given : $\angle CDE = 90^\circ$, AB = 5 cm, BD = 4 cm, CD = 9 cm, DE = ?

$$AD = \sqrt{AB^2 - DB^2} = \sqrt{25 - 16} = 3$$

$$DA \times DE = DB \times DC$$
 (Product of the length of their segment is equal.)
 $3 \times DE = 4 \times 9$

Ans.

B

х

0

o

B cm

DE = 12 cm=>

(b) Steps of Construction :

- Draw AB is 8 cm, Draw PQ the perpen-dicular bisector (i) of AB.
- (ii) Draw CD and EF both parallel to AB and each at a distance of 4 cm from AB.

(iii) AXBY is a square.

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(c) Let the no. of students planned a picnic = x.

Budget for food =
$$₹480$$

Budget for each student = $\frac{480}{2}$

If eight student failed to join the party, the cost for each student $=\frac{480}{x-8}$

x

	480 480
	$\frac{1}{x-8}-\frac{1}{x}=10$
	$\frac{480x - 480(x - 8)}{x(x - 8)} = 10$
	- (+ - 0)
⇒	480 x - 480 x + 3840
	x(x-8) = 10
⇒	$x^2 - 8x - 384 = 0$
⇒	$x^2 - 24x + 16x - 384 = 0$
	x(x-24) + 16(x-24) = 0
⇒	(x-24)(x+16) = 0
⇒	x = 24, -16
But the	number of students can not be persetion

$$x = 24$$

:. The number of student who went for picnic = x - 8 = 24 - 8 = 16 Ans.

Question 11.

(a) The weight of 50 apples were recorded as given below. Calculate the mean weight, to the nearest gram, by the Step Deviation Method.
 [5]

Weight in grams	80-85	05 00	00 05				[0]	
	00-00	00-90	90-95	95-100	100-105	105-110	110-115	L
No. of apples	5	8	10	12	0		110 110	
Iloin - I	and the second		/		o	4	31	Γ.

(b) Using a graph paper, draw an ogive for the following distribution which shows the marks obtained in the General Knowledge paper by 100 students.

	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
No. of students	5	10	20	25	15	19	00-70	10-00
Use the ogive to	estimate				10	14	9	4

[5]

(i) The median.

(ii) The number of students who score marks above 65.

Solution.

(a) Weight No. of apples Mid Value $u_i = \frac{x - A}{C}$ $f_i u_i$ (f.) (x)80-85 5 82.5 -3 -1585-90 8 87.5 -2-1690-95 10 92.5 -1 -10 95-100 1297.5 0 0 100-105 8 102.5 1 8 105-110 4 107.5 2 8 110-115 3 112.53 9 $\Sigma f_i = 50$ $\Sigma f_i u_i = -16$



Ans.