

CCE RR

ಕರ್ನಾಟಕ ಪ್ರೌಢ ಶಿಕ್ಷಣ ಪರೀಕ್ಷಾ ಮಂಡಳಿ, ಮಲ್ಲೇಶ್ವರಂ, ಬೆಂಗಳೂರು – 560 003

**KARNATAKA SECONDARY EDUCATION EXAMINATION BOARD, MALLESWARAM,
BANGALORE – 560 003**

ಎಸ್.ಎಸ್.ಎಲ್.ಸಿ. ಪರೀಕ್ಷೆ, ಜೂನ್ — 2017

S. S. L. C. EXAMINATION, JUNE, 2017

ಮಾದರಿ ಉತ್ತರಗಳು
MODEL ANSWERS

ದಿನಾಂಕ : 16. 06. 2017]

ಸಂಕೇತ ಸಂಖ್ಯೆ : **81-E**

Date : 16. 06. 2017]

CODE No. : **81-E**

ವಿಷಯ : ಗಣಿತ

Subject : MATHEMATICS

(ಹೊಸ ಪಠ್ಯಕ್ರಮ / New Syllabus)

(ಪುನರಾವರ್ತಿತ ಶಾಲಾ ಅಭ್ಯರ್ಥಿ / Regular Repeater)

(ಇಂಗ್ಲಿಷ್ ಭಾಷಾಂತರ / English Version)

[ಗರಿಷ್ಠ ಅಂಕಗಳು : 80

[Max. Marks : 80

Qn. Nos.	Ans. Key	Value Points	Marks allotted
I. 1.	B	{ 6, 7, 8 }	1
2.	C	90	1
3.	A	5	1
4.	D	$\sqrt{x - y}$	1
5.	B	18	1
6.	C	an acute angle	1
7.	D	$12\sqrt{2}$ cm	1
8.	A	13 units	1

RR-XXII-8010

[Turn over

Qn. Nos.	Value Points	Marks allotted	
II.			
9.	${}^{100}P_0 = 1$	1	
10.	Probability of a certain event is 1	1	
11.	Mid-point of the class-interval = $\frac{5 + 15}{2}$ $= \frac{20}{2} = 10$	$\frac{1}{2}$ $\frac{1}{2}$ 1	
12.	Method : 1 $\cos 48^\circ - \sin 42^\circ$ $= \sin 42^\circ - \sin 42^\circ$ $= 0$	Method : 2 $\cos 48^\circ - \sin 42^\circ$ $= \cos 48^\circ - \cos 48^\circ$ $= 0$	$\frac{1}{2}$ $\frac{1}{2}$ 1
13.	$y = 3x$ comparing with $y = mx + c$ slope $m = 3$ y -intercept = $c = 0$	$\frac{1}{2}$ $\frac{1}{2}$	1
14.	Total surface area of a solid hemi-sphere = $3\pi r^2$ sq.units		1
III.	Solution :		
15.	$n(A) = 37, n(B) = 26, n(A \cup B) = 51$ $n(A \cap B) = ?$ $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ $51 = 37 + 26 - n(A \cap B)$ $\therefore n(A \cap B) = 63 - 51$ $n(A \cap B) = 12$	1 $\frac{1}{2}$ $\frac{1}{2}$	2
16.	a) Arithmetic mean A.M. = $\frac{a+b}{2}$ b) Harmonic mean H.M. = $\frac{2ab}{a+b}$	1 1	2

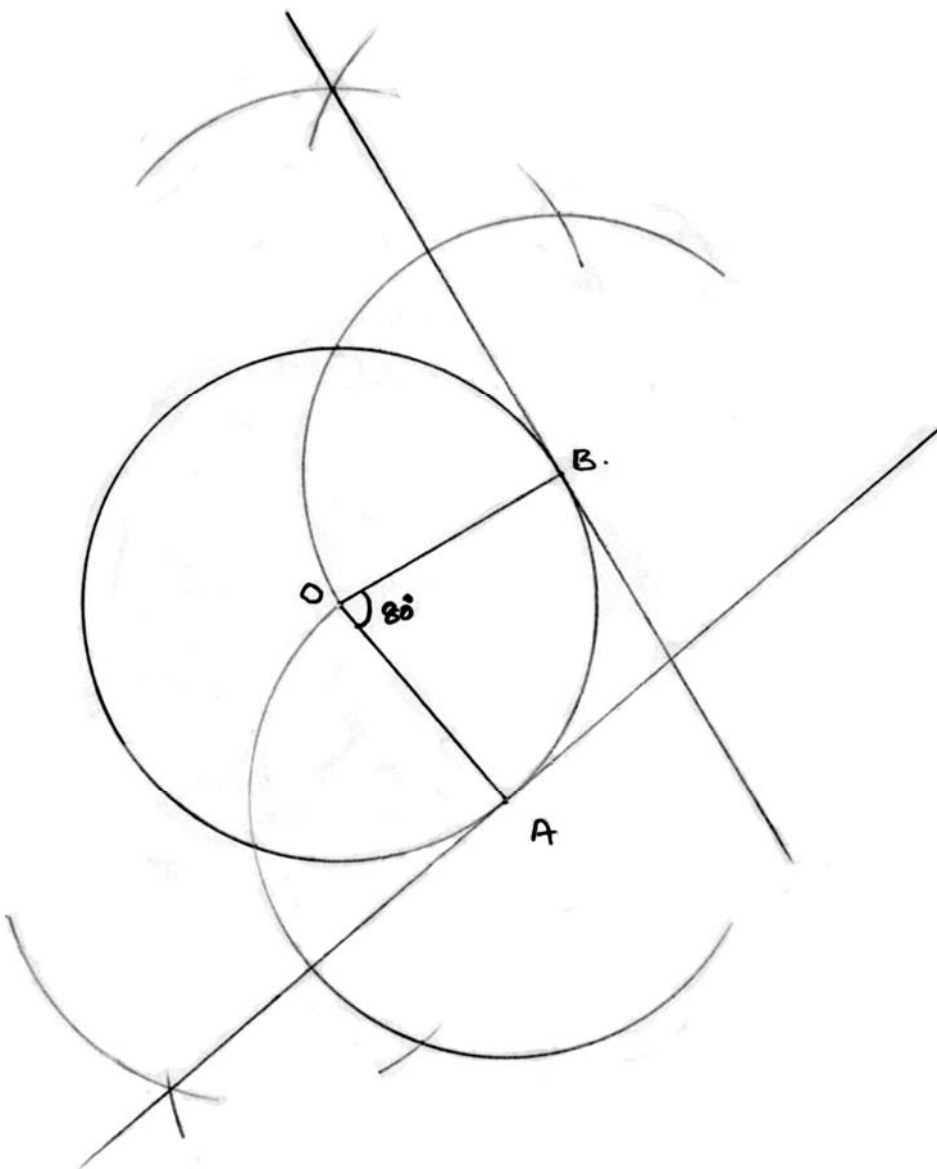
Qn. Nos.	Value Points	Marks allotted
17.	<p>Solution :</p> <p>Here $a = 2$, $r = \frac{2}{3} = \frac{2}{3} \times \frac{1}{2} = \frac{1}{3}$</p> <p>$S_{\infty} = ?$</p> $S_{\infty} = \frac{a}{1-r}$ $= \frac{2}{1-\frac{1}{3}} = \frac{2}{\frac{2}{3}}$ $= 2 \times \frac{3}{2}$ <p>$\therefore S_{\infty} = 3$</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p>
18.	<p>Let us assume, $3 + \sqrt{5}$ is a rational number</p> <p>$\Rightarrow 3 + \sqrt{5} = \frac{p}{q}$ where $p, q \in \mathbb{Z}, q \neq 0$</p> <p>$\Rightarrow -3 + \frac{p}{q} = \sqrt{5}$</p> <p>$\Rightarrow \frac{-3q+p}{q} = \sqrt{5}$</p> <p>$\Rightarrow \sqrt{5}$ is a rational number $\therefore \frac{-3q+p}{q}$ is rational</p> <p>but $\sqrt{5}$ is not a rational number</p> <p>this gives us contradiction</p> <p>\therefore our assumption $3 + \sqrt{5}$ is a rational number is wrong</p> <p>$\Rightarrow 3 + \sqrt{5}$ is an irrational number</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
19.	<p>A triangle is formed by joining 3 non-collinear points.</p> <p>\therefore Total number of triangles that can be drawn out of 8 non-collinear points = 8C_3</p> <p>Here $n = 8, r = 3$</p> ${}^nC_r = \frac{n!}{(n-r)!r!}$ ${}^8C_3 = \frac{8!}{(8-3)!3!}$ $= \frac{8 \times 7 \times \cancel{6} \times \cancel{5}!}{\cancel{5!} \times 3 \times 2}$ <p>$= 56$</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p> <p>$\frac{1}{2}$</p>

Qn. Nos.	Value Points	Marks allotted
20.	<p>Alternate method :</p> <p>Number of triangles ${}^n C_3 = \frac{n(n-1)(n-2)}{6}$</p> <p>If $n = 8$</p> ${}^8 C_3 = \frac{8 \times 7 \times 6}{6}$ $= 56$ <p>Solution :</p> $\frac{1}{8!} + \frac{1}{9!} = \frac{x}{10!}$ $\frac{1}{8!} + \frac{1}{9 \times 8!} = \frac{x}{10 \times 9 \times 8!}$ $\frac{1}{8!} \left(1 + \frac{1}{9}\right) = \frac{x}{10 \times 9 \times 8!}$ $\frac{10}{9} = \frac{x}{10 \times 9}$ $\therefore x = 100$	<p>1</p> <p>2</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p>
21.	<p>Solution :</p> <p>There are 7 marbles, out of these 4 marbles can be drawn in</p> ${}^7 C_4 = 35 \text{ ways}$ $\therefore n(S) = 35$ <p>Two marbles out of 4 red marbles can be drawn in ${}^4 C_2 = 6$ ways</p> <p>The remaining 2 marbles must be black and they can be drawn</p> <p>in ${}^3 C_2 = 3$ ways</p> $\therefore n(A) = {}^4 C_2 \times {}^3 C_2 = 6 \times 3 = 18$ $\therefore P(A) = \frac{n(A)}{n(S)} = \frac{18}{35}$	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>

Qn. Nos.	Value Points	Marks allotted																		
22.	<p>Direct method :</p> <table border="1" style="display: inline-table; vertical-align: top;"> <thead> <tr> <th>x</th> <th>x^2</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>25</td> </tr> <tr> <td>6</td> <td>36</td> </tr> <tr> <td>7</td> <td>49</td> </tr> <tr> <td>8</td> <td>64</td> </tr> <tr> <td>9</td> <td>81</td> </tr> <tr> <td>$\Sigma x = 35$</td> <td>$\Sigma x^2 = 255$</td> </tr> </tbody> </table> <p style="text-align: center;">$N = 5$</p> <p>Standard deviation</p> $\sigma = \sqrt{\frac{\Sigma x^2}{N} - \left(\frac{\Sigma x}{N}\right)^2}$ $= \sqrt{\frac{255}{5} - \left(\frac{35}{5}\right)^2}$ $= \sqrt{51 - 49}$ $= \sqrt{2}$ <p>$\sigma = 1.4$</p>	x	x^2	5	25	6	36	7	49	8	64	9	81	$\Sigma x = 35$	$\Sigma x^2 = 255$	<p>table $\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p>				
x	x^2																			
5	25																			
6	36																			
7	49																			
8	64																			
9	81																			
$\Sigma x = 35$	$\Sigma x^2 = 255$																			
	<p>Actual mean method :</p> <table border="1" style="display: inline-table; vertical-align: top;"> <thead> <tr> <th>x</th> <th>$d = x - \bar{x}$</th> <th>d^2</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>-2</td> <td>4</td> </tr> <tr> <td>6</td> <td>-1</td> <td>1</td> </tr> <tr> <td>7</td> <td>0</td> <td>0</td> </tr> <tr> <td>8</td> <td>1</td> <td>1</td> </tr> <tr> <td>9</td> <td>2</td> <td>4</td> </tr> </tbody> </table> <p>$\Sigma x = 35$ $\Sigma d^2 = 10$</p> <p>Mean = $\bar{x} = \frac{\Sigma x}{N}$</p> $= \frac{35}{5}$ $= 7$ <p>standard deviation = $\sigma = \sqrt{\frac{\Sigma d^2}{N}}$</p> $= \sqrt{\frac{10}{5}} = \sqrt{2}$ <p>$\sigma = 1.4$</p>	x	$d = x - \bar{x}$	d^2	5	-2	4	6	-1	1	7	0	0	8	1	1	9	2	4	<p>1</p> <p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p>
x	$d = x - \bar{x}$	d^2																		
5	-2	4																		
6	-1	1																		
7	0	0																		
8	1	1																		
9	2	4																		

Qn. Nos.	Value Points	Marks allotted																																				
	<p>Assumed mean method :</p> <p>Assumed mean $A = 6$ (any score can be taken)</p> <table border="1" data-bbox="392 443 1019 801"> <thead> <tr> <th>x</th> <th>$d = x - A$</th> <th>d^2</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>- 1</td> <td>1</td> </tr> <tr> <td>6</td> <td>0</td> <td>0</td> </tr> <tr> <td>7</td> <td>1</td> <td>1</td> </tr> <tr> <td>8</td> <td>2</td> <td>4</td> </tr> <tr> <td>9</td> <td>3</td> <td>9</td> </tr> </tbody> </table> <p style="text-align: center;">$N = 5$ $\Sigma d = 5$ $\Sigma d^2 = 15$</p> <p>Standard deviation $\sigma = \sqrt{\frac{\Sigma d^2}{N} - \left(\frac{\Sigma d}{N}\right)^2}$</p> <p style="text-align: right;">1</p> $= \sqrt{\frac{15}{5} - \left(\frac{5}{5}\right)^2}$ <p style="text-align: right;">1/2 2</p> $= \sqrt{3 - 1} = \sqrt{2}$ <p style="text-align: right;">1/2</p> $\sigma = 1.4$ <p>Step deviation method :</p> <p>Assumed mean $A = 7$, Common factor of the scores = $C = 1$</p> <table border="1" data-bbox="392 1256 971 1592"> <thead> <tr> <th>x</th> <th>$d = \frac{x - A}{C}$</th> <th>d^2</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>- 2</td> <td>4</td> </tr> <tr> <td>6</td> <td>- 1</td> <td>1</td> </tr> <tr> <td>7</td> <td>0</td> <td>0</td> </tr> <tr> <td>8</td> <td>1</td> <td>1</td> </tr> <tr> <td>9</td> <td>2</td> <td>4</td> </tr> </tbody> </table> <p style="text-align: center;">$N = 5$ $\Sigma d = 0$ $\Sigma d^2 = 10$</p> <p>Standard deviation = $\sigma = \sqrt{\frac{\Sigma d^2}{N} - \left(\frac{\Sigma d}{N}\right)^2} \times C$</p> <p style="text-align: right;">1</p> $= \sqrt{\frac{10}{5} - 0} \times 1$ <p style="text-align: right;">1/2 2</p> $= \sqrt{2}$ <p style="text-align: right;">1/2</p> $\sigma = 1.4$	x	$d = x - A$	d^2	5	- 1	1	6	0	0	7	1	1	8	2	4	9	3	9	x	$d = \frac{x - A}{C}$	d^2	5	- 2	4	6	- 1	1	7	0	0	8	1	1	9	2	4	
x	$d = x - A$	d^2																																				
5	- 1	1																																				
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Qn. Nos.	Value Points	Marks allotted
23.	<p>The equation is in the form of $ax^2 + bx + c = 0$</p> <p>where $a = 1, b = -2, c = -4$ 1/2</p> $\therefore x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-(-2) \pm \sqrt{(-2)^2 - 4 \times 1 \times -4}}{2 \times 1}$ $= \frac{2 \pm \sqrt{4 + 16}}{2}$ $= \frac{2 \pm 2\sqrt{5}}{2}$ $= \frac{2(1 \pm \sqrt{5})}{2}$ <p>$(1 + \sqrt{5})$ and $(1 - \sqrt{5})$ are the roots of the given quadratic equation 1/2</p> <p style="text-align: center;">OR</p> <p>This is in the form of $ax^2 + bx + c = 0$</p> <p>where $a = 1, b = -2, c = -3$ 1/2</p> $\therefore \Delta = b^2 - 4ac$ $= (-2)^2 - 4 \times 1 \times (-3)$ $= 4 + 12$ $= 16$ <p>$\Delta > 0 \therefore$ roots are real and distinct 1/2</p>	<p style="text-align: center;">2</p> <p style="text-align: center;">2</p>

Qn. Nos.	Value Points	Marks allotted
24.	<p>radius = $r = 3.5$ cm</p> <p>angle between the radii = 80°</p>  <p>circle 1/2</p> <p>angle between the radii 1/2</p> <p>tangents at A and B 1</p>	2

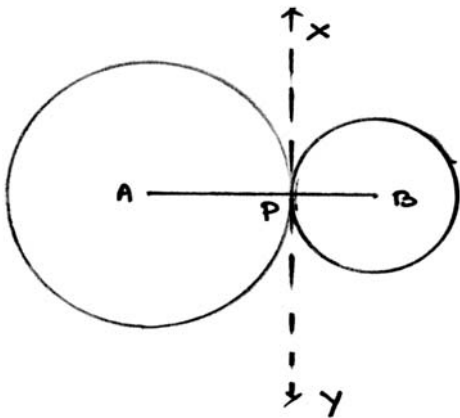
Qn. Nos.	Value Points	Marks allotted
25.	<p>In $\triangle ABC$ and $\triangle ADC$</p> <p>$\hat{BAC} = \hat{ADC}$ given</p> <p>$\hat{ACB} = \hat{ACD}$ common angle</p> <p>$\therefore \triangle ACB \sim \triangle DCA$ equiangular triangles 1</p> <p>$\therefore \frac{AC}{DC} = \frac{CB}{CA}$ AA - criteria $\frac{1}{2}$</p> <p>$\therefore AC^2 = BC \times DC$ $\frac{1}{2}$</p> <p style="text-align: center;">OR</p> <p>In $\triangle ABC$, $\hat{ABC} = 90^\circ$ and $BD \perp AC$</p> <p>$\therefore AB^2 = AD \times AC \rightarrow (1)$ corollary $\frac{1}{2}$</p> <p>similarly $BC^2 = CD \times AC \rightarrow (2)$ corollary $\frac{1}{2}$</p> <p>dividing (1) by (2) 2</p> <p>$\frac{AB^2}{BC^2} = \frac{AD \times AC}{CD \times AC}$ $\frac{1}{2}$</p> <p>$\therefore \frac{AB^2}{BC^2} = \frac{AD}{CD}$ $\frac{1}{2}$</p>	2
26.	<p>$\sin 30^\circ = \frac{1}{2}$</p> <p>$\cos 60^\circ = \frac{1}{2}, \tan 45^\circ = 1$ 1</p> <p>$\therefore \sin 30^\circ \cdot \cos 60^\circ - \tan^2 45^\circ$</p> <p>$= \frac{1}{2} \times \frac{1}{2} - (1)^2$</p> <p>$= \frac{1}{4} - 1 = \frac{1-4}{4}$ $\frac{1}{2}$</p> <p>$= -\frac{3}{4}$ $\frac{1}{2}$</p>	2

Qn. Nos.	Value Points	Marks allotted
27.	<p>Solution :</p> $(x_1, y_1) = (-5, 4)$ $(x_2, y_2) = (-7, 1)$ $\therefore d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ <p>radius of the circle = $\sqrt{[-7 - (-5)]^2 + (1 - 4)^2}$</p> $= \sqrt{(-7 + 5)^2 + (-3)^2}$ $= \sqrt{(-2)^2 + (-3)^2}$ $= \sqrt{4 + 9}$ $r = \sqrt{13}$	<p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>2</p>
28.	<p>ratio between the radii of two cylinders</p> $r_1 : r_2 = 2 : 3$ <p>ratio between their curved surface areas</p> $S_1 : S_2 = 5 : 6$ $\therefore \frac{S_1}{S_2} = \frac{2\pi r_1 h_1}{2\pi r_2 h_2}$ $\frac{5}{6} = \frac{2h_1}{3h_2}$ $\therefore \frac{h_1}{h_2} = \frac{5 \times 3}{6 \times 2} = \frac{5}{4}$ <p>ratio between their heights = 5 : 4</p>	<p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>2</p>

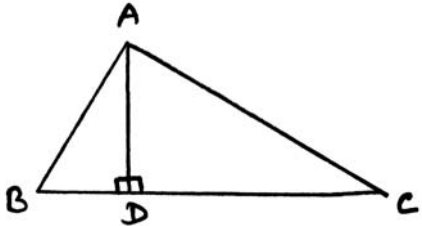
Qn. Nos.	Value Points	Marks allotted
29.	<p>Sphere - radius = $r_1 = 10$ cm Cone - height = $h_2 = 10$ cm - radius = $r_2 = 5$ cm</p> <p>Number of small cones formed = $\frac{\text{volume of the sphere}}{\text{volume of each small cone}}$ 1/2</p> $= \frac{\frac{4}{3} \pi r_1^3}{\frac{1}{3} \pi r_2^2 h_2}$ $= \frac{4 \times 10^2 \times 10 \times 10}{3 \times 3 \times 10}$ <p style="text-align: center;">= 16</p> <p>Number of small cones formed = 16 1/2</p>	2
30.	<p>Scale :</p> <p>25 m = 1 cm 50 m = 2 cm 75 m = 3 cm 100 m = 4 cm 125 m = 5 cm 200 m = 8 cm.</p> <div style="text-align: center;"> </div>	<p style="text-align: right;">Calculation 1/2 Plan drawing 1 1/2</p> <p style="text-align: center;">2</p>

Qn. Nos.	Value Points	Marks allotted
IV. 31.	<p>Rationalising factor of $\sqrt{6} - \sqrt{3}$ is $\sqrt{6} + \sqrt{3}$</p> $\therefore \frac{\sqrt{6} + \sqrt{3}}{\sqrt{6} - \sqrt{3}} \times \frac{\sqrt{6} + \sqrt{3}}{\sqrt{6} + \sqrt{3}}$ $= \frac{(\sqrt{6} + \sqrt{3})^2}{(\sqrt{6} + \sqrt{3})(\sqrt{6} - \sqrt{3})}$ $= \frac{6 + 3 + 2\sqrt{6} \cdot \sqrt{3}}{6 - 3}$ $= \frac{9 + 2\sqrt{18}}{3}$ $= \frac{9 + 6\sqrt{2}}{3}$ $= \frac{3(3 + 2\sqrt{2})}{3}$ $= 3 + 2\sqrt{2}$	<p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>3</p>
32.	$ \begin{array}{r} x^2 + 3x - 8 \\ \hline x + 1 \overline{) x^3 + 4x^2 - 5x + 6} \\ \underline{x^3 + x^2} \\ (-) \\ \hline 3x^2 - 5x + 6 \\ \underline{3x^2 + 3x} \\ (-) \\ \hline -8x + 6 \\ \underline{-8x - 8} \\ (+) \\ \hline 14 \end{array} $ <p>Quotient $q(x) = x^2 + 3x - 8$</p> <p>remainder $r(x) = 14$</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>3</p>

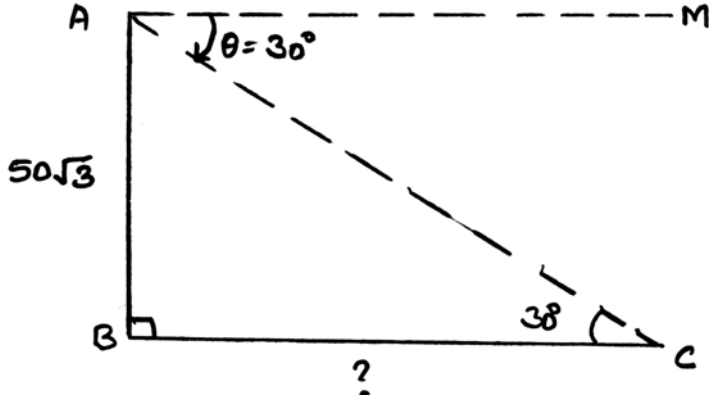
Qn. Nos.	Value Points	Marks allotted															
	<p>Verification :</p> $g(x) \times q(x) + r(x)$ $= (x+1)(x^2 + 3x - 8) + 14$ $= x^3 + 3x^2 - 8x + x^2 + 3x - 8 + 14$ $= x^3 + 4x^2 - 5x + 6$ $= p(x)$ <p>$\therefore p(x) = [g(x) \times q(x)] + r(x)$</p> <p style="text-align: center;">OR</p> <p>Synthetic division :</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 5px;">- 2</td> <td style="padding: 5px;">4</td> <td style="padding: 5px;">- 16</td> <td style="padding: 5px;">- 9</td> <td style="padding: 5px;">- 36</td> </tr> <tr> <td></td> <td></td> <td style="padding: 5px;">- 8</td> <td style="padding: 5px;">48</td> <td style="padding: 5px;">- 78</td> </tr> <tr> <td></td> <td style="padding: 5px;">4</td> <td style="padding: 5px;">- 24</td> <td style="padding: 5px;">39</td> <td style="padding: 5px;">- 114</td> </tr> </table> <p>\therefore The quotient is $4x^2 - 24x + 39$</p> <p>remainder $r(x) = - 114$</p>	- 2	4	- 16	- 9	- 36			- 8	48	- 78		4	- 24	39	- 114	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>2</p> <p>$\frac{1}{2}$</p> <p>3</p> <p>$\frac{1}{2}$</p> <p>3</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
- 2	4	- 16	- 9	- 36													
		- 8	48	- 78													
	4	- 24	39	- 114													
33.	<p>Let the three consecutive +ve integers be x, $(x+1)$ and $(x+2)$ from the statement,</p> $x^2 + (x+1)(x+2) = 92$ $x^2 + x^2 + 2x + x + 2 = 92$ $2x^2 + 3x + 2 = 92$ $2x^2 + 3x + 2 - 92 = 0$ $2x^2 + 3x - 90 = 0$ $2x^2 - 12x + 15x - 90 = 0$ $2x(x-6) + 15(x-6) = 0$ $(x-6)(2x+15) = 0$ <p>$\therefore x = 6$, or $x = -\frac{15}{2}$</p> <p>The three consecutive +ve integers are 6, 7, 8</p> <p style="text-align: center;">OR</p>	<p>$\frac{1}{2}$</p> <p>1</p> <p>$\frac{1}{2}$</p> <p>3</p> <p>$\frac{1}{2}$</p>															

Qn. Nos.	Value Points	Marks allotted
34.	Let the numbers be x, y and $x > y$	1/2
	sum of their squares is 180	
	$i.e. x^2 + y^2 = 180 \rightarrow (1)$	1/2
	Square of the smaller number is equal to 8 times the bigger number	
	$\therefore y^2 = 8x \rightarrow (2)$	1/2
	Substituting (2) in (1) we get	
	$x^2 + 8x = 180$	
	$x^2 + 8x - 180 = 0$	
	$x^2 + 18x - 10x - 180 = 0$	1/2
	$x(x + 18) - 10(x + 18) = 0$	3
$(x - 10)(x + 18) = 0$		
$\therefore x = 10 \text{ or } x = -18$	1/2	
If $x = 10$ then $y^2 = 8x$		
$y^2 = 8 \times 10$		
$y = \sqrt{80} = \sqrt{16 \times 5}$		
$= 4\sqrt{5}$	1/2	
The numbers are 10 and $4\sqrt{5}$		
	1/2	
Data : A and B are the centres of		
touching circles. P is the point of contact	1/2	

Qn. Nos.	Value Points	Marks allotted
	<p>To prove : A, P and B are collinear 1/2</p> <p>Construction : Tangent XY is drawn at P 1/2</p> <p>Proof : In the figure</p> $\left. \begin{aligned} \hat{A}PX = 90^\circ \rightarrow (1) \\ \hat{B}PX = 90^\circ \rightarrow (2) \end{aligned} \right\} \begin{array}{l} \text{radius drawn at the point of contact} \\ \text{is perpendicular to the tangent} \end{array} \quad \frac{1}{2}$ $\hat{A}PX + \hat{B}PX = 90^\circ + 90^\circ \text{ by adding (1) and (2)}$ $\hat{A}PB = 180^\circ \quad \hat{A}PB \text{ is a straight angle}$ <p>$\therefore APB$ is a straight line</p> <p>$\therefore A, P$ and B are collinear 1/2</p>	3
35.	<p>In $\triangle ABC, AB = BC = CA$</p> $AN \perp BC$ $\therefore BN = NC = \frac{1}{2} BC = \frac{1}{2} AB$ <p>In $\triangle ABN, \hat{A}NB = 90^\circ$</p> $\therefore AB^2 = AN^2 + BN^2$ <div style="text-align: right; margin-right: 100px;">1/2 + 1/2</div> $AN^2 = AB^2 - BN^2 \quad \frac{1}{2}$ $= AB^2 - \left(\frac{1}{2}AB\right)^2$ <div style="text-align: right; margin-right: 100px;">1/2</div> $= AB^2 - \frac{AB^2}{4}$ $AN^2 = \frac{4AB^2 - AB^2}{4} \quad \frac{1}{2}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $4AN^2 = 3AB^2$ </div> <div style="text-align: right; margin-right: 100px;">1/2</div> <p style="text-align: center;">OR</p>	3

Qn. Nos.	Value Points	Marks allotted
	<div style="text-align: center;">  </div> <p>In $\triangle ABD$, $\hat{A}DB = 90^\circ$ $\therefore AB^2 = AD^2 + BD^2$ $AD^2 = AB^2 - BD^2 \rightarrow (1)$</p> <p>In $\triangle ADC$, $\hat{A}DC = 90^\circ$ $\therefore AC^2 = AD^2 + DC^2$ $AD^2 = AC^2 - DC^2 \rightarrow (2)$</p> <p>from (1) and (2) $AB^2 - BD^2 = AC^2 - DC^2$ $\therefore AB^2 + DC^2 = AC^2 + BD^2$</p> <p>36. LHS = $\tan^2 A - \sin^2 A$ $= \frac{\sin^2 A}{\cos^2 A} - \sin^2 A$ $\because \tan A = \frac{\sin A}{\cos A}$ $= \frac{\sin^2 A - \sin^2 A \cos^2 A}{\cos^2 A}$ $= \frac{\sin^2 A (1 - \cos^2 A)}{\cos^2 A}$</p> <p>but $1 - \cos^2 A = \sin^2 A$ $= \frac{\sin^2 A \cdot \sin^2 A}{\cos^2 A}$ $= \frac{\sin^2 A}{\cos^2 A} \cdot \sin^2 A$ $= \tan^2 A \cdot \sin^2 A$ $\therefore \text{LHS} = \text{RHS}$</p>	<p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">3</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">3</p>

Qn. Nos.	Value Points	Marks allotted
	<p><i>Alternate method :</i></p> <p>LHS = $\tan^2 A - \sin^2 A$</p> <p>$= (\sec^2 A - 1) - \sin^2 A$ $\therefore \tan^2 A = \sec^2 A - 1$ $\frac{1}{2}$</p> <p>$= \frac{1}{\cos^2 A} - 1 - (1 - \cos^2 A)$ $\therefore \sec^2 A = \frac{1}{\cos^2 A}$ $\frac{1}{2}$</p> <p>$= \frac{1 - \cos^2 A - \cos^2 A + \cos^4 A}{\cos^2 A}$ $\sin^2 A = 1 - \cos^2 A$ $\frac{1}{2}$</p> <p>$= \frac{1 - 2\cos^2 A + \cos^4 A}{\cos^2 A}$</p> <p>$= \frac{(1 - \cos^2 A)^2}{\cos^2 A}$ $\therefore 1 - 2\cos^2 A + \cos^4 A$ 3</p> <p>$= \frac{(\sin^2 A)^2}{\cos^2 A}$ $= (1 - \cos^2 A)^2$ $\frac{1}{2}$</p> <p>$= \frac{\sin^2 A}{\cos^2 A} \cdot \sin^2 A$ $\therefore 1 - \cos^2 A = \sin^2 A$ $\frac{1}{2}$</p> <p>$= \tan^2 A \cdot \sin^2 A.$</p> <p>$\therefore$ LHS = RHS. $\frac{1}{2}$</p> <p style="text-align: center;">OR</p>	

Qn. Nos.	Value Points	Marks allotted
V. 37.	<div style="text-align: center;">  </div> <p>Let AB represents height of the building $AB = 50\sqrt{3}$ m</p> <p>BC be the distance between the building and the object Angle of depression is 30°</p> <p>Since $AM \parallel BC$, So $\hat{M}AC = \hat{A}CB = 30^\circ$</p> <p>In $\triangle ABC$, $\hat{A}BC = 90^\circ$, $\hat{A}CB = 30^\circ$</p> $\therefore \tan 30^\circ = \frac{AB}{BC}$ $\frac{1}{\sqrt{3}} = \frac{50\sqrt{3}}{BC}$ $\therefore BC = 50\sqrt{3} \times \sqrt{3}$ $= 50 \times 3$ <p>distance between the } building and the object } = 150 m</p> <p>In an AP</p> $T_3 + T_5 = 30$ $a + 2d + a + 4d = 30$ $2a + 6d = 30$ $a + 3d = 15 \rightarrow (1)$ <p>and $T_4 + T_8 = 46$</p> $a + 3d + a + 7d = 46$ $2a + 10d = 46$ $a + 5d = 23 \rightarrow (2)$	<p>1</p> <p>$\frac{1}{2}$</p> <p>3</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>

Qn. Nos.	Value Points	Marks allotted
	Subtracting (1) from (2) $\begin{array}{r} a + 5d = 23 \\ - a + 3d = 15 \\ \hline (-) \quad (-) \\ 2d = 8 \\ \therefore d = 4 \end{array}$	4
	If $d = 4$ then $a + 3d = 15$ $\begin{aligned} a + 3 \times 4 &= 15 \\ a + 12 &= 15 \\ a &= 15 - 12 = 3 \end{aligned}$	$\frac{1}{2}$
	If $a = 3$ and $d = 4$ then the AP is 3, 7, 11, 15,	$\frac{1}{2}$
	OR	
	In a GP $T_4 = 8$ $ar^3 = 8 \rightarrow (1)$	$\frac{1}{2}$
	and $T_8 = 128$ $ar^7 = 128 \rightarrow (2)$	$\frac{1}{2}$
	dividing (2) by (1) we get $\frac{\cancel{a}r^7}{\cancel{a}r^3} = \frac{128}{8}$ $r^4 = 16$ $\therefore \boxed{r = 2}$	$\frac{1}{2}$
	If $r = 2$ then $ar^3 = 8$ $\begin{aligned} a(2)^3 &= 8 \\ 8a &= 8 \\ \therefore \boxed{a = 1} \end{aligned}$	$\frac{1}{2}$
	If $a = 1$ and $r = 2$ then $S_n = \frac{a(r^n - 1)}{r - 1}$ $\therefore S_{10} = \frac{1(2^{10} - 1)}{2 - 1}$ $= 1024 - 1$ $\boxed{S_{10} = 1023}$	4

Qn. Nos.	Value Points	Marks allotted
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38.

$$x^2 - 2x - 3 = 0$$

$$\therefore y = x^2 - 2x - 3$$

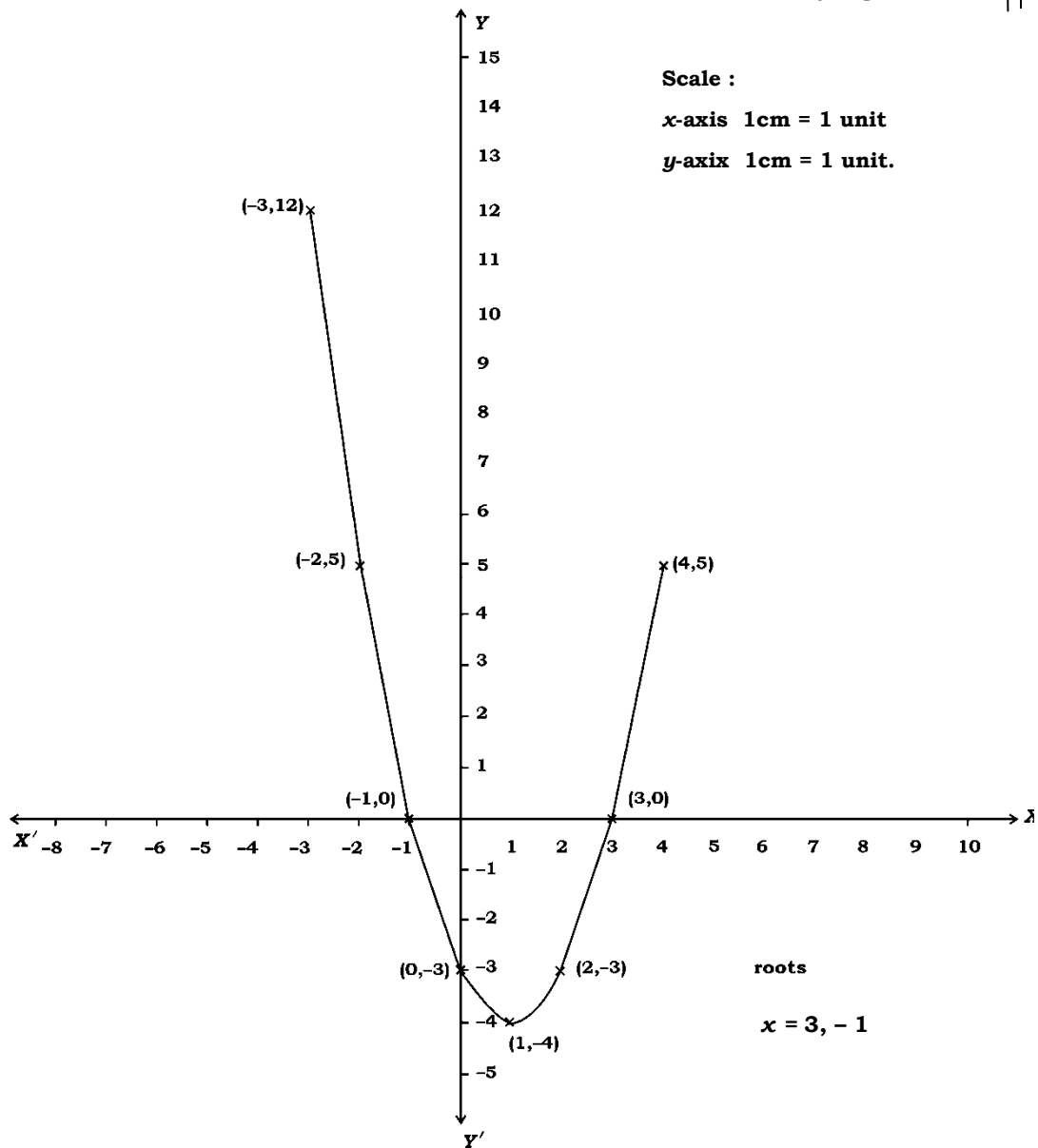
x	0	1	2	3	4	-1	-2	-3
y	-3	-4	-3	0	5	0	5	12

table 2

Drawing parabola 1

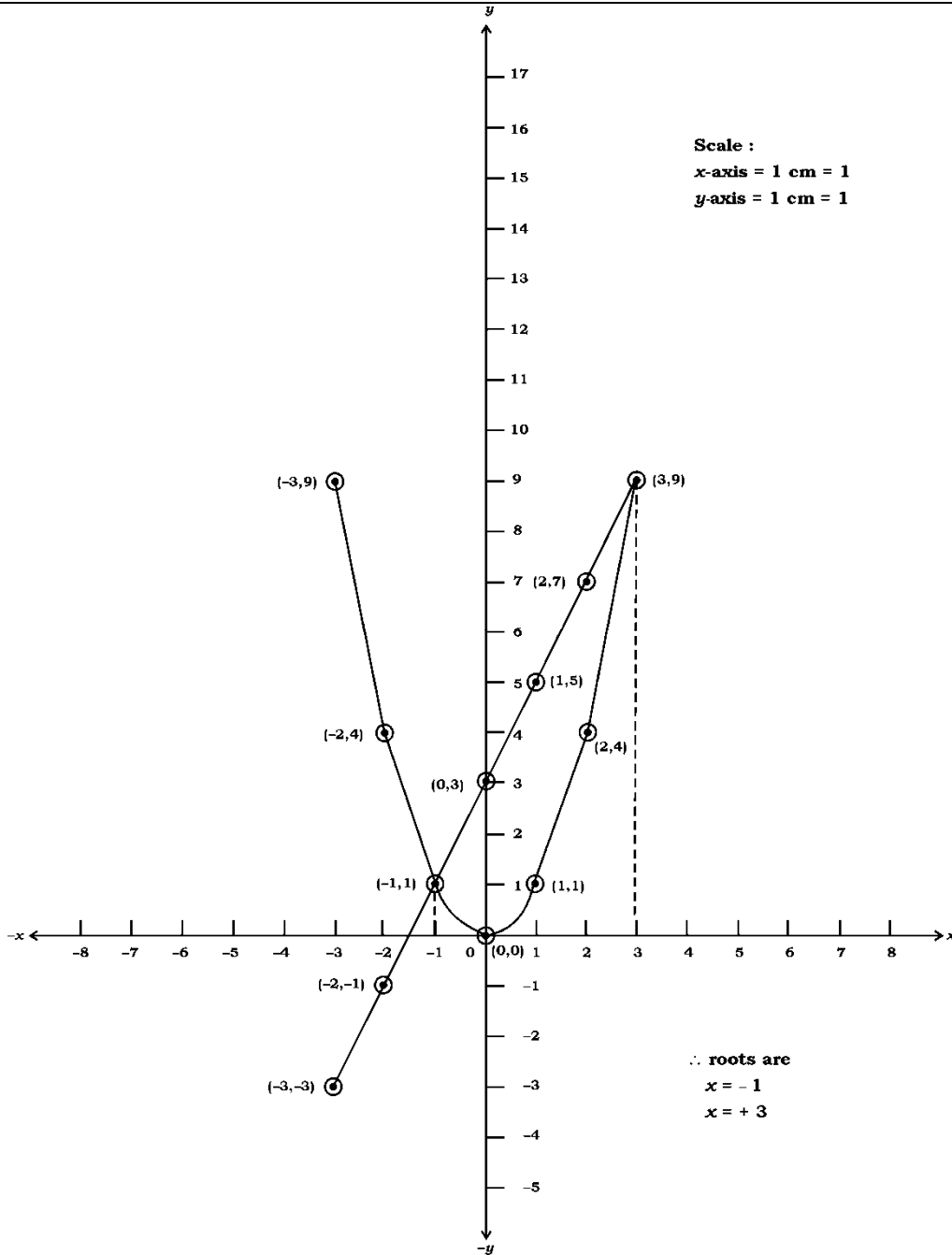
identifying roots 1

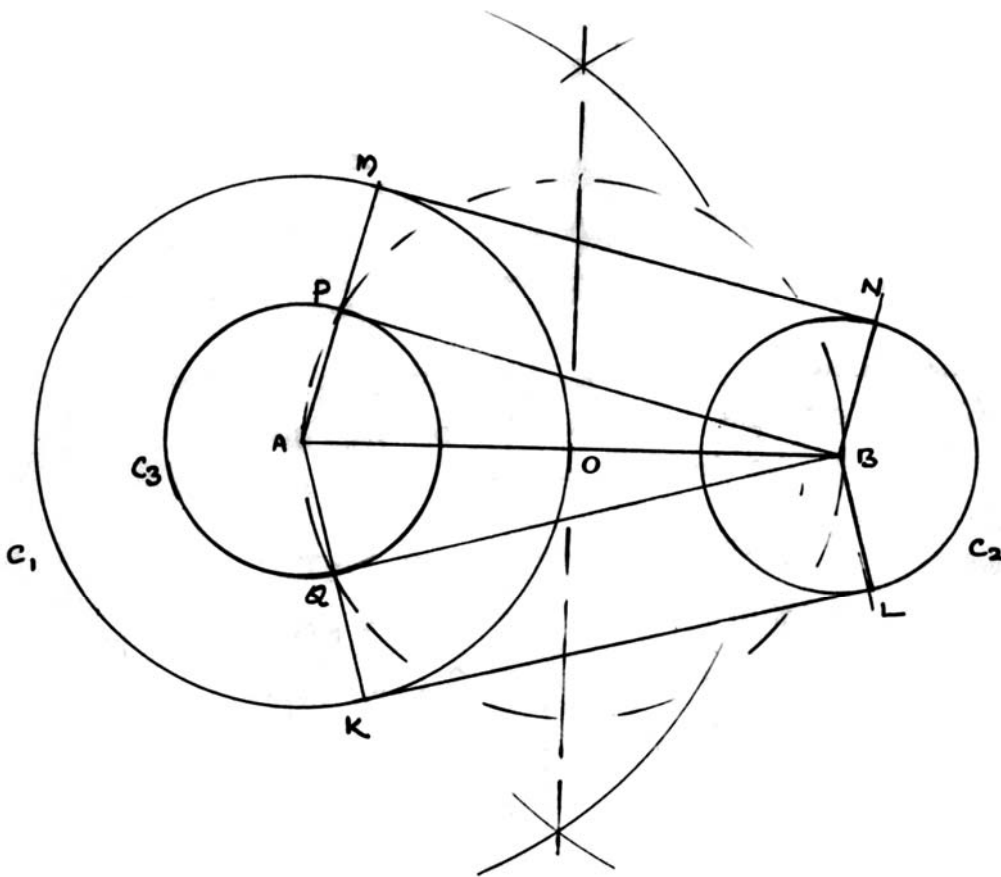
4

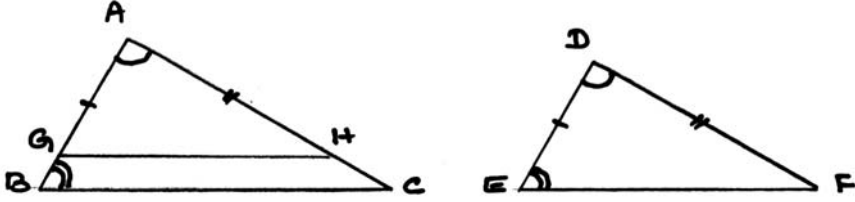


Qn. Nos.	Value Points							Marks allotted																																
	<p><i>Alternate method :</i></p> $x^2 - 2x - 3 = 0$ <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="border: 1px solid black; padding: 2px 10px;">$y = x^2$</div> <div style="border: 1px solid black; padding: 2px 10px;">$y = +2x + 3$</div> </div> <p>$y = x^2$</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td> <td>-3</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> </tr> <tr> <td>y</td> <td>9</td> <td>4</td> <td>1</td> <td>0</td> <td>1</td> <td>4</td> <td>9</td> </tr> </table> <p>$y = 2x + 3$</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td> <td>-3</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> </tr> <tr> <td>y</td> <td>-3</td> <td>-1</td> <td>1</td> <td>3</td> <td>5</td> <td>7</td> <td>9</td> </tr> </table> <div style="text-align: right; margin-top: 20px;"> <p>Table — 2</p> <p>Drawing parabola — 1</p> <p>Identifying roots — 1</p> </div>							x	-3	-2	-1	0	1	2	3	y	9	4	1	0	1	4	9	x	-3	-2	-1	0	1	2	3	y	-3	-1	1	3	5	7	9	4
x	-3	-2	-1	0	1	2	3																																	
y	9	4	1	0	1	4	9																																	
x	-3	-2	-1	0	1	2	3																																	
y	-3	-1	1	3	5	7	9																																	

Qn. Nos.	Value Points	Marks allotted
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Qn. Nos.	Value Points	Marks allotted
39.	<p> $d = 8 \text{ cm}$ $R = 4 \text{ cm}$ $r = 2 \text{ cm}$ $R - r = 4 - 2 = 2 \text{ cm}$ </p>  <p style="text-align: right;"> Length of the tangent $KL = MN = 7.8 \text{ cm}$ </p> <p style="text-align: right;"> Drawing AB and marking mid-point 1 Drawing circles C_1, C_2, C_3 $1 \frac{1}{2}$ 4 Joining BP, BQ, MN, KL 1 Measuring and writing the length of tangents $\frac{1}{2}$ </p>	

Qn. Nos.	Value Points	Marks allotted																																	
40.	<div style="text-align: center;">  </div> <p>Data : In $\triangle ABC$ and $\triangle DEF$</p> $\hat{BAC} = \hat{EDF}, \hat{ABC} = \hat{DEF}$ <p>To prove : $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$</p> <p>Construction : Points G and H are marked on AB and AC such that $AG = DE$ and $AH = DF$. G and H joined.</p> <p>Proof : In $\triangle AGH$ and $\triangle DEF$</p> <table style="width: 100%; border: none;"> <tr> <td style="width: 30%;">$AG = DE$</td> <td style="width: 40%;">construction</td> <td style="width: 30%;"></td> </tr> <tr> <td>$\hat{GAH} = \hat{EDF}$</td> <td>data</td> <td></td> </tr> <tr> <td>$AH = DF$</td> <td>construction</td> <td style="text-align: right;">1/2</td> </tr> <tr> <td>$\therefore \triangle AGH \cong \triangle DEF$</td> <td>SAS postulate</td> <td></td> </tr> <tr> <td>$\therefore GH = EF$</td> <td rowspan="2">} CPCT</td> <td rowspan="2" style="text-align: right;">1/2</td> </tr> <tr> <td>$\hat{AGH} = \hat{DEF}$</td> </tr> <tr> <td>but $\hat{DEF} = \hat{ABC}$</td> <td>data</td> <td></td> </tr> <tr> <td>$\therefore \hat{AGH} = \hat{ABC}$</td> <td>alternate angles</td> <td></td> </tr> <tr> <td>$\therefore GH \parallel BC$</td> <td></td> <td style="text-align: right;">1/2</td> </tr> <tr> <td>$\therefore \frac{AB}{AG} = \frac{BC}{GH} = \frac{AC}{AH}$</td> <td>cor. BPT</td> <td></td> </tr> <tr> <td>but $AG = DE, GH = EF, AH = DF$</td> <td></td> <td></td> </tr> <tr> <td>$\therefore \frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$</td> <td></td> <td style="text-align: right;">1/2</td> </tr> </table>	$AG = DE$	construction		$\hat{GAH} = \hat{EDF}$	data		$AH = DF$	construction	1/2	$\therefore \triangle AGH \cong \triangle DEF$	SAS postulate		$\therefore GH = EF$	} CPCT	1/2	$\hat{AGH} = \hat{DEF}$	but $\hat{DEF} = \hat{ABC}$	data		$\therefore \hat{AGH} = \hat{ABC}$	alternate angles		$\therefore GH \parallel BC$		1/2	$\therefore \frac{AB}{AG} = \frac{BC}{GH} = \frac{AC}{AH}$	cor. BPT		but $AG = DE, GH = EF, AH = DF$			$\therefore \frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$		1/2
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