

THIRUVANANTHAPURAM EDUCATIONAL DISTRICT

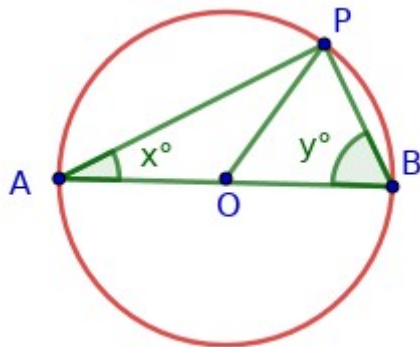
WS 2.1

MATHEMATICS

STANDARD:10

CIRCLES

1.A) In the figure AB is the diameter of the circle with centre O. P is a point on the circle. The end points of the diameter are joined to the point P .



In  $\triangle OAP$ ,

OA = \_\_\_\_\_ (Reason \_\_\_\_\_)

If  $\angle OAP = x^\circ$  Then  $\angle OPA =$  \_\_\_\_\_ (Reason \_\_\_\_\_)

In  $\triangle BOP$

OB = \_\_\_\_\_ (Reason \_\_\_\_\_)

If  $\angle OBP = y^\circ$  Then  $\angle OPB =$  \_\_\_\_\_ (Reason \_\_\_\_\_)

In  $\triangle APB$ ,

$\angle A =$  \_\_\_\_\_

$\angle B =$  \_\_\_\_\_

$\angle P = \angle APO + \angle BPO =$  \_\_\_\_\_ + \_\_\_\_\_

$\angle A + \angle B + \angle P = 180^\circ$

\_\_\_\_\_ + \_\_\_\_\_ +  $x^\circ + y^\circ = 180^\circ$

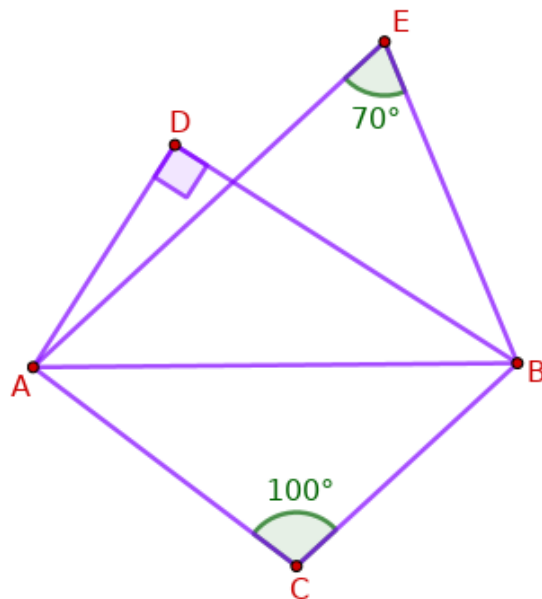
$2(\text{_____} + \text{_____}) = 180^\circ$

$x^\circ + y^\circ = \frac{180}{2} =$  \_\_\_\_\_

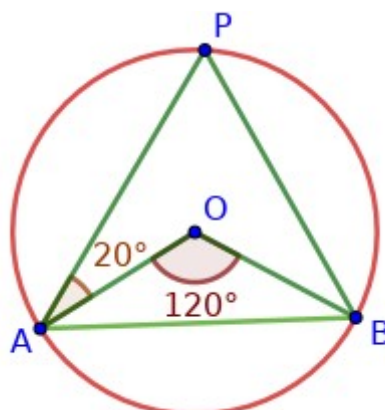
**B) In the table below fill in the blanks using the above figure**

$\angle AOP$	$\angle BOP = 180^\circ - \angle AOP$	$x^\circ = \frac{180 - \angle AOP}{2}$	$y^\circ = \frac{180 - \angle BOP}{2}$	$\angle P = x^\circ + y^\circ$
70	110	$\frac{180 - 70}{2} = 55^\circ$	$\frac{180 - 110}{2} = 35^\circ$	$55 + 35 = 90^\circ$
	80			
		30		
			45	
50				

**2. A circle is drawn with AB as diameter. Find the position of the points C, D, E related to the circle ( inside, outside or on the circle)**

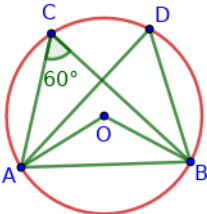
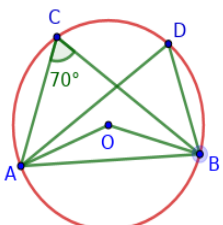


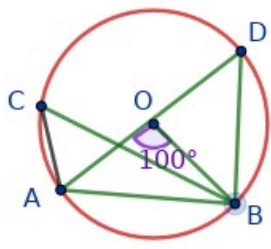
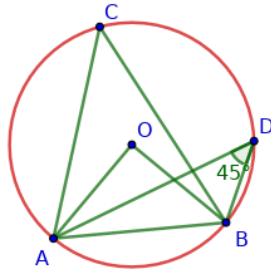
**3. In the figure O is the centre of the circle and A, B, P are points on the circle  $\angle AOB = 120^\circ$ ,  $\angle OAP = 20^\circ$ . Find all angles of  $\triangle ABP$**



Given  $\angle AOB = 120^\circ$   
 Therefore  $\angle p = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$   
 Join OP . Consider  $\triangle AOP$   
 $OA = \underline{\hspace{2cm}}$  (Reason)  
 $\triangle AOP$  is  $\underline{\hspace{2cm}}$   
 Given  $\angle OAP = 20^\circ$   
 Therefore  $\angle OPA = \underline{\hspace{2cm}}$   
 $\angle AOP = 180 - (\underline{\hspace{1cm}} + \underline{\hspace{1cm}}) = \underline{\hspace{2cm}}$   
 Therefore  $\angle B = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$   
 Consider  $\triangle BOP$   
 $\angle BOP = 360 - (\underline{\hspace{1cm}} + \underline{\hspace{1cm}})$   
 $= \underline{\hspace{2cm}}$   
 Therefore  $\angle A = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$

**4. O is the centre of the circle and A, B, C, D are points on it. Find the measures of the angles below.**

Circle	$\angle ACB$	$\angle ADB$	$\angle AOB$	$\angle OAB = \angle OBA$
	$60^\circ$	$60^\circ$	$2 \times 60^\circ = 120^\circ$	$\frac{180 - 120}{2} = 30^\circ$
	70			

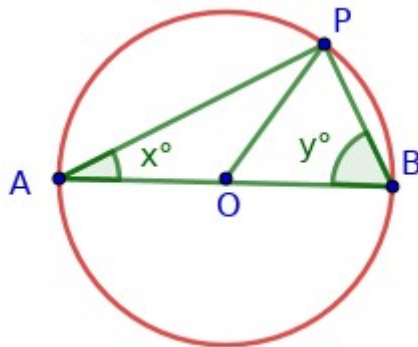
			100	
		45		

Prepared by Team Maths , Thiruvananthapuram Educational District

THIRUVANANTHAPURAM EDUCATIONAL DISTRICT

CIRCLES ( ANSWERS )

**1.A) In the figure AB is the diameter of the circle with centre O. P is a point on the circle. The end points of the diameter are joined to the point P .**



In  $\triangle OAP$ ,

$$OA = OP \text{ (Radius)}$$

$$\text{If } \angle OAP = x^\circ \text{ Then } \angle OPA = x^\circ \text{ (Isosceles triangle)}$$

In  $\triangle BOP$

$$OB = OP \text{ (Radius)}$$

$$\text{If } \angle OBP = y^\circ \text{ Then } \angle OPB = y^\circ \text{ (Isosceles triangle)}$$

In  $\triangle APB$ ,

$$\angle A = x^\circ$$

$$\angle B = y^\circ$$

$$\angle P = \angle APO + \angle BPO = x^\circ + y^\circ$$

$$\angle A + \angle B + \angle P = 180^\circ$$

$$x^\circ + y^\circ + x^\circ + y^\circ = 180^\circ$$

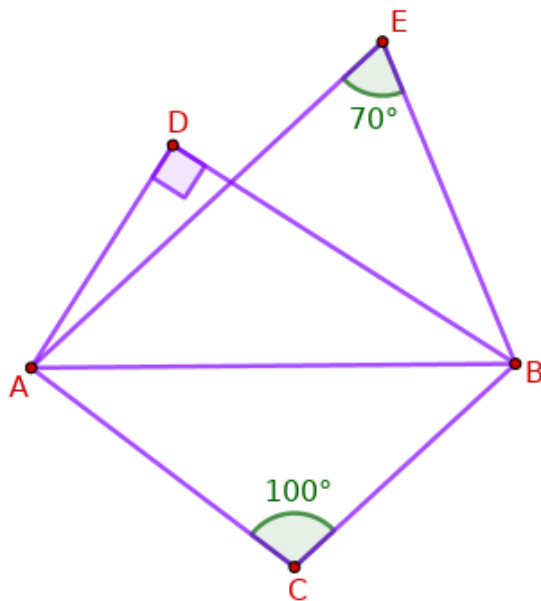
$$2(x^\circ + y^\circ) = 180^\circ$$

$$x^\circ + y^\circ = \frac{180}{2} = 90^\circ$$

**B) In the table below fill in the blanks using the above figure**

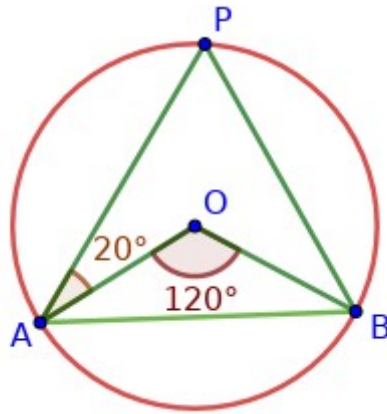
$\angle AOP$	$\angle BOP = 180^\circ - \angle AOP$	$x^\circ = \frac{180 - \angle AOP}{2}$	$y^\circ = \frac{180 - \angle BOP}{2}$	$\angle P = x^\circ + y^\circ$
$70^\circ$	$110^\circ$	$\frac{180 - 70}{2} = 55^\circ$	$\frac{180 - 110}{2} = 35^\circ$	$55^\circ + 35^\circ = 90^\circ$
$100^\circ$	$80^\circ$	$\frac{180 - 100}{2} = 40^\circ$	$\frac{180 - 80}{2} = 50^\circ$	$40^\circ + 50^\circ = 90^\circ$
$120^\circ$	$60^\circ$	$30^\circ$	$60^\circ$	$30^\circ + 60^\circ = 90^\circ$
$90^\circ$	$90^\circ$	$45^\circ$	$45^\circ$	$45^\circ + 45^\circ = 90^\circ$
$50^\circ$	$130^\circ$	$65^\circ$	$25^\circ$	$65^\circ + 25^\circ = 90^\circ$

**2. A circle is drawn with AB as diameter. Find the position of the points C, D, E related to the circle ( inside, outside or on the circle)**



- $\angle D = 90^\circ$  , The point D is on the circle.
- $\angle E = 70^\circ < 90^\circ$  , The point E is outside the circle.
- $\angle C = 100^\circ > 90^\circ$  , The point C is inside the circle.

**3. In the figure O is the centre of the circle and A, B, P are points on the circle  $\angle AOB = 120^\circ$ ,  $\angle OAP = 20^\circ$ . Find all angles of  $\triangle ABP$ .**



Given  $\angle AOB = 120^\circ$

Therefore  $\angle P = \frac{120}{2} = \underline{60^\circ}$

Join OP . Consider  $\triangle AOP$

OA = OB (Radius)

$\triangle AOP$  is isosceles triangle

Given  $\angle OAP = 20^\circ$

Therefore  $\angle OPA = \underline{20^\circ}$

$\angle AOP = 180^\circ - (20^\circ + 20^\circ) = 180^\circ - 40^\circ = 140^\circ$

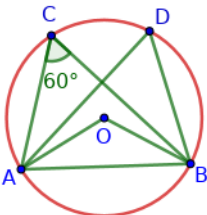
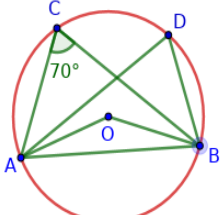
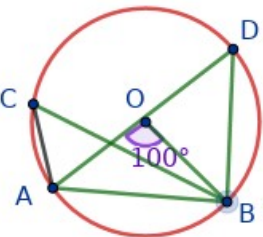
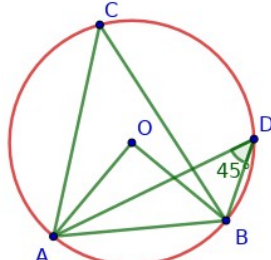
Therefore  $\angle B = \frac{140}{2} = \underline{70^\circ}$

Consider  $\triangle BOP$

$\angle BOP = 360^\circ - (\underline{120^\circ + 140^\circ}) = 360^\circ - 260^\circ$   
 $= \underline{100^\circ}$

Therefore  $\angle A = \frac{100}{2} = \underline{50^\circ}$

**4. O is the centre of the circle and A, B, C, D are points on it. Find the measures of the angles below.**

Circle	$\angle ACB$	$\angle ADB$	$\angle AOB$	$\angle OAB = \angle OBA$
	$60^\circ$	$60^\circ$	$2 \times 60^\circ = 120^\circ$	$\frac{180 - 120}{2} = 30^\circ$
	70	$70^\circ$	$2 \times 70^\circ = 140^\circ$	$\frac{180 - 140}{2} = 20^\circ$
	$50^\circ$	$50^\circ$	100	$\frac{180 - 100}{2} = 40^\circ$
	$45^\circ$	45	$2 \times 45^\circ = 90^\circ$	$\frac{180 - 90}{2} = 45^\circ$