

**CCE RR**  
**REVISED & UN-REVISED**

**B**

ಕರ್ನಾಟಕ ಪ್ರೌಢ ಶಿಕ್ಷಣ ಪರೀಕ್ಷಾ ಮಂಡಳಿ, ಮಲ್ಲೇಶ್ವರಂ, ಬೆಂಗಳೂರು – 560 003

**KARNATAKA SECONDARY EDUCATION EXAMINATION BOARD, MALLESWARAM,  
BANGALORE – 560 003**

ಎಸ್.ಎಸ್.ಎಲ್.ಸಿ. ಪರೀಕ್ಷೆ, ಜೂನ್ — 2018

**S. S. L. C. EXAMINATION, JUNE, 2018**

ಮಾದರಿ ಉತ್ತರಗಳು

**MODEL ANSWERS**

ದಿನಾಂಕ : 21. 06. 2018 ]

ಸಂಕೇತ ಸಂಖ್ಯೆ : **81-E**

Date : 21. 06. 2018 ]

CODE No. : **81-E**

ವಿಷಯ : ಗಣಿತ

**Subject : MATHEMATICS**

( ಹೊಸ ಪಠ್ಯಕ್ರಮ / New Syllabus )

( ಪುನರಾವರ್ತಿತ ಶಾಲಾ ಅಭ್ಯರ್ಥಿ / Regular Repeater )

( ಇಂಗ್ಲಿಷ್ ಭಾಷಾಂತರ / English Version )

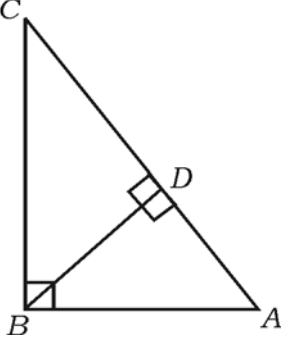
[ ಗರಿಷ್ಠ ಅಂಕಗಳು : 80

[ **Max. Marks : 80**

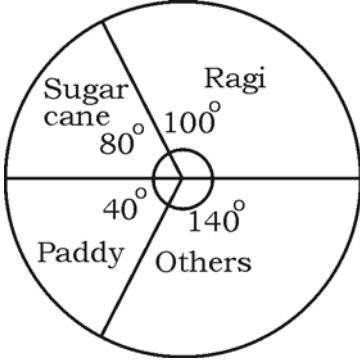
Qn. Nos.	Ans. Key	Value Points	Marks allotted
I. 1.		<p><math>A</math> and <math>B</math> are two sets, such that <math>n(A) = 37</math>, <math>n(B) = 26</math> and <math>n(A \cup B) = 51</math>; then <math>n(A \cap B)</math> is</p> <p>(A) 12 (B) 63 (C) 14 (D) 25</p> <p>Ans. :</p> <p>(A) 12</p>	1

**RR (B)-30010**

[ Turn over

Qn. Nos.	Ans. Key	Value Points	Marks allotted
2.	(C)	Geometric mean between $\frac{1}{2}$ and $\frac{1}{8}$ is (A) 16 (B) $\frac{1}{16}$ (C) $\frac{1}{4}$ (D) 4 Ans. : $\frac{1}{4}$	1
3.	(C)	HCF of any two prime numbers is (A) a prime number (B) a composite number (C) an odd number (D) an even number Ans. : an odd number	1
4.	(D)	If $f(x) = 2x^3 + 3x^2 - 11x + 6$ then the value of $f(-1)$ is (A) 0 (B) -10 (C) -18 (D) 18 Ans. : 18.	1
5.	(A)	In $\triangle ABC$ , $\angle ABC = 90^\circ$ , $BD \perp AC$ if $BD = 8$ cm and $AD = 4$ cm then the length of $CD$ is  (A) 16 cm (B) 4 cm (C) 64 cm (D) 12 cm Ans. : 16 cm	1

Qn. Nos.	Ans. Key	Value Points	Marks allotted
6.		$\frac{\sin (90^\circ - \theta)}{\cos (90^\circ - \theta)}$ where 'θ' is acute, is equal to (A) $\sec \theta$ (B) $\cot \theta$ (C) $\tan \theta$ (D) $\operatorname{cosec} \theta$ Ans. : (B) $\cot \theta$	1
7.		The co-ordinates of the mid-point of the line segment joining the points ( 2, 3 ) and ( 4, 7 ) are (A) ( - 3, - 5 ) (B) ( 1, 2 ) (C) ( 3, 5 ) (D) ( 6, 10 ) Ans. : (C) ( 3, 5 )	1
8.		Formula used to find the surface area of a sphere whose radius 'r' units is (A) $\pi r^2$ (B) $2\pi r^2$ (C) $3\pi r^2$ (D) $4\pi r^2$ Ans. : (D) $4\pi r^2$ .	1

Qn. Nos.	Value Points	Marks allotted
II.	Answer the following : <span style="float: right;"><math>6 \times 1 = 6</math></span>	
	( Question Numbers 9 to 14, give full marks to direct answers )	
9.	A boy has 2 pants and 4 shirts. How many different pairs of a pant and a shirt can he dress up with ?	
	Ans. :	
	Number of ways of pairing a pant and a shirt = $2 \times 4 = 8$	1
10.	Write sample space for the random experiment 'tossing two fair coins simultaneously once'.	
	Ans. :	
	$S = \{HH, TT, HT, TH\}$	1
11.	The given pie chart shows the annual agricultural yield of different crops in a certain place. If the total production is 3600 tons, what is the yield of Ragi in tons ?	
	 <p>A pie chart representing the annual agricultural yield of different crops. The chart is divided into four sectors: Sugar cane (80°), Ragi (100°), Paddy (40°), and Others (140°). The sectors are separated by lines that meet at the center of the circle.</p>	
	Ans. :	
	Yield of Ragi = $\frac{100}{360} \times 3600$	$\frac{1}{2}$
	= 1000 tons	$\frac{1}{2}$

Qn. Nos.	Value Points	Marks allotted
12.	<p>If <math>(x + 3)</math> is one of the factor of <math>f(x) = x^2 + 5x + 6</math>, find the other factor.</p> <p>Ans. :</p> <p>Method 1 : Factor method</p> $  \begin{array}{r}  x^2 + 5x + 6 \\  = x^2 + 3x + 2x + 6 \\  = x(x + 3) + 2(x + 3) \\  = (x + 3)(x + 2)  \end{array}  $ <div style="text-align: center;"> <math display="block">  \begin{array}{c}  6 \\  \swarrow \searrow \\  3 \quad 2  \end{array}  </math> </div> <p>The other factor is <math>(x + 2)</math></p> <p>Method 2 : Division method</p> $  \begin{array}{r}  x + 3 \overline{) x^2 + 5x + 6} \quad (x + 2) \\  \underline{x^2 + 3x} \phantom{+ 6} \\  2x + 6 \\  \underline{2x + 6} \\  0  \end{array}  $ <p>The other factor is <math>(x + 2)</math></p>	<p><math>\frac{1}{2}</math></p> <p>1</p> <p><math>\frac{1}{2}</math></p> <p>1</p>
13.	<p>What are concentric circles ?</p> <p>Ans. :</p> <p>Circles having the same centre but different radii are called concentric circles.</p>	<p>1</p>
14.	<p>Two straight lines are perpendicular to each other. If the slope of one line is <math>\frac{1}{\sqrt{3}}</math>, find the slope of the other line.</p> <p>Ans. :</p> $m_1 m_2 = -1$ $\frac{1}{\sqrt{3}} \times m_2 = -1$ $\therefore m_2 = -\sqrt{3}$ <p>Slope of the other line = <math>-\sqrt{3}</math>.</p>	<p><math>\frac{1}{2}</math></p> <p>1</p>

Qn. Nos.	Value Points	Marks allotted
III. 15.	<p>If <math>A = \{1, 2, 3\}</math> and <math>B = \{2, 3, 4, 5\}</math> are the subsets of <math>U = \{1, 2, 3, 4, 5, 6, 7, 8\}</math>, verify <math>(A \cap B)' = A' \cup B'</math>.</p> <p>Ans. :</p> $A \cap B = \{2, 3\} \quad \frac{1}{2}$ $(A \cap B)' = U - (A \cap B)$ $= \{1, 4, 5, 6, 7, 8\} \quad \dots \text{ i) } \quad \frac{1}{2}$ $A' = \{4, 5, 6, 7, 8\}$ $B' = \{1, 6, 7, 8\} \quad \frac{1}{2}$ $A' \cup B' = \{1, 4, 5, 6, 7, 8\} \quad \dots \text{ ii) }$ <p>From (i) and (ii)</p> $(A \cap B)' = A' \cup B' \quad \frac{1}{2}$	2
16.	<p>Find the sum of infinite terms of the geometric series <math>2 + \frac{2}{3} + \frac{2}{9} + \dots</math>.</p> <p>Ans. :</p> $a = 2, \quad r = \frac{1}{3}, \quad S_{\infty} = ?$ $S_{\infty} = \frac{a}{1-r} \quad \frac{1}{2}$ $= \frac{2}{1 - \frac{1}{3}} \quad \frac{1}{2}$ $= \frac{2}{\frac{3-1}{3}}$ $= \frac{2}{\frac{2}{3}} \quad \frac{1}{2}$ $= \cancel{2} \times \frac{3}{\cancel{2}}$ $S_{\infty} = 3 \quad \frac{1}{2}$	2

Qn. Nos.	Value Points	Marks allotted
17.	<p>Prove that <math>2 + \sqrt{3}</math> is an irrational number.</p> <p>Ans. :</p> <p>Let us assume <math>2 + \sqrt{3}</math> is a rational number.</p> <p><math>\Rightarrow 2 + \sqrt{3} = \frac{p}{q}</math> where <math>p, q \in \mathbb{Z}, q \neq 0</math> <span style="float: right;">1/2</span></p> <p><math>\Rightarrow \sqrt{3} = \frac{p-2q}{q}</math></p> <p><math>\Rightarrow \sqrt{3}</math> is a rational number</p> <p style="text-align: center;"><math>\therefore \frac{p-2q}{q}</math> is rational. <span style="float: right;">1/2</span></p> <p>But <math>\sqrt{3}</math> is not a rational number. This leads to a contradiction. <span style="float: right;">1/2</span></p> <p><math>\therefore</math> Our assumption that <math>2 + \sqrt{3}</math> is a rational number is wrong.</p> <p><math>\therefore 2 + \sqrt{3}</math> is an irrational number. <span style="float: right;">1/2</span></p>	2
18.	<p>Find the number of diagonals that can be drawn in an octagon.</p> <p>Ans. :</p> <p>An octagon has 8 vertices <span style="margin-left: 100px;"><math>\therefore n = 8</math></span></p> <p><math>\therefore</math> Total number of sides and diagonals <math>= {}^8C_2</math> <span style="float: right;">1/2</span></p> <p><math>{}^nC_2 = \frac{n(n-1)}{2} \Rightarrow {}^8C_2 = \frac{8(8-1)}{2}</math> <span style="float: right;">1/2</span></p> <p style="text-align: center;"><math>= 4 \times 7</math></p> <p style="text-align: center;"><math>= 28</math> <span style="float: right;">1/2</span></p> <p>28 lines includes 8 sides.</p> <p><math>\therefore</math> Number of diagonals <math>= 28 - 8</math></p> <p style="text-align: center;"><math>= 20</math> <span style="float: right;">1/2</span></p>	2

Qn. Nos.	Value Points	Marks allotted
19.	<p><i>Alternate method :</i></p> <p>Number of diagonals in a polygon of <math>n</math> sides = <math>\frac{n(n-3)}{2}</math> <span style="float: right;">1/2</span></p> <p>In an octagon <math>n = 8</math></p> <p><math>\therefore</math> Number of diagonals = <math>\frac{\cancel{8}(8-3)}{\cancel{2}}</math> <span style="float: right;">1/2</span></p> <p style="padding-left: 150px;"><math>= 4 \times 5</math> <span style="float: right;">1/2</span></p> <p style="padding-left: 150px;"><math>= 20</math> <span style="float: right;">1/2</span></p> <p>Any other correct alternate method may be given marks.</p>	2
	<p>Find the sum of all two digit natural numbers which are divisible by 5.</p> <p><i>Ans. :</i></p> <p>Two-digit numbers which are divisible by 5 = 10, 15, 20, ... 95</p> <p>Sum of all two-digit numbers = 10 + 15 + 20 + ... + 95</p> <p style="padding-left: 100px;"><math>a = 10, d = 5, T_n = 95</math></p> <p><math>\therefore T_n = a + (n-1)d</math></p> <p style="padding-left: 100px;"><math>95 = 10 + (n-1)5</math></p> <p style="padding-left: 100px;"><math>(n-1) = \frac{85}{5}</math> <span style="float: right;">1</span></p> <p style="padding-left: 100px;"><math>(n-1) = 17</math> <span style="margin-left: 100px;"><math>\therefore n = 18</math></span></p> <p><i>Method 1 :</i></p> <p>Sum of <math>n</math> natural numbers <math>S_n = \frac{n}{2} [2a + (n-1)d]</math></p> <p style="padding-left: 100px;"><math>S_{18} = \frac{18}{2} [2 \times 10 + (18-1)5]</math></p> <p style="padding-left: 150px;"><math>= 9(20 + 85)</math> <span style="float: right;">1</span></p> <p style="padding-left: 150px;"><math>= 9 \times 105</math></p> <p style="padding-left: 100px;"><math>S_{18} = 945</math></p> <p style="text-align: center;">OR</p>	



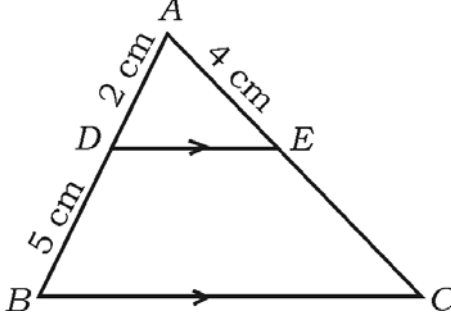


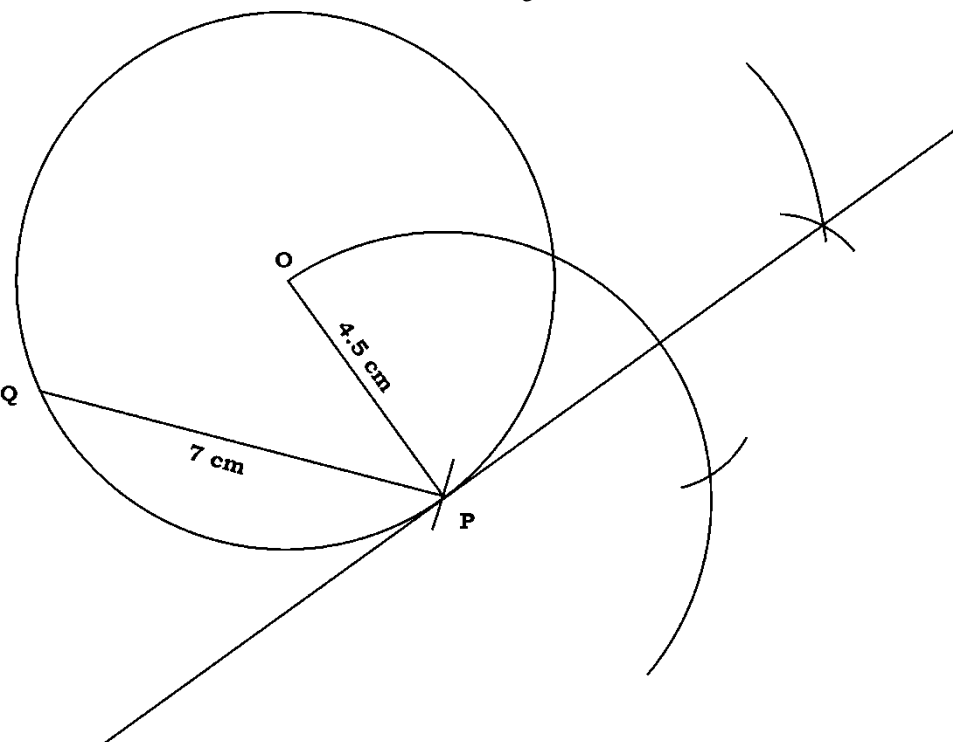
Qn. Nos.	Value Points	Marks allotted
	$4\text{-digit numbers which are less than } 2000 = 1 \times {}^4P_3$ $= 1 \times 4 \times 3 \times 2$ $= 24$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
	OR	
	$2({}^nP_2) + 50 = {}^{2n}P_2$ $2n(n-1) + 50 = 2n(2n-1)$ $2n^2 - \cancel{2n} + 50 = 4n^2 - \cancel{2n}$ $4n^2 - 2n^2 = 50$ $2n^2 = 50$ $n^2 = 25$ $\therefore n = \pm 5$ $\therefore n = 5$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
21.	<p>Two unbiased dice whose faces are numbered 1 to 6 are rolled once. Find the probability of getting a sum equal to 7 on their top faces.</p> <p>Ans. :</p> <p>Total number of possible outcomes = <math>6 \times 6 = 36</math></p> $\therefore n(s) = 36$ <p>Event of getting a sum equal to 7 = <math>A = \left\{ (1,6) (2,5) (3,4) \right\}</math>  <math>\left\{ (4,3) (5,2) (6,1) \right\}</math></p> $n(A) = 6$ <p>Probability of getting the event A = <math>P(A) = \frac{n(A)}{n(S)}</math></p> $= \frac{6}{36}$ $= \frac{1}{6}$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

2

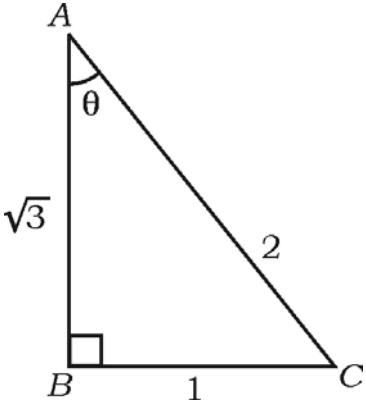
Qn. Nos.	Value Points	Marks allotted
22.	<p>Rationalise the denominator and simplify :</p> $\frac{3\sqrt{2}}{\sqrt{5}-\sqrt{2}}$ <p>Ans. :</p> <p>Rationalising factor of <math>\sqrt{5}-\sqrt{2}</math> is <math>\sqrt{5}+\sqrt{2}</math></p> $= \frac{3\sqrt{2}}{\sqrt{5}-\sqrt{2}} \times \frac{\sqrt{5}+\sqrt{2}}{\sqrt{5}+\sqrt{2}} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \quad \frac{1}{2}$ $= \frac{3\sqrt{2}(\sqrt{5}+\sqrt{2})}{(\sqrt{5})^2 - (\sqrt{2})^2} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \quad \frac{1}{2}$ $= \frac{3\sqrt{10} + 3(2)}{5-2} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \quad \frac{1}{2}$ $= \frac{3\sqrt{10} + 6}{3} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \quad \frac{1}{2}$ $= \frac{\cancel{3}(\sqrt{10} + 2)}{\cancel{3}} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \quad \frac{1}{2}$ $= \sqrt{10} + 2. \quad \frac{1}{2}$	2
23.	<p>Simplify <math>(\sqrt{75}-\sqrt{45})(\sqrt{20}+\sqrt{12})</math>.</p> <p>Ans. :</p> $(\sqrt{75}-\sqrt{45})(\sqrt{20}+\sqrt{12})$ $= (\sqrt{25 \times 3} - \sqrt{9 \times 5})(\sqrt{4 \times 5} + \sqrt{4 \times 3}) \quad \frac{1}{2}$ $= (5\sqrt{3} - 3\sqrt{5})(2\sqrt{5} + 2\sqrt{3})$ $= 5\sqrt{3}(2\sqrt{5} + 2\sqrt{3}) - 3\sqrt{5}(2\sqrt{5} + 2\sqrt{3}) \quad \frac{1}{2}$ $= 10\sqrt{15} + 10(3) - 6(5) - 6\sqrt{15} \quad \frac{1}{2}$ $= 10\sqrt{15} + \cancel{30} - \cancel{30} - 6\sqrt{15}$ $= 4\sqrt{15}. \quad \frac{1}{2}$	2

Qn. Nos.	Value Points	Marks allotted																		
24.	<p>Find the quotient and remainder by using synthetic division :</p> $(3x^3 - 2x^2 + 7x - 5) \div (x - 3)$ <p style="text-align: center;">OR</p> <p>Verify whether <math>(x - 2)</math> is a factor of <math>f(x) = x^3 - 3x^2 + 6x - 20</math> by using factor theorem.</p> <p>Ans. :</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding-right: 10px;">3</td> <td style="border: 1px solid black; padding: 5px;">3</td> <td style="border: 1px solid black; padding: 5px;">-2</td> <td style="border: 1px solid black; padding: 5px;">7</td> <td style="border: 1px solid black; padding: 5px;">-5</td> <td></td> </tr> <tr> <td></td> <td style="border: 1px solid black; padding: 5px;">0</td> <td style="border: 1px solid black; padding: 5px;">9</td> <td style="border: 1px solid black; padding: 5px;">21</td> <td style="border: 1px solid black; padding: 5px;">84</td> <td></td> </tr> <tr> <td></td> <td style="border: 1px solid black; padding: 5px;">3</td> <td style="border: 1px solid black; padding: 5px;">7</td> <td style="border: 1px solid black; padding: 5px;">28</td> <td style="border: 1px solid black; padding: 5px;"></td> <td style="padding-left: 10px;">79</td> </tr> </table> <p><math>\therefore</math> Quotient = <math>3x^2 + 7x + 28</math> <span style="float: right;">1/2</span></p> <p>Remainder = 79. <span style="float: right;">1/2</span></p> <p style="text-align: center;">OR</p> <p>Let <math>f(x) = x^3 - 3x^2 + 6x - 20</math></p> <p>If <math>(x - 2)</math> is a factor of <math>f(x)</math>,</p> <p style="padding-left: 40px;">then <math>f(2) = 0</math> <span style="float: right;">1/2</span></p> <p>Now <math>f(x) = x^3 - 3x^2 + 6x - 20</math></p> $f(2) = 2^3 - 3(2)^2 + 6(2) - 20$ $= 8 - \cancel{12} + \cancel{12} - 20$ $= -12$ <p><math>\therefore f(2) \neq 0</math> <span style="float: right;">1/2</span></p> <p><math>\therefore x - 2</math> is not a factor of <math>x^3 - 3x^2 + 6x - 20</math>. <span style="float: right;">1/2</span></p>	3	3	-2	7	-5			0	9	21	84			3	7	28		79	2
3	3	-2	7	-5																
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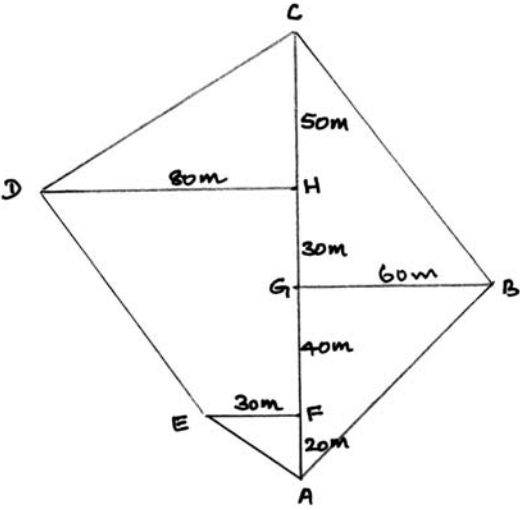
Qn. Nos.	Value Points	Marks allotted
25.	<p>In <math>\triangle ABC</math>, <math>DE \parallel BC</math>, if <math>AD = 2</math> cm, <math>DB = 5</math> cm and <math>AE = 4</math> cm, find <math>AC</math>.</p>  <p>Ans. :</p> <p>In <math>\triangle ABC</math>, <math>DE \parallel BC</math></p> $\therefore \frac{AD}{DB} = \frac{AE}{EC} \quad \text{BPT} \quad \frac{1}{2}$ $\frac{2}{5} = \frac{4}{EC} \quad \frac{1}{2}$ $EC = \frac{4^2 \times 5}{2} = 10 \text{ cm} \quad \frac{1}{2}$ $\therefore AC = AE + EC$ $= 4 + 10$ $= 14 \text{ cm.} \quad \frac{1}{2} \quad 2$ <p>Alternate method :</p> <p>In <math>\triangle ABC</math>, <math>DE \parallel BC</math></p> $\therefore \frac{AD}{AB} = \frac{AE}{AC} \quad \text{Cor. BPT} \quad \frac{1}{2}$ $\frac{2}{2+5} = \frac{4}{AC} \quad \frac{1}{2}$ $\therefore AC = \frac{7 \times 4^2}{2}$ $= 14 \text{ cm.} \quad \frac{1}{2} \quad 2$	

Qn. Nos.	Value Points	Marks allotted
26.	<p>Draw a circle of radius 4.5 cm and a chord <math>PQ</math> of length 7 cm in it. Construct a tangent at <math>P</math>.</p> <p>Ans. :</p> <p><math>r = 4.5</math> cm                      Chord <math>PQ = 7</math> cm</p>  <p style="text-align: right;">Circle —     <math>\frac{1}{2}</math> Chord —     <math>\frac{1}{2}</math> Tangent —    1</p>	2
27.	<p>Find the distance between the co-ordinates of the points ( 2, 4 ) and ( 8, 12 ) by using distance formula.</p> <p>Ans. :</p> <p>Coordinates of</p> <p style="padding-left: 100px;"><math>( x_1 \quad y_1 )</math></p> <p>Point A =            ( 2,    4 )</p> <p style="padding-left: 100px;"><math>( x_2 \quad y_2 )</math></p> <p>Point B =            ( 8,    12 )</p>	$\frac{1}{2}$



Qn. Nos.	Value Points	Marks allotted
29.	<p>In the given <math>\triangle ABC</math>, '<math>\theta</math>' is acute. Write the values of the following trigonometric ratios related to <math>\theta</math> :</p> <p>(a) <math>\sin \theta</math></p> <p>(b) <math>\cos \theta</math></p> <p>(c) <math>\operatorname{cosec} \theta</math></p> <p>(d) <math>\sec \theta</math>.</p> <div style="text-align: center;">  </div> <p>Ans. :</p> <p>a) <math>\sin \theta = \frac{\text{Opp}}{\text{Hyp}} = \frac{BC}{AC} = \frac{1}{2}</math> <span style="float: right;">1/2</span></p> <p>b) <math>\cos \theta = \frac{\text{Adj}}{\text{Hyp}} = \frac{AB}{AC} = \frac{\sqrt{3}}{2}</math> <span style="float: right;">1/2</span></p> <p>c) <math>\operatorname{cosec} \theta = \frac{1}{\sin \theta} = 2</math> <span style="float: right;">1/2</span></p> <p>d) <math>\sec \theta = \frac{1}{\cos \theta} = \frac{2}{\sqrt{3}}</math> <span style="float: right;">1/2</span></p> <p>Direct answers may be given marks.</p>	2



Qn. Nos.	Value Points	Marks allotted																		
30.	<p>Draw a plan by using the information given below :</p> <p>( Scale 20 metres = 1 cm )</p> <table border="1" data-bbox="443 421 1106 775"> <tr> <td></td> <td>Metre to C</td> <td></td> </tr> <tr> <td></td> <td>140</td> <td></td> </tr> <tr> <td>80 to D</td> <td>90</td> <td></td> </tr> <tr> <td></td> <td>60</td> <td>60 to B</td> </tr> <tr> <td>30 to E</td> <td>20</td> <td></td> </tr> <tr> <td></td> <td>From A</td> <td></td> </tr> </table> <p>Ans. :</p> <p>20 m = <math>\frac{20}{20} = 1</math> cm</p> <p>60 m = <math>\frac{60}{20} = 3</math> cm</p> <p>90 m = <math>\frac{90}{20} = 4.5</math> cm</p> <p>140 m = <math>\frac{140}{20} = 7</math> cm</p> <p>60 m = <math>\frac{60}{20} = 3</math> cm</p> <p>80 m = <math>\frac{80}{20} = 4</math> cm</p> <p>30 m = <math>\frac{30}{20} = 1.5</math> cm</p> 		Metre to C			140		80 to D	90			60	60 to B	30 to E	20			From A		<p><math>\frac{1}{2}</math></p> <p><math>1\frac{1}{2}</math></p> <p>2</p>
	Metre to C																			
	140																			
80 to D	90																			
	60	60 to B																		
30 to E	20																			
	From A																			

Qn. Nos.	Value Points	Marks allotted
IV. 31.	<p>In a harmonic progression 5th term is <math>\frac{1}{12}</math> and 11th term is <math>\frac{1}{15}</math>. Find its 25th term.</p> <p style="text-align: center;">OR</p> <p>If the third term of a geometric progression is 12 and its sixth term is 96, find the sum of first 9 terms.</p> <p>Ans. :</p> $T_5 = \frac{1}{12} \text{ and } T_{11} = \frac{1}{15}$ <p>Reciprocals of HP are in AP.</p> $\therefore a + 4d = 12 \quad \dots \text{ (i)} \quad \frac{1}{2}$ $a + 10d = 15 \quad \dots \text{ (ii)} \quad \frac{1}{2}$ <p>By solving (i) and (ii)</p> $\begin{array}{r} a + 10d = 15 \\ a + 4d = 12 \\ \hline (-) \quad (-) \end{array}$ $6d = 3$ $\therefore d = \frac{3}{6} = \frac{1}{2} \quad \frac{1}{2}$ <p>If <math>d = \frac{1}{2}</math>, then <math>a + \cancel{2}(\frac{1}{2}) = 12</math></p> $a + 2 = 12$ $a = 12 - 2$ $\therefore a = 10 \quad \frac{1}{2}$ <p>If <math>a = 10</math> and <math>d = \frac{1}{2}</math> then</p> $T_n = \frac{1}{a + (n-1)d} \quad \frac{1}{2}$	

Qn. Nos.	Value Points	Marks allotted
	$T_{25} = \frac{1}{10 + (25 - 1)\frac{1}{2}}$ $= \frac{1}{10 + \cancel{24} \times \frac{1}{2}}$ <div style="border: 1px solid black; padding: 5px; display: inline-block; margin: 10px 0;"> <math>T_{25} = \frac{1}{22}</math> </div> <p><i>Alternate method :</i></p> <p>The corresponding <math>T_5</math> and <math>T_{11}</math> of AP are</p> $T_5 = 12 \text{ and } T_{11} = 15$ $\therefore d = \frac{T_p - T_q}{p - q}$ $= \frac{T_5 - T_{11}}{5 - 11}$ $= \frac{12 - 15}{5 - 11} = \frac{-3}{-6} = \frac{1}{2}$ <p>If <math>d = \frac{1}{2}</math> then <math>a + 4(\frac{1}{2}) = 12</math></p> $a + 2 = 12$ $\therefore a = 10$ <p>If <math>a = 10</math> and <math>d = \frac{1}{2}</math></p> $T_n = \frac{1}{a + (n - 1)d}$ $T_{25} = \frac{1}{10 + (25 - 1)\frac{1}{2}}$	<p style="text-align: center;">1/2</p> <p style="text-align: center;">3</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p> <p style="text-align: center;">1/2</p>

Qn. Nos.	Value Points	Marks allotted
	$= \frac{1}{10 + \cancel{24} \times \frac{1}{2}}$ $T_{25} = \frac{1}{22}$	3
	<p style="text-align: center;">OR</p> $T_3 = 12 \quad \therefore \quad ar^2 = 12 \quad \dots (i)$ $T_6 = 96 \quad \therefore \quad ar^5 = 96 \quad \dots (ii)$ $\therefore \frac{\cancel{ar^5}}{\cancel{ar^2}} = \frac{\cancel{96}^8}{\cancel{12}}$ <p style="text-align: center;">OR</p> $ar^2 (r^3) = 96$ $12r^3 = 96$ $r^3 = 8$	1/2
	$r^3 = 8 \quad \therefore \quad r = 2$	1/2
	<p>If <math>r = 2</math> then <math>a(2)^2 = 12</math></p> $4a = 12$ $\therefore \quad a = 3$	1/2
	<p>If <math>a = 3</math> and <math>r = 2, n = 9</math> then</p> $S_n = \frac{a(r^n - 1)}{r - 1}$ $S_9 = \frac{3(2^9 - 1)}{2 - 1}$ $= 3(512 - 1)$ $= 3 \times 511$ $S_9 = 1533$	1/2
		3

Qn. Nos.	Value Points	Marks allotted																																																						
32.	<p>Calculate the variance of the following data :</p> <table border="1"> <thead> <tr> <th>Class-interval</th> <th>0-4</th> <th>5-9</th> <th>10-14</th> <th>15-19</th> <th>20-24</th> </tr> </thead> <tbody> <tr> <td>Frequency (<math>f</math>)</td> <td>1</td> <td>2</td> <td>5</td> <td>4</td> <td>3</td> </tr> </tbody> </table> <p>Ans. :</p> <p>i) <i>Step deviation method</i> :</p> <p style="text-align: center;"><math>A = 12</math>                      <math>i = 5</math></p> <table border="1"> <thead> <tr> <th>C.I.</th> <th><math>f</math></th> <th><math>x</math></th> <th><math>d = \frac{x - A}{i}</math></th> <th><math>d^2</math></th> <th><math>fd</math></th> <th><math>fd^2</math></th> </tr> </thead> <tbody> <tr> <td>0-4</td> <td>1</td> <td>2</td> <td>-2</td> <td>4</td> <td>-2</td> <td>4</td> </tr> <tr> <td>5-9</td> <td>2</td> <td>7</td> <td>-1</td> <td>1</td> <td>-2</td> <td>2</td> </tr> <tr> <td>10-14</td> <td>5</td> <td>12</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>15-19</td> <td>4</td> <td>17</td> <td>1</td> <td>1</td> <td>4</td> <td>4</td> </tr> <tr> <td>20-24</td> <td>3</td> <td>22</td> <td>2</td> <td>4</td> <td>6</td> <td>12</td> </tr> </tbody> </table> <p style="text-align: center;"><math>N = 15</math>                      <math>\Sigma fd = 6</math>    <math>\Sigma fd^2 = 22</math></p> <p>Variance = <math>\sigma^2 = \sum \frac{fd^2}{N} - \left( \frac{\Sigma fd}{N} \right)^2 \times i^2</math>                      <math>\frac{1}{2}</math></p> <p style="text-align: center;"><math>= \frac{22}{15} - \left( \frac{6}{15} \right)^2 \times 5^2</math></p> <p style="text-align: center;"><math>= (1.466 - 0.16) \times 25</math>                      <math>\frac{1}{2}</math></p> <p style="text-align: center;"><math>= 1.306 \times 25</math></p> <p style="text-align: center;"><math>= 32.6</math>                      <math>\frac{1}{2}</math></p>	Class-interval	0-4	5-9	10-14	15-19	20-24	Frequency ( $f$ )	1	2	5	4	3	C.I.	$f$	$x$	$d = \frac{x - A}{i}$	$d^2$	$fd$	$fd^2$	0-4	1	2	-2	4	-2	4	5-9	2	7	-1	1	-2	2	10-14	5	12	0	0	0	0	15-19	4	17	1	1	4	4	20-24	3	22	2	4	6	12	<p>1½</p> <p>3</p>
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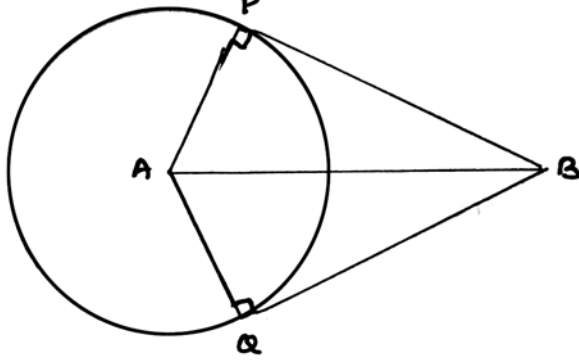
Qn. Nos.	Value Points	Marks allotted																																																																														
	<p><i>Direct method :</i></p> <table border="1"> <thead> <tr> <th>C.I.</th> <th><math>f</math></th> <th><math>x</math></th> <th><math>fx</math></th> <th><math>x^2</math></th> <th><math>fx^2</math></th> </tr> </thead> <tbody> <tr> <td>0-4</td> <td>1</td> <td>2</td> <td>2</td> <td>4</td> <td>4</td> </tr> <tr> <td>5-9</td> <td>2</td> <td>7</td> <td>14</td> <td>49</td> <td>98</td> </tr> <tr> <td>10-14</td> <td>5</td> <td>12</td> <td>60</td> <td>144</td> <td>720</td> </tr> <tr> <td>15-19</td> <td>4</td> <td>17</td> <td>68</td> <td>289</td> <td>1156</td> </tr> <tr> <td>20-24</td> <td>3</td> <td>22</td> <td>66</td> <td>484</td> <td>1452</td> </tr> </tbody> </table> <p style="text-align: center;"> <math>N = 15</math>                      <math>\Sigma fx = 210</math>                      <math>\Sigma fx^2 = 3430</math> </p> <p>Variance = <math>\sigma^2 = \Sigma \frac{fx^2}{N} - \left( \frac{\Sigma fx}{N} \right)^2</math> <span style="float: right;">1/2</span></p> <p style="text-align: center;"> <math>= \frac{3430}{15} - \left( \frac{210}{15} \right)^2</math> </p> <p style="text-align: center;"> <math>= 228.6 - 196</math> <span style="float: right;">1/2</span> </p> <p style="text-align: center;"> <math>= 32.6</math> <span style="float: right;">1/2</span> </p> <p><i>Assumed mean method :</i></p> <p style="text-align: center;">Assumed mean <math>A = 12</math></p> <table border="1"> <thead> <tr> <th>C.I.</th> <th><math>f</math></th> <th><math>x</math></th> <th><math>d = x - A</math></th> <th><math>fd</math></th> <th><math>d^2</math></th> <th><math>fd^2</math></th> </tr> </thead> <tbody> <tr> <td>0-4</td> <td>1</td> <td>2</td> <td>-10</td> <td>-10</td> <td>100</td> <td>100</td> </tr> <tr> <td>5-9</td> <td>2</td> <td>7</td> <td>-5</td> <td>-10</td> <td>25</td> <td>50</td> </tr> <tr> <td>10-14</td> <td>5</td> <td>12</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>15-19</td> <td>4</td> <td>17</td> <td>5</td> <td>20</td> <td>25</td> <td>100</td> </tr> <tr> <td>20-24</td> <td>3</td> <td>22</td> <td>10</td> <td>30</td> <td>100</td> <td>300</td> </tr> </tbody> </table> <p style="text-align: center;"> <math>N = 15</math>                      <math>\Sigma fd = 30</math>                      <math>\Sigma fd^2 = 550</math> </p>	C.I.	$f$	$x$	$fx$	$x^2$	$fx^2$	0-4	1	2	2	4	4	5-9	2	7	14	49	98	10-14	5	12	60	144	720	15-19	4	17	68	289	1156	20-24	3	22	66	484	1452	C.I.	$f$	$x$	$d = x - A$	$fd$	$d^2$	$fd^2$	0-4	1	2	-10	-10	100	100	5-9	2	7	-5	-10	25	50	10-14	5	12	0	0	0	0	15-19	4	17	5	20	25	100	20-24	3	22	10	30	100	300	3
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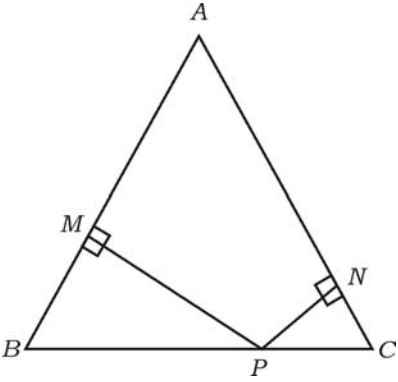
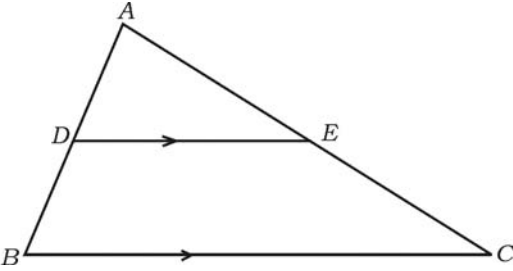
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	$\text{Variance} = \sigma^2 = \sum \frac{f d^2}{N} - \left( \frac{\sum f d}{N} \right)^2$ $= \frac{550}{15} - \left( \frac{30}{15} \right)^2$ $= 36.6 - 4$ $= 32.6$	<p>1/2</p> <p>1/2</p> <p>1/2</p> <p>3</p>																																										
	<p><i>Actual mean method :</i></p> <table border="1" data-bbox="288 869 1241 1391"> <thead> <tr> <th>C.I.</th> <th>f</th> <th>x</th> <th>fx</th> <th><math>d = x - \bar{x}</math></th> <th><math>d^2</math></th> <th><math>f d^2</math></th> </tr> </thead> <tbody> <tr> <td>0-4</td> <td>1</td> <td>2</td> <td>2</td> <td>-12</td> <td>144</td> <td>144</td> </tr> <tr> <td>5-9</td> <td>2</td> <td>7</td> <td>14</td> <td>-7</td> <td>49</td> <td>98</td> </tr> <tr> <td>10-14</td> <td>5</td> <td>12</td> <td>60</td> <td>-2</td> <td>4</td> <td>20</td> </tr> <tr> <td>15-19</td> <td>4</td> <td>17</td> <td>68</td> <td>3</td> <td>9</td> <td>36</td> </tr> <tr> <td>20-24</td> <td>3</td> <td>22</td> <td>66</td> <td>8</td> <td>64</td> <td>192</td> </tr> </tbody> </table> <p style="text-align: center;"> <math>N = 15</math>                  <math>\sum fx = 210</math>                  <math>\sum f d^2 = 490</math> </p> $\text{Mean} = \bar{x} = \frac{\sum f x}{N}$ $= \frac{210}{15} = 14$ $\text{Variance} = \sigma^2 = \frac{\sum f d^2}{N}$ $= \frac{490}{15}$ $= 32.6$	C.I.	f	x	fx	$d = x - \bar{x}$	$d^2$	$f d^2$	0-4	1	2	2	-12	144	144	5-9	2	7	14	-7	49	98	10-14	5	12	60	-2	4	20	15-19	4	17	68	3	9	36	20-24	3	22	66	8	64	192	<p>1 1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>3</p>
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Qn. Nos.	Value Points	Marks allotted
33.	<p>Solve <math>(2x + 3)(3x - 2) + 2 = 0</math> by using formula.</p> <p style="text-align: center;">OR</p> <p>If one root of the equation <math>x^2 + px + q = 0</math> is four times the other, prove that <math>4p^2 - 25q = 0</math>.</p> <p>Ans. :</p> $(2x + 3)(3x - 2) + 2 = 0$ $2x(3x - 2) + 3(3x - 2) + 2 = 0 \quad \frac{1}{2}$ $6x^2 - 4x + 9x - 6 + 2 = 0$ $6x^2 + 5x - 4 = 0 \quad \frac{1}{2}$ <p>where <math>a = 6, b = 5, c = -4</math></p> $\therefore x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad \frac{1}{2}$ $= \frac{-5 \pm \sqrt{5^2 - 4 \times 6 \times (-4)}}{2 \times 6} \quad \frac{1}{2}$ $= \frac{-5 \pm \sqrt{25 + 96}}{12}$ $= \frac{-5 \pm \sqrt{121}}{12}$ $= \frac{-5 \pm 11}{12} \quad \frac{1}{2}$ $= \frac{-5 + 11}{12} \quad \text{or} \quad \frac{-5 - 11}{12}$ $= \frac{6}{12} \quad \text{or} \quad \frac{-16}{12}$ $x = \frac{1}{2} \quad \text{or} \quad \frac{-4}{3} \quad \frac{1}{2}$ <p style="text-align: center;">OR</p>	3

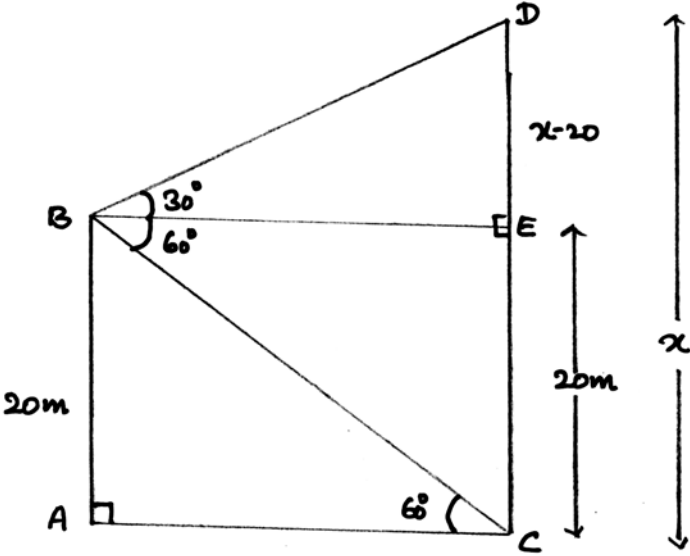


Qn. Nos.	Value Points	Marks allotted
	$x^2 + px + q = 0$ where $a = 1$ , $b = p$ , $c = q$	
	<p>If <math>m</math> and <math>n</math> are the roots</p> <p style="text-align: center;">then <math>m = 4n</math></p>	1/2
	$\therefore$ Sum of the roots = $m + n = \frac{-b}{a}$	
	$4n + n = \frac{-p}{1}$	
	$5n = -p$	
	$\therefore n = \frac{-p}{5}$ ... (i)	1/2
	Product of the roots = $mn = \frac{c}{a}$	
	$4n \times n = \frac{q}{1}$	
	$4n^2 = q$ ... (ii)	1/2
	Substituting (i) in (ii)	
	Then $4\left(\frac{-p}{5}\right)^2 = q$	1/2
	$\frac{4p^2}{25} = q$	
	$4p^2 = 25q$	1/2
	$4p^2 - 25q = 0$	1/2
		3

Qn. Nos.	Value Points	Marks allotted
34.	Prove that "The tangents drawn from an external point to a circle are equal". Ans. :	
		
	Data : A is the centre of the circle.	1/2
	B is an external point. BP and BQ are the tangents.	1/2
	To prove : $BP = BQ$	1/2
	Construction : AP, AQ and AB are joined.	1/2
	Proof: In $\triangle APB$ and $\triangle AQB$ ,	
	$\angle APB = \angle AQB$	
	Radius drawn at the point of contact is perpendicular to the tangent.	1/2
	hyp. $AB = hyp AB$	Common side
	$AP = AQ$	Radii of the same circle.
	$\therefore \triangle APB \cong \triangle AQB$	RHS theorem.
	$\therefore BP = BQ$	CPCT. 1/2
		3

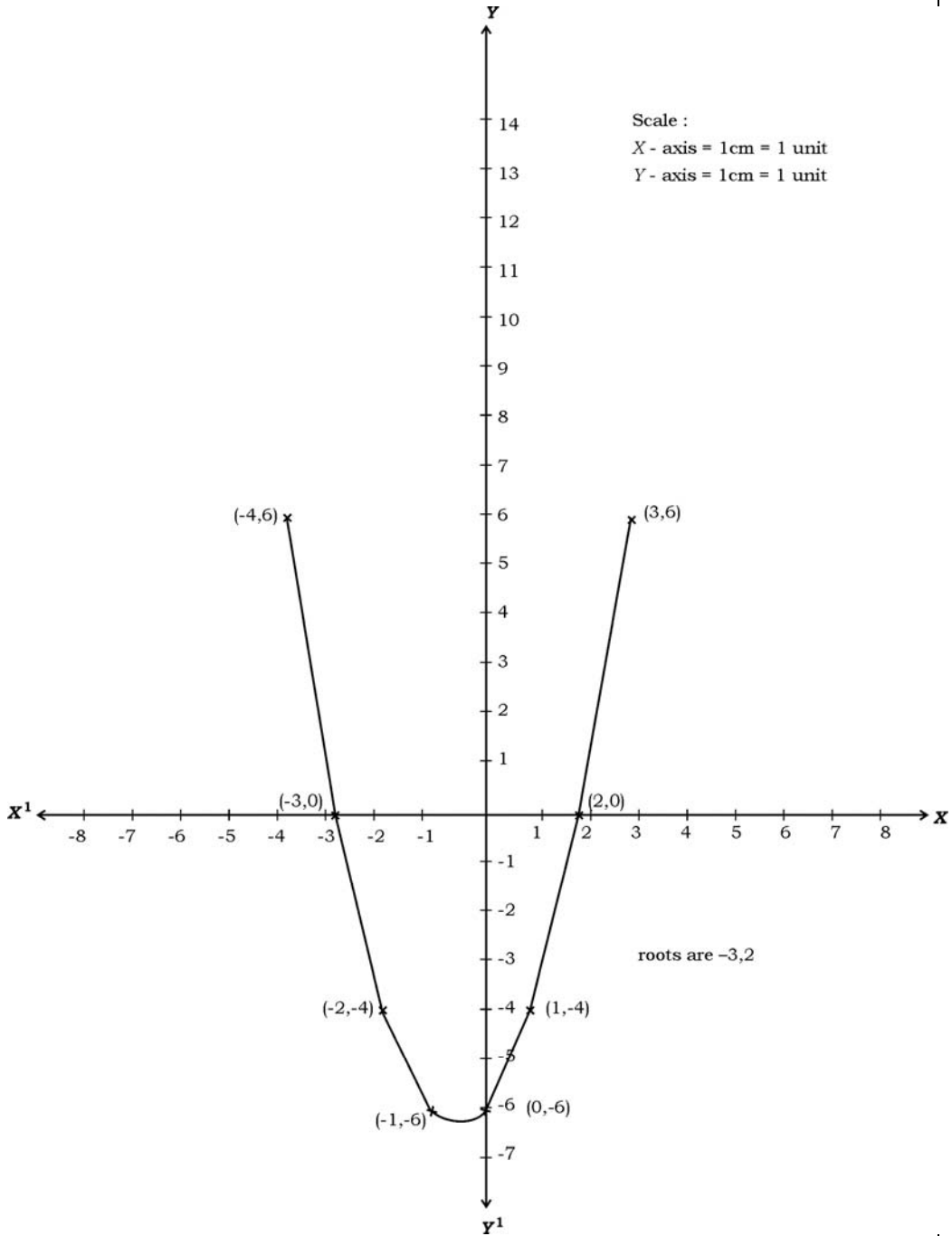
Qn. Nos.	Value Points	Marks allotted
35.	<p>In <math>\triangle ABC</math>, <math>AB = AC</math>. <math>P</math> is a point on <math>BC</math> such that <math>PN \perp AC</math> and <math>PM \perp AB</math> as shown in the figure. Prove that <math>\overline{MB} \cdot \overline{CP} = \overline{NC} \cdot \overline{BP}</math>.</p>  <p style="text-align: center;">OR</p> <p>In <math>\triangle ABC</math>, <math>DE \parallel BC</math>. If <math>3DE = 2BC</math> and the area of <math>\triangle ABC</math> is <math>81 \text{ cm}^2</math>, show that the area of <math>\triangle ADE</math> is <math>36 \text{ cm}^2</math>.</p>  <p>Ans. :</p> <p>In <math>\triangle ABC</math>, <math>AB = AC</math></p> <p><math>\therefore \hat{B} = \hat{C}</math>                      angles opposite to equal sides                      <math>\frac{1}{2}</math></p> <p>In <math>\triangle BMP</math> and <math>\triangle CNP</math></p> <p><math>\hat{BMP} = \hat{CNP}</math>                      right angles                      <math>\frac{1}{2}</math></p> <p><math>\hat{MBP} = \hat{NCP}</math>                      equal angles                      <math>\frac{1}{2}</math></p> <p><math>\therefore \triangle MBP \sim \triangle CNP</math>                      equiangular triangles                      <math>\frac{1}{2}</math></p> <p><math>\therefore \frac{MB}{NC} = \frac{BP}{CP} = \frac{MP}{NP}</math>                      AA - criteria                      <math>\frac{1}{2}</math></p> <p><math>\therefore MB \cdot CP = BP \cdot NC.</math>                      <math>\frac{1}{2}</math></p> <p style="text-align: center;">OR</p>	3

Qn. Nos.	Value Points	Marks allotted
	<p>Given <math>3DE = 2BC</math></p> $\therefore \frac{DE}{BC} = \frac{2}{3}$ <p>In <math>\Delta ADE</math> and <math>\Delta ABC</math>,</p> $\hat{A}DE = \hat{A}BC$ <p style="text-align: right;">Corresponding angles</p> $\hat{D}AE = \hat{B}AC$ <p style="text-align: right;">Common angle</p> $\therefore \Delta ADE \sim \Delta ABC$ <p style="text-align: right;">Equiangular triangles</p> $\therefore \frac{\text{Area of } \Delta ADE}{\text{Area of } \Delta ABC} = \frac{DE^2}{BC^2}$ $\frac{\text{Area of } \Delta ADE}{81} = \frac{2^2}{3^2}$ $\therefore \text{Area of } \Delta ADE = \frac{4 \times \cancel{81}^9}{\cancel{9}}$ $= 36 \text{ cm}^2.$	<p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;">3</p>
36.	<p>Prove that <math>(1 + \cot A - \operatorname{cosec} A)(1 + \tan A + \sec A) = 2</math>.</p> <p style="text-align: center;">OR</p> <p>From the top of a building 20 m high, the angle of elevation of the top of a vertical pole is <math>30^\circ</math> and the angle of depression of the foot of the same pole is <math>60^\circ</math>. Find the height of the pole.</p> <p>Ans. :</p> $= \left(1 + \frac{\cos A}{\sin A} - \frac{1}{\sin A}\right) \left(1 + \frac{\sin A}{\cos A} + \frac{1}{\cos A}\right)$ $= \left(\frac{\sin A + \cos A - 1}{\sin A}\right) \left(\frac{\cos A + \sin A + 1}{\cos A}\right)$ $= \frac{(\sin A + \cos A)^2 - 1^2}{\sin A \cos A}$ $= \frac{\sin^2 A + \cos^2 A + 2 \sin A \cos A - 1}{\sin A \cos A}$	<p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p>

Qn. Nos.	Value Points	Marks allotted
	<p>but <math>\sin^2 A + \cos^2 A = 1</math></p> $= \frac{\cancel{1} + 2 \sin A \cos A - \cancel{1}}{\sin A \cos A}$ $= \frac{2 \cancel{\sin A} \cancel{\cos A}}{\cancel{\sin A} \cancel{\cos A}}$ $= 2$	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>3</p>
	<p>OR</p> 	<p><math>\frac{1}{2}</math></p>
	<p>In <math>\triangle BED</math>, <math>\hat{DBE} = 30^\circ</math></p> $\therefore \tan 30^\circ = \frac{DE}{BE}$ $\frac{1}{\sqrt{3}} = \frac{x-20}{BE}$ $\therefore BE = \sqrt{3} (x-20)$	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>
	<p>In <math>\triangle ABC</math>, <math>\hat{ACB} = 60^\circ</math></p> $\therefore \tan 60^\circ = \frac{AB}{AC}$ $\sqrt{3} = \frac{20}{\sqrt{3} (x-20)}$	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>

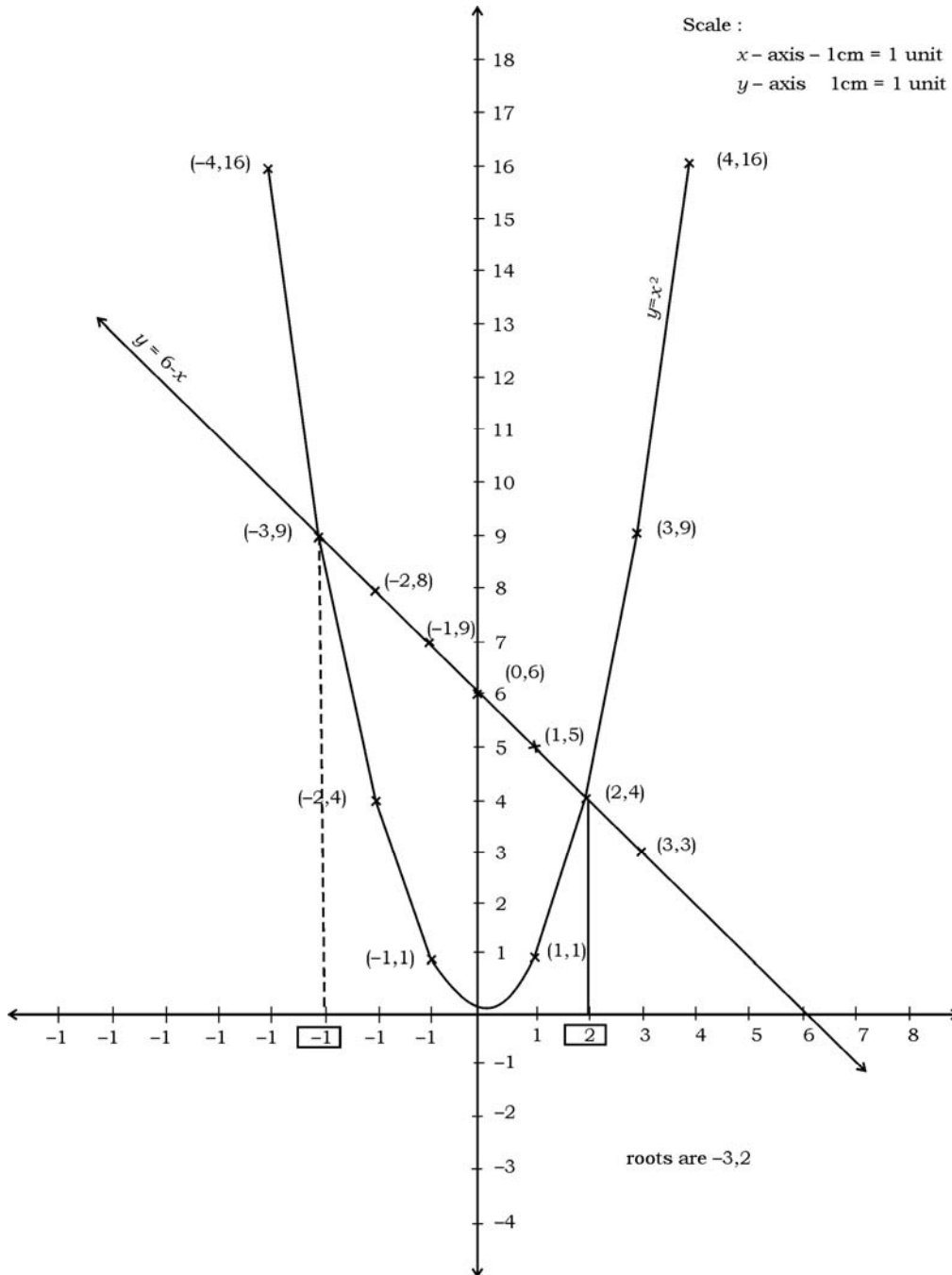
Qn. Nos.	Value Points	Marks allotted																		
V. 37.	$3(x - 20) = 20$ $3x - 60 = 20$ $\therefore 3x = 80$ $x = \frac{80}{3} = 26.6 \text{ m.}$																			
	Height of the pole = 26.6 m ( approximate ). <span style="float: right;">1/2</span>	3																		
	Solve the equation $x^2 + x - 6 = 0$ graphically.																			
	Ans. :																			
	$x^2 + x - 6 = 0$ $\therefore y = x^2 + x - 6$																			
	<table border="1" style="width: 100%; text-align: center;"> <tr> <td><math>x</math></td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>-1</td> <td>-2</td> <td>-3</td> <td>-4</td> </tr> <tr> <td><math>y</math></td> <td>-6</td> <td>-4</td> <td>0</td> <td>6</td> <td>-6</td> <td>-4</td> <td>0</td> <td>6</td> </tr> </table>	$x$	0	1	2	3	-1	-2	-3	-4	$y$	-6	-4	0	6	-6	-4	0	6	
$x$	0	1	2	3	-1	-2	-3	-4												
$y$	-6	-4	0	6	-6	-4	0	6												
	Table — <span style="float: right;">2</span>																			
	Drawing parabola — <span style="float: right;">1</span>																			
	Identifying roots — <span style="float: right;">1</span>	4																		
	Alternate method :																			
	$x^2 + x - 6 = 0$ <span style="margin-left: 100px;"><math>\therefore y = x^2</math></span> , <span style="margin-left: 20px;"><math>y = 6 - x</math></span>																			
	$y = x^2$																			
	<table border="1" style="width: 100%; text-align: center;"> <tr> <td><math>x</math></td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>-1</td> <td>-2</td> <td>-3</td> </tr> <tr> <td><math>y</math></td> <td>0</td> <td>1</td> <td>4</td> <td>9</td> <td>1</td> <td>4</td> <td>9</td> </tr> </table>	$x$	0	1	2	3	-1	-2	-3	$y$	0	1	4	9	1	4	9			
$x$	0	1	2	3	-1	-2	-3													
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	<table border="1" style="width: 100%; text-align: center;"> <tr> <td><math>x</math></td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>-1</td> <td>-2</td> <td>-3</td> </tr> <tr> <td><math>y</math></td> <td>6</td> <td>5</td> <td>4</td> <td>3</td> <td>7</td> <td>8</td> <td>9</td> </tr> </table>	$x$	0	1	2	3	-1	-2	-3	$y$	6	5	4	3	7	8	9			
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Qn. Nos.	Value Points	Marks allotted
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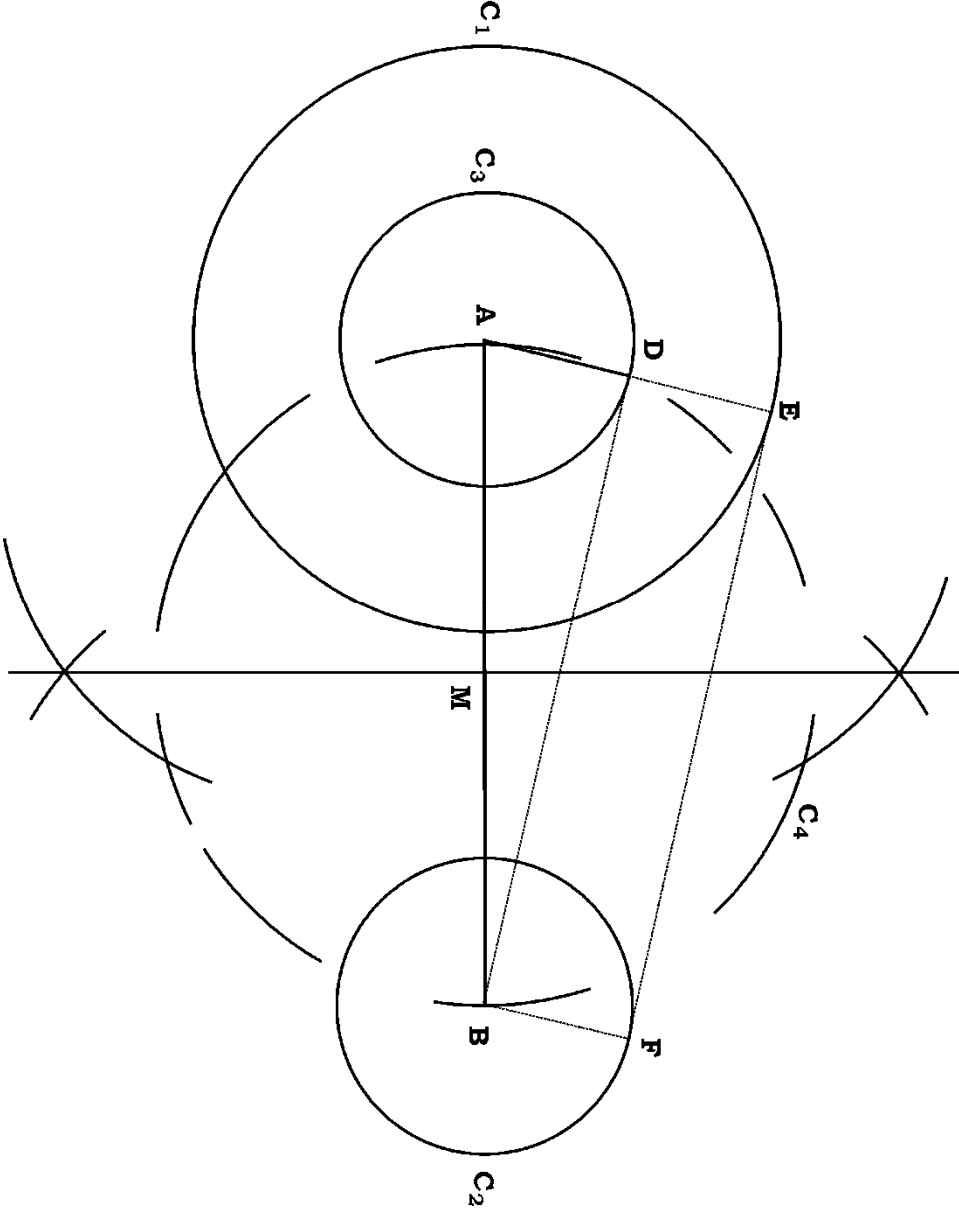


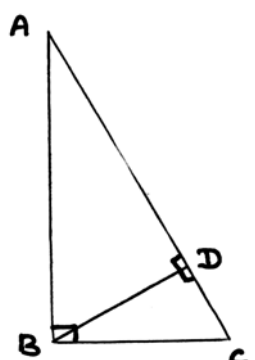
Qn. Nos.	Value Points	Marks allotted
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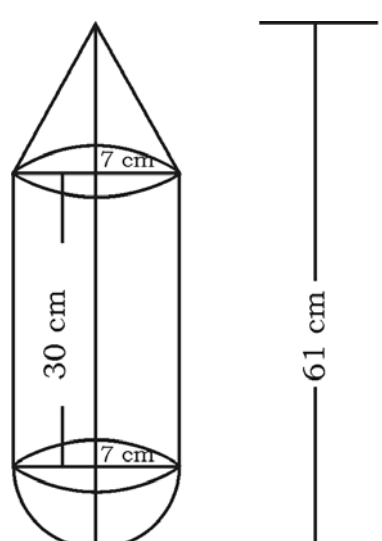
Alternate method :

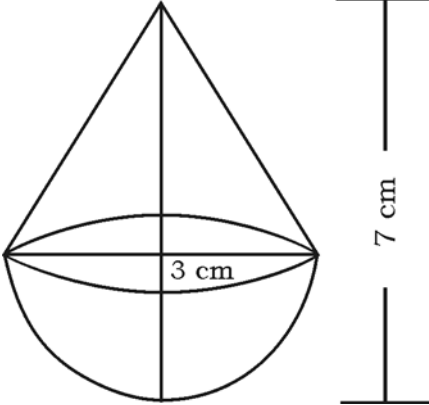




Qn. Nos.	Value Points	Marks allotted
38.	<p>Construct a direct common tangent to two circles of radii 4 cm and 2 cm whose centres are 9 cm apart. Measure and write the length of the direct common tangent.</p> <p>Ans. :</p> <p><math>R = 4 \text{ cm}, \quad r = 2 \text{ cm} \quad \therefore \quad R - r = 4 - 2 = 2 \text{ cm}</math></p> <p><math>d = 9 \text{ cm}</math></p>  <p>Length of the tangent <math>EF = 8.8 \text{ cm}</math></p>	

Qn. Nos.	Value Points	Marks allotted												
39.	Drawing $AB$ and marking mid-point —	1												
	Drawing $C_1, C_2, C_3$ —	1½												
	Joining $DB, EF$ —	1												
	Measuring and writing the length													
	of the tangent —	½												
	<p>Prove that “In a right angled triangle, square on the hypotenuse is equal to sum of the squares on the other two sides”.</p> <p>Ans. :</p>	4												
	<div style="display: flex; align-items: center; justify-content: center;">  <div style="margin-left: 20px;"> <p>Figure — ½</p> <p>Data — ½</p> <p>To prove — ½</p> <p>Construction — ½</p> </div> </div>													
	<p><i>Data :</i> In <math>\triangle ABC</math>, <math>\hat{A}BC = 90^\circ</math></p> <p><i>To prove :</i> <math>AC^2 = AB^2 + BC^2</math></p> <p><i>Construction :</i> <math>BD \perp AC</math> is drawn.</p> <p><i>Proof :</i> Comparing <math>\triangle ABC</math> and <math>\triangle ABD</math></p> <table border="0" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 50%; text-align: center;"><i>Statement</i></th> <th style="width: 50%; text-align: center;"><i>Reason</i></th> </tr> </thead> <tbody> <tr> <td style="text-align: center;"><math>\hat{A}BC = \hat{A}DB</math></td> <td>Right angles</td> </tr> <tr> <td style="text-align: center;"><math>\hat{B}AC = \hat{B}AD</math></td> <td>common angle</td> </tr> <tr> <td style="text-align: center;"><math>\therefore \triangle BAC \sim \triangle DAB</math></td> <td>Equiangular triangles</td> </tr> <tr> <td style="text-align: center;"><math>\therefore \frac{BA}{DA} = \frac{AC}{AB}</math></td> <td>AA — criteria</td> </tr> <tr> <td style="text-align: center;"><math>\therefore \boxed{AB^2 = AC \cdot AD}</math></td> <td>... (i)</td> </tr> </tbody> </table>	<i>Statement</i>	<i>Reason</i>	$\hat{A}BC = \hat{A}DB$	Right angles	$\hat{B}AC = \hat{B}AD$	common angle	$\therefore \triangle BAC \sim \triangle DAB$	Equiangular triangles	$\therefore \frac{BA}{DA} = \frac{AC}{AB}$	AA — criteria	$\therefore \boxed{AB^2 = AC \cdot AD}$	... (i)	½
<i>Statement</i>	<i>Reason</i>													
$\hat{A}BC = \hat{A}DB$	Right angles													
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$\therefore \boxed{AB^2 = AC \cdot AD}$	... (i)													

Qn. Nos.	Value Points	Marks allotted
	<p>Comparing <math>\triangle ABC</math> and <math>\triangle BDC</math></p> $\hat{A}BC = \hat{B}DC$ $\hat{A}CB = \hat{B}CD$ <p><math>\therefore \triangle BCA \sim \triangle DCB</math></p> $\therefore \frac{BC}{DC} = \frac{AC}{BC}$ <p><math>\therefore \boxed{BC^2 = AC \cdot DC}</math> ... (ii)</p> <p>By adding (i) and (ii)</p> $AB^2 + BC^2 = AC \times AD + AC \times DC$ $= AC (AD + DC) \quad \because AD + DC = AC$ $= AC \times AC$ <p><math>\therefore \boxed{AB^2 + BC^2 = AC^2}</math></p>	<p>Right angles</p> <p>common angle</p> <p>Equiangular triangles <math>\frac{1}{2}</math></p> <p>AA — criteria</p> <p><math>\frac{1}{2}</math></p> <p>4</p>
40.	<p>A solid is in the shape of a cylinder with a cone attached at one end and a hemisphere attached to the other end as shown in the figure. All of them are of the same radius 7 cm. If the total length of the solid is 61 cm and height of the cylinder is 30 cm, calculate the cost of painting the outer surface of the solid at the rate of Rs. 10 per 100 cm<sup>2</sup>.</p> <div style="text-align: center;">  </div> <p>OR</p>	

Qn. Nos.	Value Points	Marks allotted
	<p>A solid metallic cylinder of diameter 12 cm and height 15 cm is melted and recast into toys in the shape of right circular cone mounted on a hemisphere as shown in the figure. If radii of the cone and hemisphere are each equal to 3 cm and the height of the toy is 7 cm, calculate the number of such toys that can be formed.</p>  <p>The diagram shows a right circular cone on top of a hemisphere. A vertical line from the apex of the cone to the center of the hemisphere's base is labeled '3 cm'. A vertical dimension line to the right of the hemisphere is labeled '7 cm', representing the total height of the toy.</p> <p><i>Ans. :</i></p> <p>Height of the cone = Total height of the solid – ( height of the cylinder + radius of the hemisphere )</p> $= 61 - ( 30 + 7 )$ $= 61 - 37 = 24 \text{ cm.} \quad \frac{1}{2}$ <p>But 7, 24, 25 are Pythagorean triplets</p> $\therefore \text{Slant height of the cone} = l = 25 \text{ cm.} \quad \frac{1}{2}$ <p>TSA of the solid = LSA of the cone + LSA of the cylinder + LSA of the hemisphere</p> $= \pi r l + 2\pi r h + 2\pi r^2$ $= \pi r ( l + 2h + 2r )$ $= \frac{22}{7} \times 7 ( 25 + 2 \times 30 + 2 \times 7 ) \text{ sq.cm.} \quad \frac{1}{2}$ $= 22 \times 99$ $= 2178 \text{ sq.cm.} \quad \frac{1}{2}$ <p>Cost of painting at the rate of Rs. 10 per 100 cm<sup>2</sup> = <math>\frac{2178 \times 10}{100}</math></p> $= \text{Rs. } 217.8 \quad \frac{1}{2}$	4

Qn. Nos.	Value Points	Marks allotted
	<i>Alternate method :</i>	
	Height of the cone = $h = 24$ cm	$\frac{1}{2}$
	Slant height of the cone = $l = 25$ cm.	$\frac{1}{2}$
	$\therefore$ LSA of the cone = $\pi rl$ $= \pi \times 7 \times 25$ sq.cm $= 175 \pi$ sq.cm.	$\frac{1}{2}$
	LSA of the cylinder = $2\pi rh$ $= 2\pi \times 7 \times 30$ sq.cm $= 420 \pi$ sq.cm.	$\frac{1}{2}$
	LSA of the hemisphere = $2\pi r^2$ $= 2\pi \times 7^2$ $= 98\pi$ sq.cm.	$\frac{1}{2}$
	TSA of the solid = LSA of the cone + LSA of the cylinder $+ \text{LSA of the hemisphere}$ $= (175 \pi + 420 \pi + 98 \pi)$ sq.cm. $= \frac{22}{7} \times \cancel{693}^{99}$ $= 2178$ sq.cm.	$\frac{1}{2}$
	Cost of painting = $\frac{2178 \times 10}{100}$ $= \text{Rs. } 217.8$	$\frac{1}{2}$
	OR	
		4

Qn. Nos.	Value Points	Marks allotted												
	Volume of the metal cylinder = $\pi r^2 h$ cubic units	$\frac{1}{2}$												
	$\left( \begin{array}{l} r = 6 \text{ cm} \\ h = 15 \text{ cm} \end{array} \right) = \pi \times 36 \times 15 \text{ c.c.}$	$\frac{1}{2}$												
	Volume of the toy = Volume of the cone													
	$\left( \begin{array}{l} r = 3 \text{ cm} \\ h = 7 - 3 = 4 \text{ cm} \end{array} \right) +$													
	Volume of the hemisphere													
	$= \frac{1}{3} \pi r^2 h + \frac{2}{3} \pi r^3$	$\frac{1}{2}$												
	$= \frac{\pi r^2}{3} (h + 2r)$	$\frac{1}{2}$												
	$= \frac{\pi \times 3^2}{3} (4 + 6)$													
	$= 3 \times 10 \times \pi$	$\frac{1}{2}$												
	Number of toys = $\frac{\text{Volume of the cylinder}}{\text{Volume of the toy}}$	$\frac{1}{2}$												
	$= \frac{36 \times 15 \times \pi}{3 \times 10 \times \pi}$	$\frac{1}{2}$												
	$= 18$	$\frac{1}{2}$												
	<i>Alternate method :</i>													
	<table style="width: 100%; border: none;"> <tr> <td style="text-align: center;"><i>Cylinder</i></td> <td style="text-align: center;"><i>Cone</i></td> <td style="text-align: center;"><i>Hemisphere</i></td> <td></td> </tr> <tr> <td style="text-align: center;"><math>r_1 = 6 \text{ cm}</math></td> <td style="text-align: center;"><math>r_2 = 3 \text{ cm}</math></td> <td style="text-align: center;"><math>r_2 = 3 \text{ cm}</math></td> <td><math>\frac{1}{2}</math></td> </tr> <tr> <td style="text-align: center;"><math>h_1 = 15 \text{ cm}</math></td> <td style="text-align: center;"><math>h_2 = 4 \text{ cm}</math></td> <td></td> <td></td> </tr> </table>	<i>Cylinder</i>	<i>Cone</i>	<i>Hemisphere</i>		$r_1 = 6 \text{ cm}$	$r_2 = 3 \text{ cm}$	$r_2 = 3 \text{ cm}$	$\frac{1}{2}$	$h_1 = 15 \text{ cm}$	$h_2 = 4 \text{ cm}$			
<i>Cylinder</i>	<i>Cone</i>	<i>Hemisphere</i>												
$r_1 = 6 \text{ cm}$	$r_2 = 3 \text{ cm}$	$r_2 = 3 \text{ cm}$	$\frac{1}{2}$											
$h_1 = 15 \text{ cm}$	$h_2 = 4 \text{ cm}$													
	Number of toys = $\frac{\text{Volume of the metal cylinder}}{\text{Volume of the toy}}$	$\frac{1}{2}$												

Qn. Nos.	Value Points	Marks allotted
	$= \frac{\pi r_1^2 h_1}{\frac{1}{3} \pi r_2^2 h_2 + \frac{2}{3} \pi r_2^3}$	1½
	$= \frac{\pi(6^2 \times 15)}{\frac{1}{3} \times \pi \times 3^2 (4+6)}$	1
	$= \frac{\cancel{36}^{18} \times \cancel{15}^3}{\cancel{3} \times \cancel{10}_2}$	
	= 18.	½