

THIRUVANANTHAPURAM EDUCATIONAL DISTRICT

WS 3.1

MATHEMATICS

STANDARD:10

MATHEMATICS OF CHANCE (ANSWERS)

1. A box contains 10 black and 5 white balls. If a ball is taken from it what is the probability of it being black? And what is the probability of it being white?

Total number of balls in the box = 15

Total number of **black** balls in the box = 10

$$\begin{aligned} \text{Probability of getting a **black** ball} &= \frac{\text{number of black balls}}{\text{total number of balls}} \\ &= \frac{10}{15} = \frac{2}{3} \end{aligned}$$

Total number of **white** balls in the box = 5

$$\begin{aligned} \text{Probability of getting a **white** ball} &= \frac{\text{number of white balls}}{\text{total number of balls}} \\ &= \frac{5}{15} = \frac{1}{3} \end{aligned}$$

2. Numbers from 1 to 30 are written in paper slips and put in a box. Without looking one slip is taken from it.

a) What is the probability that it is an even number?

b) What is the probability that it is a prime number?

a) Total number of paper slips = 30

Even numbers from 1 to 30 are 2, 4, 6,...30

Total Number of even numbers from 1 to 30 = 15

$$\begin{aligned} \text{Probability of getting an even number} &= \frac{\text{Total Number of even numbers}}{\text{Total Number of paper slips}} \\ &= \frac{15}{30} = \frac{1}{2} \end{aligned}$$

b) The prime numbers between 1 to 30 are 2, 3, 5, 7, 11, 13, 17, 19, 23 and 29.

$$\text{Total Number of prime numbers} = \underline{10}$$

$$\begin{aligned} \text{Probability of getting a prime number} &= \frac{\text{Total Number of prime numbers}}{\text{Total Number of paper slips}} \\ &= \frac{10}{30} = \frac{1}{3} \end{aligned}$$

3. There are 18 beads in a box. Some of them are white and the remaining are black. The probability of drawing a black bead from it is $\frac{1}{3}$
Then (a) How many black beads are there in the box ?
(b) How many white beads are there in the box ?

$$\text{(a) Total number of beads} = 18$$

$$\text{Probability of getting black bead} = \frac{1}{3}$$

$$\text{Probability of getting black bead} = \frac{\text{Number of black beads}}{\text{Total number of beads}}$$

$$\frac{1}{3} = \frac{\text{Number of black beads}}{18}$$

$$3 \times \text{Number of black beads} = 18$$

$$\text{Number of black beads} = \frac{18}{3} = \underline{6}$$

$$\text{(b) Number of white beads} = 18 - \underline{6} = \underline{12}$$

4. In the figure below the length and breadth of the rectangle is 10 cm and 8 cm respectively. If we put a dot inside the rectangle without looking into it, what is the probability that it will be inside the circle?



Length of rectangle = 10

Breadth of rectangle = 8

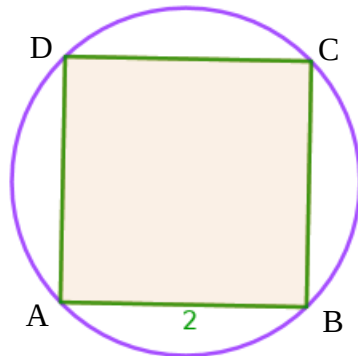
Area of rectangle = 10 x 8 = 80

Radius of the circle = $\frac{8}{2} = 4$

Area of the circle = $\pi r^2 = \pi \times 4^2 = 16\pi$

Probability = $\frac{\text{area of circle}}{\text{area of rectangle}} = \frac{16\pi}{80} = \frac{\pi}{5}$

5. In the figure, what is the probability of a dot we put without looking to be with in the square?



Length of one side of square = 2

Area of the square = 4
 $AB = BC = 2$

$AC = \sqrt{AB^2 + BC^2} = \sqrt{2^2 + 2^2} = \sqrt{4 + 4} = \sqrt{8}$

Radius of circle = $\frac{AC}{2} = \frac{\sqrt{8}}{2} = \frac{2\sqrt{2}}{2} = \sqrt{2}$

Area of circle = $\pi r^2 = \pi (\sqrt{2})^2 = 2\pi$

Probability of dot with in the square = $\frac{\text{area of square}}{\text{area of circle}} = \frac{4}{2\pi} = \frac{2}{\pi}$