

# BOARD QUESTION PAPER : OCTOBER 2013

Time:  $2 \frac{1}{2}$  Hours

Max. Marks: 60

**Note:**

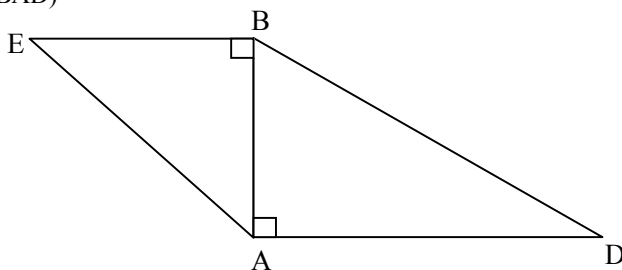
- i. Solve *All* questions. Draw diagrams wherever necessary.
- ii. Use of calculator is not allowed.
- iii. Figures to the right indicate full marks.
- iv. Marks of constructions should be distinct. They should not be rubbed off.
- v. Diagram is essential for the proof of the theorem.

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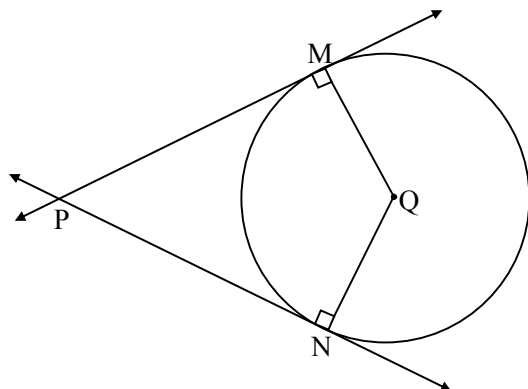
**1. Solve any six sub-questions:**

[6]

- i. In the following figure, seg  $BE \perp$  seg  $AB$  and seg  $BA \perp$  seg  $AD$ . If  $BE = 6$  and  $AD = 9$ , find  $\frac{A(\Delta ABE)}{A(\Delta BAD)}$ .



- ii. If two circles with radii 8 and 3 respectively touch internally, then find the distance between their centres.
- iii. In the following figure, Q is the centre of circle and PM and PN are tangent segments to the circle. If  $\angle MPN = 40^\circ$ , find  $\angle MQN$ .

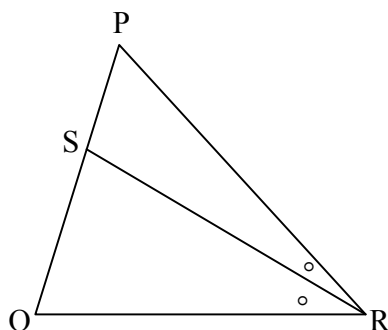


- iv. If  $\theta = -60^\circ$ , find the value of  $\cos \theta$ .
- v. Find the slope of the line passing through  $A(-2, 1)$  and  $B(0, 3)$ .
- vi. Find the area of the sector of a circle with radius 6 cm and the length of arc is 15 cm.
- vii. Using Euler's formula, find V, if  $E = 30$ ,  $F = 12$ .

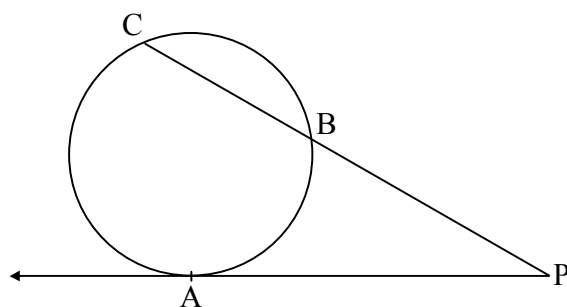
## 2. Solve any five sub-questions:

[10]

- i. In  $\Delta PQR$ , seg  $RS$  is the bisector of  $\angle PRQ$ .  $PS = 4$ ,  $SQ = 12$ ,  $PR = 13$ , find  $QR$ .



- ii. In the following figure, a tangent segment  $PA$  touching a circle in  $A$  and a secant  $PBC$  intersects the circle at points  $C$  and  $B$ . If  $AP = 13$  and  $BP = 6$ , find  $PC$ .



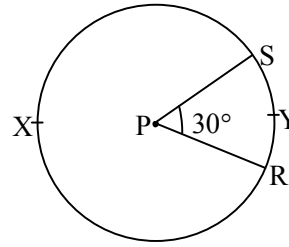
- iii. If  $\sin \theta = \frac{7}{25}$ , where  $\theta$  is an acute angle, find the value of  $\cos \theta$  using identity.
- iv. Find the trigonometric ratios  $\tan \theta$  and  $\cos \theta$  of an angle  $\theta$ , which is in standard position, whose terminal arm passes through  $(7, 24)$ .
- v.  $P(-2, -3)$  is a point on the line  $2y = \frac{11}{2}x + c$ . Find  $c$ .
- vi. The dimensions of a cuboid in cm are  $20 \times 18 \times 10$ . Find its total surface area.

## 3. Solve any four sub-questions:

[12]

- i. The ratio of the areas of two triangles with common base is  $4 : 3$ . Height of the larger triangle is  $20$  cm, then find the corresponding height of the smaller triangle.
- ii. Draw the circumcircle of  $\Delta KLM$  in which  $LM = 7$  cm,  $\angle L = 60^\circ$ ,  $\angle M = 55^\circ$ .
- iii. A boy is at a distance of  $70$  m from a tree makes an angle of elevation of  $60^\circ$  with the top of the tree. What is the height of the tree? ( $\sqrt{3} = 1.73$ )
- iv. Find the equation of the line passing through the points  $(-2, -3)$  and  $(-4, 7)$ .

- v. In the following figure, the radius of the circle is 7 cm and  $m(\text{arc RYS}) = 30^\circ$ , then find:
- Area of the circle
  - $A(P-RYS)$
  - $A(P-RXS)$ .



4. Solve any three sub-questions:

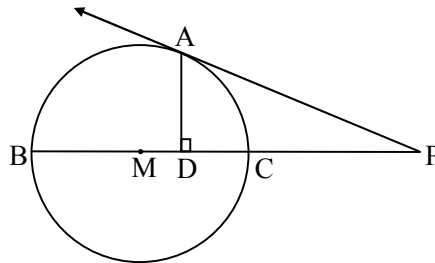
[12]

- Prove that, If a line parallel to a side of a triangle intersect the other sides in two distinct points, then the line divides those sides in proportion.
- Prove that the lengths of the two tangent segments to a circle drawn from external point are equal.
- Construct  $\triangle LMN$  such that  $LM = 6.6$  cm,  $\angle LNM = 65^\circ$ , where  $ND$  is median and  $ND = 5$  cm.
- An observer standing on a bank of river observes the top of a tree on the opposite bank making an angle of elevation  $60^\circ$ . He moves 30 m backward and observes the top of the tree making an angle of elevation  $30^\circ$ . Find the height of the tree and the width of the river. ( $\sqrt{3} = 1.73$ )

5. Solve any four sub-questions:

[20]

- Prove that, in a triangle, the angle bisector divides the side opposite to the angle in the ratio of the remaining sides.
- In the following figure,  $BC$  is a diameter of the circle with centre  $M$ .  $PA$  is a tangent at  $A$  from  $P$  which is a point on line  $BC$  and  $AD \perp BC$ . Prove that  $DP^2 = BP \times CP - BD \times CD$ .



- The length of a semicircular tunnel is 2 km and diameter is 7 m. Find the expenditure for digging the tunnel at the rate of ₹ 600 per  $m^3$ . Find the expenditure for plastering inner side of the tunnel at the rate of ₹ 50 per sq. m. ( $\pi = \frac{22}{7}$ )
- If the points  $A(1, 2)$ ,  $B(4, 6)$ ,  $C(3, 5)$  are the vertices of a  $\triangle ABC$ , find the equation of the line passing through the midpoints of  $AB$  and  $AC$ .
- Draw a triangle  $PQR$  right angled at  $Q$  such that  $PQ = 3$  cm,  $QR = 4$  cm. Now construct  $\triangle AQB$  similar to  $\triangle PQR$ , each of whose sides is  $\frac{7}{5}$  times the corresponding side of  $\triangle PQR$ .