

- i. Find the value of $\sin 75^\circ$.
- ii. Hence deduce the value of $\cos 15^\circ$.

Solution

$$\begin{aligned}\sin 75^\circ &= \sin(45^\circ + 30^\circ) \\ &= \sin 45^\circ \cos 30^\circ + \cos 45^\circ \sin 30^\circ \\ &= \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2} = \frac{\sqrt{3} + 1}{2\sqrt{2}}\end{aligned}$$

$$\cos 15^\circ = \sin (90^\circ - 15^\circ) = \sin 75^\circ$$

$$\cos 15^\circ = \frac{\sqrt{3} + 1}{2\sqrt{2}}$$