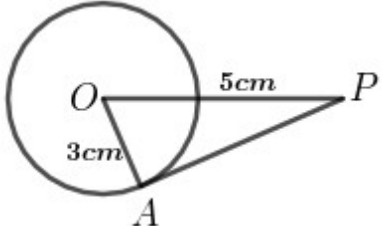
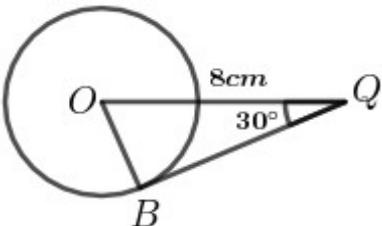
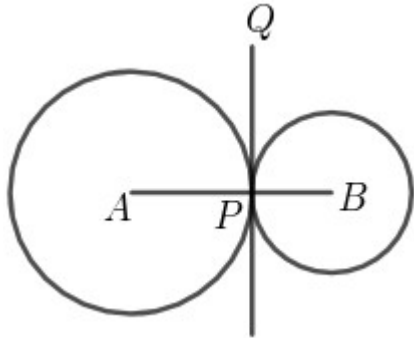
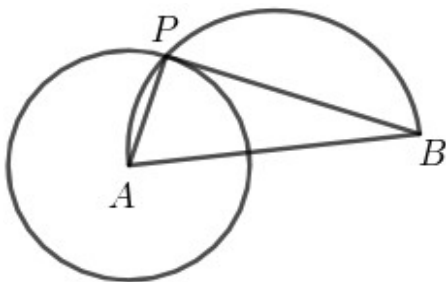


# WANDOOR GANITHAM – S.S.L.C STUDY MATERIAL 2021

## FOCUS AREA - QUESTION BANK - TANGENTS

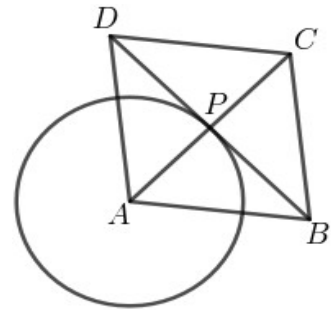
<b>1</b>	<p><i>There is a point 10 cm away from the centre of a circle of radius 6 cm . A tangent is drawn through that point .</i></p> <p>a) <i>What is the angle between a tangent at a point and the radius through that point ?</i></p> <p>b) <i>What is the length of the tangent ?</i></p>	
<b>2</b>	<p><i>In the figure ,O is the centre of the circle and AP is a tangent</i></p> <p><i>OA = 3 cm , OP = 5 cm .</i></p> <p>a) <i>What is the measure of <math>\angle OAP</math> ?</i></p> <p>b) <i>What is the length of the tangent PA ?</i></p>	
<b>3</b>	<p><i>In the figure , O is the centre of the circle and QB is a tangent . OQ = 8 cm , <math>\angle OQB = 30^\circ</math></i></p> <p>a) <i>What is the measure of <math>\angle OBQ</math> ?</i></p> <p>b) <i>What is the radius of the circle ?</i></p> <p>c) <i>What is the length of the tangent QB ?</i></p>	
<b>4</b>	<p><i>In the figure ,two circles intersect at P . PQ is a tangent to the circle with centre A .</i></p> <p>a) <i>What is the measure of <math>\angle APQ</math> ?</i></p> <p>b) <i>Prove that PQ is a tangent to the circle with centre B ?</i></p>	
<b>5</b>	<p><i>In the figure ,a circle and a semicircle intersect at P .</i></p> <p><i>A is the centre of the circle and AB is the diameter of the semicircle .</i></p> <p>a) <i>What is the measure of <math>\angle APB</math> ?</i></p> <p>b) <i>Prove that BP is a tangent to the circle with centre A ?</i></p>	

6 In the figure , diagonals of a rhombus intersect at a point

$P$  on the circle with centre  $A$  .

a) What is the measure of  $\angle APD$  ?

b) Prove that  $DP$  is a tangent to the circle with centre  $A$  ?



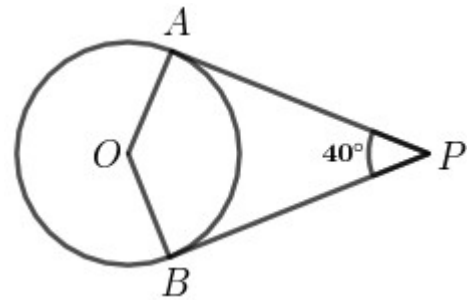
7 In the figure ,  $O$  is the centre of the circle and

the tangents through the points  $A$  and  $B$  .

intersect at  $P$  .  $\angle APB = 40^\circ$

a) What is the measure of  $\angle OAP$  ?

b) What is the measure of  $\angle AOB$  ?



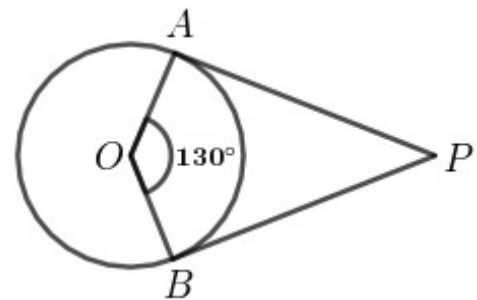
8 In the figure ,  $O$  is the centre of the circle and

the tangents through the points  $A$  and  $B$  .

$\angle AOB = 130^\circ$

a) What is the measure of  $\angle OAP$  ?

b) What is the measure of  $\angle APB$  ?



9 In the figure ,  $A$  and  $B$  are the centres of the circles .

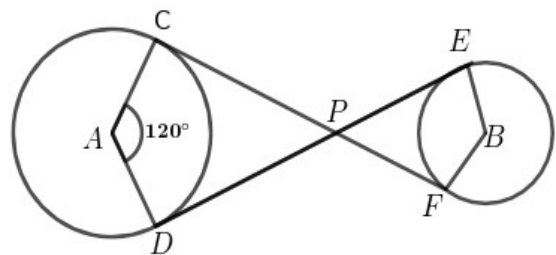
Tangents are drawn from a point  $P$  to these

circles .  $\angle CAD = 120^\circ$

a) What is the measure of  $\angle ACP$  ?

b) What is the measure of  $\angle CPD$  ?

c) What is the measure of  $\angle EBF$  ?



10 In the figure  $O$  is the centre of the incircle . The circle

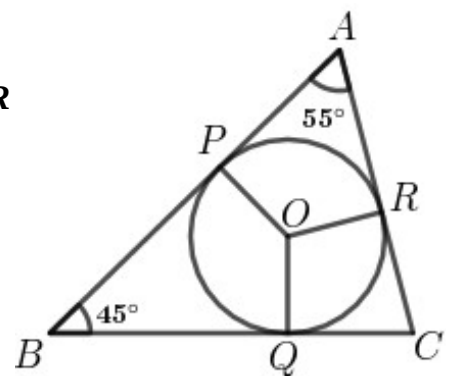
touches the sides of the triangle at the points  $P$  ,  $Q$  and  $R$

$\angle BAC = 55^\circ$  ,  $\angle ABC = 45^\circ$

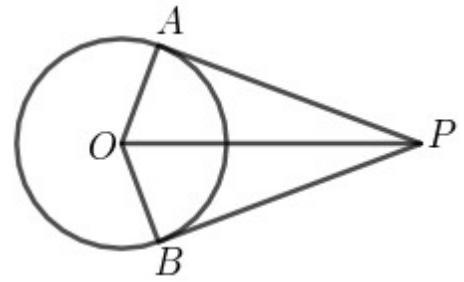
a ) What is the measure of  $\angle BPO$  ?

b) What is the measure of  $\angle POQ$  ?

c) What is the measure of  $\angle QOR$  ?

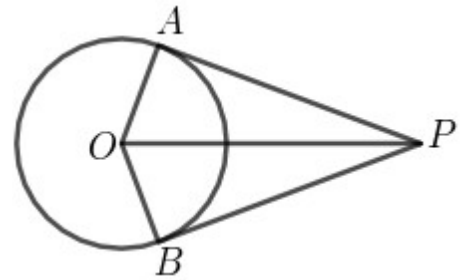


11 In the figure ,  $O$  is the centre of circle and the tangents through the points  $A$  and  $B$  intersect at  $P$ .



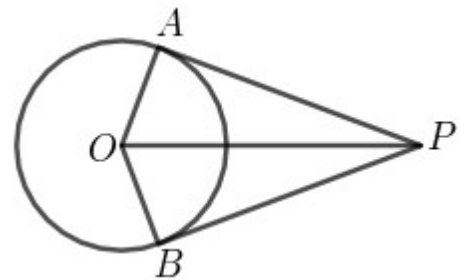
- a) What is the measure of  $\angle OAP$  ?
- b) Prove that the triangles  $AOP$  and  $BOP$  are equal ?
- c) Prove that the tangents have the same length ?

12 In the figure ,  $O$  is the centre of circle and the tangents through the points  $A$  and  $B$  intersect at  $P$ .



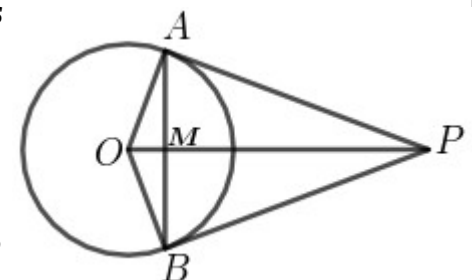
- a) What is the measure of  $\angle OAP$  ?
- b) Prove that the triangles  $AOP$  and  $BOP$  are equal ?
- c) Prove that  $OP$  is the bisector of  $\angle APB$  ?

13 In the figure ,  $O$  is the centre of circle and the tangents through the points  $A$  and  $B$  intersect at  $P$ .



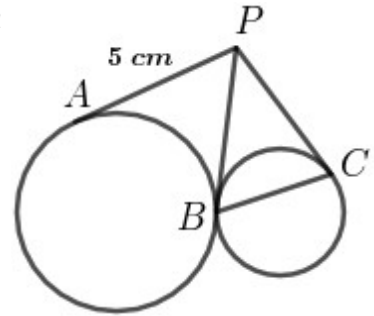
- a) What is the measure of  $\angle OAP$  ?
- b) Prove that the triangles  $AOP$  and  $BOP$  are equal ?
- c) Prove that  $OP$  is the bisector of  $\angle AOB$  ?

14 In the figure ,  $O$  is the centre of circle and the tangents through the points  $A$  and  $B$  intersect at  $P$ .



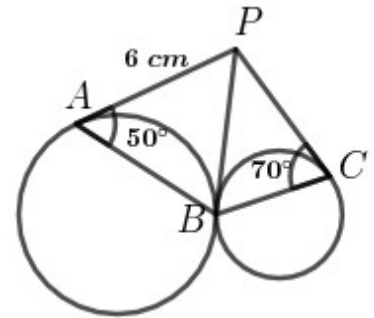
- a) What is the measure of  $\angle OAP$  ?
- b) Prove that the triangles  $AOP$  and  $BOP$  are equal ?
- c) Prove that the angles of the triangles  $AOM$  and  $BOM$  are equal ?
- d) Prove that  $OP$  is the bisector of  $AB$  ?
- e) What is the measure of  $\angle AMO$  ?

- 15 In the figure two circles intersect at B. The tangents through A, B, C meet at P. PA = 5 cm.



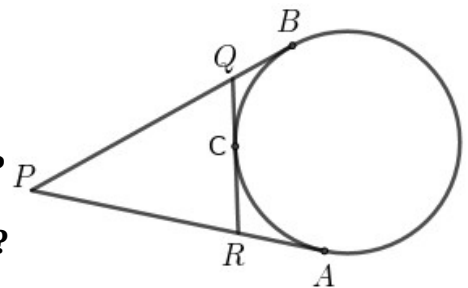
- a) What is the length of PB ?  
b) Prove that PBC is an isosceles triangle ?

- 16 In the figure two circles intersect at B. The tangents through A, B, C meet at P. PA = 6 cm,  $\angle BAP = 50^\circ$ ,  $\angle BCP = 70^\circ$



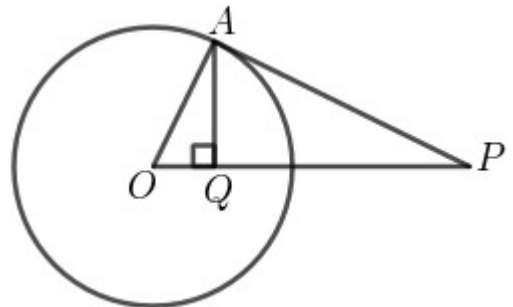
- a) What is the length of PB ?  
b) What is the measure of  $\angle APB$  ?  
c) What is the measure of  $\angle APC$  ?

- 17 In the figure, tangents through the points A and B of a circle intersect at P. QR is a tangent through C



- a) Which other line has the same length as that of PA ?  
b) Which other line has the same length as that of RC ?  
c) Prove that the perimeter of the triangle PQR is double the length of PA ?

- 18 In the figure, O is the centre of the circle. AP is a tangent. AQ is perpendicular to OP.



- a) What is the measure of  $\angle OAP$  ?  
b) Prove that the angles of the triangles OAP and OAQ are same ?  
c) Prove that  $OP \times OQ = OA^2$  ?

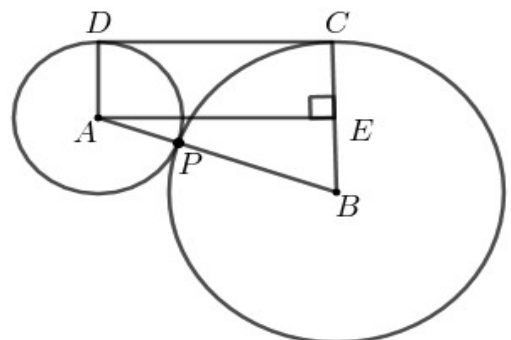
- 19 In the figure, two circles intersect at P.

CD is the common tangent of the circles.

Radius of the smaller circle is 4 cm

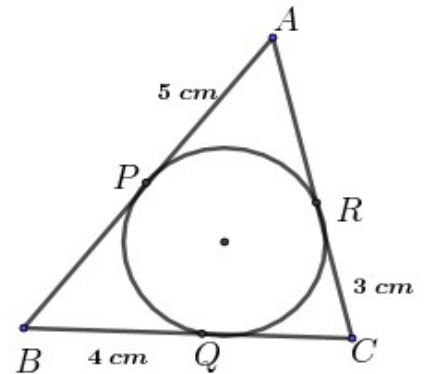
and the radius of the larger circle is 7 cm.

AE is perpendicular to BC.



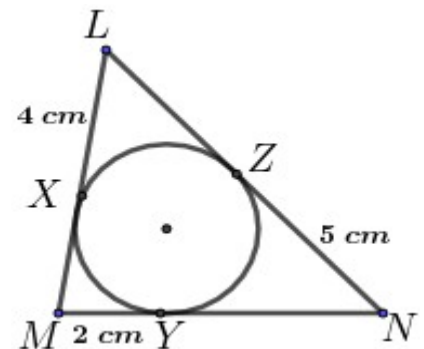
- a) What is the measure of  $\angle ADC$  ?
- b) Prove that  $AECD$  is a rectangle ?
- c) What is the length of  $BE$  ?
- d) What is the length of  $AB$  ?
- e) What is the length of the tangent  $CD$  ?

20 In the figure , the circle touches the sides of the triangle  $ABC$  at the points  $P, Q, R$  .  $AP = 5\text{ cm}$  ,  $BQ = 4\text{ cm}$    
  $CR = 4\text{ cm}$  .



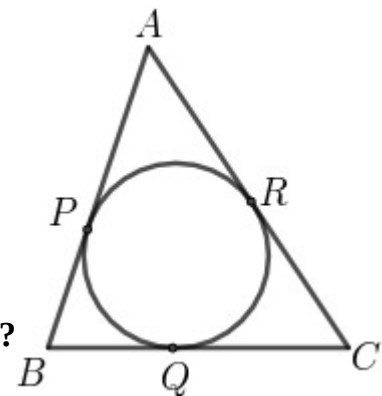
- a) What is the length of  $AR$  ?
- b) What is the length of  $BC$  ?
- c) What is the perimeter of the triangle  $ABC$  ?

21 In the figure , the circle touches the sides of the triangle  $LMN$  at the points  $X, Y, Z$  .  $LX = 4\text{ cm}$  ,  $MY = 2\text{ cm}$    
  $NZ = 5\text{ cm}$  .



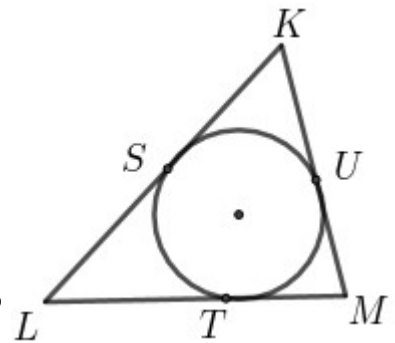
- a) What is the length of  $LZ$  ?
- b) What is the length of  $MN$  ?
- c) What is the perimeter of the triangle  $LMN$  ?

22 In the figure , the circle touches the sides of the triangle  $ABC$  at the points  $P, Q, R$  .  $AB = 10\text{ cm}$  ,  $BC = 8\text{ cm}$    
  $AC = 12\text{ cm}$  .



- a) Which other line has the same length as that of  $AP$  ?
- b) If the length  $AP$  is taken as  $x$  , what is the length of  $BQ$  ?
- c) What is the value of  $x$  ?
- d) What are the lengths of the lines  $AR, BP$  and  $CQ$  ?

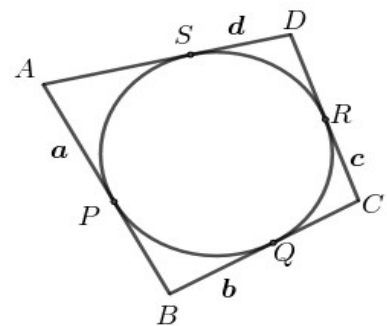
23 In the figure , the circle touches the sides of the triangle  $KLM$  at the points  $S, T, U$  .  $KL = 11\text{ cm}$  ,  $LM = 9\text{ cm}$  ,  $KM = 7\text{ cm}$ .



- Which other line has the same length as that of  $KS$  ?
- If the length  $KS$  is taken as  $x$  , what is the length of  $LT$  ?
- What is the value of  $x$  ?
- What are the lengths of the lines  $KU, LS$  and  $MT$  ?

24 In the figure , the circle touches the sides of the quadrilateral at the points  $P, Q, R, S$  .

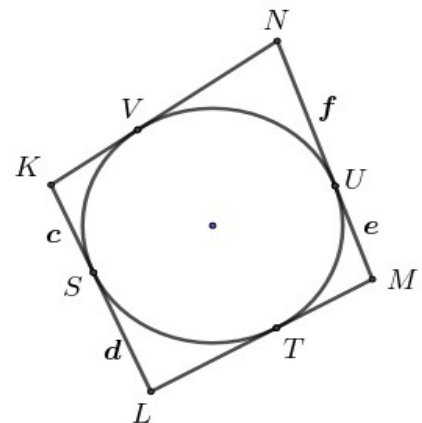
$AP = a$  ,  $BQ = b$  ,  $CR = c$  ,  $DS = d$



- What is the length of  $AS$  ?
- What is the length of  $BC$  ?
- What is the length of  $AD$  ?
- What is the perimeter of  $ABCD$  ?

25 In the figure , the circle touches the sides of the quadrilateral at the points  $S, T, U, V$

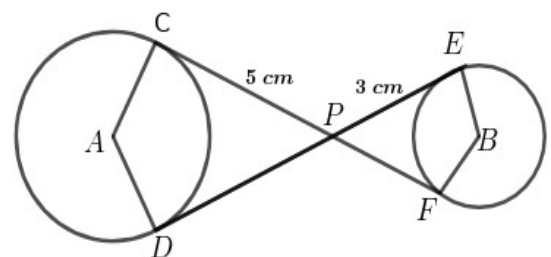
$KS = c$  ,  $LS = d$  ,  $MU = e$  ,  $NU = f$



- What is the length of  $KV$  ?
- What is the length of  $LM$  ?
- What is the length of  $KN$  ?
- What is the perimeter of  $KLMN$  ?

26 In the figure ,  $A$  and  $B$  are the centres of the circles and tangents are drawn from a point  $P$  to the circles

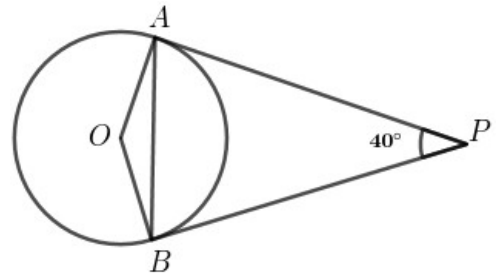
$PC = 5\text{ cm}$  ,  $PE = 3\text{ cm}$



- What is the length of  $PD$  ?
- What is the length of  $CF$  ?

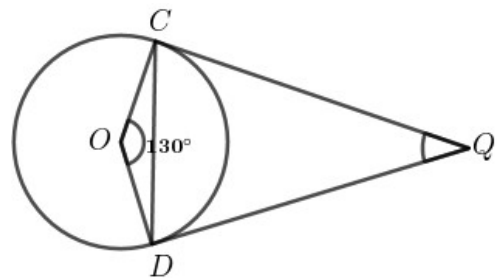


27 In the figure ,  $O$  is the centre of the circle and tangents through the points  $A$  and  $B$  intersect at  $P$ .  
 $\angle APB = 40^\circ$



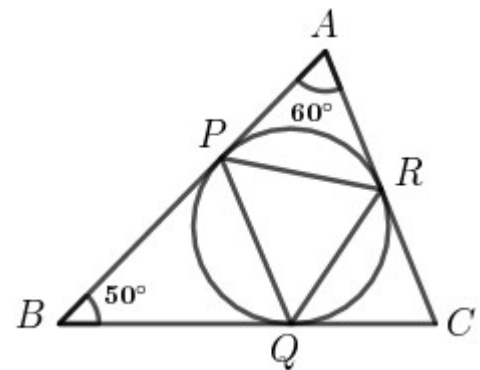
- What is the measure of  $\angle AOB$  ?
- What is the measure of  $\angle OAB$  ?
- What is the measure of  $\angle ABP$  ?

28 In the figure ,  $O$  is the centre of the circle and tangents through the points  $C$  and  $D$  intersect at  $Q$ .  
 $\angle COD = 130^\circ$



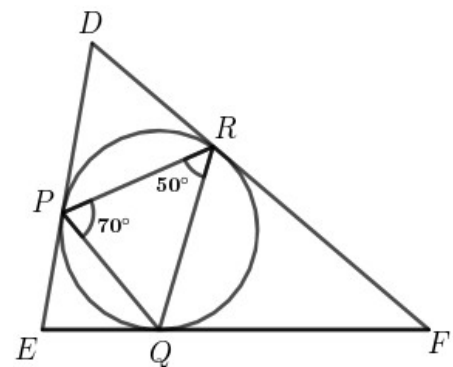
- What is the measure of  $\angle CQD$  ?
- What is the measure of  $\angle CDQ$  ?
- What is the measure of  $\angle ODC$  ?

29 In the figure , the circle touches the sides of the triangle  $ABC$  at the points  $P, Q, R$ .  
 $\angle A = 60^\circ$  ,  $\angle B = 50^\circ$



- What is the measure of  $\angle BQP$  ?
- What is the measure of  $\angle PRQ$  ?
- What is the measure of  $\angle PQR$  ?

30 In the figure , the circle touches the sides of the triangle  $DEF$  at the points  $P, Q, R$ .  
 $\angle QPR = 70^\circ$  ,  $\angle PRQ = 50^\circ$



- What is the measure of  $\angle EQP$  ?
- What is the measure of  $\angle E$  ?
- What is the measure of  $\angle F$  ?

31 In the figure ,  $O$  is the centre of the incircle .

$\angle B = 90^\circ$  ,  $BC = a$  ,  $AC = b$  ,  $AB = c$

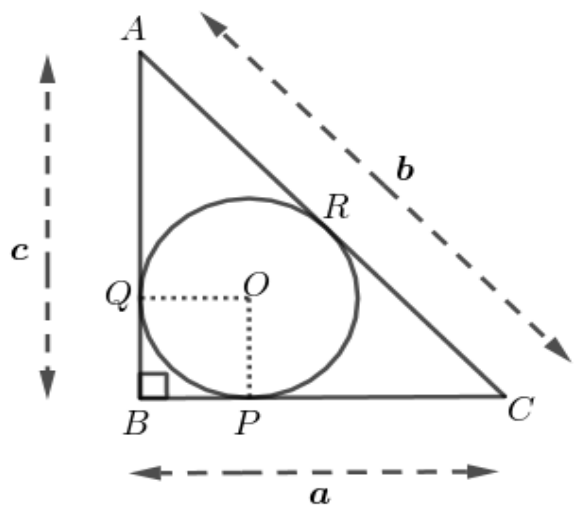
a) What is the measure of  $\angle OPB$  ?

b) Prove that  $BPOQ$  is a square ?

c) If the radius of the incircle is taken as  $r$  ,  
what is the length of  $CP$  ?

d) What is the length of  $AR$  ?

e) Prove that the diameter of the incircle is  $a + c - b$  .



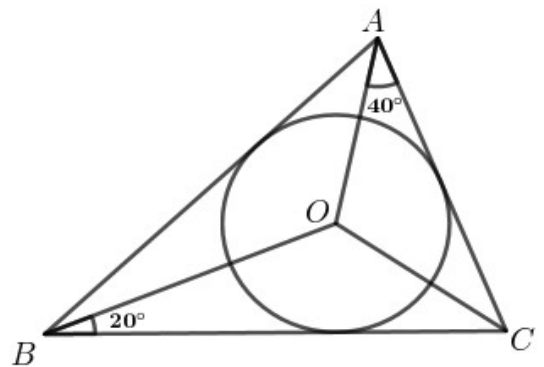
32 In the figure ,  $O$  is the centre of the incircle .

$\angle OBC = 20^\circ$  ,  $\angle OAC = 40^\circ$

a) What is the measure of  $\angle OBA$  ?

b) What is the measure of  $\angle BAC$  ?

c) What is the measure of  $\angle OCB$  ?

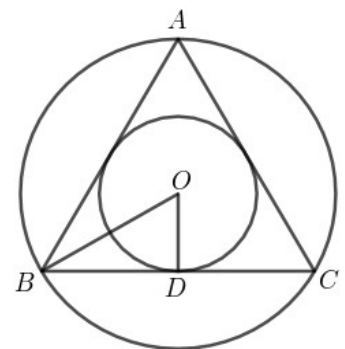


33 In the figure  $ABC$  is an equilateral triangle .  $O$  is the  
centre of the circumcircle and incircle .

a ) What is the measure of  $\angle ODB$  ?

b) What is the measure of  $\angle OBD$  ?

c) Prove that the radius of the circumcircle of  
an equilateral triangle is double its radius of the incircle



34 In the figure ,  $O$  is the centre of the triangle  $ABC$

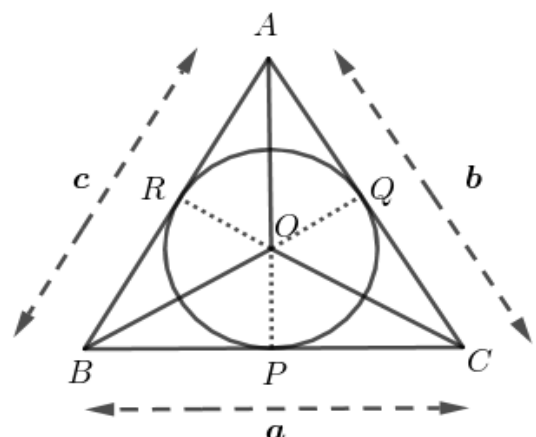
The circle touches the sides of the triangle at  $P$  ,

$Q$  ,  $R$  .  $BC = a$  ,  $AC = b$  ,  $AB = c$

a ) What is the perimeter of the triangle  $ABC$  ?

b) What is the measure of  $\angle OPB$  ?

c) What is the area of the triangle  $BOC$  ?





- d) What is the area of the triangle AOC ?
- e) Prove that the area of a triangle ABC is the product of the radius of its incircle and half its perimeter ?

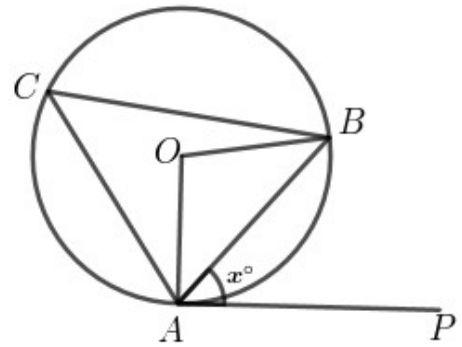
35 The side of an equilateral triangle is 4 cm

- a) What is its perimeter ?
- b) What is its area ?
- c) What is its radius of its incircle ?

36 In the figure O is the centre and AP is a tangent

$\angle BAP = x^\circ$

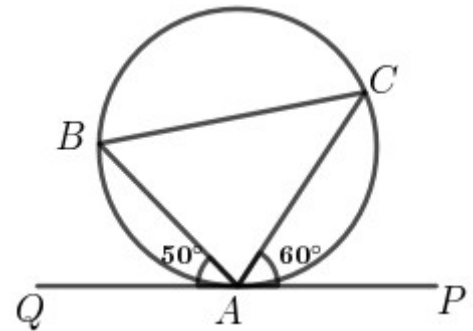
- a) What is the measure of  $\angle OAP$  ?
- b) What is the measure of  $\angle OBA$  ?
- c) What is the measure of  $\angle AOB$  ?
- d) What is the measure of  $\angle ACB$  ?



37 In the figure PQ is a tangent .

$\angle BAQ = 50^\circ, \angle CAP = 60^\circ$

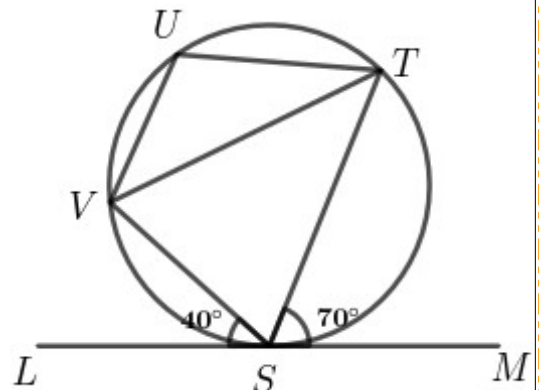
- a) What is the measure of  $\angle BCA$  ?
- b) What is the measure of  $\angle ABC$  ?



38 In the figure LM is a tangent .

$\angle LSV = 40^\circ, \angle TSM = 70^\circ$

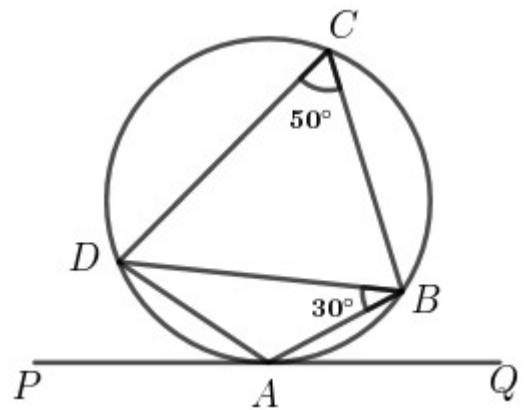
- a) What is the measure of  $\angle STV$  ?
- b) What is the measure of  $\angle SVT$  ?
- c) What is the measure of  $\angle TUV$  ?



39 In the figure  $PQ$  is a tangent.

$\angle ABD = 30^\circ$ ,  $\angle BCD = 50^\circ$

- a) What is the measure of  $\angle BAD$  ?
- b) What is the measure of  $\angle PAD$  ?
- c) What is the measure of  $\angle ADB$  ?

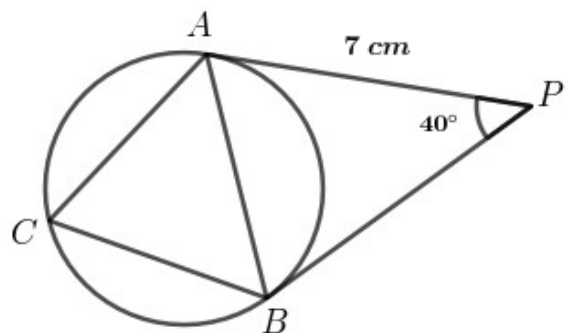


40 In the figure, tangents through the points  $A$  and  $B$

intersect at  $P$ .  $PA = 7\text{ cm}$ ,  $\angle APB = 40^\circ$

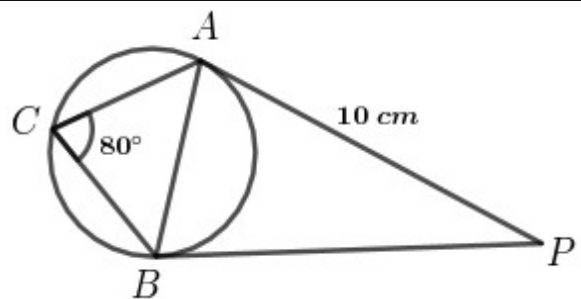
$AC = BC$

- a) What is the length of  $PB$  ?
- b) What is the measure of  $\angle ABP$  ?
- c) What is the measure of  $\angle ACB$  ?
- d) What is the measure of  $\angle CAP$  ?



41 In the figure, tangents through the points  $A$  and  $B$  intersect at  $P$ .  $AC = BC$ ,  $PA = 10\text{ cm}$

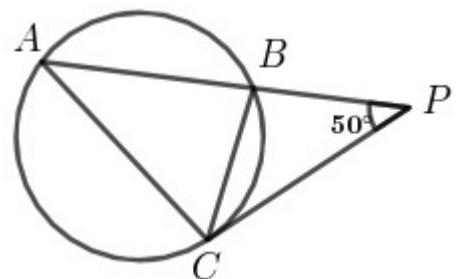
- a) What is the measure of  $\angle ABP$  ?
- b) What is the length of  $PB$  ?
- c) What is the measure of  $\angle APB$  ?
- d) What is the measure of  $\angle CAP$  ?



42 In the figure  $PC$  is a tangent.

$\angle BPC = 50^\circ$ ,  $BC = BP$

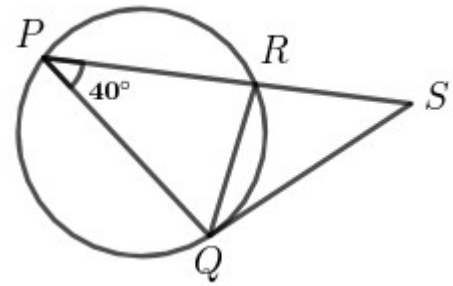
- a) What is the measure of  $\angle BCP$  ?
- b) What is the measure of  $\angle BAC$  ?
- c) What is the measure of  $\angle ABC$  ?



43 In the figure QS is a tangent .

$\angle QPR = 40^\circ$  ,  $RQ = RS$

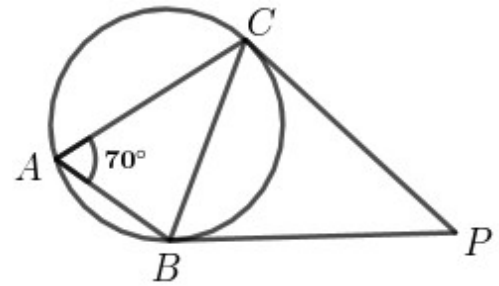
- a) What is the measure of  $\angle RQS$  ?
- b) What is the measure of  $\angle QRS$  ?
- c) What is the measure of  $\angle PQR$  ?



44 In the figure , tangents through the points

B and C intersect at P .  $\angle BAC = 70^\circ$

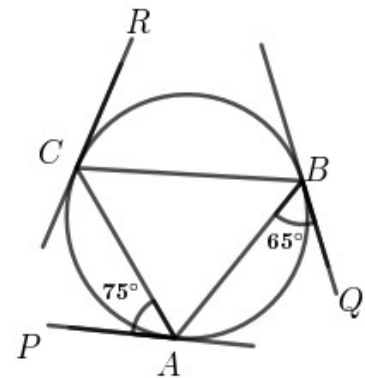
- a) What is the measure of  $\angle PBC$  ?
- b) What is the measure of  $\angle BPC$  ?



45 In the figure PA , QB and C are tangents .

$\angle CAP = 75^\circ$  ,  $\angle BAQ = 65^\circ$

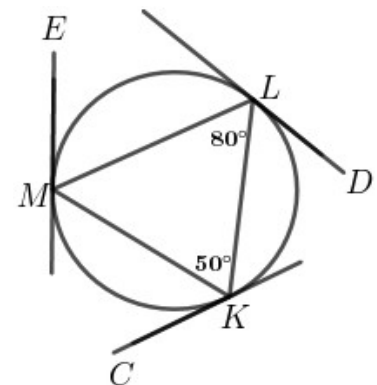
- a) What is the measure of  $\angle ABC$  ?
- b) What is the measure of  $\angle ACB$  ?
- c) What is the measure of  $\angle ACR$  ?



46 In the figure EM , CK and DL are tangents .

$\angle KLM = 80^\circ$  ,  $\angle LKM = 50^\circ$

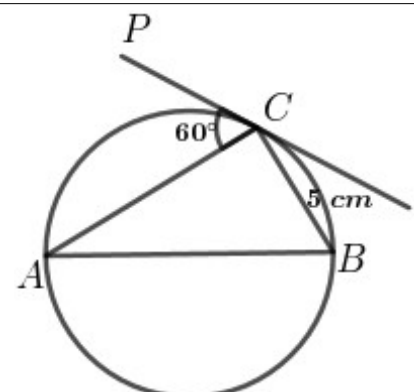
- a) What is the measure of  $\angle CKM$  ?
- b) What is the measure of  $\angle EML$  ?
- c) What is the measure of  $\angle LMD$  ?



47 In the figure AB is the diameter of the circle .

CP is a tangent .  $BC = 5$  cm .

- a) What is the measure of  $\angle ACB$  ?
- b) What is the measure of  $\angle ABC$  ?
- c) What is the diameter of the circle ?

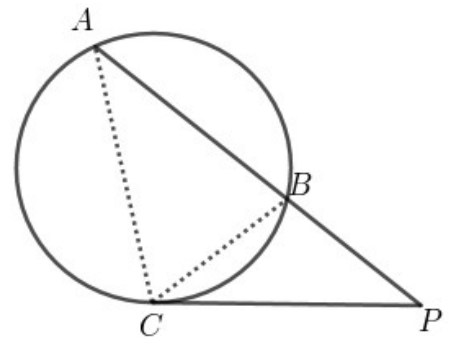


48 In the figure chord  $AB$  is extended to meet the tangent through  $C$  at  $P$ .

a) If  $\angle BCP = x^\circ$ , What is the measure of  $\angle BAC$  ?

b) Prove that the angles of triangles  $APC$  and  $BPC$  are same ?

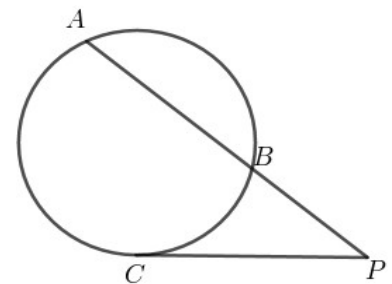
c) Prove that  $PA \times PB = PC^2$  ?



49 In the figure chord  $AB$  is extended to meet the tangent through  $C$  at  $P$ .  $PA = 9$  cm ,  $AB = 5$  cm

a) What is the length of  $PB$  ?

b) What is the length of  $PC$  ?

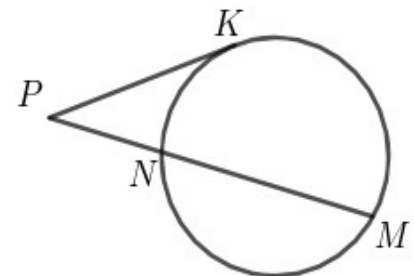


50 In the figure chord  $MN$  is extended to meet the tangent through  $K$  at  $P$ .

$PK = 8$  cm ,  $PN = 4$  cm

a)  $PM \times PN = \dots\dots\dots$

b) What is the length of  $MN$  ?



52 In the figure two chords  $AB$  and  $CD$  are extended to meet the tangent through  $E$  at  $P$ .

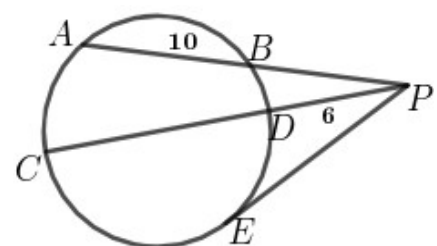
$PA = 18$  cm ,  $AB = 10$  cm ,  $PD = 6$  cm

a) What is the length of  $PB$  ?

b)  $PC \times PD = \dots\dots\dots$

c) What is the length of  $CD$  ?

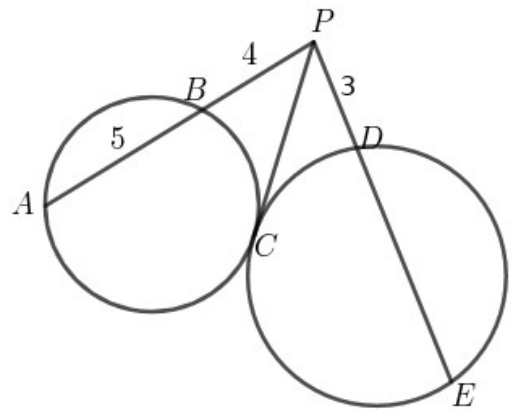
d) What is the length of the tangent  $PE$  ?



53 In the figure two circles intersect at  $C$  and  $CP$  is a common tangent to both the circles .

$AB = 5 \text{ cm}$  ,  $PB = 4 \text{ cm}$  ,  $PD = 3 \text{ cm}$

- What is the length of  $PA$  ?
- What is the length of the tangent  $PC$  ?
- What is the length of  $DE$  ?

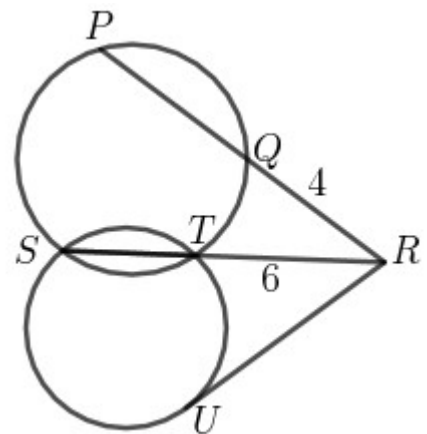


54 In the figure two circles intersect at  $S$  and  $T$  .

$RU$  is a tangent .

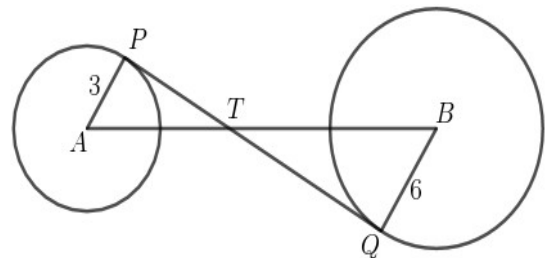
$PQ = 8 \text{ cm}$  ,  $QR = 4 \text{ cm}$  ,  $TR = 6 \text{ cm}$

- What is the length of  $PR$  ?
- What is the length of  $RS$  ?
- What is the length of the tangent  $RU$  ?

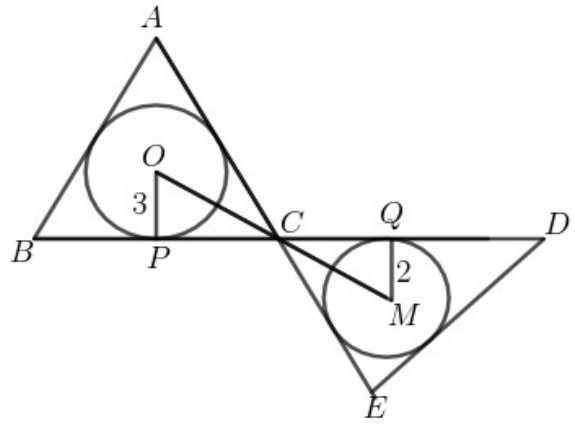


55 In the figure  $A$  and  $B$  are the centres of the circles and  $PQ$  is a common tangent .  
The distance between the centres of the circles is  $15 \text{ cm}$  . The radius of the smaller circle is  $3 \text{ cm}$  and radius of the larger circle is  $6 \text{ cm}$  .

- What is the measure of  $\angle APT$  ?
- What is the measure of  $\angle BQT$  ?
- Prove that the angles of the triangles  $APT$  and  $BQT$  are same ?
- Prove that  $\frac{AT}{BT} = \frac{1}{2}$  ?
- What is the length of the tangent  $PQ$  ?



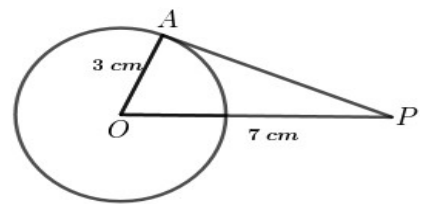
56 In the figure  $ABC$  is an equilateral triangle .  
 $O$  is the centre of the incircle of the triangle  
 $ABC$  and  $M$  is the centre of the incircle of  
the triangle  $CDE$  .  $OP = 3\text{ cm}$  ,  $MQ = 2\text{ cm}$



- What is the measure of  $\angle OPC$  ?
- What is the measure of  $\angle OCP$  ?
- What is the measure of  $\angle QCM$  ?
- What is the distance between the centres of the circles ?

57 Draw a circle of radius 4 cm and mark a point on it . Draw a tangent through that point

58 In the figure  $O$  is the centre of the circle .  
 $AP$  is a tangent .



- What is the measure of  $\angle OAP$  ?
- Draw this figure in correct measurements .

59 Draw a circle of radius 2.5 cm and mark a point 6 cm away from its centre. Draw the tangents to the circle from this point . Measure the length of the tangents .

60 Draw a circle of radius 3.5 cm and mark a point 8 cm away from its centre. Draw the tangents to the circle from this point . Measure the length of the tangents .

61 Draw a circle of radius 2.5 cm . Draw a triangle of angles  $50^\circ$  ,  $60^\circ$  ,  $70^\circ$  with all its sides touching the circle .

62 Draw a circle of radius 3 cm . Draw a triangle of angles  $55^\circ$  ,  $50^\circ$  ,  $75^\circ$  with all its sides touching the circle .

### EXTRA QUESTIONS

63 Draw a triangle of sides 3 cm , 4 cm , 6 cm . Draw its incircle and measure its radius

64 Draw a triangle of sides 4 cm , 6 cm , 7 cm . Draw its incircle and measure its radius

65 In the figure ,  $\angle B = 90^\circ$  .  $AB = f$  ,  $BC = g$  ,  $AC = h$

- What is the perimeter of the triangle ?
- What is the radius of the incircle of the triangle ?
- If the radius of the incircle is  $r$  , prove that the area of the triangle is  $r ( r + h )$

