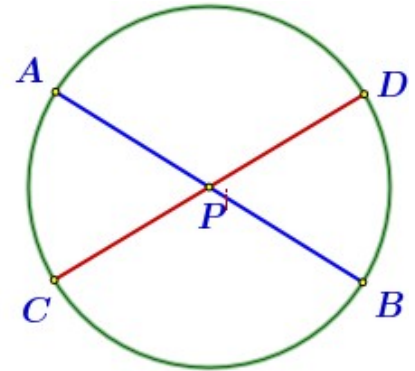


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Two intersecting chords

We know that diameter is the longest chord of a circle and two diameters intersect at the centre .

Do the lengths of the four pieces of the intersecting diameters have any peculiarity ?

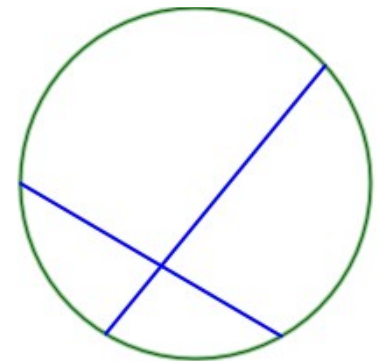


In the figure two diameters AB and CD of a circle intersect at the point P within the circle (P is the centre)

$$PA = PB = PC = PD \quad (\text{Radii of a circle are equal})$$

Do the length of the four parts of the intersecting chords within a circle (which are not the diameters) have any peculiarity ?

Are they equal ?



It is very clear from the figure that they are not equal .

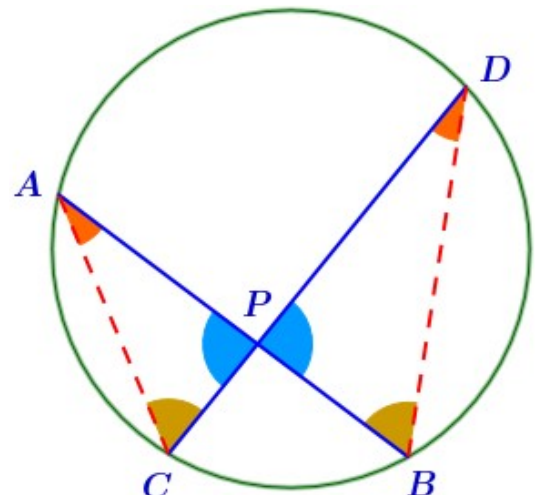
Let's discuss.

In the figure two chords AB and CD intersect at the point P .

$$\angle A = \angle D \quad (\text{All angles made by an arc on its alternate arc are equal})$$

$$\angle B = \angle C \quad (\text{All angles made by an arc on its alternate arc are equal})$$

$$\angle APC = \angle BPD \quad (\text{Opposite angles are equal})$$



Triangles APC and BPD are similar triangles . (The angles of the triangles APC are BPD equal)

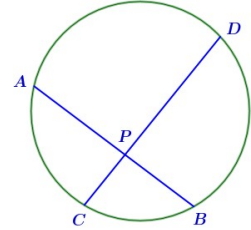
$$\frac{PA}{PD} = \frac{PC}{PB}$$

(The sides of similar triangles are scaled by the same factor)

$$PA \times PB = PC \times PD$$

In the figure two chords AB and CD of a circle intersect at the a point P within the circle , then

$$PA \times PB = PC \times PD$$



Finding

If two chords of a circle intersect within the circle , then the product of the parts of the two chords are equal .

Let's solve a problem related to this idea

1. In the figure two chords AB and CD intersect at a point P .

$$PB = 2 \text{ cm} \quad PC = 3 \text{ cm} , PD = 4 \text{ cm}$$

What is the length of AB ?

Answer.

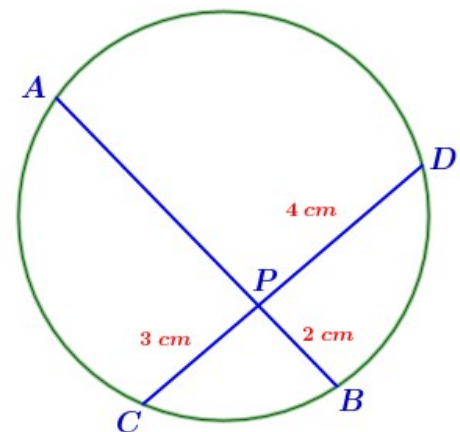
$$PA \times PB = PC \times PD$$

$$PA \times 2 = 3 \times 4$$

$$PA \times 2 = 12$$

$$PA = \frac{12}{2} = 6$$

$$AB = PA + PB = 6 + 2 = 8 \text{ cm}$$



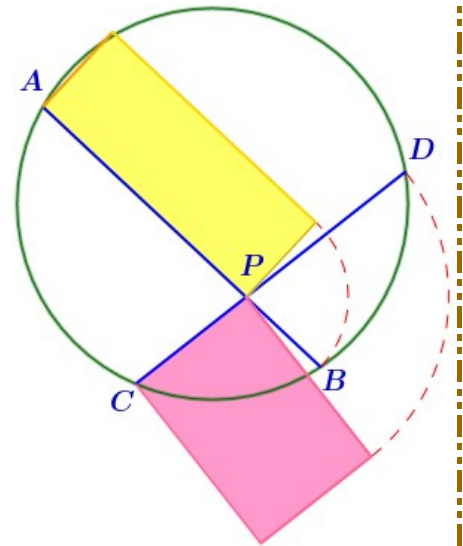
Geometrical interpretation

In the figure two chords AB and CD of a circle intersect at a point P within the circle , then

$$PA \times PB = PC \times PD$$

Area of the rectangle with sides PA and $PB = PA \times PB$

Area of the rectangle with sides PC and $PD = PC \times PD$

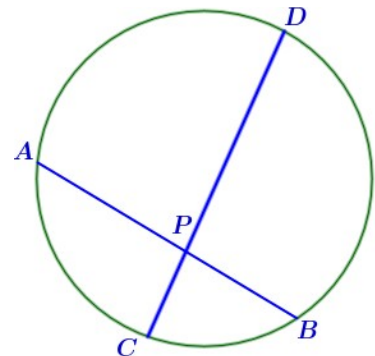


If two chords of a circle intersect within a circle, then the rectangles formed by the parts of the same chord have equal area .

More activity

In the figure two chords AB and CD of a circle intersect at a point P . $PA = 9 \text{ cm}$, $PD = 12 \text{ cm}$ and $AB = 13 \text{ cm}$

Find the lengths of PB , PC and CD ?



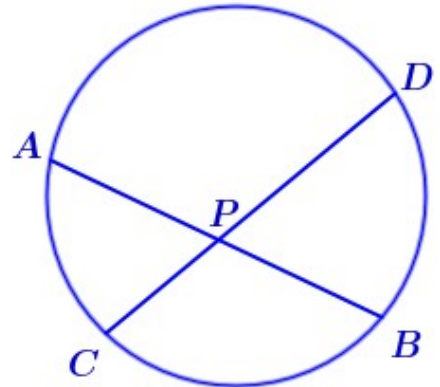
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WORKSHEET

1. In the figure two chords AB and CD intersect at P

$PA = 9 \text{ cm}$, $AB = 17 \text{ cm}$. The length of PD is twice as that of PC .

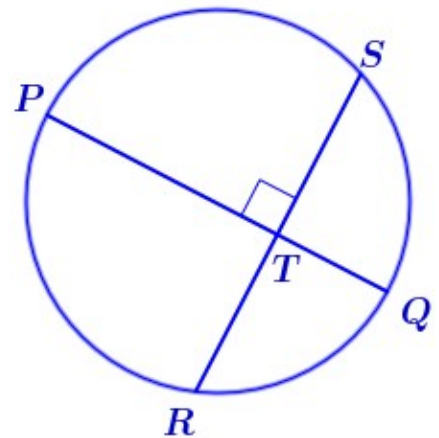
- What is the length of PB ?
- What is the length of PC ?
- What is the length of CD ?



2. In the figure PQ is the diameter of the circle and

$\angle PTS = 90^\circ$ $PQ = 13 \text{ cm}$, $TQ = 4 \text{ cm}$

- What is the length of TP ?
- What is the length of TR ?
- What is the length of RS ?

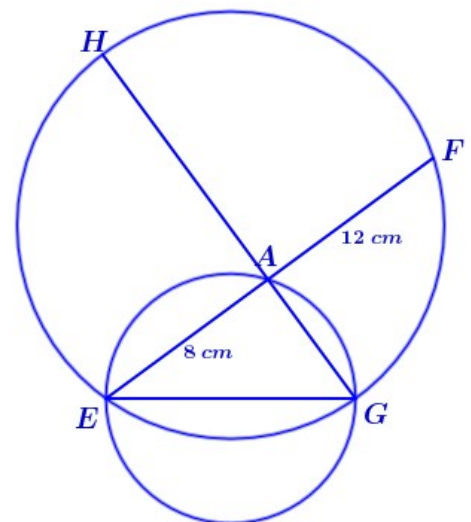


3. In the figure two chords EF and GH of the larger circle intersect at a point A on the smaller circle .

EG is the diameter of the smaller circle .

$AE = 8 \text{ cm}$, $AF = 12 \text{ cm}$ and the perimeter of the smaller circle is $10\pi \text{ cm}$.

- What is the length of EG ?
- What is the measure of $\angle EAG$?
- What is the length of AG ?
- What is the length of AH ?



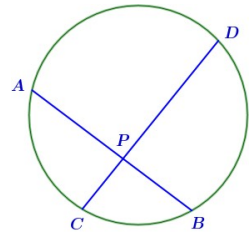
4. Draw a rectangle of length 5 cm and width 2 cm . Draw another rectangle of the same area with one side 7 cm ?

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What did we learn in the last class ?

In the figure two chords AB and CD of a circle intersect at the a point P within the circle , then

$$PA \times PB = PC \times PD$$



If two chords of a circle intersect within the circle , then the product of the parts of the two chords are equal .

Geometrical interpretation

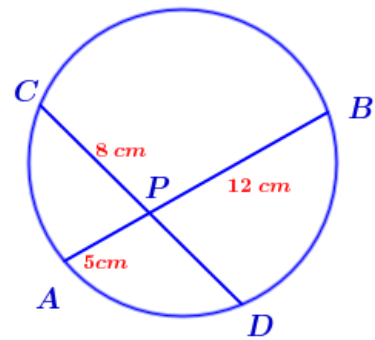
If two chords of a circle intersect within a circle, then the rectangles formed by the parts of the same chord have equal area .

Let's solve some problems related to this idea

2. In the figure two chords AB and CD of a circle intersect at a point P .

$$PA = 5 \text{ cm} , PB = 12 \text{ cm} , PC = 8 \text{ cm}$$

What is the length of PD ?



Answer

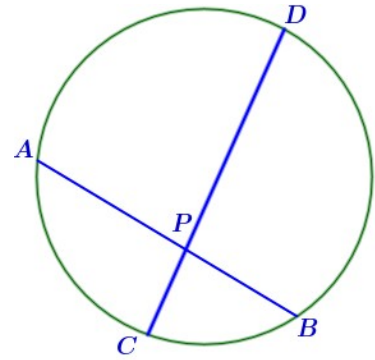
$$PA \times PB = PC \times PD$$

$$5 \times 12 = 8 \times PD$$

$$8 \times PD = 60$$

$$PD = \frac{60}{8} = 7.5 \text{ cm}$$

2. In the figure two chords AB and CD of a circle intersect at a point P . $PA = 9$ cm, $PD = 12$ cm and $AB = 13$ cm. Find the lengths of PB , PC and CD ?



Answer

$$PB = AB - PA = 13 - 9 = 4 \text{ cm}$$

$$PA \times PB = PC \times PD$$

$$9 \times 4 = PC \times 12$$

$$PC \times 12 = 36$$

$$PC = \frac{36}{12} = 3 \text{ cm}$$

$$CD = PC + PD = 3 + 12 = 15 \text{ cm}$$

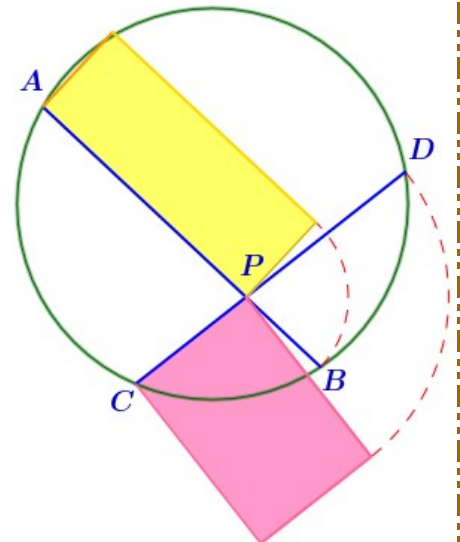
Let's discuss a construction base on this idea

In the figure two chords AB and CD of a circle intersect at a point P within the circle, then

$$PA \times PB = PC \times PD$$

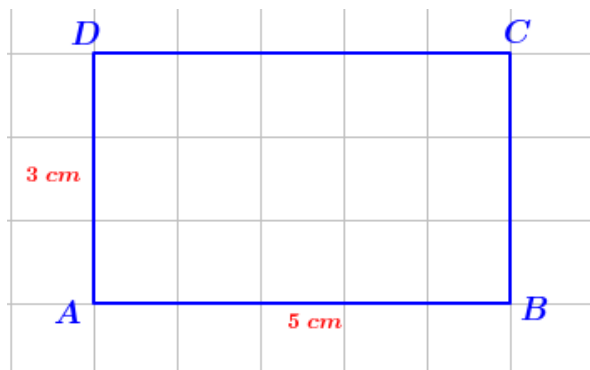
Area of the rectangle with sides PA and $PB = PA \times PB$

Area of the rectangle with sides PC and $PD = PC \times PD$

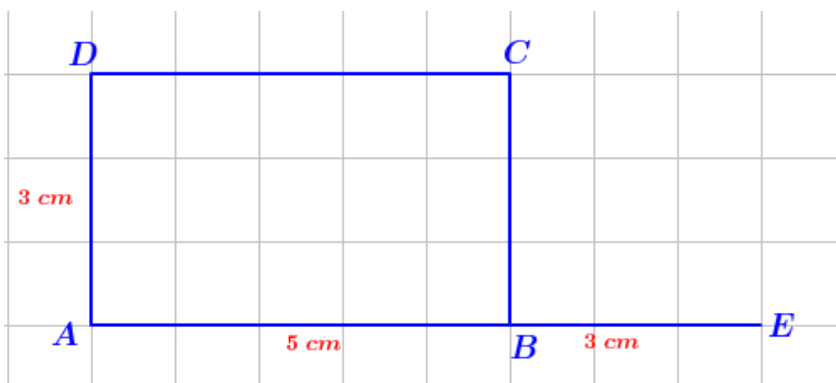


- Draw a rectangle of length 5 cm and width 3 cm. Draw another rectangle of the same area with one side 6 cm ?

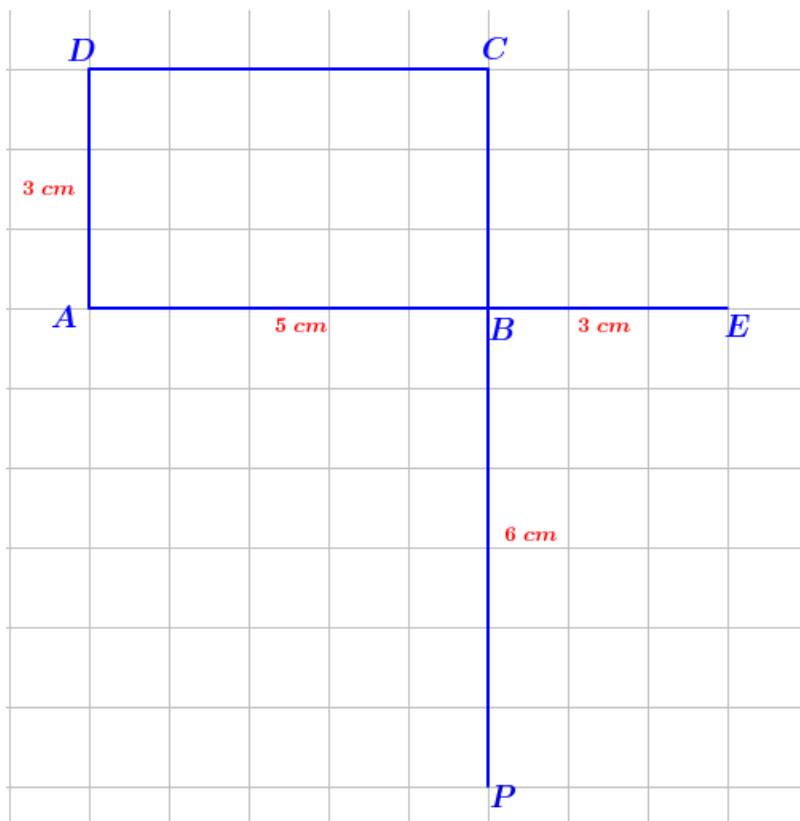
Step 1 : Draw a rectangle of width 5 cm and height 3 cm.



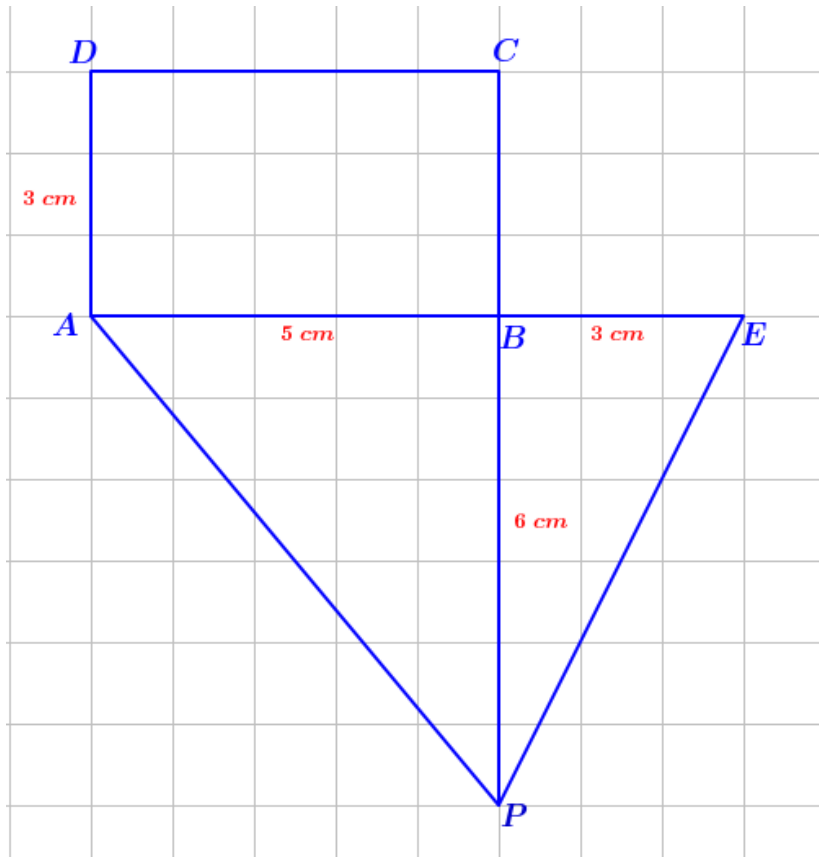
Step 2 : Extend the line AB by 3 cm.



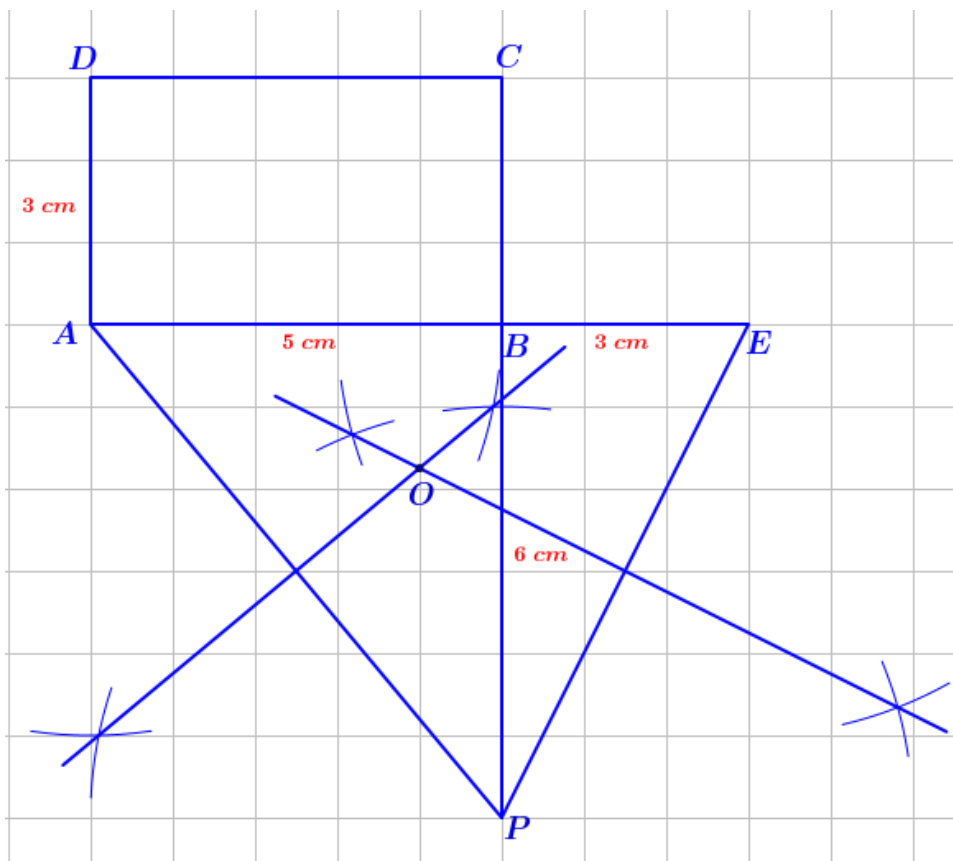
Step 3 : Extend the line CB downwards by 6 cm and mark a point P.



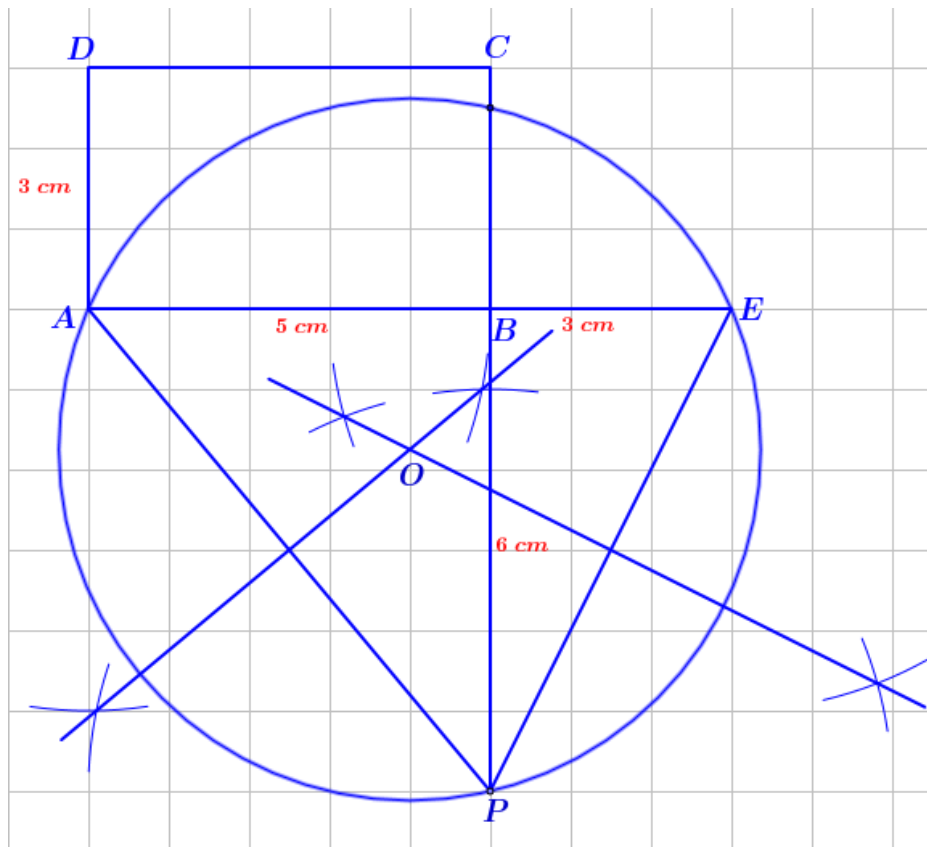
Step 4 : Join the points A, E and P to form a triangle.



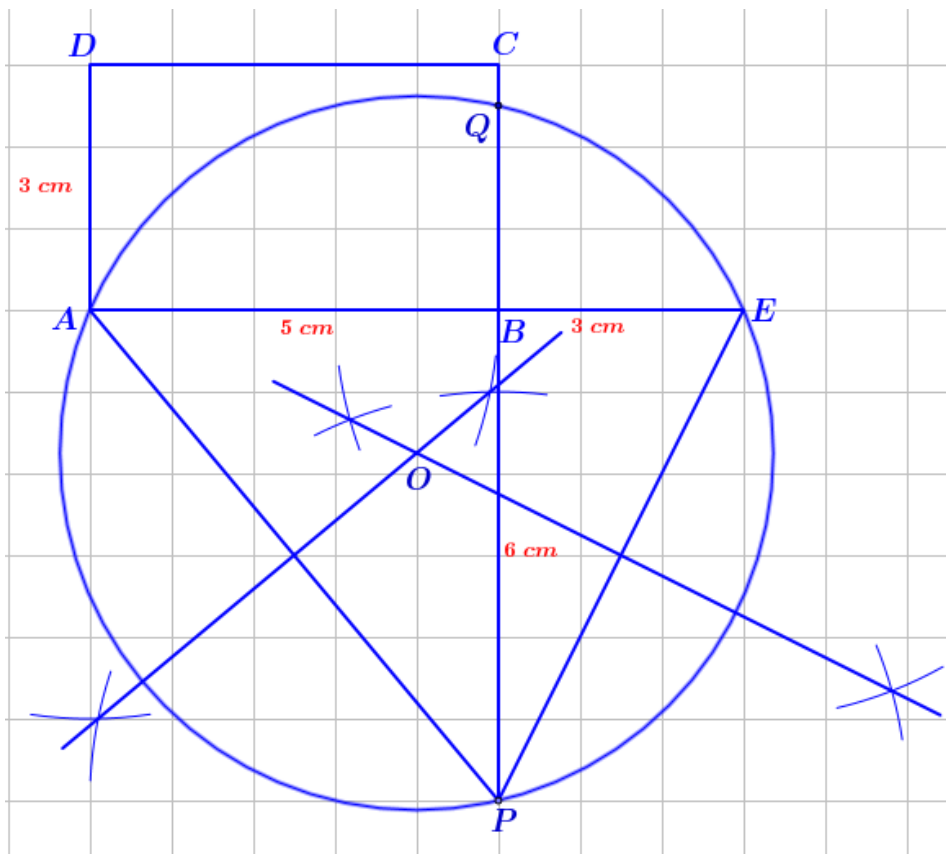
Step 5 : Draw the perpendicular bisectors of the lines AP and EP . They intersect at O .



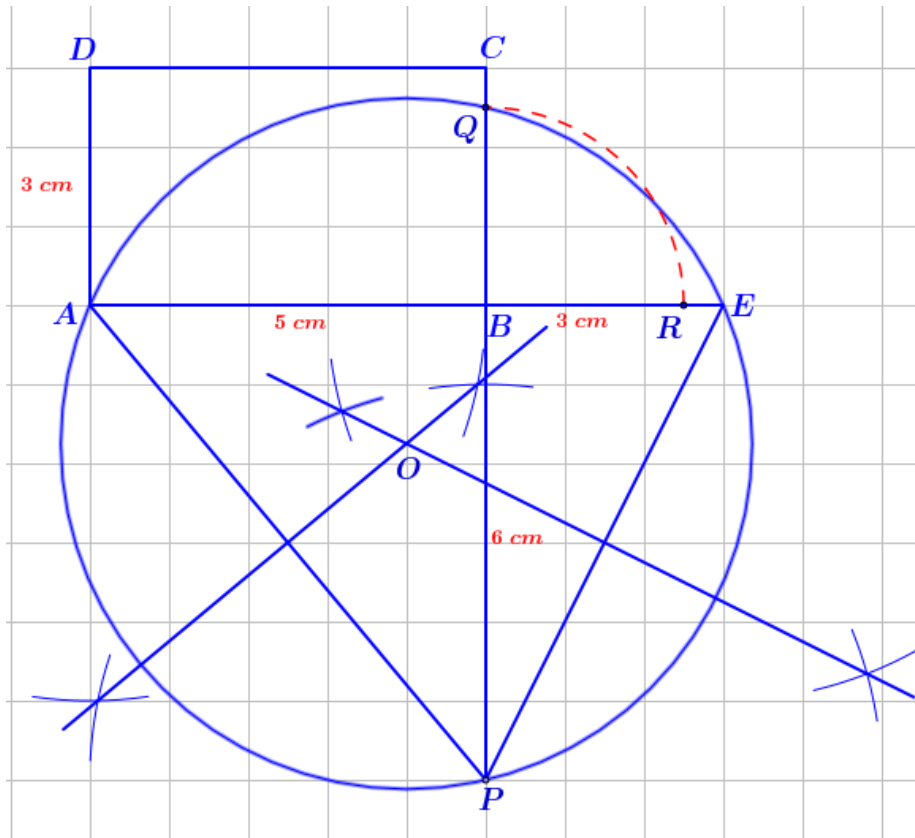
Step 6 : Draw the circumcircle of the triangle AEP . The centre of the circumcircle is O .



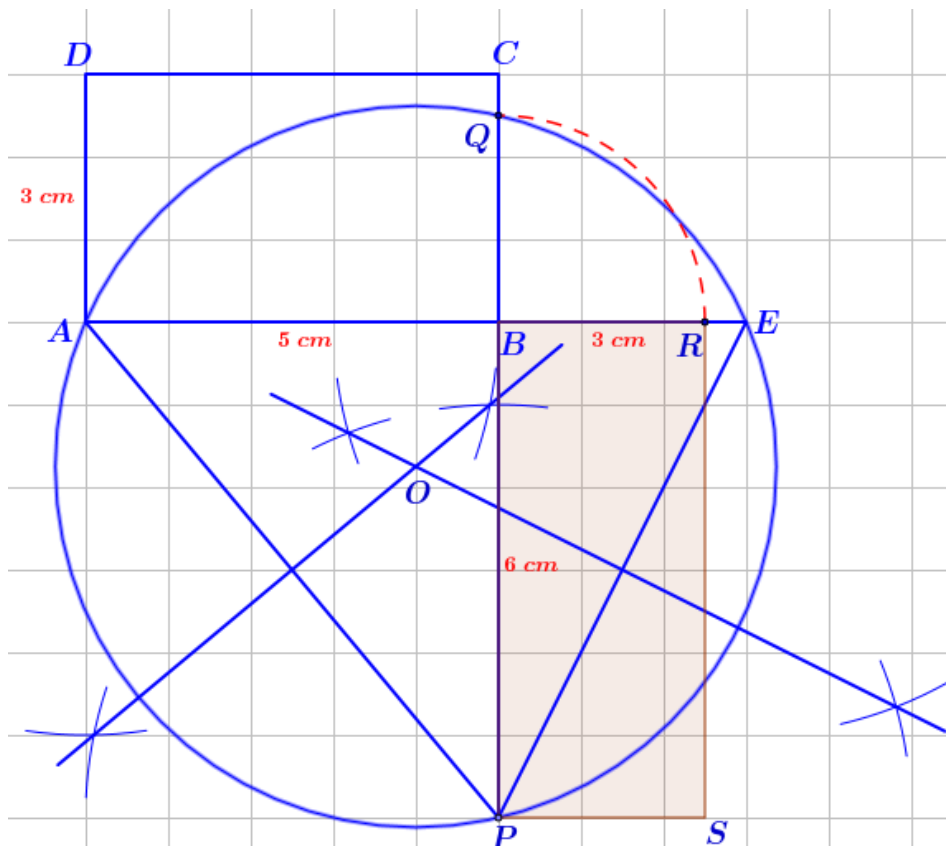
Step 7 : The circumcircle meets the line BC at Q .



Step 8 : Draw an arc with centre B and radius BQ . The arc meets the line BE at R .



Step 9 : Draw a rectangle with width BP and height BR .



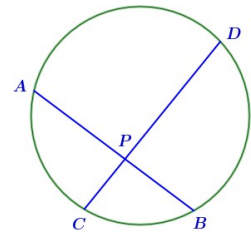
More activity

Draw a rectangle of length 4 cm and width 3 cm. Draw another rectangle of the same area with one side 5 cm ?

ONLINE MATHS CLASS - X - 34 (24 / 09 /2020)

What did we learn in the last class ?

In the figure two chords AB and CD of a circle intersect at the a point P within the circle , then $PA \times PB = PC \times PD$



If two chords of a circle intersect within the circle , then the product of the parts of the two chords are equal .

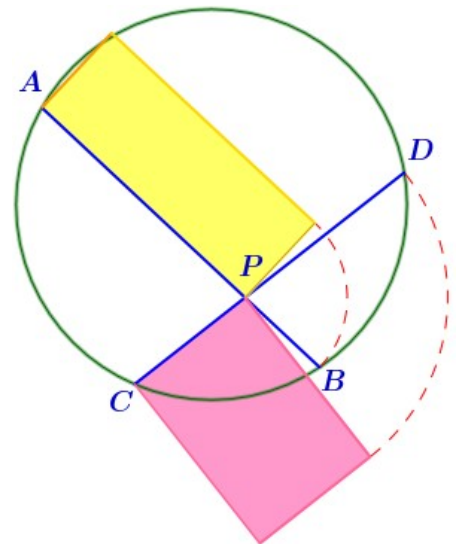
Geometrical interpretation

In the figure two chords AB and CD of a circle intersect at a point P within the circle , then

$$PA \times PB = PC \times PD$$

Area of the rectangle with sides PA and PB = $PA \times PB$

Area of the rectangle with sides PC and PD = $PC \times PD$



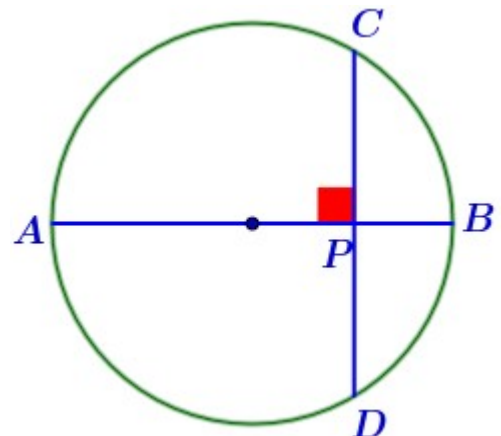
If two chords of a circle intersect within a circle, then the rectangles formed by the parts of the same chord have equal area .

A square with the same area as a rectangle

In the figure AB is the diameter of the circle and CD is a chord perpendicular to it . Then we have

$$PA \times PB = PC \times PD$$

(The perpendicular drawn from the centre of a circle to a chord bisects the chord)



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$PC = PD$ (Perpendicular from the centre of a circle to a chord bisects the chord)

$$PA \times PB = PC \times PD$$

$$= PC \times PC$$

$$= PC^2$$

The product of the parts into which a diameter of a circle is cut by a perpendicular chord, is equal to the square of the half the chord .

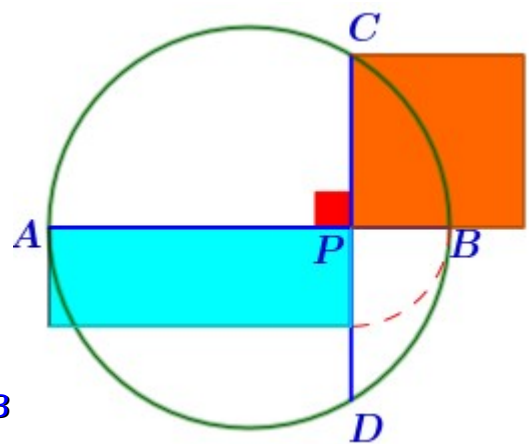
Geometrical interpretation

In the figure AB is the diameter of the circle and CD is a chord perpendicular to it . Then we have ,

$$PA \times PB = PC^2$$

Area of the rectangle with sides PA and PB = $PA \times PB$

Area of the square with side PC = PC^2

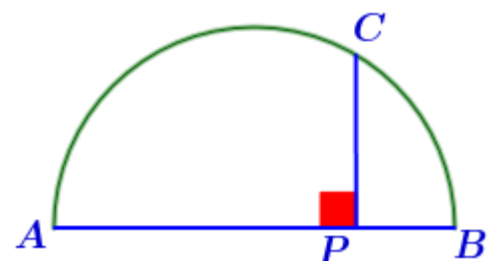


The area of the rectangle formed into which a diameter of a circle is cut by a perpendicular chord is equal to the square of the half the chord .

We can state this result in another way as follows .

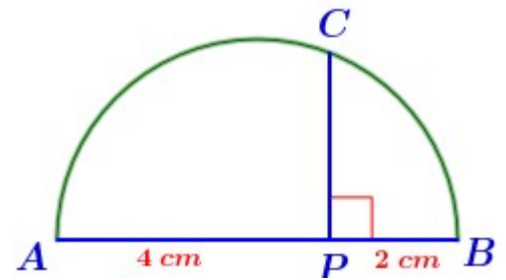
In the figure AB is the diameter of the circle and P is a point on it . The perpendicular to AB drawn through P intersect the circle at C , then

$$PA \times PB = PC^2$$



Let's solve some problems related to this idea

1. In the figure AB is the diameter of the circle and P is a point on it. The perpendicular to AB drawn through P intersect the circle at C . $PA = 4 \text{ cm}$, $PB = 2 \text{ cm}$
What is the length of PC ?



Answer

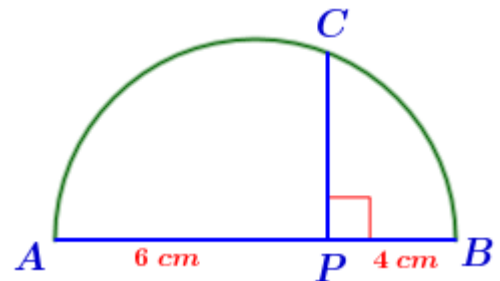
$$PA \times PB = PC^2$$

$$4 \times 2 = PC^2$$

$$PC^2 = 8$$

$$PC = \sqrt{8} = 2\sqrt{2} \text{ cm}$$

2. In the figure AB is the diameter of the circle and P is a point on it. The perpendicular to AB drawn through P intersect the circle at C . $PA = 6 \text{ cm}$, $PB = 4 \text{ cm}$
What is the length of PC ?



Answer

$$PA \times PB = PC^2$$

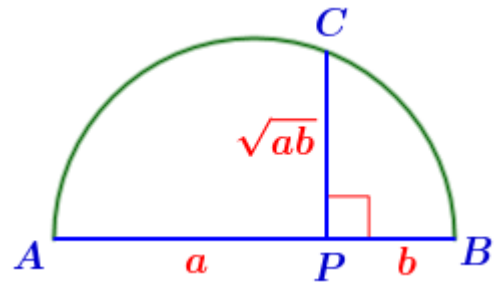
$$6 \times 4 = PC^2$$

$$PC^2 = 24$$

$$PC = \sqrt{24} = 2\sqrt{6} \text{ cm}$$

NB :

In the figure AB is the diameter of the circle and P is a point on it . The perpendicular to AB drawn through P intersect the circle at C . $PA = a$, $PB = b$



$$PA \times PB = PC^2$$

$$a \times b = PC^2$$

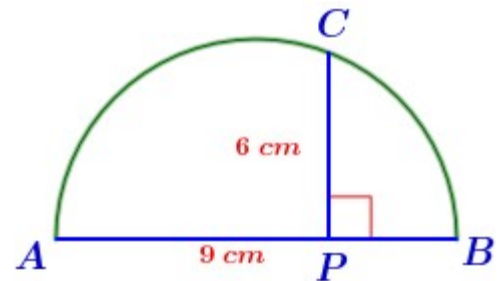
$$PC^2 = ab$$

$$PC = \sqrt{ab}$$

Thus we can use this method to draw some lines of irrational lengths .

(example : $\sqrt{5}$, $\sqrt{7}$, $\sqrt{8}$,)

3 . In the figure AB is the diameter of the circle and P is a point on it . The perpendicular to AB drawn through P intersect the circle at C . $PA = 9$ cm , $PC = 6$ cm



What is the length of PB ?

Answer

$$PA \times PB = PC^2$$

$$9 \times PB = 6^2$$

$$9 \times PB = 36$$

$$PB = \frac{36}{9} = 4 \text{ cm}$$

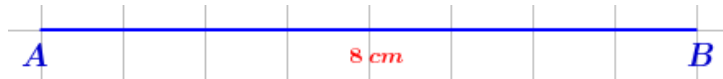
Constructions

4. Draw a line of length $\sqrt{12}$ cm

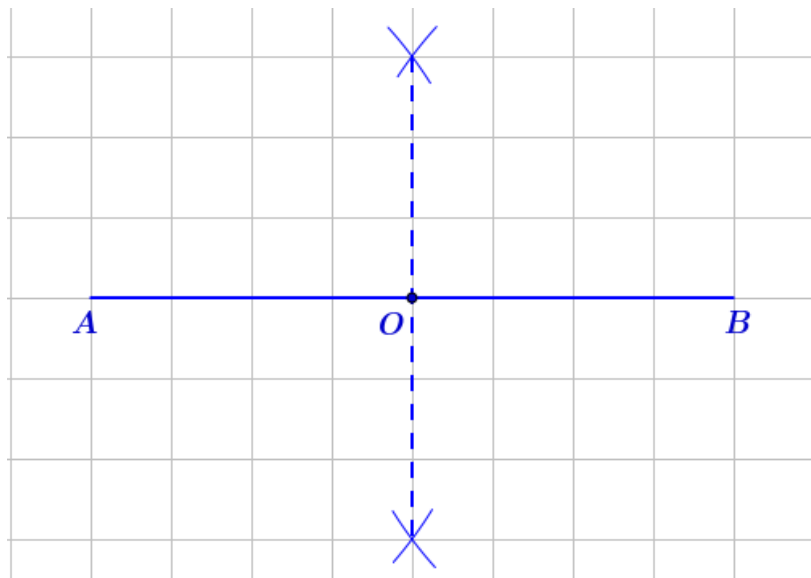
Answer

$$(PA \times PB = PC^2 \implies 6 \times 2 = 12 = (\sqrt{12})^2)$$

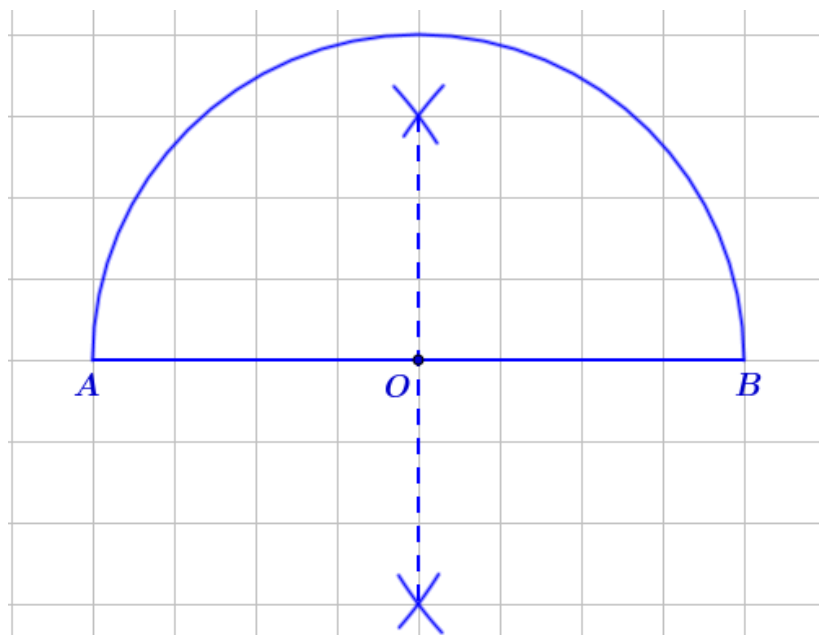
Step 1 : Draw a line AB of length 8 cm .



Step 2 : Mark the midpoint (O) of the line AB .

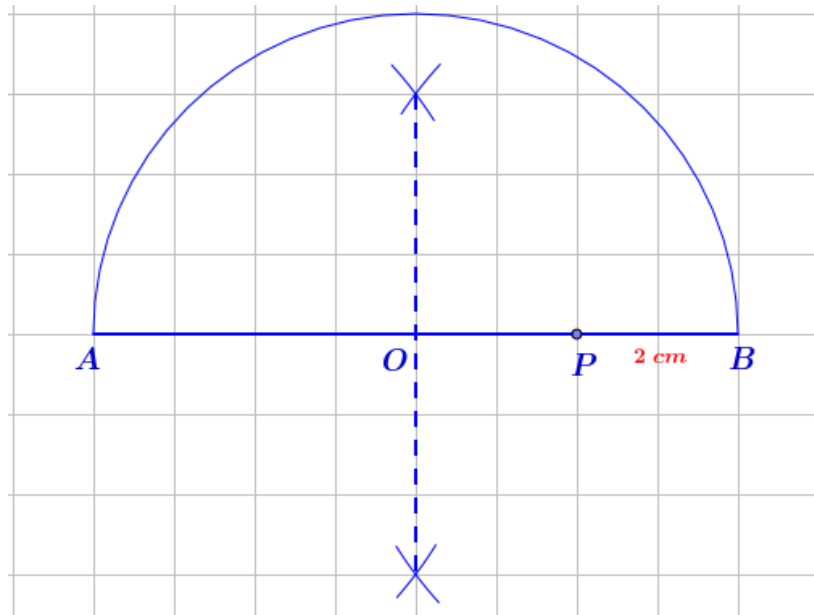


Step 3 : Draw a semicircle with AB as diameter .

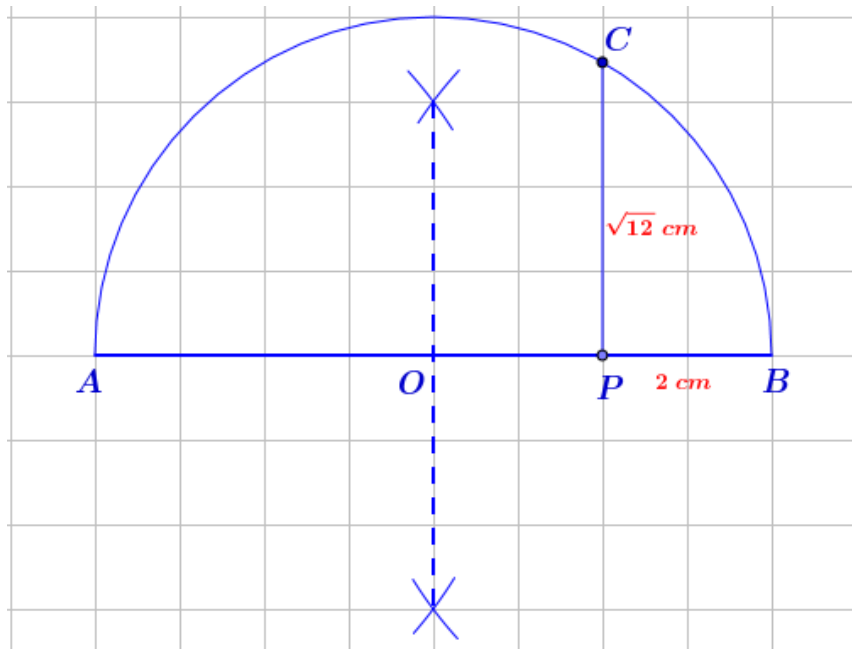


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Step 4 : Mark a point P on AB 6 cm away from A .



Step 5 : The perpendicular to AB drawn through P intersect the circle at C . Draw the line CP

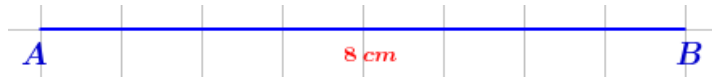


5) Draw a square of area 15 cm^2

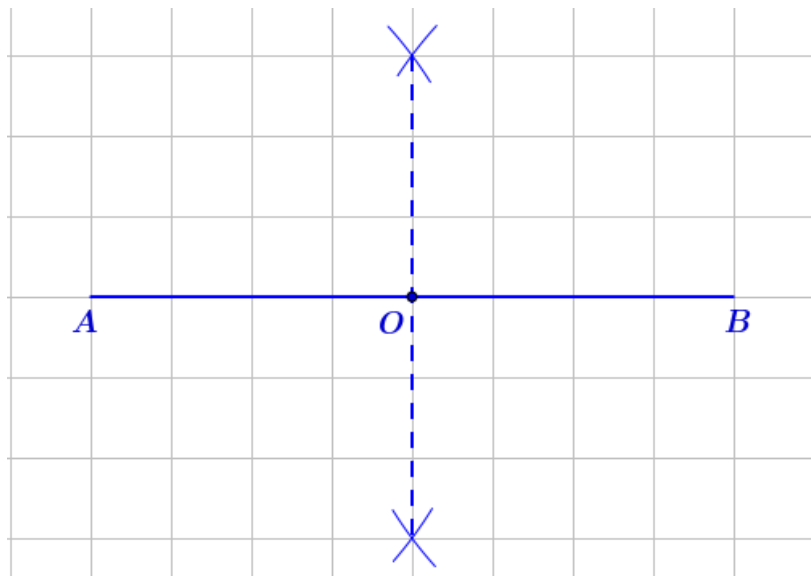
$$\text{Area} = 15 \text{ cm}^2 \implies \text{A side} = \sqrt{15} \text{ cm}$$

$$(PA \times PB = PC^2 \implies 5 \times 3 = 15 = (\sqrt{15})^2)$$

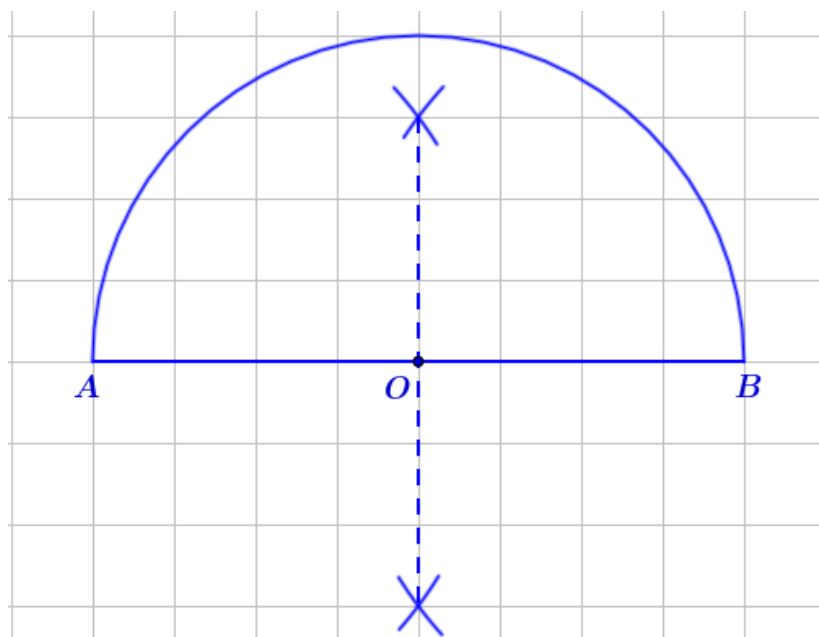
Step 1 : Draw a line AB of length 8 cm .



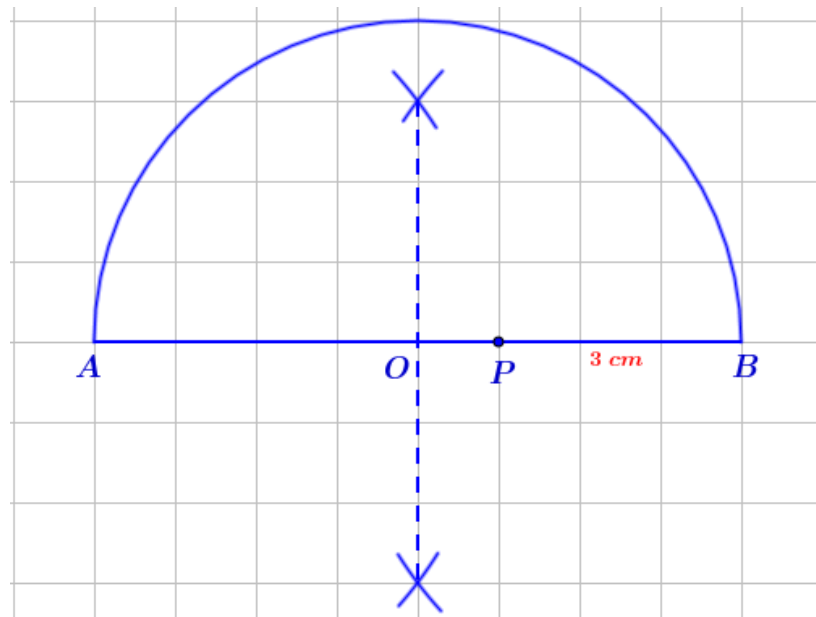
Step 2 : Mark the midpoint (O) of the line AB .



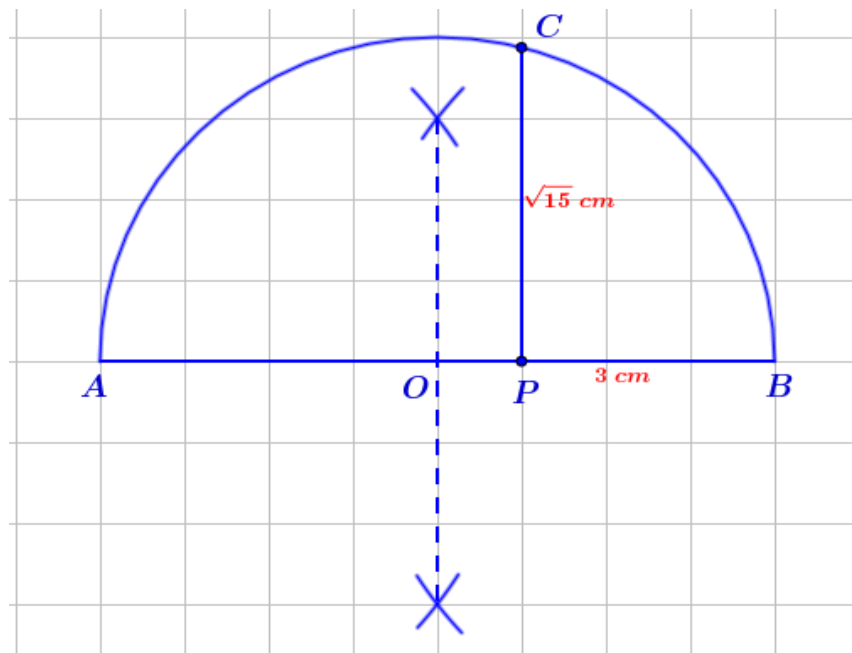
Step 3 : Draw a semicircle with AB as diameter .



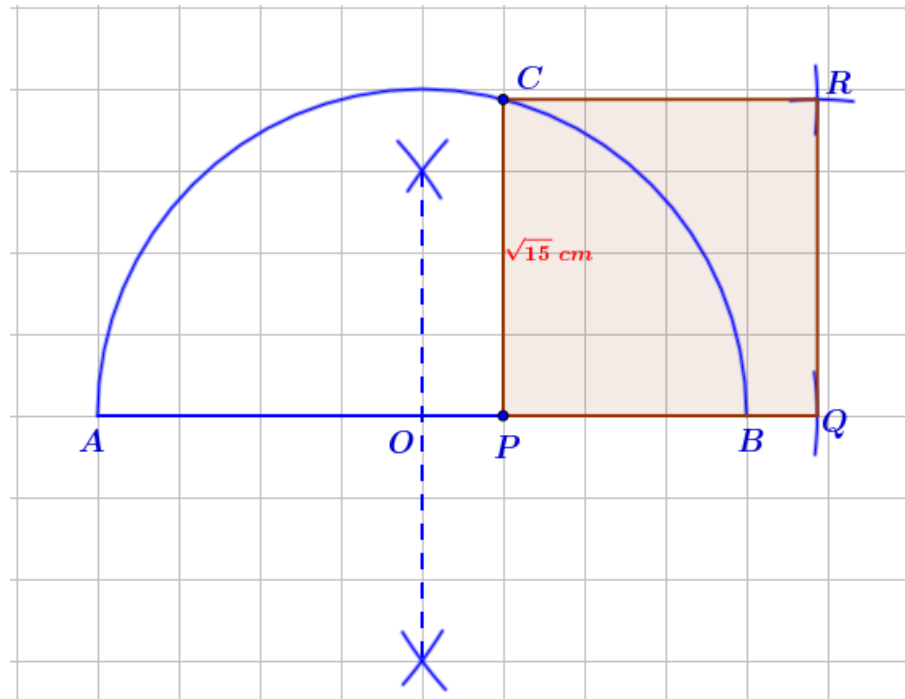
Step 4 : Mark a point P on AB 5 cm away from A .



Step 5 : The perpendicular to AB drawn through P intersect the circle at C . Draw the line CP



Step 6 : Draw a square with PC as side .



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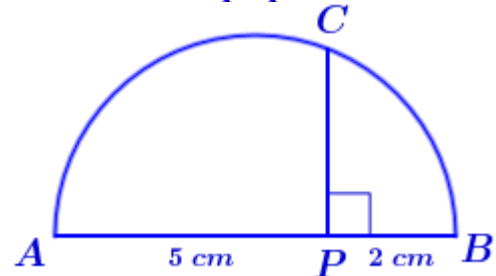
WORKSHEET

1. In the figure AB is the diameter of the semicircle and the line PC is perpendicular to AB

$PA = 5 \text{ cm}$, $PB = 2 \text{ cm}$

a) What is the length of PC ?

b) Draw a line of length $\sqrt{7} \text{ cm}$?



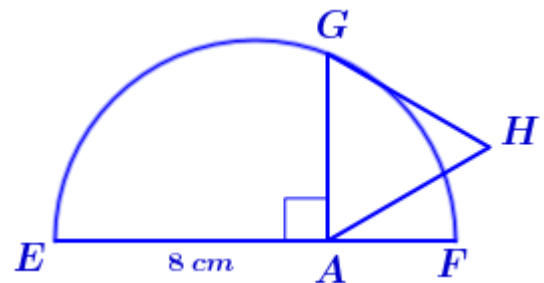
2. In the figure EF is the diameter of the semicircle and the line AG is perpendicular to EF .

AGH is an equilateral triangle. Radius of the semicircle

is 5 cm and $AE = 8 \text{ cm}$

a) $AE \times AF = \text{-----}$

b) What is the perimeter of the triangle AGH ?



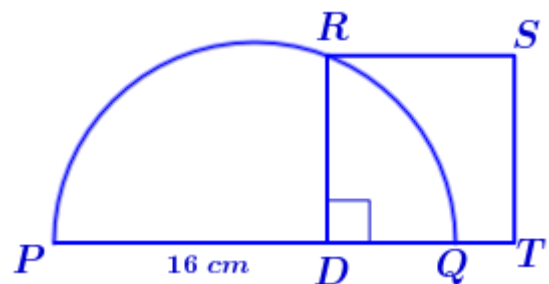
3. In the figure PQ is the diameter of the semicircle and the line DR is perpendicular to PQ .

$DRST$ is a square. Radius of the semicircle is 10 cm and $DP = 16 \text{ cm}$

a) $DP \times DQ = \text{-----}$

b) What is the area of the square $DRST$?

c) What is the perimeter of the square $DRST$?



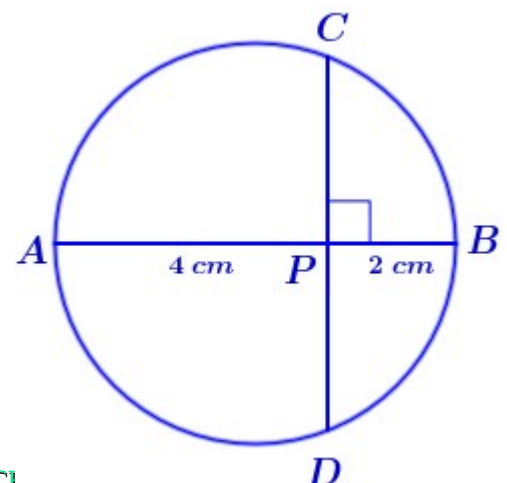
4. In the figure AB is the diameter of the circle and the line CD is a chord perpendicular

to AB . $PA = 4 \text{ cm}$, $PB = 2 \text{ cm}$

a) What is the length of PC ?

b) What is the length of PD ?

c) Draw an equilateral triangle of a side $\sqrt{32} \text{ cm}$?



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