

CBSE XTH EXAMINATION-2019
SUBJECT : MATHEMATICS

CODE NO. 30/2/1

CLASS : X

HINTS & SOLUTIONS

Section - A

1. HCF (336, 54) = 6.
 LCM × HCF = 336 × 54

$$\text{LCM} = \frac{336 \times 54}{6} = 3024$$

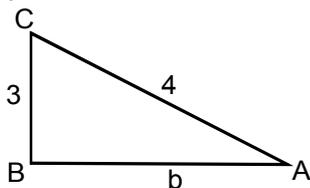
2. $2x^2 - 4x + 3 = 0$
 $D = b^2 - 4ac$
 $= 16 - 4(2)(3)$
 $= 16 - 24$
 $= -8$ $\Delta < 0$
 Roots are not real or imaginary roots.

3. Given AP $\frac{1}{a}, \frac{3-a}{3a}, \frac{3-2a}{3a}$ where $a \neq 0$
 $d = a_2 - a_1$
 $= \frac{3-a}{3a} - \frac{1}{a}$
 $= \frac{3-a-3}{3a}$
 $= \frac{-a}{3a} = \frac{-1}{3}$

4. $\sin^2 60^\circ + 2 \tan 45^\circ - \cos^2 30^\circ$
 Now we know $\sin 60^\circ = \frac{\sqrt{3}}{2}$
 $\therefore \sin^2 60^\circ = \frac{3}{4}$
 $\tan 45^\circ = 1$
 $\cos 30^\circ = \frac{\sqrt{3}}{2}$
 Substituting the value
 $\frac{3}{4} + 2(1) - \frac{3}{4} = 2$

OR

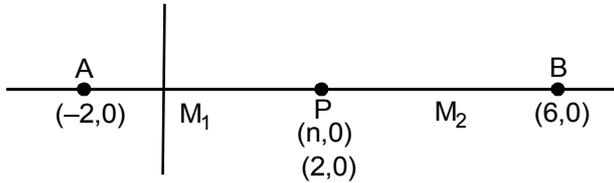
$\sin A = \frac{3}{4}$



$$\cos A = \sqrt{1 - \sin^2 A} = \sqrt{1 - \frac{9}{16}} = \frac{\sqrt{7}}{4}$$

$$\sec A = \frac{4}{\sqrt{7}}$$

5. $M_1 = M_2$



$AP = PB$

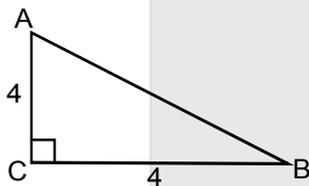
$$\sqrt{[x - (-2)]^2} = \sqrt{(6 - x)^2}$$

$$x + 2 = 6 - x$$

$$2x = 4$$

$$x = 2$$

6.



Isosceles triangle right angled at C.

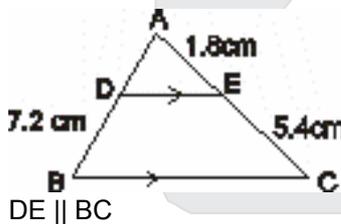
$$AC = BC$$

$$\text{Now } AB^2 = (AC)^2 + (BC)^2$$

$$AB^2 = (4)^2 + (4)^2 = 32$$

$$AB = \sqrt{32} = 4\sqrt{2}$$

OR



Using BPT $\frac{AD}{DB} = \frac{AE}{EC}$

$$\frac{AD}{7.2} = \frac{1.8}{5.4}$$

$$AD = \frac{1.8 \times 7.2}{5.4} = 2.4 \text{ cm}$$

Section - B

7. LCM of 306 & 657

$$306 = 2 \times 3 \times 3 \times 17$$

$$657 = 3 \times 3 \times 73$$

$$\therefore \text{HCF} = 3 \times 3 = 9$$

$$\text{HCF} \times \text{LCM} = 306 \times 657$$

$$\text{LCM} = \frac{306 \times 657}{9} = 22338$$

8. Given A (x, 4), B (-4, 6), C (-2, 3) Collinear

Area of triangle = 0

$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$\frac{1}{2} [x(6 - 3) + (-4)[3 - 4] - (-2)[y - 6]] = 0$$

$$x(3) + 4 + 12 - 2y = 0$$

$$3x - 2y + 16 = 0$$

$$3x - 2y = 16$$

OR

Let A (1, -1)

B (-4, 6)

C (-3, -5)

Area of triangle

$$= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$\frac{1}{2} [1(6 - (-5)) + (-4)(-5 - (-1)) + (-3)(-1 - 6)]$$

$$\frac{1}{2} [11 + 16 + 21]$$

$$\frac{1}{2} [48]$$

24 sq units

9. Type of marble, Blue, black, green

$$P(\text{Blue}) = \frac{1}{5}$$

$$P(\text{Black}) = \frac{1}{4}$$

Let total marbles = x

$$P(\text{green}) = 1 = [P(\text{Blue}) + P(\text{Black})]$$

$$= 1 - \left[\frac{1}{5} + \frac{1}{4} \right] = 1 - \left[\frac{4+5}{20} \right] = 1 - \frac{9}{20} = \frac{11}{20}$$

$$P(\text{green}) = \frac{11}{20}$$

Now green marbles = 11

Hence total no. of marbles = 20

10. Given eq $x + 2y = 5$ & $3x + ky + 15 = 0$

$$x + 2y - 5 = 0$$

For unique solution

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

$$\frac{1}{3} \neq \frac{2}{k}$$

Hence $k \neq 6$

Any real value except 6

11. Let the larger supplementary angle be x
 \therefore other angle = $180 - x$
 A/c to problem
 $x = 180 - x + 18^\circ$
 $2x = 198$
 $x = 99^\circ$
 \therefore 99, 81

OR

Let present age of sumit = $3x$
 \therefore Present age of his son = x
 Five years later sumit = $3x + 5$
 Five years later Son = $x + 5$
 A/c to problem

$$3x + 5 = 2 \frac{1}{2} [x + 5]$$

$$3x + 5 = \frac{5}{2} [x + 5]$$

$$6x + 10 = 5x + 25$$

$$x = 15$$

Son's age = 15 years

Sumit's age = 45 years

12. Given

| CI | frequency |
|-------|-----------|
| 25-30 | 25 |
| 30-35 | 34 f_0 |
| 35-40 | 50 f_1 |
| 40-45 | 42 f_2 |
| 45-50 | 38 |
| 50-55 | 14 |

$$\text{Mode} = \ell + \frac{f_1 + f_0}{2f_1 - f_0 - f_2} \times h$$

$$\text{Modal class} = 35 - 40$$

$$\ell = \text{lower limit of modal class} = 35$$

$$h = \text{class size} = 35 - 30 = 5$$

$$f_1 = 50$$

$$f_0 = 34$$

$$f_2 = 42$$

$$\begin{aligned} \text{mode} &= 35 + \frac{50 - 34}{100 - 34 - 42} \times 5 \\ &= 35 + \frac{16}{100 - 76} \times 5 = 35 + \frac{80}{24} = \frac{920}{24} = 38.34 \end{aligned}$$

Section - C

13. Given $\sqrt{3}$ is an irrational number
We need to prove $2 + 5\sqrt{3}$ is also an irrational number

Let $2 + 5\sqrt{3}$ be a rational no in form of $\frac{p}{q}$

$$\therefore 2 + 5\sqrt{3} = \frac{p}{q}$$

$$2 - \frac{p}{q} = 5\sqrt{3}$$

Rational $\leftarrow \frac{2q-p}{5q} = \sqrt{3} \rightarrow$ Irrational

Now $\frac{2q-p}{5q}$ is a rational number

But $\sqrt{3}$ is irrational
Since rational \neq Irrational
This is a contradiction
 \therefore Our assumptions is incorrect
Hence $2 + 5\sqrt{3}$ is irrational

OR

Given numbers 2048 and 960
Divide the larger number by smaller one
 $2048 = 960(2) + 128$
 $960 = 128(7) + 64$
 $128 = 2(64) + 0$
Now remainder is zero
 \therefore 64 is HCF

14. **Given :** two right triangles ABC and DCB are on the same hypotenuse BC

To Prove : $AP \times PC = BP \times PD$

Proof : In $\triangle ABC$ & $\triangle DCB$

$$\angle A = \angle D \quad \{\text{each } 90^\circ\}$$

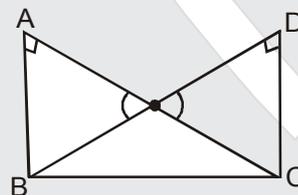
$$\angle APB = \angle DPC \quad \{\text{vertically opp } \angle A\}$$

By A-A similarity

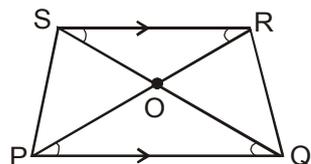
$\triangle ABP \sim \triangle DCP$

$$\frac{BP}{CP} = \frac{AP}{DP} \quad \{\text{Corresponding sides of similar } \triangle \text{ are proportional}\}$$

$$AP \times PC = BP \times PD$$



OR



In trapezium $PQ \parallel RS$ & $PQ = 3RS$

Now in $\triangle POQ$ & $\triangle ROS$
 $\angle OPQ = \angle ORS$ {Let int \angle s}

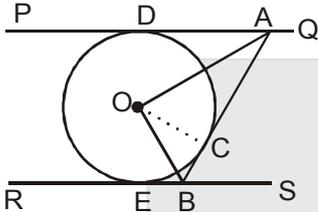
$$\angle OQP = \angle OSR$$

Using A – A criterion
 $\therefore \triangle POQ \sim \triangle ROS$

Now $\therefore \frac{\text{ar } POQ}{\text{ar } ROS} = \left(\frac{PQ}{RS}\right)^2$

$$= \left(\frac{3RS}{RS}\right)^2 = \frac{9}{1}$$

15.



Given : In $C(O, r)$ $PQ \parallel RS$ are two parallel tangents.
 AB is also tangent.

To Prove : $\angle AOB = 90^\circ$

Construction : Join OD, OE & OC

Proof : In $\triangle AOD$ & $\triangle AOC$

$$OD = OC$$

{equal radius}

$$OA = OA$$

{Common}

$$AD = AC$$

{Tangent from ext point is equal }

$$\therefore \triangle AOD \cong \triangle AOC$$

{By SSS congruency }

$$\therefore \angle AOD = \angle AOC$$

{y Cpct} \quad \dots (i)

Similarly In $\triangle BOC$ & $\triangle BOE$

$$OC = OE$$

$$OB = OB$$

$$BC = BE$$

\therefore By SSS

$$\triangle BOC \cong \triangle BOE$$

$\therefore \angle BOC = \angle BOE$ By cpct \quad \dots (ii)

Now $\angle DOE = 180^\circ$ (angle on a straight line)

$$\therefore \angle AOD + \angle AOC + \angle BOE + \angle BOC = 180^\circ$$

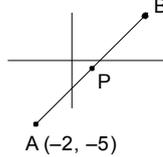
From eqⁿ (i) & (ii)

$$2\angle AOC + 2\angle BOC = 180^\circ$$

$$2(\angle AOC + \angle BOC) = 180^\circ$$

$$\angle AOB = 90^\circ$$

16. Let $A(-2, -5) = (x_1, y_1)$
 $B(6, 3) = (x_2, y_2)$



Let the ratio

Be $\lambda : 1$

$$\text{Coordinate of } P = \left[\frac{\lambda(6) + 1(-2)}{\lambda + 1}, \frac{\lambda(3) + 1(-5)}{\lambda + 1} \right]$$

$$P = \left[\frac{6\lambda - 2}{\lambda + 1}, \frac{3\lambda - 5}{\lambda + 1} \right]$$

Now P lies on line

$$x - 3y = 0$$

$$\frac{6\lambda - 2}{\lambda + 1} - 3\left(\frac{3\lambda - 5}{\lambda + 1}\right) = 0$$

$$\frac{6\lambda - 2}{\lambda + 1} - \left(\frac{9\lambda - 15}{\lambda + 1}\right) = 0$$

$$\frac{6\lambda - 2 - 9\lambda + 15}{\lambda + 1} = 0$$

$$13 - 3\lambda = 0$$

$$13 = 3\lambda$$

$$\frac{\lambda}{1} = \frac{13}{3}$$

Line segment is divided in ratio 13 : 3.

∴ Point of intersection

$$x = \frac{6\lambda - 2}{\lambda + 1} = \frac{6\left(\frac{13}{3}\right) - 2}{\left(\frac{13}{3}\right) + 1}$$

$$= \frac{\frac{24}{3} - 2}{\frac{13}{3} + 1} = \frac{72 - 6}{16} = \frac{9}{2}$$

$$y = \frac{3\lambda - 5}{\lambda + 1} = \frac{3\left(\frac{13}{3}\right) - 5}{\frac{13}{3} + 1} = \frac{8}{\frac{16}{3}} = \frac{24}{16} = \frac{3}{2}$$

$$\text{Point} = \left(\frac{9}{2}, \frac{3}{2}\right)$$

17. Solve

$$\left(\frac{3 \sin 43^\circ}{\cos 47^\circ}\right)^2 - \frac{\cos 37^\circ \operatorname{cosec} 53^\circ}{\tan 5^\circ \tan 25^\circ \tan 45^\circ \tan 65^\circ \tan 85^\circ}$$

$$\left(\frac{3 \cos 47^\circ}{\cos 47^\circ}\right)^2 - \frac{\cos 37^\circ \cdot \frac{1}{\sin 53^\circ}}{\tan 5^\circ \cdot \tan 25^\circ (1) \cot 25^\circ \cdot \cot 5^\circ}$$

$$9 - \frac{\cos 37^\circ \cdot \frac{1}{\cos 37^\circ}}{1} = 9 - 1 = 8$$

18. Given Square OABC is inscribed in quadrant OPBQ.
OA = 15

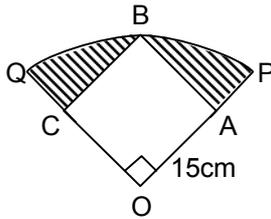


Figure - 4

To find area of shaded region.

Area of shaded region = Area of quadrant – Area of square

$$= \frac{1}{4}(\pi r^2) - (OA)^2$$

Now radius of quadrant = Length of diagonal

$$\text{Now } OB = \sqrt{(OA)^2 + (AB)^2}$$

$$r = OB = \sqrt{(15)^2 + (15)^2} = 15\sqrt{2} \text{ cm}$$

∴ Area of shaded region

$$= \frac{1}{4}(3.14) (15\sqrt{2})^2 - (15)^2$$

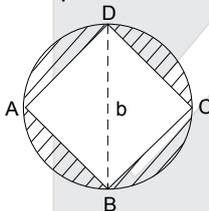
$$= \frac{3.14 \times 225 \times 2}{4} - 225 \text{ cm}^2$$

$$= 128.25 \text{ cm}^2$$

OR

Given

ABCD is a square with side $2\sqrt{2}$ cm.



To find Area of shaded region

Diameter of circle = Length of diagonal of square

$$\text{Now } BD = \sqrt{(2\sqrt{2})^2 + (2\sqrt{2})^2}$$

$$BD = 4 \text{ cm}$$

Radius OB = 2 cm

Required Area = Area of circle – Area of square

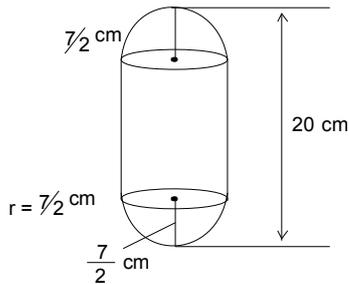
$$= \pi r^2 - a^2$$

$$= 3.14 \times (2)^2 - (2\sqrt{2})^2$$

$$= 12.56 - 8$$

$$= 4.56 \text{ cm}^2$$

19.



Total height = 20 cm

$$\therefore \text{Height of cylinder} = 20 - \frac{7}{2} - \frac{7}{2} = 13 \text{ cm.}$$

And radius at ends = $\frac{7}{2}$ cm.

\therefore Total volume of solid = Vol of cylinder + 2 \times Vol of hemisphere

$$\begin{aligned} &= \pi r^2 h + 2 \times \frac{2}{3} \pi r^3 \\ &= \left(\frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 13 \right) + \left(2 \times \frac{2}{3} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times \frac{7}{2} \right) \\ &= 500.5 + 179.67 \text{ cm}^3 \\ &= 680.17 \text{ cm}^3. \end{aligned}$$

20. Using step deviation method

| C1 | u_i | f_i | $d_i = u_i - a$ | $u_i = \frac{d_i}{a}$ | $f_i u_i$ |
|-------|----------|------------------|-----------------|-----------------------|----------------------|
| Mass | | | $= u_i - 47.5$ | | |
| 30-35 | 32.5 | 14 | -15 | -3 | -42 |
| 35-40 | 37.5 | 16 | -10 | -2 | -32 |
| 40-45 | 42.5 | 28 | -5 | -1 | -28 |
| 45-50 | 47.5 = a | 23 | 0 | 0 | 0 |
| 50-55 | 52.5 | 18 | 5 | 1 | 18 |
| 55-60 | 57.5 | 8 | 10 | 2 | 16 |
| 60-65 | 62.5 | 3 | 15 | 3 | 9 |
| | | $\sum f_i = 110$ | | | $\sum f_i u_i = -59$ |

Let assumed mean $a = 47.5$

$$\begin{aligned} \text{Mean} &= a + \frac{\sum f_i u_i}{\sum f_i} \times h \\ &= 47.5 + \frac{(-59)}{110} \times 5 \\ &= 47.5 - 2.68 \\ &= 44.82 \end{aligned}$$

21.

Given Polynomial

$$F(x) = 3x^4 - 9x^3 + x^2 + 15x + k$$

$$g(x) = 3x^2 - 5$$

Completely divisible

\therefore remainder = 0

$$\begin{array}{r}
 \overline{) \begin{array}{l} 3x^4 - 9x^3 + x^2 + 15x + k \\ 3x^4 \\ \hline -9x^3 - 6x^2 + 15x + k \\ -9x^3 + 15x \\ \hline 6x^2 + k \\ 6x^2 - 10 \\ \hline k + 10 = 0 \\ k = -10 \end{array} \\
 \end{array}$$

OR

$$\begin{aligned}
 \text{Given } P(x) &= 7y^2 - \frac{11}{3}y - \frac{2}{3} \\
 &= \frac{1}{3}(21y^2 - 11y - 2) \\
 &= \frac{1}{3}(21y^2 - 14y + 3y - 2) \\
 &= \frac{1}{3}(7y(3y - 2) + (3y - 2)) \\
 &= \frac{1}{3}(7y + 1)(3y - 2)
 \end{aligned}$$

to find zero we equate $P(x) = 0$

$$\text{Zeroes of polynomial} \Rightarrow \frac{2}{3} \text{ \& } \frac{-1}{7}$$

$$\text{Now sum of zeroes} = -\frac{b}{a}$$

$$\frac{2}{3} + \left(-\frac{1}{7}\right) = -\left(\frac{-11}{3 \times 7}\right) = \frac{11}{21}$$

$$\frac{14 - 3}{21} = \frac{11}{21} = \frac{11}{21}$$

$$\text{Product of zeroes} = \frac{c}{a}$$

$$\left(\frac{2}{3}\right)\left(\frac{-1}{7}\right) = \frac{-2}{21}$$

$$\frac{-2}{21} = \frac{-2}{21}$$

Hence verified

22. $x^2 + px + 16 = 0$
For equal roots $D = 0$

$$\begin{aligned}
 b^2 - 4ac &= 0 \\
 p^2 - 4(16)(1) &= 0 \\
 p^2 &= 64
 \end{aligned}$$

$$p = \pm 8$$

Now if $p = 8$

$$x^2 + 8x + 16 = 0$$

$$(x + 4)^2 = 0$$

$$x = -4$$

if $p = -8$

$$x^2 - 8x + 16 = 0$$

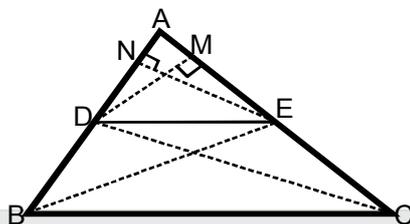
$$(x - 4)^2 = 0$$

$$x = 4$$

Section - D

23. **Given :** A $\triangle ABC$ in which a line parallel to side BC intersects other two sides AB and AC at D and E respectively.

To Prove : $\frac{AD}{DB} = \frac{AE}{EC}$.



Construction : Join BE and CD and draw $DM \perp AC$ and $EN \perp AB$.

Proof : Area of $\triangle ADE = \frac{1}{2}$ (base \times height) = $\frac{1}{2}$ AD \times EN.

Area of $\triangle ADE$ is denoted as ar(ADE).

So, $\text{ar}(\triangle ADE) = \frac{1}{2}$ AD \times EN and $\text{ar}(\triangle BDE) = \frac{1}{2}$ DB \times EN.

Therefore, $\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle BDE)} = \frac{\frac{1}{2} \text{AD} \times \text{EN}}{\frac{1}{2} \text{DB} \times \text{EN}} = \frac{\text{AD}}{\text{DB}}$... (i)

Similarly, $\text{ar}(\triangle ADE) = \frac{1}{2}$ AE \times DM and $\text{ar}(\triangle DEC) = \frac{1}{2}$ EC \times DM.

And $\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle DEC)} = \frac{\frac{1}{2} \text{AE} \times \text{DM}}{\frac{1}{2} \text{EC} \times \text{DM}} = \frac{\text{AE}}{\text{EC}}$... (ii)

Note that $\triangle BDE$ and $\triangle DEC$ are on the same base DE and between the two parallel lines BC and DE.

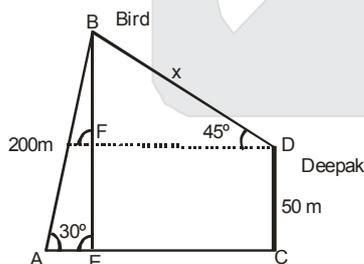
So, $\text{ar}(\triangle BDE) = \text{ar}(\triangle DEC)$... (iii)

Therefore, from (i), (ii) and (iii), we have :

$$\frac{AD}{DB} = \frac{AE}{EC}$$

Hence Proved.

- 24.



$\triangle ACB$

$$\sin 30^\circ = \frac{BE}{AB}$$

$$\frac{1}{2} = \frac{BE}{200}$$

$$BE = 100 \text{ m}$$

Now $BE = BF + FE$ [$\because FE = DC = 50 \text{ m}$]

$$100 = BE + 50$$

$$BF = 50 \text{ m}$$

$$\text{In } \triangle BFD \Rightarrow \sin 45^\circ = \frac{BF}{BD}$$

$$\frac{1}{\sqrt{2}} = \frac{50}{x}$$

$$BD = x = 50\sqrt{2} \text{ m}$$

Distance of bird from Deepak is $50\sqrt{2}$ m

25. $h_1 =$ height of cylinder = 220 cm

$$r_1 = 12 \text{ cm}$$

$$V_1 = \pi r_1^2 h_1$$

$$V_1 = \pi(144)(220)$$

$$= 31680 \pi \text{ cm}^3$$

Now $h_2 =$ height of another cylinder = 60 cm

$r_2 =$ radius of another cylinder = 8 cm

$$V_2 = \pi(r_2)^2 h_2$$

$$= \pi(64)(60)$$

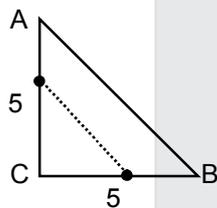
$$= 3840 \pi \text{ cm}^3$$

Total vol of pole = $31680 \pi + 3840 \pi$

$$= 111532.8 \text{ cm}^3$$

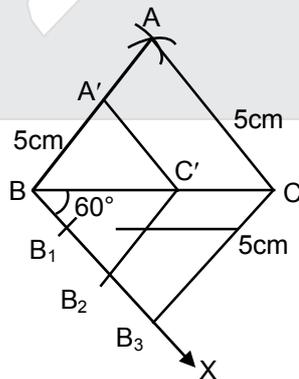
Required weight = $111532.8 \times 8 \text{ gm} = 892.26 \text{ kg}$

26. Construct



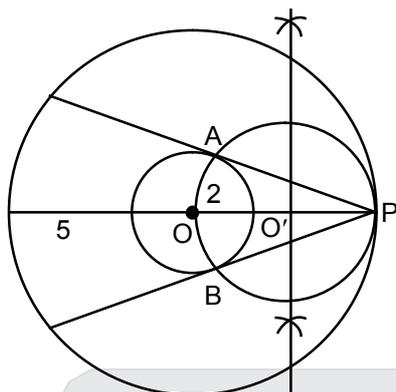
Steps of construction

- (i) Draw $BC = 5 \text{ cm}$.
- (ii) Taking B and C as centre and radius equal to 5 cm draw arc and join AB and AC, thus equilateral $\triangle ABC$ is formed.
- (iii) With B as centre, draw a ray BX making an acute angle CBX with BC.



- (iv) Along BX, mark off three points B_1, B_2, B_3 such that $BB_1 = B_1B_2 = B_2B_3$
- (v) Join B_3C .
- (vi) Draw $B_2C' \parallel B_3C$, meeting BC at C' .
- (vii) From C' draw $C'A' \parallel CA$, meeting BA at A' . thus $BC'A'$ is required triangle, each of whose sides is $\frac{2}{3}$ of corresponding sides of $\triangle ABC$.

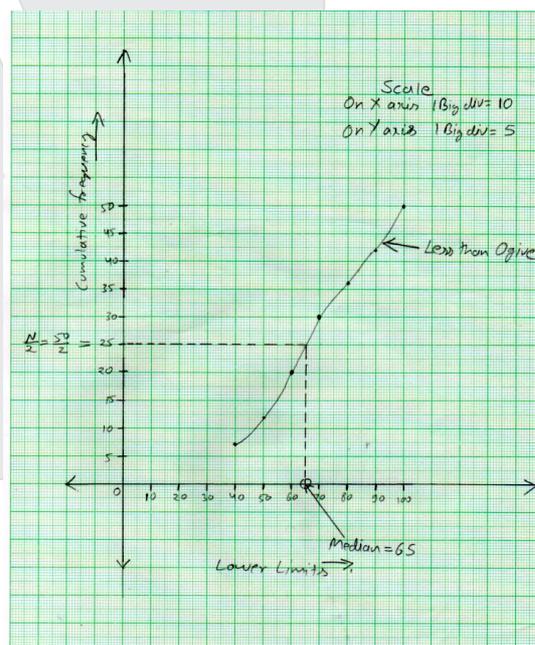
OR



- (i) Draw a circle of radius 2 cm with centre O.
- (ii) Draw another circle of radius 5 cm with same centre O.
- (iii) Take a point P on second circle and join OP.
- (iv) Draw \perp bisector of OP which intersect OP at O'.
- (v) Taking O' as centre and OO' as radius, draw a circle to intersect the first circle in two points say A and B.
- (vi) Join PA and PB these are required triangle from P.

27.

| CI | Frequency | Cumulative frequency (less than type) |
|----------|-----------|--|
| 30 – 40 | 7 | 7 |
| 40 – 50 | 5 | 12 |
| 50 – 60 | 8 | 20 |
| 60 – 70 | 10 | 30 |
| 70 – 80 | 6 | 36 |
| 80 – 90 | 6 | 42 |
| 90 – 100 | 8 | 50 = N |



28.

$$\frac{\tan \theta}{1 - \cot \theta} + \frac{\cot \theta}{1 - \tan \theta} = 1 + \sec \theta \operatorname{cosec} \theta$$

$$\frac{\frac{\sin \theta}{\cos \theta}}{1 - \frac{\cos \theta}{\sin \theta}} + \frac{\frac{\cos \theta}{\sin \theta}}{1 - \frac{\sin \theta}{\cos \theta}}$$

$$\frac{\sin \theta}{\cos \theta} \times \frac{\sin \theta}{\sin \theta - \cos \theta} + \frac{\cos \theta}{\sin \theta} \times \frac{\cos \theta}{\cos \theta - \sin \theta}$$

$$\frac{\sin^2 \theta}{\cos \theta (\sin \theta - \cos \theta)} + \frac{\cos^2 \theta}{\cos \theta (\sin \theta - \cos \theta)}$$

$$\frac{\sin^3 \theta - \cos^3 \theta}{\sin \theta \cos \theta (\sin \theta - \cos \theta)}$$

$$\frac{(\sin \theta - \cos \theta) (\sin^2 \theta + \sin \theta \cos \theta + \cos^2 \theta)}{(\sin \theta \cos \theta) (\sin \theta - \cos \theta)}$$

$$\frac{1 + \sin \theta \cos \theta}{\sin \theta \cos \theta}$$

$$1 + \sec \theta \operatorname{cosec} \theta$$

OR

$$\frac{\sin \theta}{\cot \theta + \operatorname{cosec} \theta} = 2 + \frac{\sin \theta}{\cot \theta - \operatorname{cosec} \theta}$$

LHS $\frac{\sin \theta}{\frac{\cos \theta}{\sin \theta} + \frac{1}{\sin \theta}} \Rightarrow \frac{\sin^2 \theta}{\cos \theta + 1} \times \frac{1 - \cos \theta}{1 - \cos \theta}$

$$\Rightarrow \frac{\sin^2 \theta (1 - \cos \theta)}{1 - \cos^2 \theta}$$

$$\Rightarrow \frac{\sin^2 \theta (1 - \cos \theta)}{\sin^2 \theta}$$

$$\Rightarrow 1 - \cos \theta$$

RHS $2 + \frac{\sin \theta}{\cot \theta - \operatorname{cosec} \theta}$

$$\Rightarrow 2 + \frac{\sin \theta}{\frac{\cos \theta}{\sin \theta} - \frac{1}{\sin \theta}} \Rightarrow 2 + \frac{\sin^2 \theta}{\cos \theta - 1} \Rightarrow 2 - \frac{\sin^2 \theta}{\cos \theta - 1} \times \frac{\cos \theta + 1}{\cos \theta + 1}$$

$$\Rightarrow \frac{2 - (1 + \cos \theta)}{1 - \cos \theta}$$

$$\Rightarrow \frac{1 - \cos \theta}{1 - \cos \theta}$$

LHS = RHS

29. Let -82 be the a_n term
 $a = -7$, $d = -12 - (-7) = -12 + 7 = -5$
 $a_n = a + (n - 1)d$
 $-82 = (-7) + (n - 1)(-5)$
 $\frac{75}{5} = n - 1$
 $15 = n - 1$
 $n = 16$, so -82 is the 16th term.
 Let -100 be the a_m term
 $a_m = a + (m - 1)d$
 $-100 = (-7) + (m - 1)(-5)$
 $\frac{93}{5} = m - 1$
 $m = \frac{93}{5} + 1 = \frac{98}{5}$
 as m is not a natural number so -100 will not be the term of the A.P.

OR

$$a = 45$$

$$d = 39 - 45 = -6$$

$$\text{Let } S_n = 180 = \frac{n}{2} (2a + (n-1)d)$$

$$180 = \frac{n}{2} [90 + (n-1)(-6)]$$

$$180 = n [45 + (n-1)(-3)]$$

$$60 = n [15 + (n-1)(-1)]$$

$$60 = 15n - n^2 + n$$

$$n^2 - 16n + 60 = 0$$

$$(n-10)(n-6) = 0$$

$$n = 10 \text{ or } 6$$

Reason for double answer in that the given AP is decreasing AP and after some terms the terms are became negative.

30. Let the marks in Hindi and English are x, y respectively.

$$x + y = 30 \quad \Rightarrow \quad y = 30 - x.$$

ATQ

$$(x+2)(y-3) = 210$$

$$(x+2)(30-x-3) = 210$$

$$(x+2)(27-x) = 210$$

$$-x^2 + 25x + 54 = 210$$

$$x^2 - 25x + 156 = 0$$

$$(x-12)(x-13) = 0$$

$$x = 12 \text{ or } 13.$$

$$\text{If } x = 12 \text{ then } y = 30 - x = 30 - 12 = 18$$

$$\text{If } x = 13 \text{ then } y = 30 - x = 30 - 13 = 17$$

So marks in Hindi and English is 12 and 18 or 13 and 17.