

ONLINE MATHS CLASS - X - 37 (29 / 09 /2020)

WORKSHEET

1. One is asked to say a letter in the English alphabet .

- a) How many letters are there in English alphabet ?
- b) What is the probability of telling a vowel ?
- c) What is the probability of telling a consonant ?
- d) What is the sum of the probabilities of telling a vowel and not telling a vowel ?

2. One is asked to say a two digit number .

- a) How many two digit numbers are there ?
- b) What is the probability of getting a number in which one of the digits is 1 ?
- c) What is the probability of getting a number in which the product of the digits is a prime number ?

3. There are 10 red and 7 blue balls in a basket . A ball is taken from it

- a) What is the probability of getting a red ball ?
- b) What is the probability of getting a blue ball ?
- c) What is the sum of the probabilities of getting a red ball and not getting a red ball ?
- d) If three more blue balls are added to the basket and one ball is taken , what is the probability of getting a red ball ?

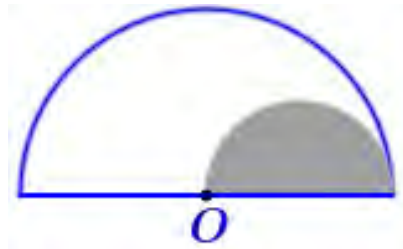
4. One is asked to say a three digit number .

- a) How many three digit numbers are there ?
- b) What is the probability of getting a number whose digits are same ?
- c) What is the probability of getting a number in which all digits are different ?

ONLINE MATHS CLASS - X - 38 (01 / 10 /2020)

WORRK SHEET

1. There are two semicircles in the figure . O is the centre of the larger semicircle . Put a dot in this figure without looking .



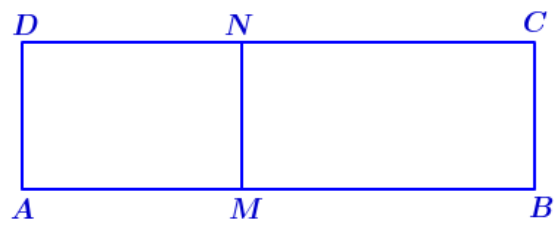
- If the radius of the smaller semi circle is r , What is the radius of the larger semicircle ?
- What is the probability that the dot would be within the smaller semicircle ?
- What is the probability that the dot would be outside the smaller semicircle ?

2. In the figure , an equilateral triangle is drawn inside a circle . Put a dot in this figure without looking .



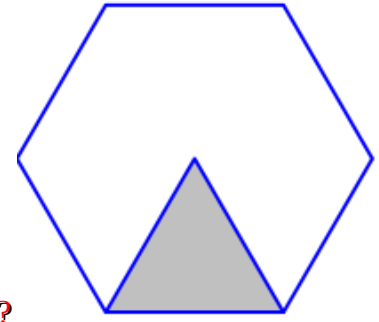
- If the radius of the circle is r , What is the length of the side of the triangle ?
- What is the probability that the dot would be within the triangle ?
- What is the probability that the dot would be outside the triangle ?

3. Two rectangles are joined in the figure . If we put a dot in the figure without looking , the probability of it would be within the rectangle $AMND$ is $\frac{4}{9}$



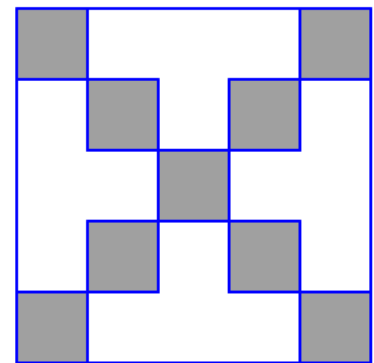
- What is the probability that the dot would be within the rectangle $MBCN$?
- If $AM = 8\text{ cm}$ and $MN = 5\text{ cm}$, what is the area of the rectangle $ABCD$?
- If the area of the rectangle $AMND$ is y and the probability of the dot would be within this rectangle is $\frac{y}{x}$, what is the area of the rectangle $MBCN$?

4. In the figure , an equilateral triangle is drawn inside a regular hexagon . Put a dot in this figure without looking .



- What is the maximum number of triangles of the given size can be cut from the hexagon ?
- What is the probability that the dot would be within the triangle ?
- What is the probability that the dot would be outside the triangle ?

5. In the figure , small equal squares are drawn inside a square . Put a dot in this figure without looking .



- What is the maximum number of small squares of the given size can be cut from the larger square ?
- What is the probability that the dot would be within the shaded portion ?
- What is the probability that the dot would be outside the shaded portion ?

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What did we learn in the last class ?

The probability is mathematically analysed by converting it into number by calculating how many of the favourable outcomes out of total outcomes .

$$\text{Probability} = \frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}}$$

Let's solve some problems related to this idea .

- (1) A box contains 6 black and 4 white balls. If a ball is taken from it, what is the probability of it being black? And the probability of it being white?

Answer.

$$\text{Total number of outcomes} = 10$$

$$\text{Probability of it being black} = \frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}} = \frac{6}{10} = \frac{3}{5}$$

$$\text{Probability of it being white} = \frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}} = \frac{4}{10} = \frac{2}{5}$$

- (2) A bag contains 3 red beads and 7 green beads. Another contains one red and one green more. The probability of getting a red from which bag is more?

Answer.

First bag

$$\text{Total number of outcomes} = 10$$

$$\text{Probability of getting red} = \frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}} = \frac{3}{10}$$

Second bag

Total number of outcomes = 12

Probability of getting red = $\frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}} = \frac{4}{12} = \frac{1}{3}$

$\frac{1}{3}$ is larger than $\frac{3}{10}$

$$\begin{array}{l} \frac{3}{10} \quad \leftarrow \quad \frac{1}{3} \\ 3 \times 3 \quad \quad 1 \times 10 \\ 9 < 10 \implies \frac{3}{10} < \frac{1}{3} \end{array}$$

The probability of getting a red from the second bag is more .

(3). Numbers 1 to 50 are written on slips of paper and put in a box . A slip is drawn from it , but before doing so , one must make a guess about the number , either prime number or a multiple of 5 . Which is a better guess ? Why ?

Answer .

Total number of outcomes = 50

Prime numbers = 2 , 3 , 5 , 7 , 11 , 13 , 17 , 19 , 23 , 29 , 31 , 37 , 41 , 43 , 47

Number of favourable outcomes = 15

Probability of getting a prime number = $\frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}} = \frac{15}{50} = \frac{3}{10}$

Multiples of five = 5 , 10 , 15 , 20 , 25 , 30 , 35 , 40 , 45 , 50

Number of favourable outcomes = 10

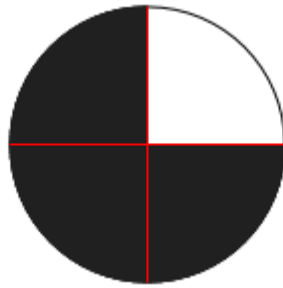
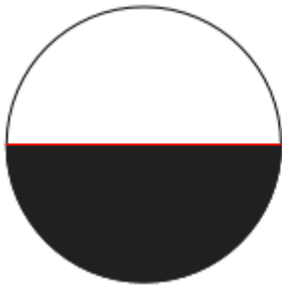
Probability of getting a multiple of five = $\frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}} = \frac{10}{50} = \frac{1}{5}$

$\frac{3}{10}$ is larger than $\frac{1}{5}$

$$\begin{array}{l} \frac{3}{10} \quad \leftarrow \quad \frac{1}{5} \\ 3 \times 5 \quad \quad 1 \times 10 \\ 15 > 10 \implies \frac{3}{10} > \frac{1}{5} \end{array}$$

The guess of prime number is better .

Geometrical probability



In the figure first circle is divided into two equal parts , second circle is divided into four equal parts and the third circle divided into eight equal parts .

In the first figure Half of the portion is black . That is $\frac{1}{2}$ th part of the total area is black and

$\frac{1}{2}$ th part is white .

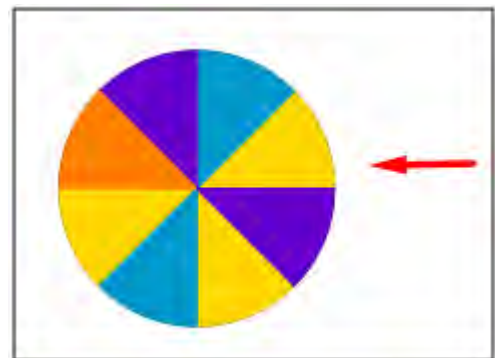
$\frac{3}{4}$ th part of total area is black and $\frac{1}{4}$ th part of the area is white in the second figure .

$\frac{5}{8}$ th part of total area is black and $\frac{3}{8}$ th part of the area is white in the second figure .

Activity 1.

A circular disc is divided into eight equal parts and are coloured (spinning wheel) . It spins on a board .

What is the probability of getting yellow against the arrow when it stops ?



Here three out of eight parts are yellow .

Probability of getting yellow = $\frac{3}{8}$

Here probability is calculated in terms of the areas of the geometrical figures .

Here probability is how much part is the desired area out of the total area . It is known as the geometrical probability

Let's solve some problems related to this idea .

(1) If you shut your eyes and put a dot in this rectangle .

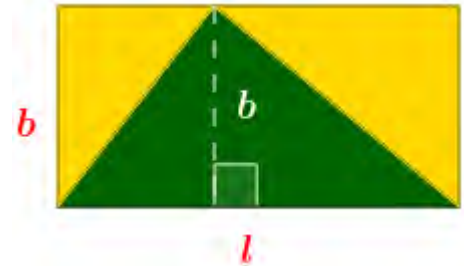
What is the probability that it would be within the green triangle ?



Answer

Area of the rectangle = $l \times b$

Area of the triangle = $\frac{1}{2} l \times b$



Half the area of the rectangle is that of the triangle .

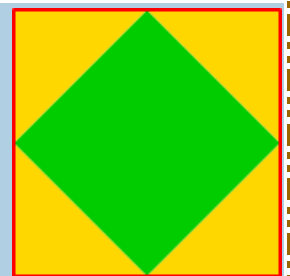
probability that the dot would be within the green triangle = $\frac{1}{2}$

NB :

$$\begin{aligned} \text{probability that it would be within the green triangle} &= \frac{\text{Area of the triangle}}{\text{Area of the rectangle}} \\ &= \frac{\frac{1}{2} l \times b}{l \times b} = \frac{1}{2} \end{aligned}$$

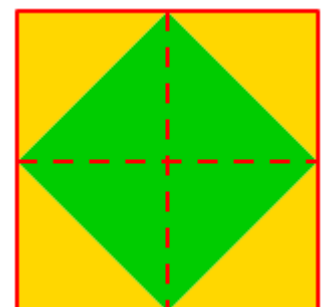
(2) In the figure a square got by joining the mid points of a larger square

If we put a dot in the larger square without looking , what is the probability of it being within the green square ?



Answer

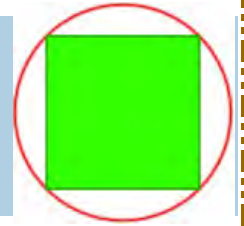
(If we join the midpoints of the bigger rectangle (diagonals of the smaller rectangle) , we get eight right angled triangles . They are equal triangles , so their areas are equal .)



4 out of 8 equal triangles are green .

$$\text{Probability of the dot being within the green square} = \frac{4}{8} = \frac{1}{2}$$

(3) A square with all vertices on a circle is given . What is the probability of a dot put without looking to be within the square ?



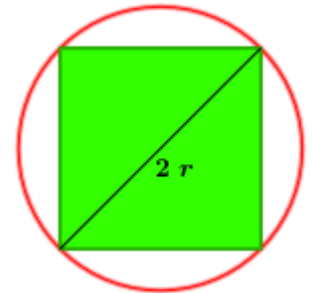
Answer

Take , radius of the circle = r

Diagonal of the square = Diameter of the circle

$$a \sqrt{2} = 2 r$$

$$a = \frac{2 r}{\sqrt{2}} = \sqrt{2} r$$



Probability of the dot being within the green square = $\frac{\text{Area of the square}}{\text{Area of the circle}}$

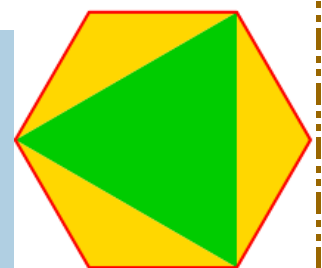
$$\text{Area of the square} = a^2 = (\sqrt{2} r)^2 = 2 r^2$$

$$\text{Area of the circle} = \pi r^2$$

Probability of the dot being within the green square = $\frac{\text{Area of the square}}{\text{Area of the circle}} = \frac{2 r^2}{\pi r^2} = \frac{2}{\pi}$

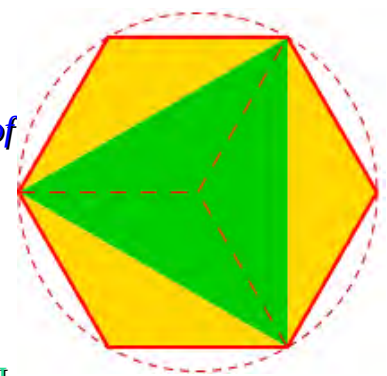
(3) A triangle got by joining alternate vertices of a regular hexagon .

If put a dot without looking in this hexagon , what is the probability of it being within the green triangle ?



Answer

(If we join the ends of the triangle to the centre of the circumcircle of the hexagon , we get three green triangles and three yellow triangles . They are equal triangles . So their areas are same .)

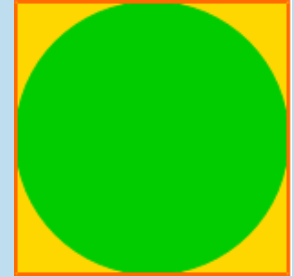


3 out of 6 triangles are green .

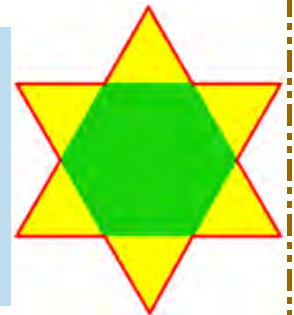
Probability of the dot being within the green square = $\frac{3}{6} = \frac{1}{2}$

More activities

(1). Consider a circle exactly fitting inside the square . If we put a dot without looking in this square , what is the probability of it being within the circle ? .



(2). A regular hexagon formed by two overlapping equilateral triangles. If we put a dot without looking in this figure , what is the probability of it being within the hexagon ?



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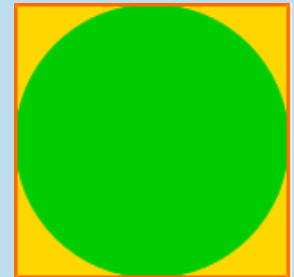
What did we learn in the last class ?

Probability can be calculated in terms of the areas of the geometrical figures .

Here probability is how much part is the desired area out of the total area . It is known as the geometrical probability

Let's solve some problems related to this idea .

(1). Consider a circle exactly fitting inside the square . If we put a dot without looking in this square , what is the probability of it being within the circle ? .



Answer .

Probability of the dot being within the circle = $\frac{\text{Area of the circle}}{\text{Area of the square}}$

Diameter of the circle = Side of the square

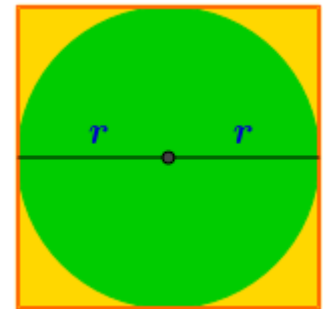
Take , radius of the circle = r

Side of the square = $2r$

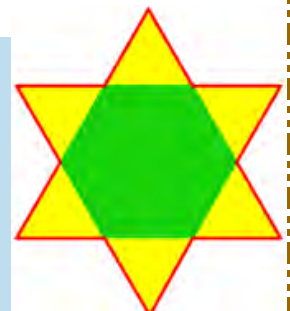
Area of the circle = πr^2

Area of the square = side \times side = $2r \times 2r = 4r^2$

Probability of the dot being within the circle = $\frac{\text{Area of the circle}}{\text{Area of the square}} = \frac{\pi r^2}{4 r^2} = \frac{\pi}{4}$



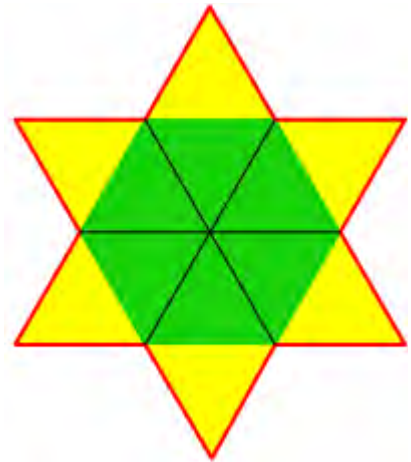
(2). A regular hexagon formed by two overlapping equilateral triangles. If we put a dot without looking in this figure , what is the probability of it being within the hexagon ?



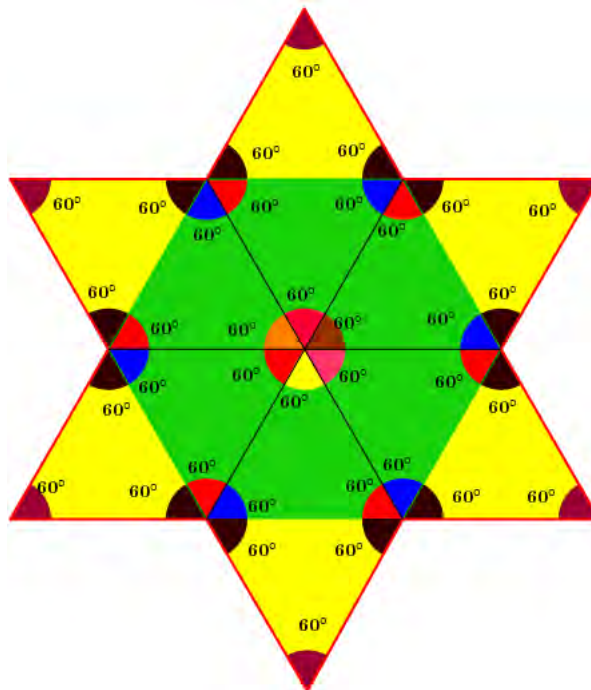
Answer .

We can cut the regular hexagon in the figure into 6 equilateral triangles as shown . Then there are 12 triangles and they are equal triangles .

$$\text{Probability of the dot being within the hexagon} = \frac{6}{12} = \frac{1}{2}$$

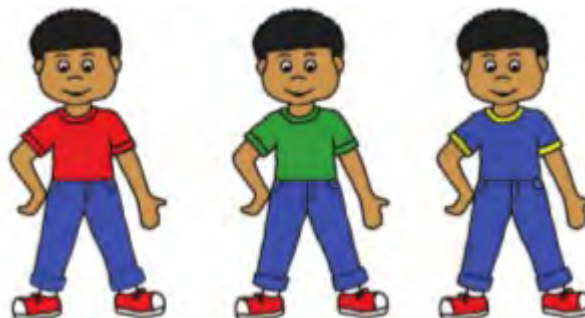


NB :

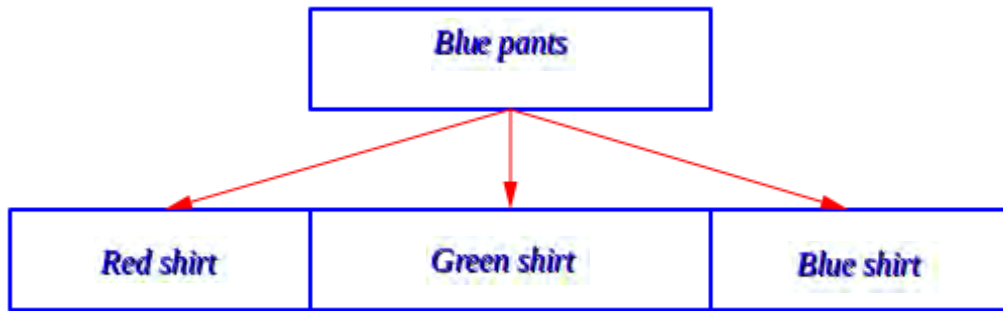


PAIRS

(1) Looking for a clean dress , Johny found a pair of blue pants and three shirts , red , green and blue . In how many ways he can wear the dress ?



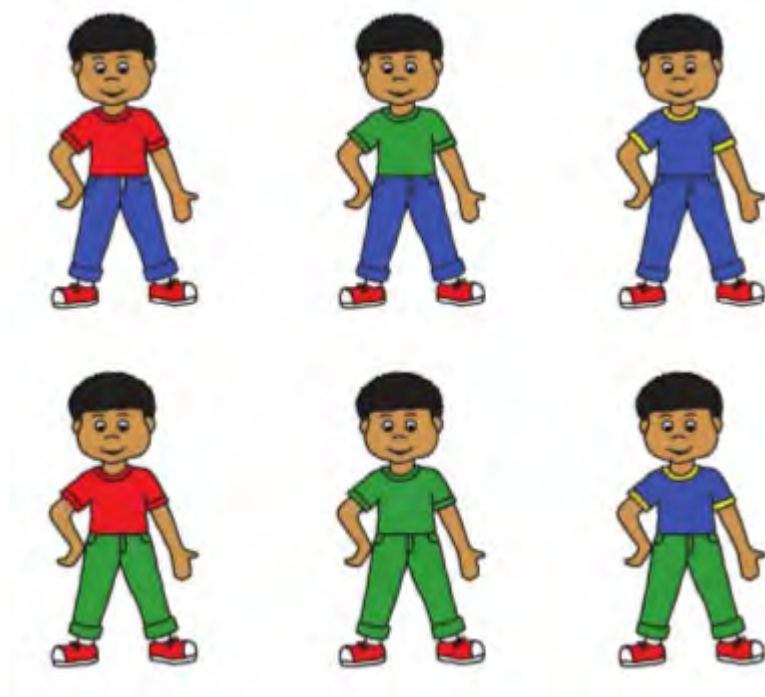
He can wear the dress in three different ways as shown above .



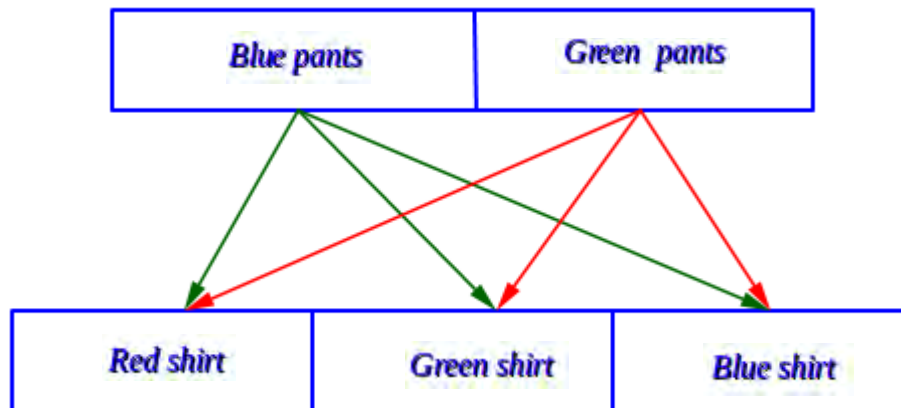
We can write these as pairs .

(Blue pants , Red shirt) , (Blue pants , Green shirt) , (Blue pants , Blue shirt)

(2) If Johny got two pants , blue and green in colour and three shirts red , green and blue in colour , in how many ways he could have worn the dress ? What was the probability of wearing shirt and pants of the same colour ?



He could have worn the dress in six different ways as shown above .



We can write these as pairs .

(Blue pants , Red shirt) , (Blue pants , Green shirt) , (Blue pants , Blue shirt)

(Green pants , Red shirt) , (Green pants , Green shirt) , (Green pants , Blue shirt)

Total number of results = 6

Favourable results = (Blue pants , Blue shirt) , (Green pants , Green shirt)

Number of favourable results = 2

Probability of wearing shirt and pants of the same colour = $\frac{\text{Number of favourable results}}{\text{Total number of results}}$

$$= \frac{2}{6} = \frac{1}{3}$$

(3) A box contains four slips numbered 1 , 2 , 3 , 4 and another box contains two slips 1 , 2

One slip is taken from each

- What are the possible pairs ?
- What is the probability of both the numbers being odd ?
- What is the probability of both the numbers being even ?
- What is the probability of one odd and the other even ?
- What is the probability of both the numbers being same ?

Answer .

a) (1, 1), (1, 2)

(2, 1), (2, 2)

(3, 1), (3, 2)

(4, 1), (4, 2)

Total number of results = 8

b) Favourable results = (1, 1), (3, 1)

Number of favourable results = 2

$$\begin{aligned} \text{Probability of both the numbers being odd} &= \frac{\text{Number of favourable results}}{\text{Total number of results}} \\ &= \frac{2}{8} = \frac{1}{4} \end{aligned}$$

c) Favourable results = (2, 2), (4, 2)

Number of favourable results = 2

$$\begin{aligned} \text{probability of both the numbers being even} &= \frac{\text{Number of favourable results}}{\text{Total number of results}} \\ &= \frac{2}{8} = \frac{1}{4} \end{aligned}$$

d) Favourable results = (1, 2), (2, 1), (3, 2), (4, 1)

Number of favourable results = 4

$$\begin{aligned} \text{Probability of one odd and the other even} &= \frac{\text{Number of favourable results}}{\text{Total number of results}} \\ &= \frac{4}{8} = \frac{1}{2} \end{aligned}$$

e) Favourable results = (1, 1), (2, 2)

Number of favourable results = 2

$$\text{Probability of both the numbers being same} = \frac{\text{Number of favourable results}}{\text{Total number of results}} = \frac{2}{8} = \frac{1}{4}$$

(4) From all two digit numbers with either digits 1, 2 or 3 one number is chosen

a) What is the probability of both the digits being same ?

b) What is the probability of the sum of the digits being 4 ?

Answer .

Total results = 11, 12, 13, 21, 22, 23, 31, 32, 33

Total number of results = 9

a) Favourable results = 11, 22, 33

Number of favourable results = 3

Probability of both the numbers being same = $\frac{\text{Number of favourable results}}{\text{Total number of results}} = \frac{3}{9} = \frac{1}{3}$

b) Favourable results = 13, 22, 31

Number of favourable results = 3

Probability of the sum of the digits being 4 = $\frac{\text{Number of favourable results}}{\text{Total number of results}} = \frac{3}{9} = \frac{1}{3}$

(4) A box contains ten slips numbered 1 to 10 and another box contains five slips from 1 to 5. One slip is taken from each. What is the probability of both the numbers being odd ?

Answer .

Total number of results = $10 \times 5 = 50$

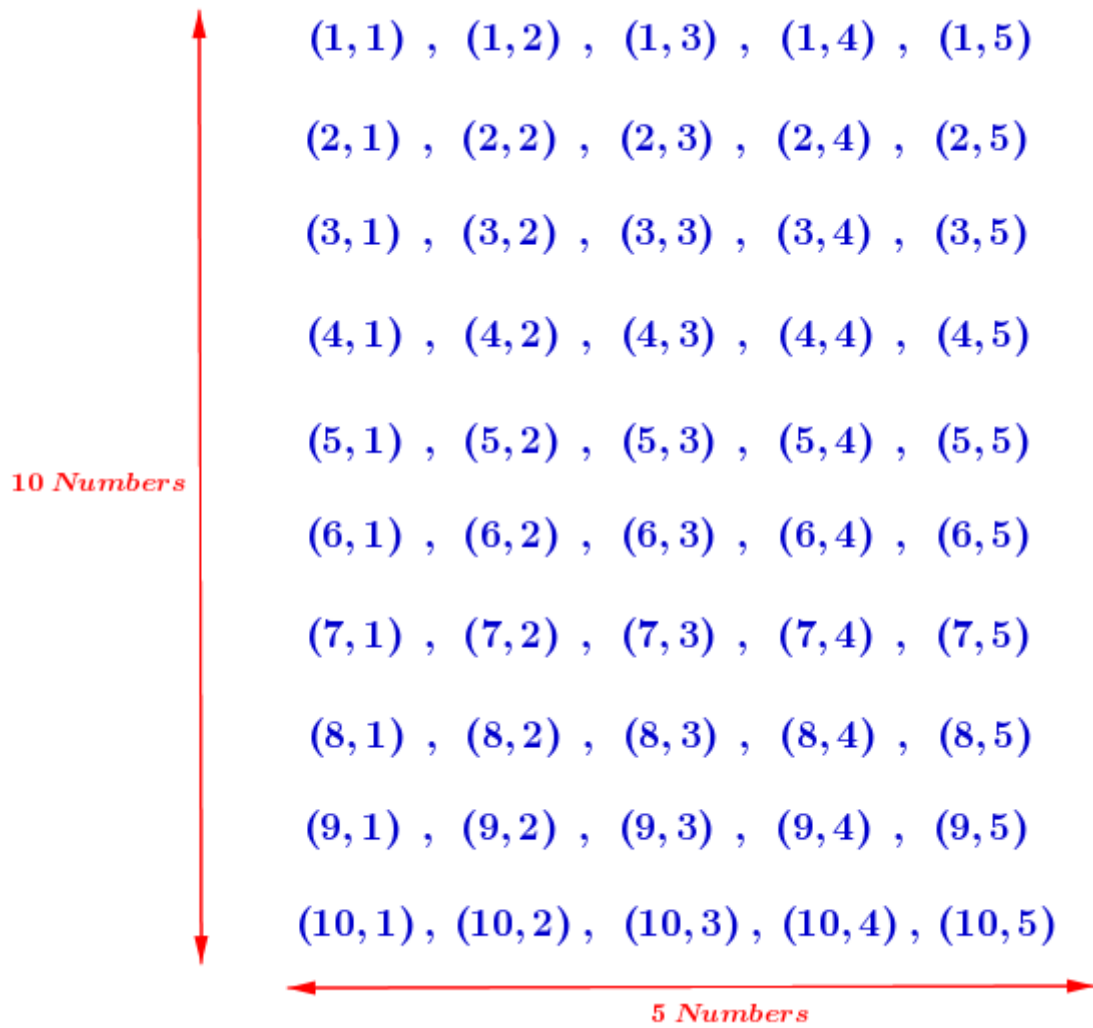
Number of odd numbers in the first box = 5

Number of odd numbers in the second box = 3

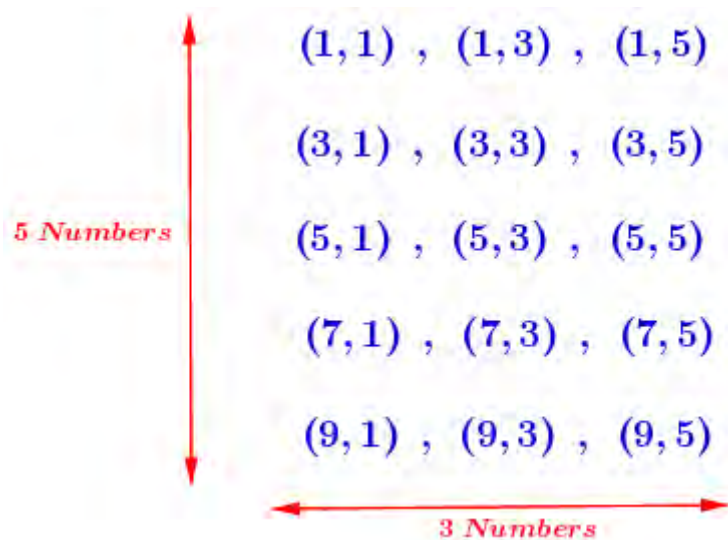
Number of favourable results = $5 \times 3 = 15$

Probability of both the numbers being odd = $\frac{\text{Number of favourable results}}{\text{Total number of results}} = \frac{15}{50} = \frac{3}{10}$

NB :



Total number of results = $10 \times 5 = 50$



Number of pairs in which two numbers are odd = $5 \times 3 = 15$

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WORK SHEET

(1) There are two boxes contain some slips numbered from 1 .One slip is taken from each .

The numbers on the slips in each box is given in the table below .Complete the table.

Box 1	Box 2	Possible pairs	Number of pairs	Product of the number of slips in each box
1, 2	1	(1, 1) , (1, 2)	2	$2 \times 1 = 2$
1, 2	1, 2	(1, 1) , (1, 2) (2, 1) , (2, 2)	4	$2 \times 2 = 4$
1, 2, 3	1, 2	(1, 1) , (1, 2) (2, 1) , (2, 2) (3, 1) , (3, 2)	6	$3 \times 2 = 6$
1, 2 , 3	1, 2 , 3	-----	-----	-----
1, 2 , 3, 4	1, 2	-----	-----	-----
1, 2 , 3, 4, 5	1, 2 , 3	-----	-----	-----
1, 2 , 3, 4, 5, 6	1, 2 , 3, 4	-----	-----	-----

(3) A box contains five slips numbered 1 , 2 , 3 , 4 , 5 and another box contains three slips

1 , 2 , 3 One slip is taken from each

- What are the possible pairs ?
- What is the probability of both the numbers being odd ?
- What is the probability of both the numbers being even ?
- What is the probability of the sum of the digits being even ?