## Physics Class Notes

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## Mirror Equation and Focal length

Mirror equation is the relation between object distance (u), image distance (v), and focal length (f) of the mirror.
$1 / \mathrm{f}=1 / \mathrm{u}+1 / \mathrm{v}$ is the mirror equation.
Or $\mathbf{f}=\mathbf{u v} /(\mathbf{u}+\mathbf{v})$.

## New Cartesian Sign Convention.

While measuring distance in optical experiments the sign also is to be taken into account. For this the following rules are to be adopted.

- Distances are measured considering the pole of the mirror as the origin (O).
- Those measured to the right from $\mathbf{O}$ are positive and those in the opposite direction are negative.
- Distances measured upward from $X$ axis are positive and those downwards are negative. The incident ray is to be considered as travelling left to right.
Record the measurements shown in the figure using the New Cartesian Sign Convention.


Distance to the object from the mirror (u) = Negative
Distance to the image from the mirror (v) = Negative

Height of the object (OB)
Height of the image (IM)
= Positive
$=$ Negative.

- The given figure shows the image formation by a concave mirror. Analyse the figure and write down different measures using New Cartesian Sign Convention.


| Distance of the object from the mirror (u) | -60 cm |
| :---: | :---: |
| Distance of image from the mirror (v) | -20 cm |
| Focal length (f) | -15 cm |
| Radius of curvature (R) | -30 cm |
| Height of the object (OB) | +12 cm |
| Height of the image (IM) | -4 cm |

- When an object is placed in front of a concave mirror at a distance 30 cm from an image is obtained on a screen at a distance of $\mathbf{2 0} \mathbf{~ c m}$ from the mirror. Find the focal length of the mirror?
Ans: $\mathbf{u}=-30 \mathrm{~cm}, \mathbf{v}=-20 \mathrm{~cm}$

$$
\begin{aligned}
\mathbf{f} & =\mathbf{u v} /(\mathbf{u}+\mathbf{v}) \\
& =(-30 \times-20) /(-30+-20) \\
& =600 /(-50)=-12 \mathrm{~cm} .
\end{aligned}
$$

- An object is placed in front of a concave mirror 20 cm away from it. If its focal length is $\mathbf{4 0} \mathbf{~ c m}$, locate the position of the image and its nature.
Ans: $\mathbf{u}=-20 \mathrm{~cm}, \mathbf{f}=-40 \mathrm{~cm}$

$$
\begin{aligned}
\mathrm{v} & =\mathrm{fu} /(\mathrm{u}-\mathrm{f}) \\
& =(-40 \times-20) /(-20-(-40)) \\
& =800 /(-20+40) \\
& =800 / 20 \\
& =40 \mathrm{~cm}
\end{aligned}
$$

Since ' $v$ ' is positive the image is virtual and erect.

- When an object is placed in front of a concave mirror at a distance 15 cm an image is formed on a screen 10 cm away from the mirror. If the object is placed 30 cm away what is the distance to the image?
Ans: $\mathbf{u}=-\mathbf{1 5} \mathbf{c m}, \mathbf{v}=-10 \mathrm{~cm}$

$$
\begin{aligned}
f & =u v /(u+v) \\
& =(-15 \times-10) /(-15+-10) \\
& =150 /-25 \\
& =-6 \mathrm{~cm}
\end{aligned}
$$

If the object is placed 30 cm away

$$
\begin{aligned}
\mathbf{u} & =-30 \mathrm{~cm} \\
\mathbf{v} & =\mathbf{f u} /(\mathbf{u - f}) \\
& =(-6 \mathrm{x}-30) /(-30-(-6)) \\
& =180 /(-30+6) \\
& =180 /-24 \\
& =-7.5 \mathrm{~cm} .
\end{aligned}
$$

Since ' $v$ ' is negative image is real and inverted.

## Homework

1. An image is placed in front of a concave mirror $\mathbf{4 0} \mathbf{~ c m}$ away from it. If its focal length is $\mathbf{8 0}$ cm , locate the position of the image and find the nature of the image.
