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ಕರ್ನಾಟಕ ಪ್ರೌಢ ಶಿಕ್ಷಣ ಪರೀಕ್ಷಾ ಮಂಡಳಿ, ಮಲ್ಲೇಶ್ವರಂ, ಬೆಂಗಳೂರು – 560 003

**KARNATAKA SECONDARY EDUCATION EXAMINATION BOARD, MALLESWARAM,
BANGALORE – 560 003**

ಎಸ್.ಎಸ್.ಎಲ್.ಸಿ. ಪರೀಕ್ಷೆ, ಮಾರ್ಚ್ / ಏಪ್ರಿಲ್ — 2019

S. S. L. C. EXAMINATION, MARCH/APRIL, 2019

ಮಾದರಿ ಉತ್ತರಗಳು

MODEL ANSWERS

ದಿನಾಂಕ : 25. 03. 2019]

ಸಂಕೇತ ಸಂಖ್ಯೆ : **81-E**

Date : 25. 03. 2019]

CODE No. : **81-E**

ವಿಷಯ : ಗಣಿತ

Subject : MATHEMATICS

(ಹೊಸ ಪಠ್ಯಕ್ರಮ / New Syllabus)

(ಶಾಲಾ ಅಭ್ಯರ್ಥಿ / Regular Fresh)

(ಇಂಗ್ಲಿಷ್ ಭಾಷಾಂತರ / English Version)

[ಗರಿಷ್ಠ ಅಂಕಗಳು : **80**

[**Max. Marks : 80**

| Qn. Nos. | Ans. Key | Value Points | Marks allotted |
|-------------|-------------|--|-------------------|
| I. 1. | | If the n -th term of an arithmetic progression $a_n = 24 - 3n$, then its 2nd term is (A) 18 (B) 15 (C) 0 (D) 2 Ans. : (A) 18 | 1 |

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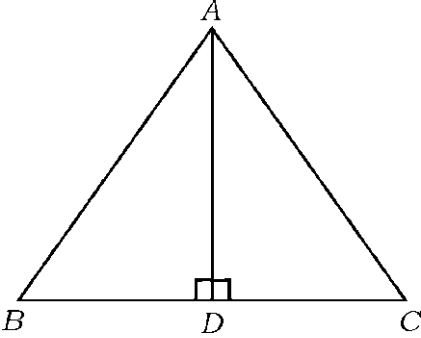
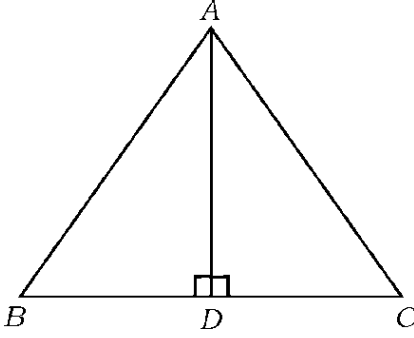
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| Qn. Nos. | Ans. Key | Value Points | Marks allotted |
|-------------|-------------|--|-------------------|
| 2. | (D) | <p>The lines represented by $2x + 3y - 9 = 0$ and $4x + 6y - 18 = 0$ are</p> <p>(A) Intersecting lines (B) Perpendicular lines to each other (C) Parallel lines (D) Coincident lines</p> <p><i>Ans. :</i> Coincident lines</p> | 1 |
| 3. | (B) | <p>A straight line which passes through two points on a circle is</p> <p>(A) a chord (B) a secant (C) a tangent (D) the radius</p> <p><i>Ans. :</i> a secant</p> | 1 |
| 4. | (C) | <p>If the area of a circle is 49π sq.units then its perimeter is</p> <p>(A) 7π units (B) 9π units (C) 14π units (D) 49π units</p> <p><i>Ans. :</i> 14π units</p> | 1 |
| 5. | (D) | <p>“The product of two consecutive positive integers is 30.” This can be expressed algebraically as</p> <p>(A) $x(x + 2) = 30$ (B) $x(x - 2) = 30$ (C) $x(x - 3) = 30$ (D) $x(x + 1) = 30$</p> <p><i>Ans. :</i> $x(x + 1) = 30$</p> | 1 |

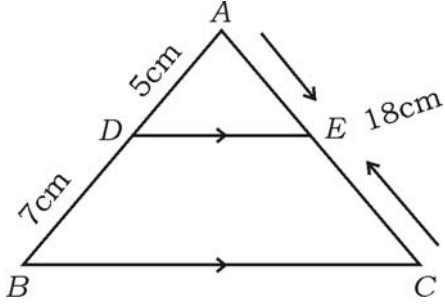
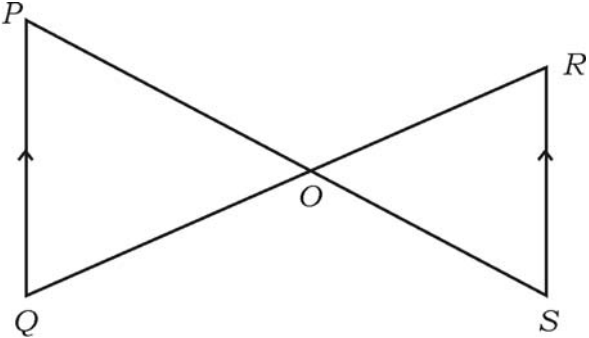
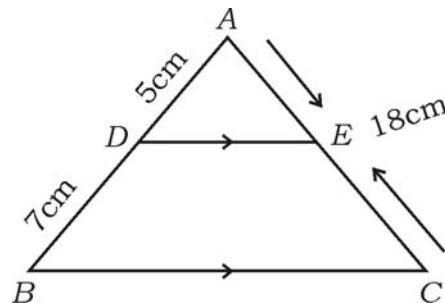
| Qn. Nos. | Ans. Key | Value Points | Marks allotted |
|-------------|-------------|--|-------------------|
| 6. | | <p>If a and b are any two positive integers then $\text{HCF} (a, b) \times \text{LCM} (a, b)$ is equal to</p> <p>(A) $a + b$</p> <p>(B) $a - b$</p> <p>(C) $a \times b$</p> <p>(D) $a \div b$</p> <p>Ans. :</p> | 1 |
| 7. | (C) | <p>The value of $\cos 48^\circ - \sin 42^\circ$ is</p> <p>(A) 0</p> <p>(B) $\frac{1}{4}$</p> <p>(C) $\frac{1}{2}$</p> <p>(D) 1</p> <p>Ans. :</p> | 1 |
| 8. | (B) | <p>If $P (A) = 0.05$ then $P (\bar{A})$ is</p> <p>(A) 0.59</p> <p>(B) 0.95</p> <p>(C) 1</p> <p>(D) 1.05</p> <p>Ans. :</p> | 1 |

| Qn. Nos. | Value Points | Marks allotted |
|---|--|----------------|
| II. | Answer the following : $6 \times 1 = 6$ (Question Numbers 9 to 14, give full marks to direct answers) | |
| 9. | The given graph represents a pair of linear equations in two variables. Write how many solutions these pair of equations have. | |
| | | |
| | Ans. : one or unique | 1 |
| 10. | $17 = 6 \times 2 + 5$ is compared with Euclid's Division lemma $a = bq + r$, then which number is representing the remainder ? | |
| | Ans. : 5 | 1 |
| 11. | Find the zeroes of the polynomial $P(x) = x^2 - 3$. | |
| Ans. : $x^2 - 3 = 0$ $(x + \sqrt{3})(x - \sqrt{3}) = 0$ $x = +\sqrt{3}, \quad x = -\sqrt{3}$ $\frac{1}{2} + \frac{1}{2}$ | | |
| Direct answer give full marks. | | 1 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|----------------|
| 12. | Write the degree of the polynomial $P(x) = 2x^2 - x^3 + 5$. Ans. : 3 | 1 |
| 13. | Find the value of the discriminant of the quadratic equation $2x^2 - 4x + 3 = 0$. Ans. : $b^2 - 4ac$ 1/2 $= (-4)^2 - 4 \times 2 \times 3$ $= 16 - 24$ $= -8$ 1/2 | 1 |
| 14. | Write the formula to calculate the curved surface area of the frustum of a cone. Ans. : $\pi l (r_1 + r_2)$ | 1 |
| III. 15. | Find the sum of first twenty terms of Arithmetic series $2 + 7 + 12 + \dots$ using suitable formula. 2 Ans. : $a = 2$ $d = 7 - 2 = 5$ $n = 20$ $S_n = \frac{n}{2} [2a + (n - 1)d]$ 1/2 $S_{20} = \frac{20}{2} [2 \times 2 + (20 - 1) \times 5]$ 1/2 $= 10 [4 + 19 \times 5]$ $= 10 \times 99$ 1/2 $S_{20} = 990$ 1/2 | 2 |

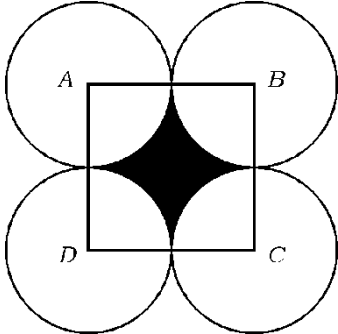
| Qn. Nos. | Value Points | Marks allotted |
|----------|---|----------------|
| 16. | In ΔABC , $AD \perp BC$ and $AD^2 = BD \times CD$. Prove that | |
| | $AB^2 + AC^2 = (BD + CD)^2.$ | 2 |
| |  | |
| | Ans. : | |
| |  | |
| | In ΔABD $AB^2 = AD^2 + BD^2 \quad \dots (i)$ | $\frac{1}{2}$ |
| | In ΔADC $AC^2 = AD^2 + CD^2 \quad \dots (ii)$ | $\frac{1}{2}$ |
| | (i) + (ii) | |
| | $AB^2 + AC^2 = 2AD^2 + BD^2 + CD^2$ | $\frac{1}{2}$ |
| | Put $AD^2 = BD \times CD$ | |
| | $AB^2 + AC^2 = 2BD \cdot CD + BD^2 + CD^2$ | $\frac{1}{2}$ |
| | $AB^2 + AC^2 = (BD + CD)^2$ | |

2

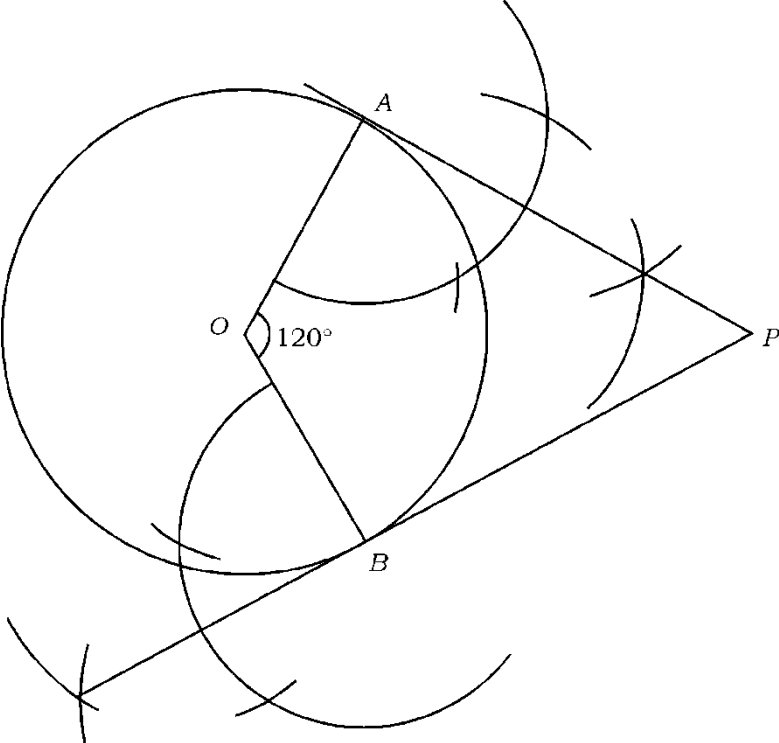
| Qn. Nos. | Value Points | Marks allotted |
|----------|--|----------------|
| 17. | <p>In $\triangle ABC$, $DE \parallel BC$. If $AD = 5$ cm, $BD = 7$ cm and $AC = 18$ cm, find the length of AE.</p> <div style="text-align: center;">  </div> <p style="text-align: center;">OR</p> <p>In the given figure if $PQ \parallel RS$, prove that $\triangle POQ \sim \triangle SOR$.</p> <div style="text-align: center;">  </div> <p>Ans. :</p> <div style="text-align: center;">  </div> <p>In $\triangle ABC$, $DE \parallel BC$</p> $\therefore \frac{AD}{AB} = \frac{AE}{AC} \quad \frac{1}{2}$ $\frac{5}{12} = \frac{AE}{18} \quad \frac{1}{2}$ | 2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|--|
| 18. | $\frac{5}{12} \times 18 = AE$ $AE = \frac{15}{2}$ $AE = 7.5 \text{ cm}$ | $\frac{1}{2}$ $\frac{1}{2}$ 2 |
| | <p data-bbox="284 577 794 611"><i>Note : Alternate method give marks.</i></p> <p data-bbox="774 645 821 678" style="text-align: center;">OR</p> <div data-bbox="550 689 1050 974" style="text-align: center;"> </div> <p data-bbox="284 1003 603 1037">In ΔPOQ and ΔSOR</p> <p data-bbox="371 1048 981 1081">$\angle P = \angle S$ (Alternate angles)</p> <p data-bbox="371 1104 981 1137">$\angle Q = \angle R$ (Alternate angles)</p> <p data-bbox="371 1160 842 1193">$\angle POQ = \angle ROS$ (V.O.A.)</p> <p data-bbox="707 1227 938 1261">(A.A. criterion)</p> <p data-bbox="371 1283 603 1317">$\Delta POQ \sim \Delta SOR.$</p> | $1\frac{1}{2}$ $\frac{1}{2}$ 2 |
| | <p data-bbox="284 1384 1305 1417">Solve the following pair of linear equations by any suitable method : 2</p> $x + y = 5$ $2x - 3y = 5.$ <p data-bbox="284 1619 371 1653"><i>Ans. :</i></p> <p data-bbox="284 1675 595 1709"><i>Substitution method :</i></p> $x + y = 5 \quad \dots \text{ (i)}$ $2x - 3y = 5 \quad \dots \text{ (ii)}$ $x + y = 5$ $y = 5 - x$ | $\frac{1}{2}$ |

| Qn. Nos. | Value Points | Marks allotted |
|-------------|---|-------------------|
| | Substitute the value of y in equation (ii) we get | |
| | $2x - 3(5 - x) = 5$ | $\frac{1}{2}$ |
| | $2x - 15 + 3x = 5$ | |
| | $5x - 15 = 5$ | |
| | $5x = 5 + 15$ | |
| | $5x = 20$ | |
| | $x = \frac{20}{5}$ | |
| | $x = 4$ | $\frac{1}{2}$ |
| | Substituting the value of x in equation (i) | |
| | $x + y = 5$ | |
| | $4 + y = 5$ | |
| | $y = 5 - 4$ | |
| | $y = 1$ | $\frac{1}{2}$ |
| | Elimination method : | |
| | $x + y = 5$ | |
| | $x + y = 5 \quad \dots (i) \times 2$ | |
| | $2x - 3y = 5 \quad \dots (ii)$ | |
| | $2x + 2y = 10 \quad \dots iii$ | |
| | $2x - 3y = 5 \quad \dots ii$ | $\frac{1}{2}$ |
| | $\begin{array}{r} (-) \quad (+) \quad (-) \quad (iii) - (ii) \\ \hline 5y = 5 \\ y = \frac{5}{5} \end{array} \quad y = 1$ | $\frac{1}{2}$ |
| | Substitute the value of y in equation (i) | |
| | $x + y = 5$ | $\frac{1}{2}$ |
| | $x + 1 = 5$ | |
| | $x = 5 - 1$ | |
| | $x = 4$ | $\frac{1}{2}$ |

| Qn. Nos. | Value Points | Marks allotted |
|-------------|--|--|
| | <p><i>Cross multiplication method :</i></p> $\begin{array}{ccc} x & y & 1 \\ 1 & -5 & 1 \\ -3 & -5 & 2 \end{array} \quad \begin{array}{c} 1 \\ -3 \end{array}$ $\frac{x}{-5-15} = \frac{y}{-10+5} = \frac{1}{-3-2}$ $\frac{x}{-20} = \frac{y}{-5} = \frac{1}{-5}$ $\frac{x}{-20} = \frac{1}{-5}$ $-5x = -20$ $x = \frac{-20}{-5}$ $x = 4$ $\frac{y}{-5} = -\frac{1}{5}$ $-5y = -5$ $y = \frac{-5}{-5}$ $y = 1$ | <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p> |
| 19. | <p>In the figure, $ABCD$ is a square of side 14 cm. A, B, C and D are the centres of four congruent circles such that each circle touches externally two of the remaining three circles. Find the area of the shaded region.</p>  | 2 |
| | <p><i>Ans. :</i></p> | |

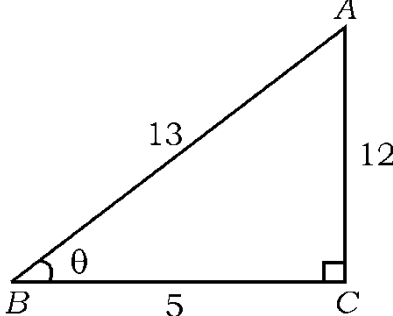
| Qn. Nos. | Value Points | Marks allotted |
|-------------|---|-------------------|
| | Area of the shaded region = Area of square – 4 × area of quadrant | 1/2 |
| | Area of a square = (side) ² = (14) ² | |
| | Area of the square = 196 cm ² | 1/2 |
| | Area of a quadrant = $\frac{1}{4} \pi r^2$ | |
| | 4 × Area of quadrant = $4 \times \frac{1}{4} \pi r^2$ = $4 \times \frac{1}{4} \times \frac{22}{7} \times 7^2$ | 1/2 |
| | 4 × Area of quadrant = 22 × 7 = 154 cm ² | |
| | Area of shaded region = 196 – 154 | |
| | Area of shaded region = 42 cm ² | 1/2 |
| | <i>Alternate method :</i> | |
| | Area of the shaded region = Area of a square – 4 × area of quadrant | 1/2 |
| | Area of a square = (side) ² = (14) ² | |
| | Area of the square = 196 cm ² | 1/2 |
| | Area of a quadrant = $\frac{\theta}{360^\circ} \times \pi r^2$ | |
| | 4 × area of a quadrant = $4 \times \frac{90^\circ}{360^\circ} \times \frac{22}{7} \times 7 \times 7$ = 154 cm ² | 1/2 |
| | Area of shaded region = 196 – 154 | |
| | Area of shaded region = 42 cm ² . | 1/2 |
| | <i>Note :</i> Any alternate method marks can be given. [Area of shaded region = Area of a square – Area of a circle] | 2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|----------------|
| 20. | <p>Draw a circle of radius 4 cm and construct a pair of tangents such that the angle between them is 60°.</p> <p>Ans. :</p> <p>Angle between the radius = $180^\circ - 60^\circ = 120^\circ$</p>  <p style="text-align: right;">Circle — $\frac{1}{2}$ Radii — $\frac{1}{2}$ Tangents — $\frac{1}{2}$</p> | 2 |
| 21. | <p>Find the co-ordinates of point which divides the line segment joining the points A (4, -3) and B (8, 5) in the ratio 3 : 1 internally.</p> <p>Ans. :</p> <p>Let P (x, y) be the required point</p> $(x, y) = \left(\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right)$ <p>OR $(x, y) = \left(\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right)$</p> | 2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|---|------------------------------------|
| | $= \left(\frac{3 \times (8) + (4)}{3+1}, \frac{3 \times (5) + 1 \times (-3)}{3+1} \right)$ $= \left(\frac{24+4}{4}, \frac{15-3}{4} \right)$ $= \left(\frac{28}{4}, \frac{12}{4} \right)$ | 1/2 |
| 22. | <p>Prove that $3 + \sqrt{5}$ is an irrational number.</p> <p><i>Ans. :</i></p> <p>Let us assume $3 + \sqrt{5}$ is a rational number</p> $3 + \sqrt{5} = \frac{p}{q} \text{ where } p, q \in \mathbb{Z}, q \neq 0$ $\sqrt{5} = \frac{p}{q} - 3$ <p>Rearranging this equation</p> $\sqrt{5} = \frac{p-3q}{q}$ <p>Since p and q are integers we get $\frac{p-3q}{q}$ is rational</p> <p>So $\sqrt{5}$ is rational.</p> <p>But this contradicts the fact that $\sqrt{5}$ is irrational</p> <p>$\therefore 3 + \sqrt{5}$ is irrational</p> | 1/2 2 1/2 1/2 1/2 2 |
| 23. | <p>The sum and product of the zeroes of a quadratic polynomial</p> $P(x) = ax^2 + bx + c$ <p>are -3 and 2 respectively. Show that $b + c = 5a$.</p> <p><i>Ans. :</i></p> | 2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|---|----------------|
| | <p>Let α and β are the zeroes of the quadratic polynomial $P(x)$</p> $\alpha + \beta = -3 \quad \frac{1}{2}$ $-\frac{b}{a} = -3$ $-b = -3a$ $b = 3a \quad \dots (i) \quad \frac{1}{2}$ $\alpha\beta = 2$ $\frac{c}{a} = 2$ $c = 2a \quad \dots (ii) \quad \frac{1}{2}$ <p>(i) + (ii) gives</p> $b + c = 3a + 2a$ $b + c = 5a. \quad \frac{1}{2}$ | 2 |
| 24. | <p>Find the quotient and the remainder when $P(x) = 3x^3 + x^2 + 2x + 5$ is divided by $g(x) = x^2 + 2x + 1$.</p> <p>Ans. :</p> $ \begin{array}{r} \quad \quad \quad 3x - 5 \\ x^2 + 2x + 1 \quad) \quad 3x^3 + x^2 + 2x + 5 \quad (\\ \underline{3x^3 + 6x^2 + 3x} \\ (-) \quad (-) \quad (-) \\ \quad \quad \quad -5x^2 - x + 5 \\ \quad \quad \quad -5x^2 - 10x - 5 \\ \quad \quad \quad \underline{+9x + 10} \\ \quad \quad \quad (+) \quad (+) \quad (+) \\ \quad \quad \quad \end{array} $ <p>Quotient = $3x - 5$ $\frac{1}{2}$</p> <p>Remainder = $9x + 10$ $\frac{1}{2}$</p> | 2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|---|
| 25. | <p>Solve $2x^2 - 5x + 3 = 0$ by using formula.</p> <p>Ans. :</p> <p>Comparing the equation with</p> $ax^2 + bx + c = 0$ $a = 2 \quad b = -5 \quad c = 3$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4 \times 2 \times 3}}{2 \times 2}$ $x = \frac{5 \pm \sqrt{25 - 24}}{4}$ $x = \frac{5 \pm \sqrt{1}}{4}$ $x = \frac{5 \pm 1}{4}$ $x = \frac{5+1}{4}, \quad x = \frac{5-1}{4}$ $x = \frac{6}{4} \quad x = \frac{4}{4}$ $x = \frac{3}{2} \quad x = 1$ | <p>2</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p> |
| 26. | <p>The length of a rectangular field is 3 times its breadth. If the area of the field is 147 sq.m, find its length and breadth.</p> <p>Ans. :</p> <p>Let the breadth be x</p> <p>\therefore Length = $3x$</p> $A = l \times b$ $147 = 3x \times x$ $147 = 3x^2$ $x^2 = \frac{147}{3}$ | <p>2</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> |

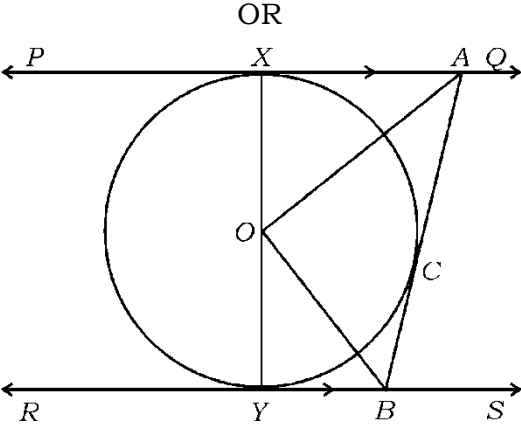
| Qn. Nos. | Value Points | Marks allotted |
|----------|---|----------------|
| 27. | $x^2 = 49$ $x = \pm \sqrt{49}$ $x = \pm 7$ $\therefore \text{Breadth } (x) = 7 \text{ cm}$ $\text{Length } (3x) = 3 \times 7 = 21 \text{ cm}$ | 2 |
| | <p>If $\sin \theta = \frac{12}{13}$, find the values of $\cos \theta$ and $\tan \theta$.</p> | |
| | OR | |
| | <p>If $\sqrt{3} \tan \theta = 1$ and θ is acute, find the value of $\sin 3\theta + \cos 2\theta$.</p> | |
| | <p>Ans. :</p> | |
| |  | $\frac{1}{2}$ |
| | $AB^2 = AC^2 + BC^2$ | |
| | $13^2 = 12^2 + BC^2$ | |
| | $169 = 144 + BC^2$ | |
| | $BC^2 = 169 - 144$ | |
| | $BC^2 = 25 \quad BC = \sqrt{25}$ | |
| | $BC = 5$ | |
| | $\cos \theta = \frac{BC}{AC} = \frac{5}{13}$ | $\frac{1}{2}$ |
| | $\tan \theta = \frac{AC}{BC} = \frac{12}{5}$ | $\frac{1}{2}$ |
| | OR | 2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|---|
| | $\sqrt{3} \tan \theta = 1$ $\tan \theta = \frac{1}{\sqrt{3}}$ $\tan \theta = \tan 30^\circ$ $\theta = 30^\circ$ $\sin 3\theta = \sin 3 \times 30^\circ = \sin 90^\circ = 1$ $\cos 2\theta = \cos 2 \times 30^\circ = \cos 60^\circ = \frac{1}{2}$ $\sin 3\theta + \cos 2\theta = 1 + \frac{1}{2} = 1\frac{1}{2}$ $\sin 3\theta + \cos 2\theta = \frac{3}{2}$ | <p style="text-align: right;">1/2</p> <p style="text-align: right;">1</p> <p style="text-align: right;">1/2</p> |
| 28. | <p>Prove that $\left(\frac{1 + \cos \theta}{1 - \cos \theta} \right) = (\operatorname{cosec} \theta + \cot \theta)^2$.</p> <p>Ans. :</p> <p>L.H.S. = $\left(\frac{1 + \cos \theta}{1 - \cos \theta} \right)$</p> $= \frac{(1 + \cos \theta)}{(1 - \cos \theta)} \times \frac{(1 + \cos \theta)}{(1 + \cos \theta)}$ $= \frac{(1 + \cos \theta)^2}{1^2 - \cos^2 \theta}$ $= \frac{(1 + \cos \theta)^2}{\sin^2 \theta}$ $= \left(\frac{1 + \cos \theta}{\sin \theta} \right)^2$ $= \left(\frac{1}{\sin \theta} + \frac{\cos \theta}{\sin \theta} \right)^2$ $\frac{1 + \cos \theta}{1 - \cos \theta} = (\operatorname{cosec} \theta + \cot \theta)^2 = \text{R.H.S.}$ <p>Any alternative method, marks can be awarded.</p> | <p style="text-align: right;">2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">2</p> |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|----------------|
| 29. | <p>A cubical die numbered from 1 to 6 are rolled twice. Find the probability of getting the sum of numbers on its faces is 10. 2</p> <p>Ans. :</p> $n(S) = 36 \quad \frac{1}{2}$ $n(A) = \{(5, 5) (4, 6) (6, 4)\} = 3 \quad \frac{1}{2}$ $P(A) = \frac{n(A)}{n(S)} \quad \frac{1}{2}$ $= \frac{3}{36} \quad \frac{1}{2}$ | 2 |
| 30. | <p>The radii of two circular ends of a frustum of a cone shaped dustbin are 15 cm and 8 cm. If its depth is 63 cm, find the volume of the dustbin. 2</p> <p>Ans. :</p> $r_1 = 15 \text{ cm} \quad r_2 = 8 \text{ cm} \quad h = 63 \text{ cm}$ $\text{Volume of dustbin (V)} = \frac{1}{3}\pi h (r_1^2 + r_2^2 + r_1 r_2) \quad \frac{1}{2}$ $= \frac{1}{3} \times \frac{22}{7} \times 63 (15^2 + 8^2 + 15 \times 8) \quad \frac{1}{2}$ $= 66 (225 + 64 + 120) \quad \frac{1}{2}$ $= 66 \times 409$ | 2 |
| | <p>Volume of dustbin (V) = 26994 cm³. ½</p> | 2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|---|----------------|
| IV. 31. | <p>Prove that “the lengths of tangents drawn from an external point to a circle are equal”.</p> <p style="text-align: right;">3</p> <p style="text-align: center;">OR</p> <p>In the given figure PQ and RS are two parallel tangents to a circle with centre O and another tangent AB with point of contact C intersecting PQ at A and RS at B. Prove that $\angle AOB = 90^\circ$.</p> | |
| | | |
| | <p>Ans. :</p> <div style="text-align: center;"> </div> | 1/2 |
| | <p><i>Data :</i> O is the centre of the circle P is an external point PQ and PR are the tangents</p> | 1/2 |
| | <p><i>To prove :</i> $PQ = PR$</p> | 1/2 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|--|
| | <p><i>Construction :</i> OQ, OR and OP are joined</p> <p><i>Proof:</i> In $\triangle POQ$ and $\triangle POR$</p> <p>$\angle PQO = \angle PRO$ (Radius drawn at the point of contact is perpendicular to the tangent)</p> <p>$hyp\ OP = hyp\ OP$ (Common side)</p> <p>$OQ = OR$ (Radii of same circle)</p> <p>$\therefore \triangle POQ \cong \triangle POR$ (R.H.S. theorem)</p> <p>$\therefore PQ = PR$</p> <p><i>Alternate method :</i></p> <div data-bbox="502 1064 1093 1467" style="text-align: center;"> </div> <p><i>Proof:</i> We are given a circle with centre O a point P lying outside the circle and two tangents PQ and PR on the circle from P.</p> <p>We are required to prove that $PQ = PR$</p> <p>For this we join OP, OQ and OR.</p> <p>Then $\angle OQP$ and $\angle ORP$ are right angles because these are angles between the radii and tangents.</p> | <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>3</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> |

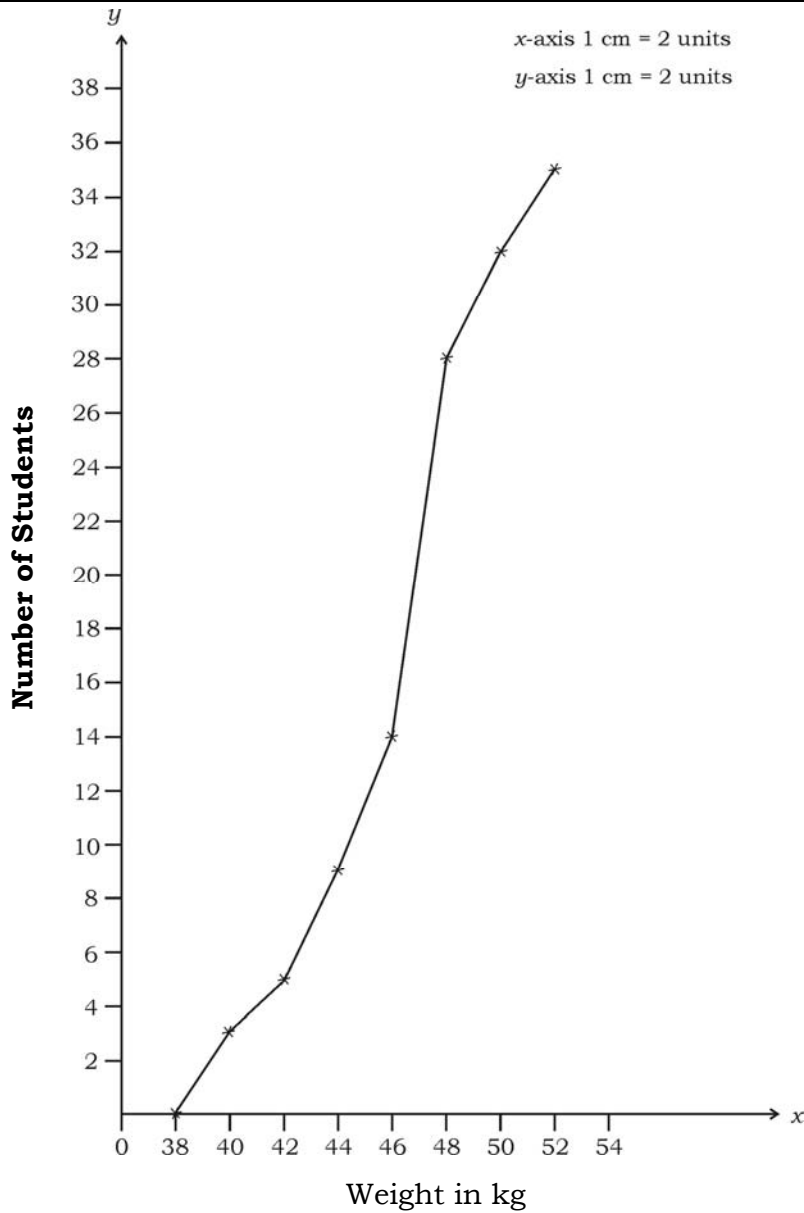
| Qn. Nos. | Value Points | Marks allotted |
|----------|---|--|
| | <p>According to theorem 4.1 they are right angles</p> <p>Now in right triangles angles OQP and ORP</p> <p>$OQ = OR$ (Radii of same circle)</p> <p>$OP = OP$ (common)</p> <p>Therefore $\Delta OQP = \Delta ORP$ (R.H.S.)</p> <p>This gives $PQ = PR$.</p> | <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>3</p> |
| |  <p>Let $\angle OAB = x$</p> <p>$\therefore \angle OAX = x$</p> <p>$\angle OBA = y$</p> <p>$\angle OBY = y$</p> <p>$PQ \parallel RS$</p> <p>$\therefore \angle XAB + \angle YBA = 180^\circ$</p> <p>$2x + 2y = 180^\circ$</p> <p>$2(x + y) = 180^\circ$</p> <p>$x + y = \frac{180^\circ}{2}$</p> <p>$x + y = 90^\circ$</p> | <p>$\frac{1}{2}$</p> <p>1</p> |

| Qn. Nos. | Value Points | Marks allotted | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------------|--|---|---------------------|-------|---|-------|----|--------|----|---------|----|---------|---|---------|---|----------------|---------------------|---------|---|---------|---|---------|---|---------|---|---------|---|----------|---|--|
| | <p>In $\triangle AOB$</p> $\angle OAB + \angle OBA + \angle AOB = 180^\circ$ $x + y + \angle AOB = 180^\circ$ $90^\circ + \angle AOB = 180^\circ \quad (\because x + y = 90^\circ)$ $\angle AOB = 180^\circ - 90^\circ$ $\angle AOB = 90^\circ$ | <p>1</p> <p>$\frac{1}{2}$</p> <p>3</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 32. | <p>Calculate the median of the following frequency distribution table : 3</p> <table border="1" data-bbox="571 902 1137 1294"> <thead> <tr> <th>Class-interval</th> <th>Frequency (f_i)</th> </tr> </thead> <tbody> <tr> <td>1 — 4</td> <td>6</td> </tr> <tr> <td>4 — 7</td> <td>30</td> </tr> <tr> <td>7 — 10</td> <td>40</td> </tr> <tr> <td>10 — 13</td> <td>16</td> </tr> <tr> <td>13 — 16</td> <td>4</td> </tr> <tr> <td>16 — 19</td> <td>4</td> </tr> </tbody> </table> <p style="text-align: right;">$\Sigma f_i = 100$</p> <p style="text-align: center;">OR</p> <p>Calculate the mode for the following frequency distribution table.</p> <table border="1" data-bbox="571 1458 1137 1850"> <thead> <tr> <th>Class-interval</th> <th>Frequency (f_i)</th> </tr> </thead> <tbody> <tr> <td>10 — 25</td> <td>2</td> </tr> <tr> <td>25 — 40</td> <td>3</td> </tr> <tr> <td>40 — 55</td> <td>7</td> </tr> <tr> <td>55 — 70</td> <td>6</td> </tr> <tr> <td>70 — 85</td> <td>6</td> </tr> <tr> <td>85 — 100</td> <td>6</td> </tr> </tbody> </table> <p style="text-align: right;">$\Sigma f_i = 30$</p> <p>Ans. :</p> | Class-interval | Frequency (f_i) | 1 — 4 | 6 | 4 — 7 | 30 | 7 — 10 | 40 | 10 — 13 | 16 | 13 — 16 | 4 | 16 — 19 | 4 | Class-interval | Frequency (f_i) | 10 — 25 | 2 | 25 — 40 | 3 | 40 — 55 | 7 | 55 — 70 | 6 | 70 — 85 | 6 | 85 — 100 | 6 | |
| Class-interval | Frequency (f_i) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 — 4 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 — 7 | 30 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7 — 10 | 40 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 — 13 | 16 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 13 — 16 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 16 — 19 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Class-interval | Frequency (f_i) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 — 25 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 — 40 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 40 — 55 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 55 — 70 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 70 — 85 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 85 — 100 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Qn. Nos. | Value Points | | | Marks allotted |
|-------------|---|------------------|-----------------------------|-------------------|
| | <i>Class-interval</i> | <i>Frequency</i> | <i>Cumulative frequency</i> | |
| | 1 — 4 | 6 | 6 | |
| | 4 — 7 | 30 | 36 | |
| | 7 — 10 | 40 | 76 | 1/2 |
| | 10 — 13 | 16 | 92 | |
| | 13 — 16 | 4 | 96 | |
| | 16 — 19 | 4 | 100 | |
| | $\frac{n}{2} = \frac{100}{2} = 50$ | | | |
| | Lower limit of median class | $l = 7$ | | |
| | C.F. of class preceding median class | $c.f. = 36$ | | |
| | Frequency of median class | $f = 40$ | | |
| | Class size | $h = 3$ | | |
| | Median = $l + \left[\frac{\frac{n}{2} - c.f.}{f} \right] \times h$ | 1/2 | | |
| | $= 7 + \left[\frac{50 - 36}{40} \right] \times 3$ | 1/2 | | |
| | $= 7 + \left[\frac{14}{40} \right] \times 3$ | | | |
| | $= 7 + \frac{21}{20}$ | | | |
| | $= 7 + 1.05$ | | | |
| | Median = 8.05 | 1/2 | | 3 |
| | OR | | | |
| | Lower limit | $l = 40$ | | |
| | Frequency of modal class | $f_1 = 7$ | | |
| | Frequency of preceding modal class | $f_0 = 3$ | | |

| Qn. Nos. | Value Points | Marks allotted | | | | | | | | | | | | | | | | | |
|------------------|--|--|------------------|--------------------|--------------|---|--------------|---|--------------|---|--------------|---|--------------|----|--------------|----|--------------|----|--------------|
| 33. | Succeeding modal class $f_2 = 6$ | | | | | | | | | | | | | | | | | | |
| | Class size $h = 15$ | 1 | | | | | | | | | | | | | | | | | |
| | Mode = $l + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$ | $\frac{1}{2}$ | | | | | | | | | | | | | | | | | |
| | $= 40 + \left[\frac{7 - 3}{14 - 6 - 3} \right] \times 15$ | $\frac{1}{2}$ | | | | | | | | | | | | | | | | | |
| | $= 40 + \left[\frac{4}{5} \right] \times 15$ | | | | | | | | | | | | | | | | | | |
| | $= 40 + \frac{4}{5} \times 15$ | $\frac{1}{2}$ | | | | | | | | | | | | | | | | | |
| | $= 40 + 12$ | | | | | | | | | | | | | | | | | | |
| | Mode = 52 | $\frac{1}{2}$ | | | | | | | | | | | | | | | | | |
| | During the medical check-up of 35 students of a class, their weights were recorded as follows. Draw a less than type of ogive for the given data : | 3 | | | | | | | | | | | | | | | | | |
| | Ans. : | <table border="1" data-bbox="568 1267 1139 1877"> <thead> <tr> <th data-bbox="568 1267 852 1375">Weight (in kg)</th> <th data-bbox="852 1267 1139 1375">Number of students</th> </tr> </thead> <tbody> <tr> <td data-bbox="568 1375 852 1438">Less than 38</td> <td data-bbox="852 1375 1139 1438">0</td> </tr> <tr> <td data-bbox="568 1438 852 1500">Less than 40</td> <td data-bbox="852 1438 1139 1500">3</td> </tr> <tr> <td data-bbox="568 1500 852 1563">Less than 42</td> <td data-bbox="852 1500 1139 1563">5</td> </tr> <tr> <td data-bbox="568 1563 852 1626">Less than 44</td> <td data-bbox="852 1563 1139 1626">9</td> </tr> <tr> <td data-bbox="568 1626 852 1688">Less than 46</td> <td data-bbox="852 1626 1139 1688">14</td> </tr> <tr> <td data-bbox="568 1688 852 1751">Less than 48</td> <td data-bbox="852 1688 1139 1751">28</td> </tr> <tr> <td data-bbox="568 1751 852 1814">Less than 50</td> <td data-bbox="852 1751 1139 1814">32</td> </tr> <tr> <td data-bbox="568 1814 852 1877">Less than 52</td> <td data-bbox="852 1814 1139 1877">35</td> </tr> </tbody> </table> | Weight (in kg) | Number of students | Less than 38 | 0 | Less than 40 | 3 | Less than 42 | 5 | Less than 44 | 9 | Less than 46 | 14 | Less than 48 | 28 | Less than 50 | 32 | Less than 52 |
| Weight (in kg) | Number of students | | | | | | | | | | | | | | | | | | |
| Less than 38 | 0 | | | | | | | | | | | | | | | | | | |
| Less than 40 | 3 | | | | | | | | | | | | | | | | | | |
| Less than 42 | 5 | | | | | | | | | | | | | | | | | | |
| Less than 44 | 9 | | | | | | | | | | | | | | | | | | |
| Less than 46 | 14 | | | | | | | | | | | | | | | | | | |
| Less than 48 | 28 | | | | | | | | | | | | | | | | | | |
| Less than 50 | 32 | | | | | | | | | | | | | | | | | | |
| Less than 52 | 35 | | | | | | | | | | | | | | | | | | |

| Qn. Nos. | Value Points | Marks allotted |
|----------|--------------|----------------|
|----------|--------------|----------------|



x and y axis scale — 1/2
 Plotting points — 1 1/2
 Drawing graph — 1

3

Note : Scale, x-axis, y-axis can be changed.

34. The seventh term of an Arithmetic progression is four times its second term and twelfth term is 2 more than three times of its fourth term. Find the progression. 3

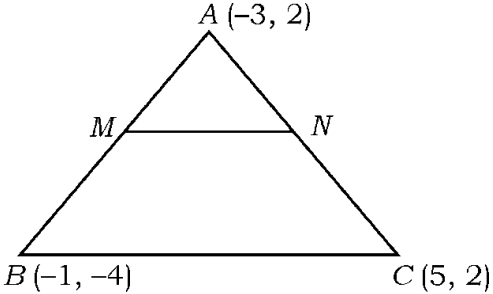
OR

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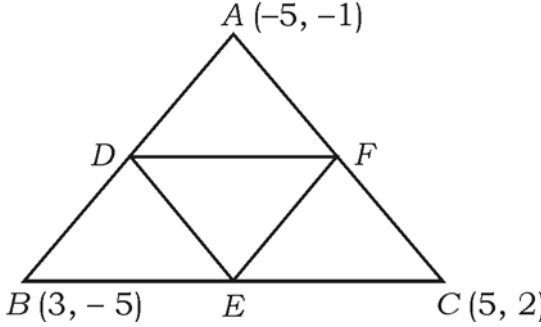
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| Qn. Nos. | Value Points | Marks allotted |
|----------|--|---|
| | <p>A line segment is divided into four parts forming an Arithmetic progression. The sum of the lengths of 3rd and 4th parts is three times the sum of the lengths of first two parts. If the length of fourth part is 14 cm, find the total length of the line segment.</p> <p>Ans. :</p> $\left. \begin{aligned} a_7 = T_7 &= 4(T_2) a_2 \\ a + 6d &= 4(a + d) \\ a + 6d &= 4a + 4d \\ 6d - 4d &= 4a - a \end{aligned} \right\}$ $2d = 3a \quad \dots (i)$ $a_{12} = T_{12} = 3T_4 (a_4) + 2$ $a + 11d = 3(a + 3d) + 2$ $a + 11d = 3a + 9d + 2$ $11d - 9d = 3a - a + 2$ $2d = 2a + 2 \quad \dots (ii)$ <p>substituting (i) in (ii)</p> $3a = 2a + 2$ $3a - 2a = 2$ $a = 2$ $2d = 3a$ $2d = 3 \times 2$ $2d = 6$ $d = \frac{6}{2}$ $d = 3$ | <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> |

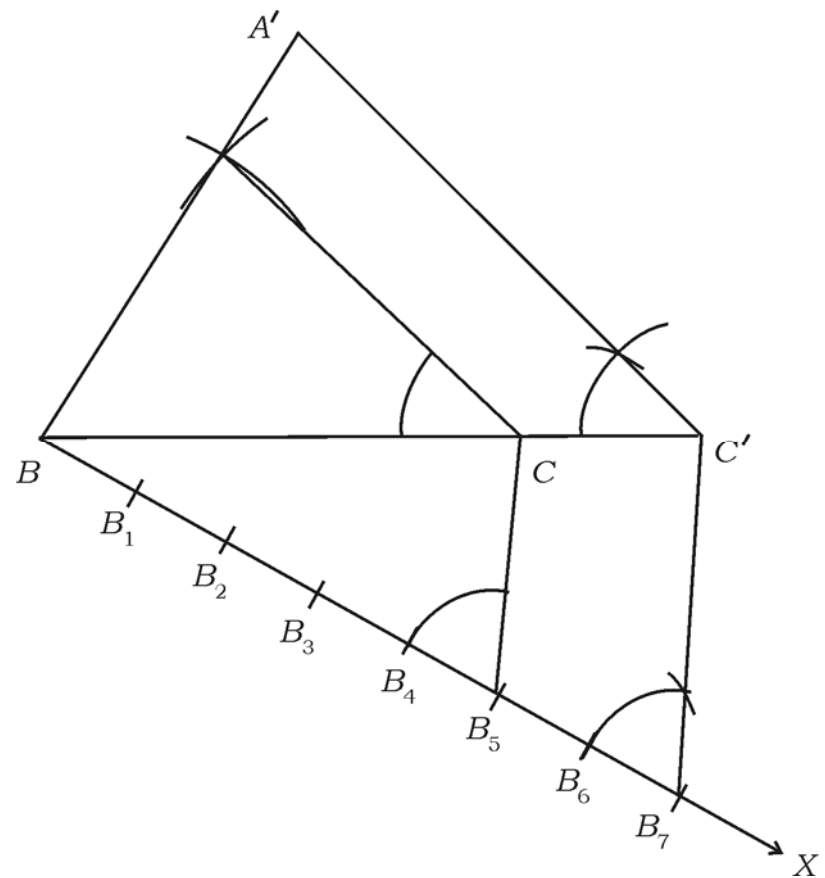
| Qn. Nos. | Value Points | Marks allotted |
|-------------|---|--|
| | <p>\therefore The required sequence</p> $a, \quad a + d, \quad a + 2d$ $2, \quad 2 + 3, \quad 2 + 2 \times 3$ <p>The required sequence 2, 5, 8</p> <p style="text-align: center;">OR</p> <p>Let the four parts of the line segment be</p> $a - 3d, \quad a - d, \quad a + d, \quad a + 3d$ <p>According to the data</p> $(a + d + a + 3d) = 3(a - 3d + a - d)$ $2a + 4d = 3(2a - 4d)$ $2(a + 2d) = 3 \times 2(a - 2d)$ $a + 2d = 3a - 6d$ $2d + 6d = 3a - a$ $2a = 8d$ $a = \frac{8d}{2}$ $a = 4d$ $a + 3d = 14$ $4d + 3d = 14$ $7d = 14$ $d = \frac{14}{7}$ $d = 2$ $a = 4d$ $a = 4 \times 2$ $a = 8$ | <p>$\frac{1}{2}$</p> <p>3</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> |

| Qn. Nos. | Value Points | Marks allotted |
|----------|---|---|
| 35. | <p>∴ Length of the line segment =</p> $= a - 3d + a - d + a + d + a + 3d$ $= 4a$ $= 4 \times 8 = 32 \text{ cm.}$ <p><i>Note</i> : Any alternate method marks can be given.</p> <p>The vertices of a ΔABC are $A(-3, 2)$, $B(-1, -4)$ and $C(5, 2)$. If M and N are the mid-points of AB and AC respectively, show that $2MN = BC$.</p> <p style="text-align: center;">OR</p> <p>The vertices of a ΔABC are $A(-5, -1)$, $B(3, -5)$, $C(5, 2)$. Show that the area of the ΔABC is four times the area of the triangle formed by joining the mid-points of the sides of the triangle ABC.</p> <p><i>Ans.</i> :</p> <div style="text-align: center;">  </div> <p>Co-ordinates of $M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$</p> $= \left(\frac{-1 - 3}{2}, \frac{-4 + 2}{2} \right)$ <p>Co-ordinates of $M = (-2, -1)$</p> <p>Co-ordinates of $N = \left(\frac{5 - 3}{2}, \frac{2 + 2}{2} \right)$</p> $= \left(\frac{2}{2}, \frac{4}{2} \right)$ <p>Co-ordinates of $N = (1, 2)$</p> <p>Length of $MN = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$</p> | <p style="text-align: right;">$\frac{1}{2}$</p> <p style="text-align: right;">3</p> <p style="text-align: right;">3</p> <p style="text-align: right;">1</p> <p style="text-align: right;">$\frac{1}{2}$</p> |

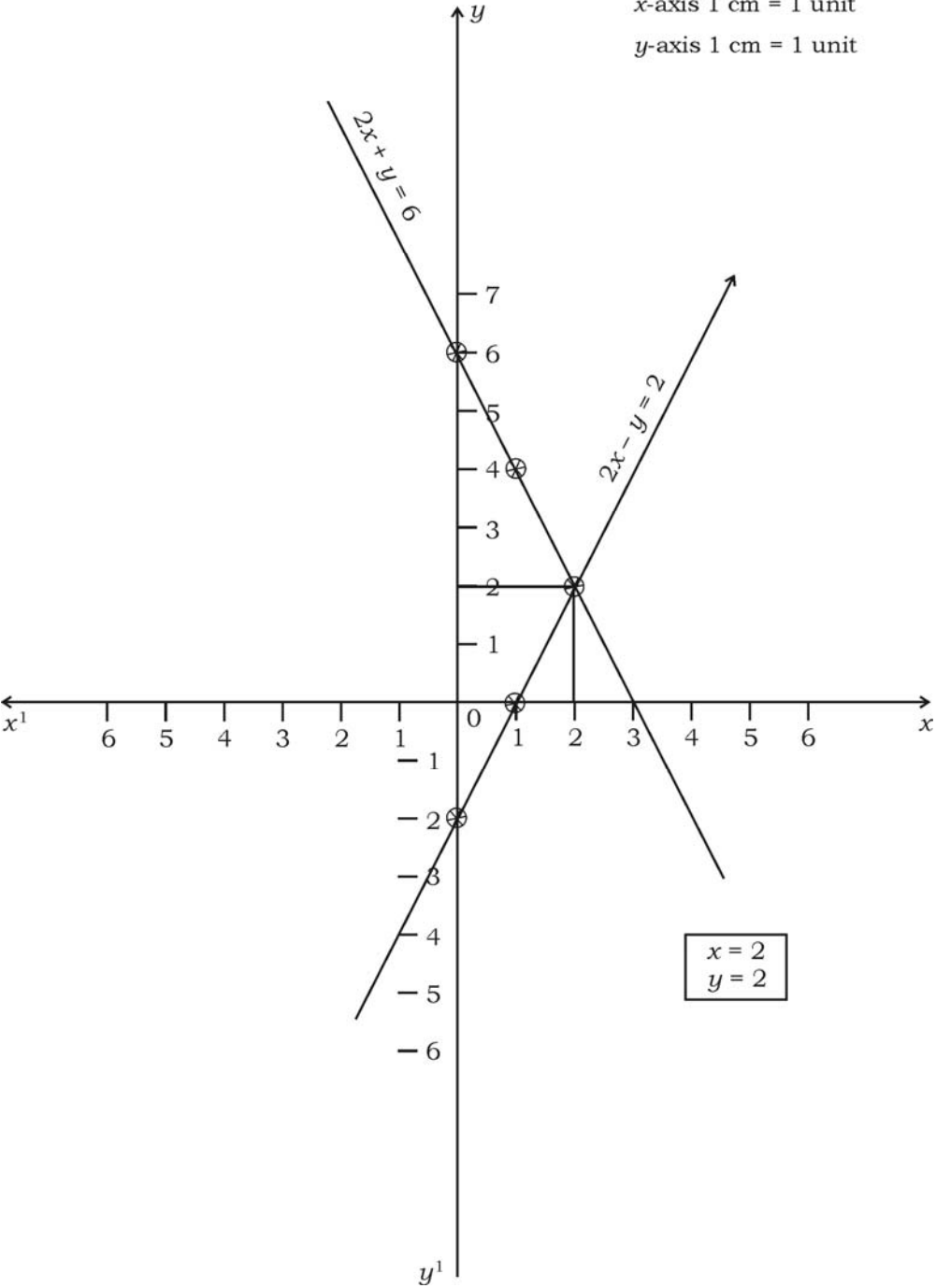
| Qn. Nos. | Value Points | Marks allotted |
|-------------|--|-------------------|
| | $= \sqrt{(1+2)^2 + (2+1)^2}$ $= \sqrt{3^2 + 3^2}$ $= \sqrt{9+9} = \sqrt{18}$ $= \sqrt{9 \times 2} = 3\sqrt{2}$ $MN = 3\sqrt{2}$ | 1/2 |
| | <p>Length of $BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$</p> $= \sqrt{(5+1)^2 + (2+4)^2}$ $= \sqrt{6^2 + 6^2}$ $= \sqrt{36+36}$ $= \sqrt{72}$ $= \sqrt{36 \times 2}$ $BC = 6\sqrt{2}$ | 1/2 |
| | $2MN = 2 \times 3\sqrt{2}$ $= 6\sqrt{2}$ | |
| | $\therefore 2MN = BC$ | 1/2 |
| | OR | |
| | | 3 |

| Qn. Nos. | Value Points | Marks allotted |
|-------------|--|-------------------|
| | <div style="text-align: center;">  <p style="text-align: center;"> $A(-5, -1)$ $B(3, -5)$ E $C(5, 2)$ </p> </div> <p> $(x_1, y_1) = (-5, -1), (x_2, y_2) = (3, -5), (x_3, y_3) = (5, 2)$ </p> <p>Area of triangle $ABC =$</p> $= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ $= \frac{1}{2} [-5(-5 - 2) + 3(2 + 1) + 5(-1 + 5)] \quad \frac{1}{2}$ $= \frac{1}{2} [-5 \times (-7) + 3 \times 3 + 5 \times 4]$ $= \frac{1}{2} [35 + 9 + 20]$ $= \frac{1}{2} \times 64 \quad \frac{1}{2}$ <p>Area of $\Delta ABC = 32$ sq.units</p> <p>Co-ordinates of $D = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$</p> $= \left(\frac{-5 + 3}{2}, \frac{-1 - 5}{2} \right)$ $= \left(\frac{-2}{2}, \frac{-6}{2} \right)$ <p>Co-ordinates of $D = (-1, -3)$</p> | |

| Qn. Nos. | Value Points | Marks allotted |
|-------------|--|---|
| | <p>Co-ordinates of $E = \left(\frac{3+5}{2}, \frac{-5+2}{2} \right)$ $= \left(\frac{8}{2}, \frac{-3}{2} \right)$</p> <p>Co-ordinates of $E = \left(4, \frac{-3}{2} \right)$</p> <p>Co-ordinates of $F = \left(\frac{-5+5}{2}, \frac{-1+2}{2} \right)$ $= \left(\frac{0}{2}, \frac{1}{2} \right)$</p> <p>Co-ordinates of $F = \left(0, \frac{1}{2} \right)$</p> <p>$(x_1, y_1) = (-1, -3)$ $(x_2, y_2) = \left(4, -\frac{3}{2} \right)$ $(x_3, y_3) = \left(0, \frac{1}{2} \right)$</p> <p>Area of $\Delta DEF =$ $= \frac{1}{2} \left[-1 \left(\frac{-3}{2} - \frac{1}{2} \right) + 4 \left(\frac{1}{2} + 3 \right) + 0 \left(-3 + \frac{3}{2} \right) \right]$ $= \frac{1}{2} \left[-1 \times (-2) + 4 \times \frac{7}{2} + 0 \right]$ $= \frac{1}{2} [2 + 14]$ $= \frac{1}{2} \times 16$</p> <p>$\Delta DEF = 8$ sq. units</p> <p>\therefore Area of $\Delta ABC = 4 \times$ area of ΔDEF</p> <p>$32 = 4 \times 8$</p> <p>$32 = 32$</p> <p><i>Note : Any alternate method can be given marks.</i></p> | <p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>3</p> |

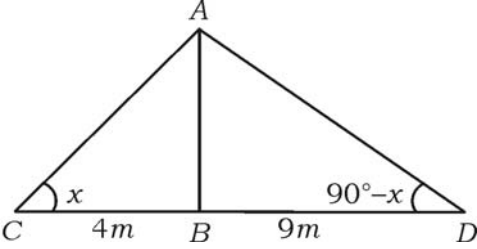
| Qn. Nos. | Value Points | Marks allotted |
|----------|--|----------------|
| 36. | <p>Construct a triangle with sides 5 cm, 6 cm and 7 cm and then construct another triangle whose sides are $\frac{7}{5}$ of the corresponding sides of the first triangle.</p> <p>Ans. :</p>  <p>Constructing given triangle 1</p> <p>Drawing acute angle line and dividing into 7 parts $\frac{1}{2}$</p> <p>Drawing parallel lines (one pair) $\frac{1}{2}$</p> <p>Drawing parallel line (another pair) $\frac{1}{2}$</p> <p>Triangle $A'BC'$ $\frac{1}{2}$</p> | 3 |

| Qn. Nos. | Value Points | Marks allotted | | | | | | | | | | | | | | | | |
|----------|---|----------------|---|---|---|---|---|---|---|---|---|---|---|---|----|---|---|--|
| V. 37. | <p>Find the solution of the following pairs of linear equation by the graphical method :</p> $2x + y = 6$ $2x - y = 2$ <p>Ans. :</p> $2x + y = 6$ $y = 6 - 2x$ <table border="1" data-bbox="381 902 863 1016"> <tr> <td>x</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td>y</td> <td>6</td> <td>4</td> <td>2</td> </tr> </table> $2x - y = 2$ $y = 2x - 2$ <table border="1" data-bbox="381 1180 863 1294"> <tr> <td>x</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td>y</td> <td>-2</td> <td>0</td> <td>2</td> </tr> </table> <p>Tables —</p> <p>Drawing or Plotting 2 straight lines —</p> <p>Identifying Intersecting straight line points and answer —</p> <p>Note : Any two points can be taken for each equation.</p> | x | 0 | 1 | 2 | y | 6 | 4 | 2 | x | 0 | 1 | 2 | y | -2 | 0 | 2 | <p>4</p> <p>2</p> <p>1</p> <p>1</p> <p>4</p> |
| x | 0 | 1 | 2 | | | | | | | | | | | | | | | |
| y | 6 | 4 | 2 | | | | | | | | | | | | | | | |
| x | 0 | 1 | 2 | | | | | | | | | | | | | | | |
| y | -2 | 0 | 2 | | | | | | | | | | | | | | | |

| Qn. Nos. | Value Points | Marks allotted |
|----------|---|----------------|
| 38. | <p data-bbox="975 309 1222 338">x-axis 1 cm = 1 unit</p> <p data-bbox="975 349 1222 378">y-axis 1 cm = 1 unit</p>  | 4 |

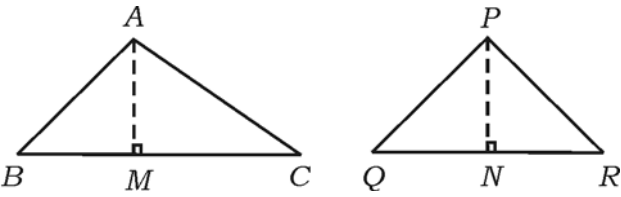
38. The angles of elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower and in the same straight line with it are complementary. Find the height of the tower.

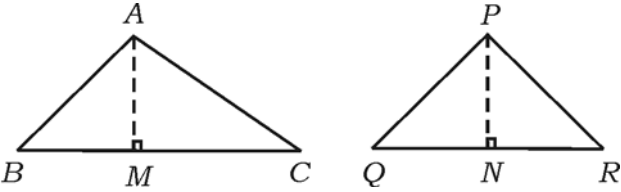
Ans. :

| Qn. Nos. | Value Points | Marks allotted |
|----------|--|--|
| |  | 1/2 |
| | <p>Let AB be tower</p> $\angle ACB = x^\circ$ <p>$\therefore \angle ADB = 90^\circ - x$</p> <p>In $\triangle ABC$</p> $\tan x = \frac{AB}{BC}$ $\tan x = \frac{AB}{4} \quad \dots (i)$ <p>In $\triangle ADB$</p> $\tan (90^\circ - x) = \frac{AB}{9}$ $\cot x = \frac{AB}{9} \quad \dots (ii)$ <p>(i) \times (ii)</p> $\tan x \times \cot x = \frac{AB}{4} \times \frac{AB}{9}$ $\tan x \times \frac{1}{\tan x} = \frac{AB^2}{36}$ $1 = \frac{AB^2}{36}$ $AB^2 = 36$ $AB = \pm \sqrt{36} \quad AB = \pm 6$ <p>\therefore Height of the tower $AB = 6$ m.</p> <p><i>Note :</i> C and D can be taken on the same side of AB.</p> <p><i>Alternate method :</i></p> $\cot x = \frac{AB}{9} \quad \frac{1}{\tan x} = \frac{AB}{9} \quad \frac{1}{\frac{AB}{4}} = \frac{AB}{9}$ $\frac{4}{AB} = \frac{AB}{9} \quad AB^2 = 36 \quad AB = \pm 6$ <p>$AB = 6$ m.</p> | 1/2 1/2 1/2 1 1/2 1/2 4 |

| Qn. Nos. | Value Points | Marks allotted |
|---|--|----------------|
| 39. | <p>The bottom of a right cylindrical shaped vessel made from metallic sheet is closed by a cone shaped vessel as shown in the figure. The radius of the circular base of the cylinder and radius of the circular base of the cone each is equal to 7 cm. If the height of the cylinder is 20 cm and height of cone is 3 cm, calculate the cost of milk to fill completely this vessel at the rate of Rs. 20 per litre. 4</p> | |
| | | |
| OR | | |
| <p>A hemispherical vessel of radius 14 cm is fully filled with sand. This sand is poured on a level ground. The heap of sand forms a cone shape of height 7 cm. Calculate the area of ground occupied by the circular base of the heap of the sand.</p> | | |
| Ans. : | | |
| | | |
| <p>Volume of the vessel is equal to</p> <p>Volume of the cylinder – Volume of cone 1/2</p> <p>Volume of the cylinder = $\pi r^2 h$ 1/2</p> <p style="text-align: center;">$= \frac{22}{7} \times 7^2 \times 20$</p> <p>Volume of the cylinder = 3080 cm^3 1/2</p> | | |

| Qn. Nos. | Value Points | Marks allotted | | | | |
|---------------------|---|-------------------|-------------|---------------------|---------------------|--|
| | $\text{Volume of the cone} = \frac{1}{3} \pi r^2 h$ $= \frac{1}{3} \times \frac{22}{7} \times 7^2 \times 3$ | 1/2 | | | | |
| | $\text{Volume of the cone} = 154 \text{ cm}^3$ | 1/2 | | | | |
| | $\text{Volume of vessel} = \text{Volume of cylinder} - \text{volume of cone}$ $= 3080 - 154$ $= 2926 \text{ cm}^3$ $= \frac{2926}{1000} = 2.926 \text{ litres.}$ | 1/2 1/2 | | | | |
| | $\therefore \text{Cost of milk to fill this vessel at the rate of Rs. 20 per litre}$ $= 2.926 \times 20$ $= 58.520$ $= \text{Rs. } 58.520$ | 1/2 | | | | |
| | OR | | | | | |
| | $\text{Volume of the hemisphere} = \frac{2}{3} \pi r^3$ | 1/2 | | | | |
| | $\text{Volume of the cone} = \frac{1}{3} \pi r^2 h$ | 1/2 | | | | |
| | <table style="width: 100%; border: none;"> <tr> <td style="text-align: center; width: 50%;"><u>Hemisphere</u></td> <td style="text-align: center; width: 50%;"><u>Cone</u></td> </tr> <tr> <td style="text-align: center;">$r = 14 \text{ cm}$</td> <td style="text-align: center;">$h = 7 \text{ cm.}$</td> </tr> </table> | <u>Hemisphere</u> | <u>Cone</u> | $r = 14 \text{ cm}$ | $h = 7 \text{ cm.}$ | |
| <u>Hemisphere</u> | <u>Cone</u> | | | | | |
| $r = 14 \text{ cm}$ | $h = 7 \text{ cm.}$ | | | | | |
| | $\text{Volume of hemisphere} = \text{Volume of cone}$ $\frac{2}{3} \pi r^3 = \frac{1}{3} \pi r^2 h$ $2 \times (14)^3 = r^2 \times 7$ $r^2 = \frac{2 \times (14)^3}{7}$ $= \frac{2 \times 14 \times 14 \times 14}{7}$ $r^2 = 196 \times 4$ $r^2 = 784$ | 1/2 1 | | | | |

| Qn. Nos. | Value Points | Marks allotted |
|----------|---|----------------|
| | $r = \sqrt{784}$ $r = 28 \text{ cm}$ <p>∴ The area occupied by the circular base of the heap of the sand on the ground</p> $= \pi r^2 \quad \frac{1}{2}$ $= \frac{22}{7} \times (28)^2$ $= \frac{22}{7} \times 28 \times 28 \quad \frac{1}{2}$ $= 2464 \text{ cm}^2 \quad \frac{1}{2}$ | 4 |
| 40. | <p>Prove that “the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides”.</p> <p>Ans. :</p> <div style="text-align: center;">  </div> <p style="text-align: right;">$\frac{1}{2}$</p> <p><i>Data :</i> $\triangle ABC \sim \triangle PQR$ $\frac{1}{2}$</p> <p><i>To prove :</i> $\frac{\text{Area of } \triangle ABC}{\text{Area of } \triangle PQR} = \frac{BC^2}{QR^2}$ $\frac{1}{2}$</p> <p><i>Construction :</i> Draw $AM \perp BC$ and $PN \perp QR$ $\frac{1}{2}$</p> <p><i>Proof :</i> In $\triangle AMB$ and $\triangle PQN$</p> <p>$\angle ABM = \angle PQN$ (Data)</p> <p>$\angle AMB = \angle PNQ = 90^\circ$ (Construction)</p> <p>$\triangle AMB \sim \triangle PQN$ $\frac{1}{2}$</p> <p>∴ $\frac{AM}{PN} = \frac{AB}{PQ}$ A.A criteria</p> <p>But $\frac{BC}{QR} = \frac{AB}{PQ}$ Data</p> <p>∴ $\frac{AB}{PQ} = \frac{BC}{QR}$ $\frac{1}{2}$</p> | 4 |

| Qn. Nos. | Value Points | Marks allotted |
|----------|---|---|
| | $\frac{\text{Area of } \triangle ABC}{\text{Area of } \triangle PQR} = \frac{\frac{1}{2} \times BC \times AM}{\frac{1}{2} \times QR \times PN}$ $= \frac{BC}{QR} \times \frac{AM}{PN}$ $= \frac{BC}{QR} \times \frac{BC}{QR}, \left[\frac{AM}{PN} = \frac{BC}{QR} \right]$ $= \frac{BC^2}{QR^2}$ <p style="text-align: center;">∴ $\frac{\text{Area of } \triangle ABC}{\text{Area of } \triangle PQR} = \frac{BC^2}{QR^2}$</p> <p><i>Alternate method :</i></p> <div style="text-align: center;">  </div> <p><i>Data :</i> We are given two triangles ABC and PQR such that</p> $\triangle ABC \sim \triangle PQR$ <p>We need to prove that</p> $\frac{\text{ar} (ABC)}{\text{ar} (PQR)} = \left(\frac{AB}{PQ} \right)^2 = \left(\frac{BC}{QR} \right)^2 = \left(\frac{CA}{RP} \right)^2$ <p>For finding areas of two triangles</p> <p>Draw altitudes AM and PN of the triangles</p> <p>Now $\frac{\text{ar} (ABC)}{\text{ar} (PQR)} = \frac{\frac{1}{2} BC \times AM}{\frac{1}{2} QR \times PN}$ $= \frac{BC}{QR} \times \frac{AM}{PN} \quad \dots (i)$</p> | <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">4</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> |

| Qn. Nos. | Value Points | Marks allotted |
|-------------|---|---|
| | <p>Now in ΔABM and ΔPQN</p> $\angle B = \angle Q \quad (\text{As } \Delta ABC \sim \Delta PQR)$ $\angle M = \angle N \quad (\text{each is of } 90^\circ)$ <p>$\Delta ABM \sim \Delta PQN$ (A. A. criterion)</p> <p>Therefore $\frac{AM}{PN} = \frac{AB}{PQ}$... (ii)</p> <p>Also $\Delta ABC \sim \Delta PQR$ (given)</p> $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{CA}{RP}$... (iii) <p>Therefore $\frac{\text{ar}(ABC)}{\text{ar}(PQR)} = \frac{AB}{PQ} \times \frac{AM}{PN}$</p> <p>From (i) and (iii)</p> $= \frac{AB}{PQ} \times \frac{AB}{PQ} \quad (\text{from (i) and (iii)})$ $= \left(\frac{AB}{PQ}\right)^2$ <p>Now using (iii) we get</p> $\frac{\text{ar}(ABC)}{\text{ar}(PQR)} = \left(\frac{AB}{PQ}\right)^2 = \left(\frac{BC}{QR}\right)^2 = \left(\frac{CA}{RP}\right)^2$ | <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> |