

ANSWERS KEY

CHEMISTRY

1. c 2. d 3. b 4. c 5. b 6. d 7. c 8. a 9. d 10. b 11. a 12. c 13. c
14. b 15. b 16. b 17. b 18. c 19. d 20. c 21. b 22. b 23. b 24. b 25. a 26.
27. c 28. c 29. c 30. b

PHYSICS

1. a 2. b 3. b 4. c 5. c 6. c 7. d 8. b 9. b 10. d 11. b 12. b 13. d
14. c 15. b 16. a 17. d 18. a 19. b 20. b 21. a 22. a 23. c 24. b 25. d 26. b
27. a 28. a 29. a 30. d

MATHEMATICS

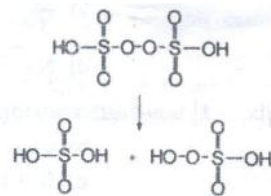
1. d 2. a 3. b 4. a 5. b 6. b 7. a 8. a 9. c 10. b 11. b 12. c 13. a
14. d 15. d 16. a 17. d 18. d 19. a 20. b 21. a 22. a 23. b 24. d 25. c 26. a
27. a 28. c 29. b 30. d

HINTS AND EXPLANATION

CHEMISTRY

Sol 1.

Hydrolysis of peroxodisulphuric acid produces sulphuric acid and peroxomonosulphuric acid



Sol 2.

Electronegativity of an element is its tendency to acquire electrons.

Sol 3.

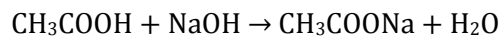
$$K_a = 1.0 \times 10^{-9};$$

$$\alpha = \sqrt{\frac{K_a}{c}} = \sqrt{\frac{1.0 \times 10^{-9}}{0.1}} = 1.0 \times 10^{-4}$$

$$[H^+] = c\alpha = 0.1 \times 1.0 \times 10^{-4} = 1.0 \times 10^{-5}$$

$$pH = -\log [H^+] = -\log (1.0 \times 10^{-5}) = 5$$

Sol 4.

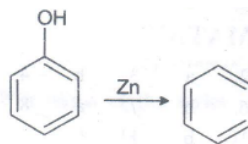


Weak acid strong base

CH_3COONa is a salt of weak acid and strong base so its aqueous solution is basic

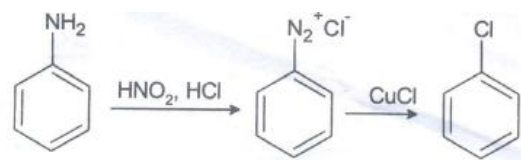
Sol 5.

Phenol on heating with Zn dust forms benzene.



Sol 6.

An aromatic amine quickly reacts with HNO_2 , HCl to form an aryl diazonium salt, which decomposes in the presence of copper (I) chloride to form the desired aryl halide. The reaction is called Sandmeyer reaction



Sol 7.

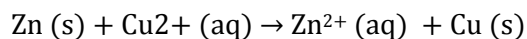
Wurtz reaction is used for converting alkyl halides into alkanes; $RX + Na + XR \rightarrow R-R$

Clemmensen reduction, Wolf Kishner reaction and reaction with HI/P are used for conversion of

$>C=O$ to $>CH_2$.

Sol 8.

For the cell, Zn |Zn²⁺ (0.1M)|| Cu²⁺ (0.01 M) | Cu; the cell reaction is



Applying Nernst equation.

$$E_{\text{cell}} = E^{\circ}_{\text{cell}} - \frac{0.0591}{n} \log \frac{a_{\text{Zn}^{2+}}}{a_{\text{Cu}^{2+}}}$$

$$E_{\text{cell}} = 1.10 - \frac{0.0591}{2} \log \frac{0.1}{0.01}$$

$$= 1.10 - \frac{0.0591}{2} \log 10$$

$$= 1.10 - 0.0295 = 1.07045 \text{ V} = 1.07 \text{ V}$$

Sol 9.

$$M_1 V_1 + M_2 V_2 = M_3 V_3$$

$$0.1 \times 100 + 0.2 \times 25 = M_3 \times 125$$

$$10 + 5 = 15 = M_3 \times 125$$

$$M_3 = 15 / 125 = 0.12 \text{ M}$$

Sol 10.

$$\Delta n_{(\text{g})} = 12 - 15 = -3$$

$$\Delta H = \Delta E + \Delta n_{(\text{g})} RT$$

$$\text{or } \Delta H - \Delta E = \Delta n_{(\text{g})} RT$$

$$\Delta H - \Delta E = -3 \times 8.314 \text{ J mol}^{-1} \text{ K}^{-1} \times 298 \text{ K}$$

$$= -7432.716 \text{ J mol}^{-1} = -7.432 \text{ kJ mol}^{-1}$$

Sol 11.

$$\alpha = 10\% = 0.1, c = 0.01,$$

$$[\text{H}^+] = c\alpha = 0.1 \times 2 \times 0.01 = 2.0 \times 10^{-3}$$

(one mol H₂CO₃ gives two H⁺ ions)

$$\text{pK} - \log [\text{H}^+] = -\log (2.0 \times 10^{-3})$$

$$= -\log 2 + 3 = -0.3010 + 3 = 2.699$$

Sol 12.

Lines in the Balmer series are in the visible region of spectrum.

Sol 13.

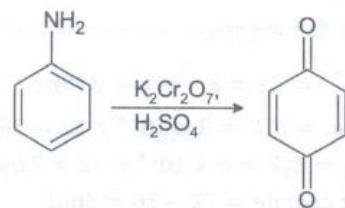
Chlorine cannot be dried by passing over anhyd, CaCl_2

Sol 14.

Oxidation number of Br in $\text{Br}_2 = 0$; in $\text{Br} = -1$ and in $\text{BrO}_3 = +5$

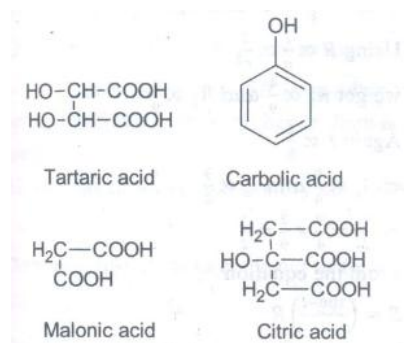
Sol 15.

The reaction between aniline and $\text{K}_2\text{Cr}_2\text{O}_7 / \text{H}_2\text{SO}_4$ gives p-benzoquinone.



Sol 16.

Carbolic acid (phenol) does not contain a COOH group.



Sol 17.

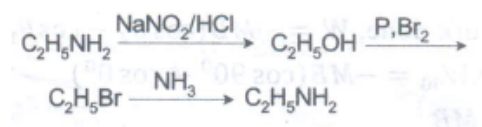
Trichloroacetic acid is the strongest acid out of the given options.

Sol 18.

In match box, sides $a \neq b \neq c$; $\alpha = \beta = \gamma = 90^\circ$, so the kind of symmetry is orthorhombic.

Sol 19.

$\text{X} = \text{C}_2\text{H}_5\text{OH}$; $\text{X} = \text{C}_2\text{H}_5\text{Br}$; $\text{Y} = \text{C}_2\text{H}_5\text{NH}_2$



Sol 20.

Correct order of boiling points is

Alkane > alkene >> alkyne

Sol 21.

The conversion of a gas to a liquid is exothermic so more heat is liberated when HCl (l) is formed instead of HC (g), i.e., $X < y$.

Sol 22.

Incomplete combustion of petrol or diesel oil in automobile engines can be best detected by testing the fuel gases for the presence CO

Sol 23.

D-Aldopentose is represented by structure B. The compound contains a chain of five carbons, with terminal CHO group and penultimate carbon has OH group on the right hand side.

Sol 24.

C_2H_4 and H_2O are neutral ligands, therefore oxidation state of Mo in the given complex is

$$2x - 8 = -2 \quad 2x - 6 \text{ or } x = 3.$$

Sol 25.

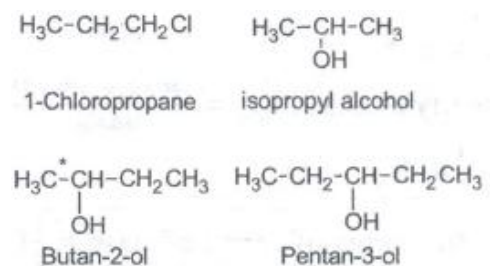
Freundlich's adsorption isotherm is $\frac{x}{m} = kp^{1/n}$

Sol 26.

It is a metallic hydride

Sol 27.

Butan-2-ol is optically active due to presence of a chiral centre.



Sol 28.

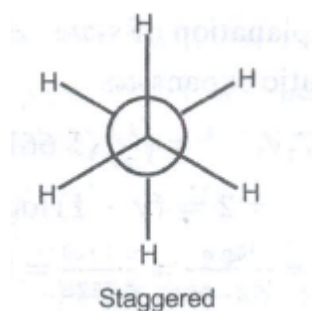
The large increase in rate of a reaction on rise in temperature is due to the increase in the fraction of molecules having energy $>$ threshold

Sol 29.

Degree of hydration in an aqueous solution decreases as the size of metal ion increases and consequently ionic mobility increases.

Sol 30.

Dihedral angle in the staggered conformation of ethane is of 60° .



PHYSICS

Sol 1.

$$\% \text{ age error in } C = 0.1 / 2 \times 100 = 5\%$$

$$\% \text{ age error in } V = 0.5 / 25 \times 100 = 2\%$$

$$\begin{aligned} \text{Error in } Q &= CV + (\% \text{ age error in } C + \% \text{ age error in } V) \\ &= 2 \times 25 + (5 + 2)\% = 3.5 C \end{aligned}$$

Sol 2.

$$\text{Using } v^2 - u^2 = 2gh$$

$$\text{we have } v = \sqrt{2gh} \text{ at } u = 0$$

$$\therefore \frac{v_2}{v_1} = \sqrt{\frac{h_2}{h_1}} = \sqrt{\frac{1.8}{5}} = \frac{3}{5}$$

$$\text{Loss in velocity} = \frac{v_1 - v_2}{v_1} = 1 - \frac{v_2}{v_1}$$

$$= 1 - \frac{3}{5} = \frac{2}{5}$$

Sol 3.

$$l_1 = 2l_2 = \frac{2}{3}l$$

Force constant $K \propto \frac{1}{\text{length of spring}}$

$$\therefore K_1 = \frac{3}{2}K$$

Sol 4.

As $P = Fv = C$

$$\Rightarrow \frac{mdv}{dt} v = C$$

$$\text{or } v dv = \frac{C dt}{m}$$

Integrating

$$\frac{v^2}{2} = \frac{ct}{m}$$

$$\Rightarrow \left(\frac{ds}{dt}\right)^2 = \frac{2ct}{m} \text{ or } \frac{ds}{dt} = \sqrt{\frac{2ct}{m}} \Rightarrow S \propto t^{3/2}$$

Sol 5.

$$\text{Velocity of C.M. } V_{cm} = \frac{(40 \times 2) + (30 \times -3)}{40 + 30}$$

$$= -\frac{1}{7} m/s$$

Sol 6.

Using $g_d = g \left(1 - \frac{d}{R}\right)$ as $d = \frac{R}{2}$

$$g_d = g \left(1 - \frac{R}{2R}\right) = \frac{g}{2}$$

$$\therefore \text{weight} = mg_d = \frac{mg}{2} = \frac{w}{2}$$

Sol 7.

Upthrust is zero because weight of liquid is zero due to zero gravity.

Sol 8.

Both statements are true but statement 2 is not the correct explanation of Statement 1.

Sol 9.

For adiabatic expansion

$$TV^{\gamma-1} = T_1V_1^{\gamma-1} = \left(\frac{T}{2}\right) (5.66V)^{\gamma-1}$$

$$\text{or } (5.66)^{\gamma-1} = 2 \Rightarrow (\gamma - 1) \log 5.66 = \log 2$$

$$\text{i.e. } \gamma - 1 = \frac{\log 2}{\log 5.66} = \frac{0.3010}{0.7528} = 0.4$$

$$\Rightarrow \gamma = 1.4$$

Sol 10.

From the equation $r = 1 + \frac{2}{f}$

$$1.4 = 1 + \frac{2}{f} = 0.4$$

$$\Rightarrow f = \frac{2}{0.4}$$

$$\Rightarrow f = 5$$

Sol 11.

The value of x is such that echoes are heard 0 1s and 2s

$$\text{i.e. } 510 = x + 2x = 3x$$

$$\Rightarrow x \frac{510}{3} = 100 \text{ m}$$

$$V = \frac{x+x}{1} = 2x = 2 \times 100 = 200 \text{ m/s}$$

Sol 12.

$$\text{Here } q_1 = c_1 V = 3 \times 10^{-6} \times 12 = 36 \mu\text{C}$$

$$\text{and } q_2 = c_2 V = 6 \times 10^{-6} \times 12 = 72 \mu\text{C}$$

$$\therefore \text{Net charge} = 72 - 36 = 36 \mu\text{C}$$

This charge gets distributed among two capacitors

$$\therefore V_1 = \frac{12}{3} = 4V \text{ and } V_2 = \frac{24}{6} = 4V$$

Sol 13.

$$\text{Using } R \propto \frac{1}{a} \propto \frac{1}{r^2}$$

$$\text{We get } R_1 \propto \frac{4}{9} \text{ and } R_2 \propto \frac{2}{9}$$

$$\text{Again } I \propto \frac{1}{R}$$

$$\Rightarrow I_1 \propto \frac{9}{4} \text{ and } I_2 \propto \frac{9}{2}$$

$$\Rightarrow \frac{I_1}{I_2} = \frac{9}{4} \times \frac{2}{9} = \frac{1}{2}$$

Sol 14.

From the equation

$$S = \left(\frac{100-t}{20} \right) R$$

$$S = \left(\frac{100-20}{20} \right) R = 4R$$

$$\text{and } S' = \left(\frac{100-40}{40} \right) (R + 15) = \frac{6}{4} (R + 15)$$

$$\text{As } S' = S$$

$$4R = \frac{6}{4} (R + 15)$$

$$\Rightarrow R = 9 \Omega$$

Sol 15.

$$\text{Work done, } W = - MB (\cos \theta_2 - \cos \theta_1)$$

$$\text{i.e. } W_{90} = - MB (\cos 90^\circ - \cos 0^\circ) = MB / 2$$

$$= MV$$

$$\text{and } W_{60} = - MB (\cos 60^\circ - \cos 0^\circ) = MB / 2$$

$$\text{Given that } W_{90} = nW_{60}$$

$$n = \frac{W_{90}}{W_{60}} = \frac{MB}{MB/2} = 2$$

Sol 16.

As we know that

$$Q = CV, q_0 = CV_0, q = q_0 \cos \omega t$$

$$\cos \omega t = \frac{q}{q_0} = \frac{v}{v_0} = \frac{6}{12} = \frac{1}{2}$$

$$\Rightarrow \omega t = \frac{\pi}{3} \text{ rad where } \omega = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{(2 \times 10^{-6})(0.6 \times 10^{-3})}}$$

$$= \frac{10^5}{\sqrt{2}} \text{ rad/s}$$

$$\text{Again } I = \frac{dq}{dt} = \frac{d}{dt} (q_0 \cos \omega t) = -q_0 \omega \sin \omega t$$

$$\text{Or } I = CV_0 \omega \sin \omega t = CV_0$$

$$I = (2 \times 10^{-6}) (12) \times \frac{10^5}{\sqrt{2}} \times \frac{\sqrt{3}}{2}$$

$$I = 0.6 \text{ A}$$

Sol 17.

Time taken by loop to cover 5m is given by

$$t_1 = \sqrt{\frac{2h}{g}} = \sqrt{\frac{2 \times 5}{10}} = 1 \text{ s}$$

e.m.f induced, $e = Blv$

$$\therefore \text{current } I = \frac{e}{r} = \frac{Blv}{r} \text{ And Force } F = BIl = \frac{B^2 l^2 v^2}{R} \text{ (upwards) But } v = \sqrt{2gh} = \sqrt{2 \times 10 \times 5} = 10 \text{ m/s}$$

$$\Rightarrow F = \frac{(1)^2 \times (0.25)^2 \times 10}{0.125} = 5 \text{ N (upwards) But } F = mg = 0.5 \times 10 = 5 \text{ N (downwards) acceleration.}$$

$$\text{The time taken for complete entry into field } t_2 = \frac{2}{10} = 0.2 \text{ s}$$

When loop just starts to come out of field, then

$$15 = 10t_3 + \frac{1}{2} g t_3^2$$

$$\text{Or } t_3^2 + 2t_3 - 3 = 0$$

Solving $t_3 = 1 \text{ s}$

$$\therefore \text{Total time taken} = t_1 + t_2 + t_3$$

$$= 1 + 0.2 + 1 = 2.2 \text{ s}$$

Sol 18.

$$\text{As } U = \frac{1}{2} \epsilon_0 E^2$$

$$= \frac{1}{2} (8.85 \times 10^{-12}) (48)^2 = 1 \times 10^{-8} \text{ J/ m}^3$$

Sol 19.

$$\text{Here } f = \frac{R}{2} = -\frac{40}{2} = -20 \text{ cm Using } \frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$-\frac{1}{200} + \frac{1}{v} = -\frac{1}{20}$$

$$\frac{1}{v} = -\frac{1}{20} + \frac{1}{200} = -\frac{9}{200} \Rightarrow v = -\frac{200}{9} \text{ cm}$$

$$\text{As } \frac{I}{O} = -\frac{v}{u} \Rightarrow I = -\frac{v}{u} \times O$$

$$= -\frac{200}{9 \times 200} \times 5 = -\frac{5}{9} = -0.55 \text{ cm}$$

Sol 20.

$$\text{Number of fringes} = \frac{\text{Length of region}}{\text{Fringe width}}$$

Also Fringe width \propto Wavelength

$$\therefore \text{Now number of fringes} = \frac{600}{400} \times 12 = 18$$

Sol 21.

$$\text{Given } i_p + 90^\circ + r = 180^\circ$$

$$\text{i.e. } i_p = 90^\circ - r$$

$$\text{As } i_p = -r = 22^\circ \Rightarrow 90^\circ - r - r = 22^\circ \Rightarrow 2r = 68^\circ$$

$$\text{Or } r = 34^\circ$$

Sol 22.

Making use of Moseley's law for K_α line, we get

$$\frac{1}{\lambda} = \frac{3}{4} R (z-1)^2 \Rightarrow \frac{1}{0.76 \times 10^{-10}} = \frac{3}{4} (1.09 \times 10^7) (z-1)^2$$

$$\text{Or } \frac{4 \times 10^3}{0.76} = 3 \times 1.09 (z-1)^2 \Rightarrow (z-1)^2 = \frac{4 \times 10^3}{0.76 \times 3 \times 1.09} = 1600$$

$$\Rightarrow z-1 = 40 \text{ or } z = 41$$

Sol 23.

As $r \propto n^2$, $v \propto \frac{1}{n}$ and $T \propto \frac{r}{v}$

$$\therefore \frac{r_1}{r_2} = \frac{n_1^2}{n_2^2}, \frac{v_1}{v_2} = \frac{n_2}{n_1} \text{ and } \frac{T_1}{T_2} = \frac{r_1 v_2}{r_2 v_1} = \frac{n_1^3}{n_2^3}$$

i.e. $\frac{\theta}{1} = \frac{2^3}{1}$ i. e. $n_1 = 2c$ and $n_2 = 4$ and $n_2 = 1$

Sol 24.

Using $B = \frac{\mu_0 e v}{4\pi r^2}$

$$B = \frac{10^{-7}(1.6 \times 10^{-19})(2.2 \times 10^6)}{(0.5 \times 10^{-10})^2} = 14T$$

Sol 25.

The truth table represents OR gate

Sol 26.

The frequencies given in the choices (3) and (4) have high penetration power and will be digested by the earth, whereas the radiation of 10 KHz in choice (1) will not be feasible due to the size of antenna.

Sol 27.

The potential difference will depend only on the charge on inner surface, in such cases. As the charge on the inner sphere is unchanged, the potential difference V will also remain unchanged.

Sol 28.

If the charge is positive, it will be accelerated parallel and will be anti parallel to the electric field if it is a negative charge. As the charge moves either parallel or anti parallel to electric and magnetic field, the net magnetic force on it will be zero and its path will be a straight line.

Sol 29.

$$\text{As } 36 \text{ km/h} = 36 \times \frac{5}{18} = 10 \text{ km/s}$$

The apparent frequency of sound heard by car

$$f' = f \left(\frac{n+n_0}{n-n_s} \right) = 8 \left(\frac{320+10}{320-10} \right) = 8.5 \text{ KHz}$$

Sol 30.

$$\text{As } \vec{L} = m (\vec{r} \times \vec{v})$$

The direction of angular momentum will be same as that of $(\vec{r} \times \vec{v})$

MATHEMATICS

Sol 1.

$A \cup B$ will contain minimum number of elements, if A is subset of B and in that case $n(A \cup B) = 5$
Therefore option (d) is correct.

Sol 2.

Obviously $A = B$ is the correct answer.

Sol 3.

$$\text{Given } w = \frac{z-1}{z+1}$$

$$\Rightarrow w = \frac{(z-1)(z-1)}{(z+1)(z-1)}$$

$$= \frac{z^2 - 2z + 1}{z^2 - 1}$$

$$= \frac{(x^2 + y^2) - 2(x + iy) + 1}{x^2 + y^2 - 1}$$

$$= \frac{(x^2 + y^2 - 2x + 1) - 2iy}{x^2 + y^2 - 1}$$

$$\Rightarrow \text{Re}(w) = \frac{(x^2 + y^2 - 2x + 1)}{x^2 + y^2 - 1}$$

Sol 4.

$$|(x - 1) + iy| < |(x - 3) + iy|$$

$$\Rightarrow (x - 1)^2 + y^2 < (x - 3)^2 + y^2$$

$$\Rightarrow (x - 1)^2 < (x - 3)^2$$

$$\Rightarrow -(x - 3) < x - 1 < x - 3$$

$$\Rightarrow 4 < 2x$$

$$\Rightarrow 2 < x$$

Sol 7.

If $p + q + r = m$, then the number of ways of arranging 'm' things is $m! / p!q!r!$

Hence, the total number of different combinations of letters of the word ADVANCED are $\frac{8!}{2!2!}$

$$= \frac{8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{(2 \times 1)(2 \times 1)} = 10080$$

Sol 8.

There are $(m + 1)$ choices for each of n different books. So, the total number of choices is $(m + 1)^n$ including one choice in which we do not select any book. Hence, the required number of ways is

$$(m + 1)^n - 1$$

Sol 9.

$$\begin{aligned} & \frac{1}{1.2} - \frac{1}{2.3} + \frac{1}{3.4} - \dots\dots\dots \\ &= \left(1 - \frac{1}{2}\right) - \left(\frac{1}{2} - \frac{1}{3}\right) + \left(\frac{1}{3} - \frac{1}{4}\right) \dots\dots\dots \\ &= 1 - \frac{1}{2} + \frac{1}{2} - \frac{1}{3} + \frac{1}{3} - \frac{1}{4} \dots\dots\dots \\ &= 2\left(1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} \dots\dots\dots\right) - 1 \\ &= 2 \log (1 + 1) - 1 \\ &= \log 2^2 - \log e = \log \frac{4}{e} \end{aligned}$$

Sol 10.

Here $a = {}^nC_r$, $b = {}^nC_{r+1}$ and $c = {}^nC_{c+2}$

Put $n = 2$, $r = 0$ we get $a = 1$, $b = 2$ and $c = 1$

Only option (b) holds the condition i.e.

$$n = \frac{2ac + ab + bc}{b^2 - ac}$$

Sol 12.

The r^{th} term of the series is given by

$$t_r = (2r - 1)(2r + 1) = 4r^2 - 1$$

Therefore, S_n , the sum to n terms of the series is given by

$$\begin{aligned} S_n &= 4 \sum_{r=1}^n r^2 - n = 4 \frac{n(n+1)(2n+1)}{6} - n \\ &= \frac{2(2n^3 + 3n^2 + n) - 6n}{6} = \frac{8n^3 + 12n^2 + 4n - 6n}{6} \\ &= \frac{8n^3 + 12n^2 - 2n}{6} \\ &= \frac{4n^3 + 6n^2 - n}{3} \end{aligned}$$

Sol 13.

$$\begin{aligned} \lim_{x \rightarrow 0} \frac{5^x - 6^x}{7^x - 8^x} &= \lim_{x \rightarrow 0} \frac{5^x \log 5 - 6^x \log 6}{7^x \log 7 - 8^x \log 8} \\ &= \frac{\log 5 - \log 6}{\log 7 - \log 8} = \log \left(\frac{5}{6} \right) / \log \left(\frac{7}{8} \right) \end{aligned}$$

Sol 14.

$$\begin{aligned} Rf'(0) &= \lim_{h \rightarrow 0} \frac{f(0+h) - f(0)}{h} \\ &= \lim_{h \rightarrow 0} \frac{|h|^2 - 0}{h} = \lim_{h \rightarrow 0} \frac{h^2}{h} \\ &= \lim_{h \rightarrow 0} h^1 = 0 \end{aligned}$$

$$\begin{aligned} Lf'(0) &= \lim_{h \rightarrow 0} \frac{f(0-h) - f(0)}{-h} \\ &= \lim_{h \rightarrow 0} \frac{|-h|^2}{-h} = \lim_{h \rightarrow 0} \frac{h^2}{-h} \\ &= -\lim_{h \rightarrow 0} h^1 = 0 \end{aligned}$$

$$\therefore Rf'(0) = Lf'(0) = 0.$$

$$\text{Hence, } f'(0) = 0$$

Sol 15.

$$y = ax^{n+1} + bx^{-n}$$

$$y' = a(n+1)x^n - bnx^{-n-1}$$

$$y'' = a(n+1)nx^{n-1} - bn(-n-1)x^{-n-2}$$

$$y'' = n(n+1)[ax^{n+1} + bx^{-n}]$$

multiply x^2 on both sides

$$\begin{aligned} x^2 \frac{d^2y}{dx^2} &= n(n+1)[ax^{n+1} + bx^{-n}] \\ &= n(n+1)y \end{aligned}$$

Sol 16.

$$\int (\operatorname{cosec}^2 x - 1) dx = -\cot x - x + c$$

Sol 17.

$$\begin{aligned} I &= \frac{1}{2} \int_0^{\frac{\pi}{2}} (1 - \cos 2x) dx \\ &= \frac{1}{2} \left[x - \frac{\sin 2x}{2} \right]_0^{\frac{\pi}{2}} \\ &= \frac{1}{2} \left(\frac{\pi}{2} - 0 \right) = \frac{\pi}{4} \end{aligned}$$

Sol 18.

$$\begin{aligned} \frac{d^2y}{dx^2} &= \left[1 + \left(\frac{dy}{dx} \right)^2 \right]^{3/4} \\ \Rightarrow \left(\frac{d^2y}{dx^2} \right)^4 &= \left[1 + \left(\frac{dy}{dx} \right)^2 \right]^2 \end{aligned}$$

Therefore order = 2 and degree = 4

Sol 19.

Given three lines will be concurrent if

$$\begin{bmatrix} p & q & r \\ q & r & p \\ r & p & q \end{bmatrix} = 0, \text{ which gives } p + q + r = 0$$

Sol 20.

$$\begin{aligned} x^2 + 4x + 3y + 5 &= 0 \\ \Rightarrow x^2 + 4x &= -3y - 5 \\ \Rightarrow x^2 + 4x + 4 &= -3y - 5 + 4 \\ \Rightarrow (x + 2)^2 &= 3y - 1 \\ \Rightarrow (x + 2)^2 &= -3 \left(y + \frac{1}{3} \right) \end{aligned}$$

Sol 21.

$$\begin{aligned} \text{Since } (\vec{a} \cdot \vec{c}) \times \vec{c} &= \vec{a} \times (\vec{a} \times \vec{c}) \\ \therefore (\vec{a} \cdot \vec{c}) \vec{b} - (\vec{b} \cdot \vec{c}) \vec{a} &= (\vec{a} \cdot \vec{c}) \vec{b} \\ \Rightarrow (\vec{b} \cdot \vec{c}) \vec{a} &= (\vec{a} \cdot \vec{b}) \vec{c} \end{aligned}$$

Sol 22.

Exhaustive number of cases = $6^3 = 216$. The same number can appear on each of the dice in the following ways: (1, 1, 1), (2, 2, 2) (6, 6, 6)

So favourable number of cases = 6

Hence, required probability = $\frac{6}{216} = 1/36$

Sol 23.

The total number of ways in which 2 integers can be chosen from the given 40 integers is

$${}^{40}C_2 = 780.$$

The sum of the selected numbers is odd if exactly one of them is odd and other is even.

Therefore, favorable number of cases.

$$= {}^{20}C_1 \times {}^{20}C_1 = 400$$

Hence, the required probability = $\frac{400}{780} = \frac{20}{39}$

Sol 25.

$$\sin \frac{5\pi}{6} = \sin \left(\pi - \frac{5\pi}{6} \right)$$

$$\Rightarrow \sin^{-1} \left(\sin \frac{5\pi}{6} \right) = \sin^{-1} \left(\sin \left(\pi - \frac{5\pi}{6} \right) \right)$$

$$\Rightarrow \sin^{-1} \left(\sin \frac{5\pi}{6} \right) = \left(\pi - \frac{5\pi}{6} \right) = \frac{\pi}{6}$$

Sol 27.

$$\frac{1}{1.2} + \frac{1}{3.4} + \frac{1}{5.6} + \dots \dots \dots \infty$$

$$= \left(1 - \frac{1}{2} \right) + \left(\frac{1}{3} - \frac{1}{4} \right) + \left(\frac{1}{5} - \frac{1}{6} \right) + \dots \dots \dots \text{to } \infty$$

log2

Sol 28.

$$Rf'(1) = \lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{[1+h]}{-h} = \lim_{h \rightarrow 0} \frac{0-1}{-h} = \infty$$

$\therefore Rf'(1) \neq Lf'(1)$. So, $f'(1)$ does not exist.

Sol 29.

To find out the x intercept we will put y and z as 0, so x intercept is - 4.

Similarly y and z intercept is 2 and $\frac{4}{3}$. Hence their sum is $4 + 2 + \frac{4}{3} = \frac{22}{3}$