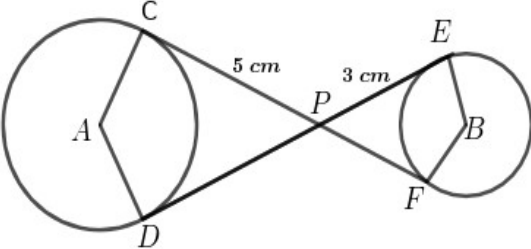
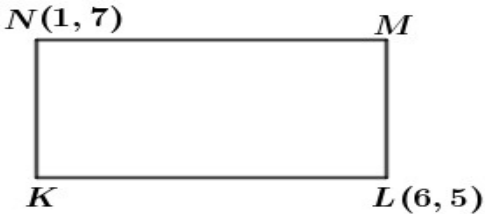
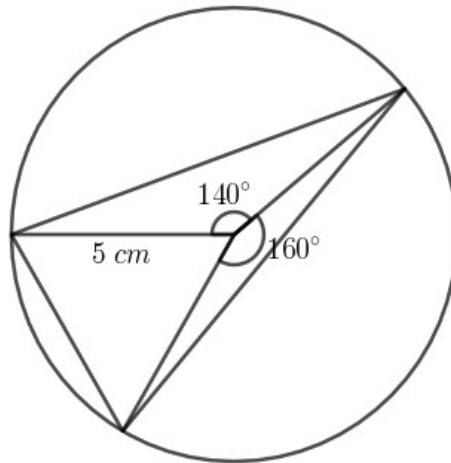


	<p><u>Answer .</u></p> $\sin A = \frac{\text{opposite side of } \angle A}{\text{hypotenuse}} = \frac{BC}{AC} = \frac{3}{5} \implies \cos C = \frac{\text{adjacent side of } \angle C}{\text{hypotenuse}} = \frac{BC}{AC} = \frac{3}{5}$
5	<p>What are the coordinates of the midpoint of the line joining the points (1 , 2) , (5 , 8)</p> <p>((6 , 8) , (8 , 6) , (3 , 5) , (4 , 3))</p>
	<p><u>Answer .</u></p> $\left(\frac{1+5}{2}, \frac{2+8}{2} \right) = \left(\frac{6}{2}, \frac{10}{2} \right) = (3,5)$
<p>For questions from 6 to 10 carries 2 scores each .</p>	
6	<p>Fifth term of an arithmetic sequence is 21 and its ninth term is 37 .</p> <p>a) What is its common difference ?</p> <p>b) What is its first term ?</p>
	<p><u>Answer .</u></p> <p>a) $\text{common difference} = \frac{\text{term difference}}{\text{position difference}} = \frac{37-21}{9-5} = \frac{16}{4} = 4$</p> <p>b) $\text{First term} = x_5 - 4 \times d = 21 - 4 \times 4 = 21 - 16 = 5$</p> <p>{ or $\text{First term} = x_9 - 8 \times d = 37 - 8 \times 4 = 37 - 32 = 5$ }</p>
7	<p>In the figure ,A and B are the centres of the circles and tangents are drawn from a point P to the circles . PC = 5 cm , PE = 3 cm</p> <p>a) What is the length of PD ?</p> <p>b) What is the length of CF ?</p>
	
	<p><u>Answer .</u></p> <p>a) PD = 5 cm . (PC = PD , The tangents to a circle from a point are of the same length)</p> <p>b) CF = PC + PF = 5 + 3 = 8 cm . (PE =PF = 3 cm)</p>

8	<p>The base radius and height of a cone are 9 centimetres and 12 centimetres .</p> <p>a) What is its slant height ?</p> <p>b) What is its curved surface area ?</p> <p><u>Answer.</u></p> <p>a) Slant height = $\sqrt{r^2+h^2}=\sqrt{9^2+12^2}=\sqrt{81+144}=\sqrt{225}=15$ cm</p> <p>b) Curved surface area = $\pi \times r \times l = \pi \times 9 \times 15 = 135\pi$ sq. cm</p>
9	<p>A circle of radius 5 is drawn with origin as centre.</p> <p>a) Write down the coordinates of a point at which the circle cuts the x-axis ?</p> <p>b) If (p , q) is a point on this circle , prove that $p^2 + q^2 = 25$.</p> <p><u>Answer.</u></p> <p>a) (5 , 0) or (- 5 , 0)</p> <p>b) Radius = 5 $\implies \sqrt{(p-0)^2+(q-0)^2}=5 \implies \sqrt{p^2+q^2}=5$</p> $p^2+q^2 = 5^2 = 25$
10	<p>In the figure sides of the rectangle KLMN are parallel to the axes .</p> <p>a)What are the coordinates of K ?</p> <p>b)What are the coordinates of M ?</p> <div style="text-align: center;">  </div> <p><u>Answer.</u></p> <p>a) Coordinates of K = (1 , 5)</p> <p>b) Coordinates of M = (6 , 7)</p>
<p>For questions from 11 to 20 carries 3 scores each .</p>	
11	<p>Draw a triangle of circumradius 5 cm and two of the angles 70° and 80° .</p>



12 Consider the arithmetic sequence 8 , 15 , 22 ,

a) What is its common difference ?

b) What is its sixth term ?

c) What is the sum of first 11 terms of this sequence ?

Answer .

a) Common difference = $15 - 8 = 7$

b) Sixth term = $8 + 5 \times 7 = 8 + 35 = 43$

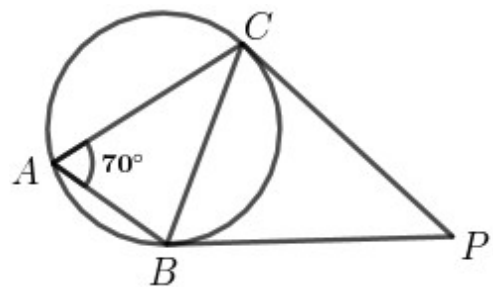
c) Sum of first 11 terms = $11 \times \text{midterm} = 11 \times x_6 = 11 \times 43 = 473$

13 In the figure , tangents through the points

B and C intersect at P . $\angle BAC = 70^\circ$

a) What is the measure of $\angle PBC$?

b) What is the measure of $\angle BPC$?

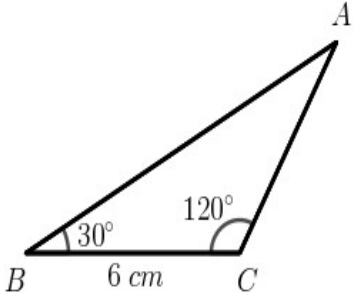


Answer .

a) $\angle PBC = 70^\circ$ (In a circle , the angle which a chord makes with the tangent at one end on any side is equal to the angle which it makes on the part of the circle on the other side)

b) $\angle PBC = \angle PCB = 70^\circ$ ($PB = PC$)

$\angle BPC = 180 - (70 + 70) = 180 - 140 = 40^\circ$.

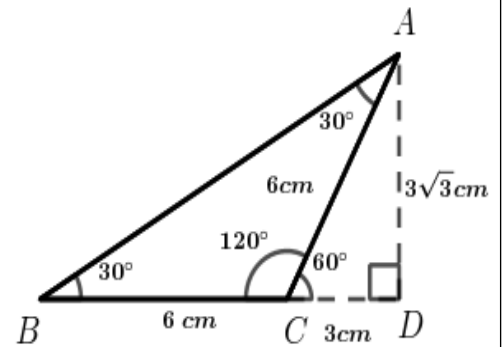
14	<p>A dice with faces numbered from 1 to 6 is rolled .</p> <p>a) What is the probability of getting an even number ?</p> <p>b) What is the probability of getting an odd number ?</p> <p>c) What is the probability of getting a perfect square ?</p>
	<p><u>Answer .</u></p> <p>a) Probability of getting an even number = $\frac{\text{Number of favourable results}}{\text{Total number of results}}$</p> <p style="text-align: center;">$= \frac{3}{6}$</p> <p>b) Probability of getting an odd number = $\frac{3}{6}$</p> <p>c) Probability of getting a perfect square = $\frac{2}{6}$</p> <p style="text-align: center;">{ Favourable results == > a) (2 , 4 , 6) b) (1 , 3 , 5) c) (1 , 4) }</p>
15	<p>When each side of a square was increased by 4 metres , the area became 256 square metres .</p> <p>a) Write down a second degree equation by taking the side of the original square as x</p> <p>b) What was the length of a side of the original square ?</p>
	<p><u>Answer .</u></p> <p>a) $(x+4)^2 = 256$</p> <p>b) $x+4 = \sqrt{256} = 16$</p> <p style="text-align: center;">$x = 16 - 4 = 12 \implies$ side of the original square = 12 m</p>
16	<p>In triangle ABC , $\angle B = 30^\circ$, $\angle C = 120^\circ$, $BC = 6\text{ cm}$</p> <p>a) What is the measure of $\angle A$?</p> <p>b) What is the perpendicular distance from A to the side BC</p> <p>c) What is the area of the triangle ?</p> <div style="text-align: right;">  </div>

Answer .

a) $\angle A = 180 - (30 + 120) = 180 - 150 = 30^\circ$

b) ABC is an isosceles triangle .

So $BC = AC = 6 \text{ cm}$.



Draw the perpendicular from A to the side BC .

In triangle ACD , $AD = 3\sqrt{3} \text{ cm}$

c) Area of the triangle ABC = $\frac{1}{2} \times BC \times AD = \frac{1}{2} \times 6 \times 3\sqrt{3} = 9\sqrt{3} \text{ sq. cm}$

17 If $p(x) = x^2 - 8x + 15$

a) Find $p(3)$?

b) Check whether $x - 5$ is a factor of $p(x)$ or not ?

c) Write $p(x)$ as the product of two first degree polynomials ?

Answer .

a) $p(3) = 3^2 - 8 \times 3 + 15 = 9 - 24 + 15 = 24 - 24 = 0$

b) $p(5) = 5^2 - 8 \times 5 + 15 = 25 - 40 + 15 = 40 - 40 = 0 \implies x - 5$ is a factor .

c) $p(x) = (x - 3)(x - 5)$

18 The marks obtained by 9 students in a maths exam are given below .

68 , 72 , 76 , 62 , 70 , 64 , 60 , 74 , 66

a) What is the mean mark ? .

b) What is the median mark .

Answer .

a) $Mean = \frac{60 + 62 + 64 + 66 + 68 + 70 + 72 + 74 + 76}{9} = \frac{612}{9} = 68$

b) 60 , 62 , 64 , 66 , 68 , 70 , 72 , 74 , 76

Median = 68

- 19 The base radii of two cones are in the ratio 3 : 4 and their slant heights are in the ratio 5 : 6
- If the base radius of the first cone is taken as $3r$, what will be the base radius of the second cone ?
 - What is the ratio of their curved surface areas ?
 - If the curved surface area of the first cone is 180π square centimetres, what will be the curved surface area of the second cone ?

Answer.

a) $r_1 = 3r \implies r_2 = 4r$

b) $l_1 = 5l \implies l_2 = 6l$

Ratio of the curved surface areas = $\pi \times 3r \times 5l : \pi \times 4r \times 6l = 15 : 24$

c) Curved surface area of the second cone = $\frac{24 \times 180}{15} = 288\pi$ sq.cm

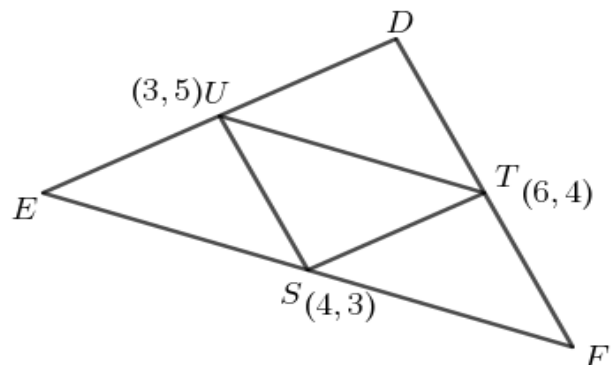
- 20 In the figure S, T, U are the midpoints of the sides of the triangle DEF

$S(4, 3)$, $T(6, 4)$, $U(3, 5)$

a) What are the coordinates of E ?

b) What are the coordinates of F ?

c) What are the coordinates of D ?



Answer.

a) $(3+4-6, 5+3-4) = (1, 4)$ (ESTU is a parallelogram)

b) $(4+6-3, 3+4-5) = (7, 2)$ (SFTU is a parallelogram)

c) $(3+6-4, 5+4-3) = (5, 6)$ (STDU is a parallelogram)

For questions from 21 to 30 carries 4 scores each .

21 Compute the following sums .

a) $1 + 2 + 3 + 4 + 5 + \dots + 20$

b) $4 + 8 + 12 + 16 + 20 + \dots + 80$

c) $5 + 9 + 13 + 17 + 21 + \dots + 81$

d) $9 + 17 + 25 + 33 + 41 + \dots + 161$

Answer.

a) $1 + 2 + 3 + 4 + 5 + \dots + 20 = \frac{20 \times 21}{2} = 210$

b) $4 + 8 + 12 + 16 + 20 + \dots + 80 = 4 \times 210 = 840$

c) $5 + 9 + 13 + 17 + 21 + \dots + 81 = 840 + 20 \times 1 = 840 + 20 = 860$

d) $9 + 17 + 25 + 33 + 41 + \dots + 161 = 840 + 860 = 1700$

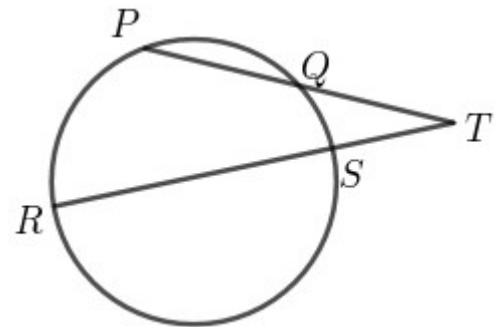
22 In the figure ,chords PQ and RS are extended to meet at T. RT = 18 cm ,RS = 14 cm

Q is the midpoint of PT .

a) **What is the length of TS ?**

b) **TP x TQ =**

c) **What is the length of PQ**



Answer.

a) $TS = 18 - 14 = 4 \text{ cm}$

b) $TP \times TQ = TR \times TS = 18 \times 4 = 72$

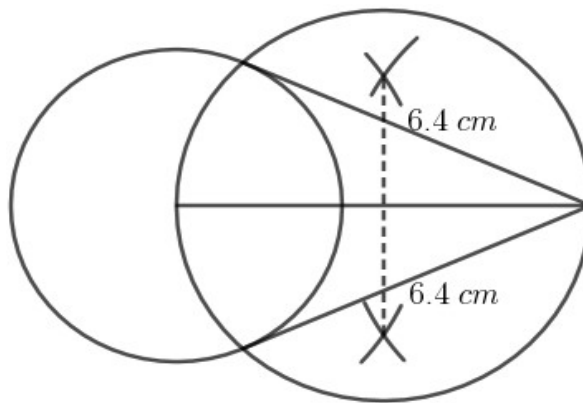
c) $TQ = PQ$ (Q is the mid point of PT)

$2TQ \times TQ = 72$

$TQ^2 = \frac{72}{2} = 36 \implies TQ = \sqrt{36} = 6$

$PQ = 6 \text{ cm}$

- 23 Draw a circle of radius 3 cm and mark a point 7 cm away from its centre.
Draw the tangents to the circle from this point . Measure the length of the tangents .



- 24 One is asked to say a two -digit number .
- How many two digit numbers are there ?
 - What is the smallest possible product of the digits ?
 - What is the largest possible product of the digits ?
 - What is the probability of the product of the digits being a perfect square ?

Answer .

a) 90

b) 0

c) 81

d) Favourable results = 11 , 14 , 22 , 41 , 19 , 33 , 91 , 28 , 44 , 82 , 55 , 49 , 66 , 94 ,
77 , 88 , 99

Probability of the product of

the digits being a perfect square = $\frac{\text{Number of favourable results}}{\text{Number of total results}}$

$$= \frac{17}{90}$$

25 The longer side of a rectangle is 4 centimetres more than its shorter side . The area of the rectangle is 672 square centimetres .

a) Write down a second degree equation by taking the shorter side as x

b) What are the lengths of its the sides ?

Answer .

a) Shorter side = x

Longer side = $x+4$

$$(x+4)x = 672 \implies x^2+4x = 672$$

b) $x^2+4x +2^2= 672+2^2$

$$(x+2)^2 = 672+4=676$$

$$x+2 = \sqrt{676}=26$$

$$x = 26-2 = 24$$

Shorter side = $x = 24 \text{ cm}$

Longer side = $x+4 = 24+4 = 28 \text{ cm}$

26 A man standing on the top of a building sees the base of a tower at a depression of 45° and its top at a depression of 30° . The distance between the building and tower is 90 metres .

a) Draw a rough figure based on the given details ?

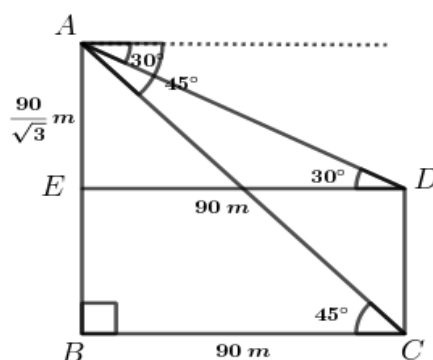
b) What is the height of the building ?

c) What is the height of the tower ?

Answer .

Height of the building = CD

Height of the tower = AB



b) In triangle ABC ,

$$AB = BC = 90 \text{ m} \quad (AB : BC : AC := 1 : 1 : \sqrt{2})$$

$$\text{Height of the tower} = AB = 90 \text{ m}$$

c) In triangle AED ,

$$DE = 90 \text{ m} \implies AE = \frac{90}{\sqrt{3}} \text{ m} \quad (AE : DE : AD := 1 : \sqrt{3} : 2)$$

$$\text{Height of the building} = CD = BE = AB - AE = 90 - \frac{90}{\sqrt{3}} \text{ m}$$

27 If $p(x) = x^2 + 3x + 2$

a) Find $p(1)$?

b) Write a factor of $p(x) - p(1)$?

c) Write $p(x) - p(1)$ as the product of two first degree polynomials ?

Answer .

a) $p(1) = 1^2 + 3 \times 1 + 2 = 1 + 3 + 2 = 6$

b) $(x - 1)$

c) $p(x) - p(1) = x^2 + 3x + 2 - 6 = x^2 + 3x - 4$

$$x^2 + 3x - 4 = (x - 1)(x + 4)$$

28 55 households in a neighbourhood are sorted according to their monthly income in the table below .

Monthly income (Rs)	Number of households
4000	6
5000	9
6000	10
7000	9
8000	8
9000	7
10000	6

- a) If the households are arranged in increasing order of monthly income , what is the monthly income of the household at the 26th position ?
- b) If the households are arranged in increasing order of monthly income , the monthly income of the household at what position is taken as the median ?
- c) Find the median of the monthly income ?

Answer .

Monthly income	Number of households
Up to 4000	6
Up to 5000	15
Up to 6000	25
Up to 7000	34
Up to 8000	42
Up to 9000	49
Up to 10000	55

a) Monthly income of the 26th household = Rs 7000

b) $N=55$

$$\frac{N+1}{2} = \frac{55+1}{2} = \frac{56}{2} = 28$$

Median = Monthly income of the 28th household .

c) median monthly income = Rs 7000

29 A sector of area 100π square centimetres is rolled up into a cone of base radius 5 centimetres .

- a) What is curved surface area of the cone ?
- b) What is the slant height of the cone ?
- c) What is the radius of the sector ?
- d) What is the central angle of the sector ?

Answer .

a) curved surface area of the cone = Area of the sector = 100π sq.cm

$$\text{b) } \pi \times r \times l = 100\pi \implies \pi \times 5 \times l = 100\pi \implies l = \frac{100\pi}{5\pi} = 20$$

Slant height of the cone = 20 cm

c) Radius of the sector = Slant height of the cone = 20 cm

$$\text{d) } \frac{x}{360} = \frac{r}{R} \implies \frac{x}{360} = \frac{5}{20} \implies x = \frac{5 \times 360}{20} = 90^\circ$$

Central angle of the sector = 90°

30 The vertices of a triangle are A (1 , 9) , B (4 , 6) , C (3 , 11)

a) What is the length of AB ?

b) What is the length of BC ?

c) Prove that ABC is a right triangle ?

Answer .

$$\text{a) } AB = \sqrt{(4-1)^2 + (6-9)^2} = \sqrt{3^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18}$$

$$\text{b) } BC = \sqrt{(3-4)^2 + (11-6)^2} = \sqrt{(-1)^2 + 5^2} = \sqrt{1+25} = \sqrt{26}$$

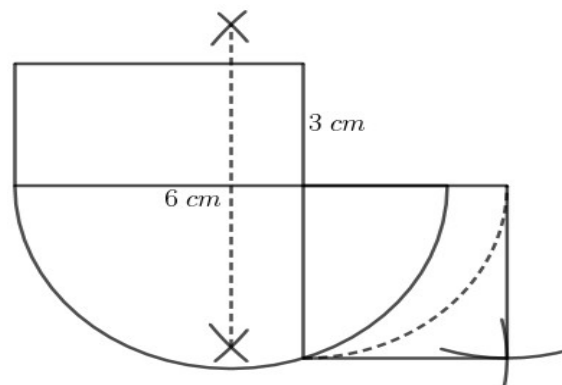
$$\text{c) } AC = \sqrt{(3-1)^2 + (11-9)^2} = \sqrt{2^2 + 2^2} = \sqrt{4+4} = \sqrt{8}$$

$$AB^2 + AC^2 = (\sqrt{18})^2 + (\sqrt{8})^2 = 18 + 8 = 26 = (\sqrt{26})^2 = BC^2$$

So ABC is a right triangle .

For questions from 31 to 45 carries 5 scores each .

31 Draw a rectangle of width 6 cm and height 3 cm . Draw a square of the same area .



32 Look at the number pattern given below.

1

2 3

4 5 6

7 8 9 10

.....

.....

- a) Write down the next two more lines of this pattern ?
- b) How many numbers are there in the 20th line ?
- c) What is the last number in the 19th line ?
- d) What is the first number in the 20th line ?

Answer.

a) 11 12 13 14 15

16 17 18 19 20 21

b) 20

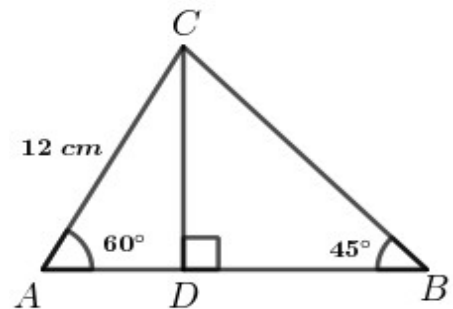
c) $\frac{19 \times 20}{2} = 190$

d) $190 + 1 = 191$

33 In the figure $AC = 12\text{ cm}$, $\angle A = 60^\circ$, $\angle B = 45^\circ$

The line CD is perpendicular to the side AB .

- a) What is the measure of $\angle ACB$?
- b) What is the length of CD ?
- c) What is the area of triangle ABC ?



d) What is the ratio of the length of the sides if the ratio of angles of a triangle is 3:4:5

Answer .

a) $\angle ACB = 30 + 45 = 75^\circ$

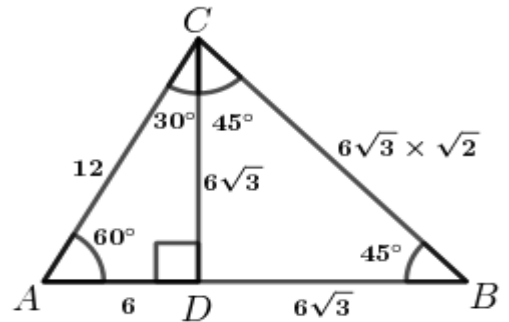
b) $CD = 6\sqrt{3} \text{ cm}$

c) Area of the triangle ABC = $\frac{1}{2} \times AB \times CD$
 $= \frac{1}{2} \times (6 + 6\sqrt{3}) \times 6\sqrt{3} \text{ sq. cm}$

d) Ratio of the angles = 3:4:5

Angles = $180 \times \frac{3}{12}$, $180 \times \frac{4}{12}$, $180 \times \frac{5}{12} = 45^\circ$, 60° , 75°

Ratio of the sides = $12 : 6\sqrt{6} : 6\sqrt{3} + 6 = 2 : \sqrt{6} : \sqrt{3} + 1$



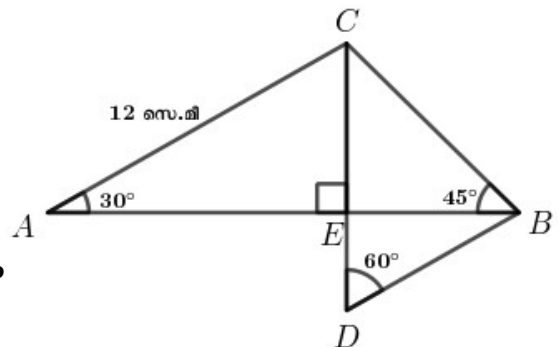
34 In the figure $\angle BAC = 30^\circ$, $\angle ABC = 45^\circ$, $\angle AEC = 90^\circ$, $\angle BDE = 60^\circ$, $AC = 12 \text{ cm}$

a) What is the length of CE ?

b) What is the length of BE ?

c) What is the length of AB ?

d) What is the area of the triangle BCD ?



Answer .

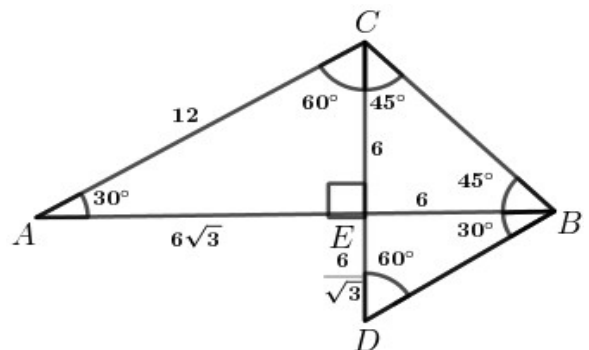
a) $CE = 6 \text{ cm}$

b) $BE = 6 \text{ cm}$

c) $AB = 6\sqrt{3} + 6 \text{ cm}$

d) $CD = 6 + \frac{6}{\sqrt{3}} \text{ cm}$

Area of the triangle BCD = $\frac{1}{2} \times CD \times BE = \frac{1}{2} \times (6 + \frac{6}{\sqrt{3}}) \times 6 \text{ sq. cm}$



35 If $x^2+3x-18=(x-a)(x-b)$

a) What is the value of $a+b$?

b) What is the value of ab ?

c) Write $x^2+3x-18$ as the product of two first degree polynomials ?

Answer .

a) $a+b=-3$

b) $ab=-18$

c) $a=-6$

$b=3$

$x^2+3x-18 = (x+6)(x-3)$

36 Consider the arithmetic sequence 63 , 58 , 53 ,

a) What is its common difference ?

b) What is the remainder when each positive term of this sequence is divided by 5 ?

c) Which is the smallest positive number in this sequence ?

d) What is its algebraic form ?

e) How many positive numbers are there in this sequence ?

Answer .

a) -5

b) 3

c) 3

d) $dn+f-d = -5n+63-(-5) = -5n+68$

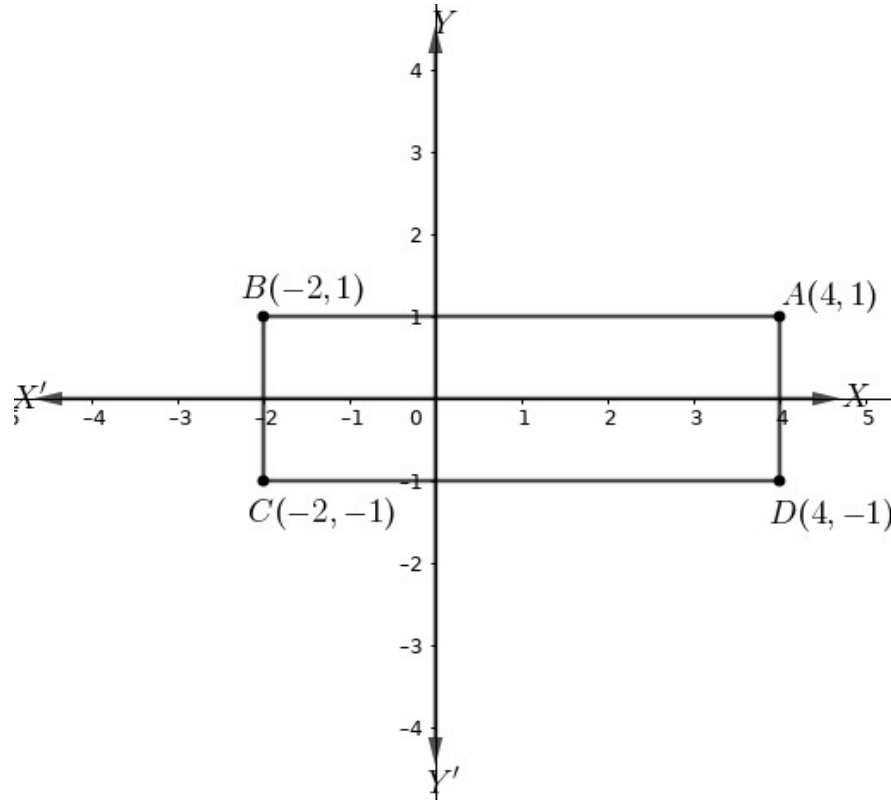
e) $x_n=3 \rightarrow -5n+68=3 \rightarrow 5n=65 \rightarrow n=\frac{65}{5}=13$

- 37 a) Draw the axes and mark the following points $A(4, 1)$, $B(-2, 1)$, $C(-2, -1)$
 $D(4, -1)$.

b) Write the most suitable name of the quadrilateral ABCD ?

Answer.

a)



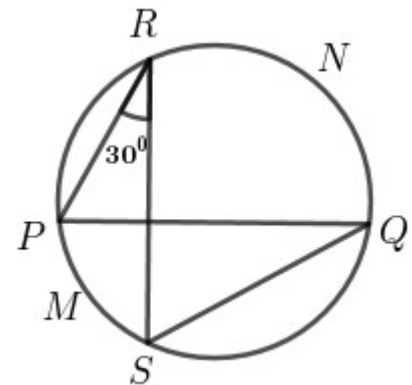
b) Rectangle

- 38 In the figure the chords PQ and RS are perpendicular to each other. $\angle PRS = 30^\circ$

a) What is the measure of $\angle PQS$?

b) What is the central angle of the arc PMS ?

c) What is the sum of the central angles of the arcs PMS and RNQ ?



Answer.

a) $\angle PQS = \angle PRS = 30^\circ$ (All angles made by an arc on the alternate arc are equal)

b) Central angle of the arc PMS = $2 \times \angle PRS = 2 \times 30 = 60^\circ$

(The central angle of an arc is double the angle made by it on the alternate arc)

c) $\angle RPQ = \angle RSQ = 60^\circ$

Central angle of the arc RNQ = $2 \times \angle RPQ = 2 \times 60^\circ = 120^\circ$

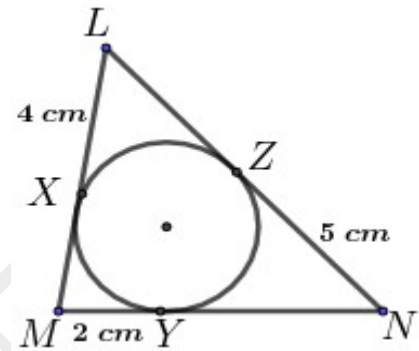
Sum of the central angles of the arcs PMS and RNQ = $60^\circ + 120^\circ = 180^\circ$

39 In the figure , the circle touches the sides of the triangle LMN at the points X , Y , Z
 $LX = 4 \text{ cm}$, $MY = 2 \text{ cm}$, $NZ = 5 \text{ cm}$.

a) What is the length of LZ ?

b) What is the length of MN ?

c) What is the perimeter of the triangle LMN ?



Answer .

a) $LZ = LX = 4 \text{ cm}$ (The tangents to a circle from a point are of the same length)

b) $MX = MY = 2 \text{ cm}$

$YN = NZ = 5 \text{ cm}$

$MN = 2 + 5 = 7 \text{ cm}$

c) $LN = 5 + 4 = 9 \text{ cm}$

$LM = 4 + 2 = 6 \text{ cm}$

Perimeter of the triangle LMN = $LM + MN + LN = 6 + 7 + 9 = 22 \text{ cm}$

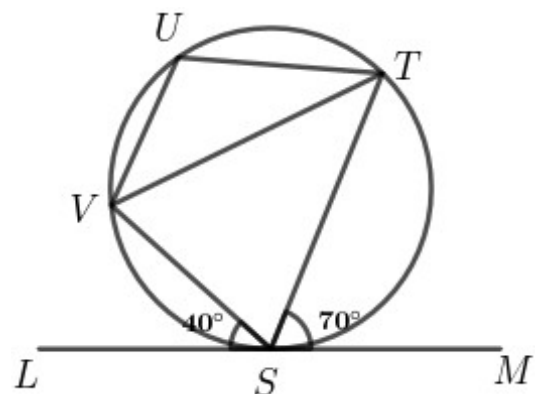
40 In the figure LM is a tangent . $TU = VU$

$\angle LSV = 40^\circ$, $\angle TSM = 70^\circ$

a) What is the measure of $\angle STV$?

b) What is the measure of $\angle SVT$?

c) What is the measure of $\angle TUV$?



Answer .

a) $\angle STV = 40^\circ$ (In a circle , the angle which a chord makes with the tangent at one end on any side is equal to the angle which it makes on the part of the circle on the other side)

b) $\angle SVT = 70^\circ$

c) $\angle TSV = 180 - 110 = 70^\circ$ (Sum of the angles of a triangle is 180°)

$\angle TUV = 110^\circ$ (STUV is cyclic . The opposite angles of a cyclic quadrilateral are supplementary)

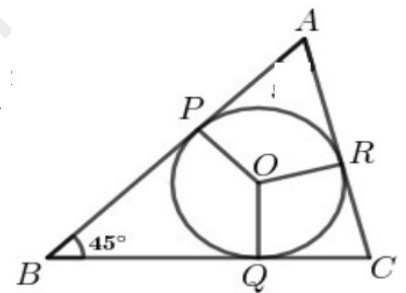
d) $\angle TVU = \frac{180 - 110}{2} = \frac{70}{2} = 35^\circ$ (TU = VU)

41 In the figure O is the centre of the incircle . The circle touches the sides of the triangle at the points P , Q and R

$\angle ABC = 45^\circ$

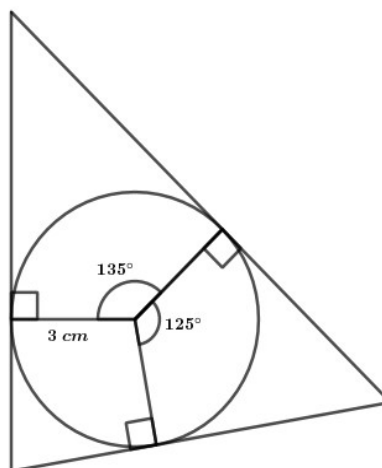
a) What is the measure of $\angle POQ$?

b) Draw a circle of radius 3 cm . Draw a triangle of angles 45° , 55° , 80° with all its sides touching this circle .

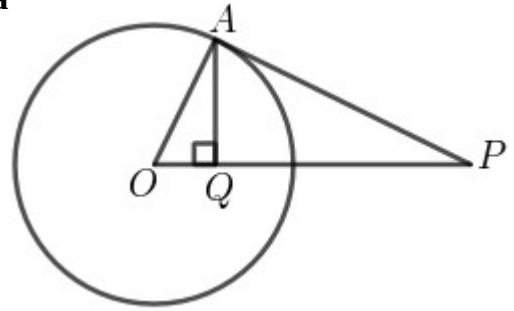


Answer .

a) $\angle POQ = 180 - 45 = 135^\circ$ (In a circle , the angles between the radii through two points and the angle between the tangents at these points are supplementary)



42 In the figure, O is the centre of the circle. AP is a tangent. AQ is perpendicular to OP.



- What is the measure of $\angle OAP$?
- Prove that the angles of the triangles OAP and OAQ are same ?
- Prove that $OP \times OQ = OA^2$?

Answer .

- $\angle OAP = 90^\circ$ (The tangent at a point on a circle is perpendicular to the radius through that point)
- $\angle OAP = \angle OQA = 90^\circ$, $\angle AOP = \angle AOQ$, $\angle OPA = \angle OAQ$
- Since the angles of the triangles OAP and OAQ are equal , their sides taken in the order of size , are in the same ratio

$$\frac{OP}{OA} = \frac{OA}{OQ}$$

$$OP \times OQ = OA \times OA$$

$$OP \times OQ = OA^2$$

43 A conical fire work is of base perimeter 10π centimetres and height 12 centimetres . 10000 such fire works are to be wrapped in colour paper .The price of the colour paper is 10 rupees per square metre.

- What is the base radius of a fire work ?
- What is the slant height of a fire work ?
- What is the surface area of a fire work ?
- What is the total cost ?

(hint : $\pi = 3.14$)

Answer .

a) Radius of a fire work = $\frac{10 \pi}{2 \pi} = 5 \text{ cm}$

b) Slant height of a fire work = $\sqrt{r^2+h^2} = \sqrt{5^2+12^2} = 13 \text{ cm}$

c) Surface area of a fire work = $\pi \times 5^2 + \pi \times 5 \times 13 = 90 \pi \text{ sq. cm}$
= $\frac{90 \pi}{10000} \text{ sq. m}$

d) Total cost = $\frac{90 \times 3.14}{10000} \times 10000 \times 10 = \text{Rs } 2826$

44 The vertices of a triangle are A (3 , 5) , B (9 , 13) , C (10 , 6) .

a) What is the length of the side AB ?

b) Prove that ABC is an isosceles triangle ?

c) What are the coordinates of the midpoint of AB ?

d) What is the area of the triangle ABC ?

Answer .

a) $AB = \sqrt{(9-3)^2 + (13-5)^2} = \sqrt{6^2 + 8^2} = \sqrt{36+64} = \sqrt{100} = 10$

b) $BC = \sqrt{(10-9)^2 + (6-13)^2} = \sqrt{1^2 + (-7)^2} = \sqrt{1+49} = \sqrt{50}$

$AC = \sqrt{(10-3)^2 + (6-5)^2} = \sqrt{7^2 + 1^2} = \sqrt{49+1} = \sqrt{50}$

ABC is an isosceles triangle (BC = AC)

c) Coordinates of the midpoint of AB = $(\frac{3+9}{2}, \frac{5+13}{2}) = (\frac{12}{2}, \frac{18}{2}) = (6,9)$

d) Perpendicular distance from C to the side AB = $h = \sqrt{(6-10)^2 + (9-6)^2} = 5$

(The line joining the common vertex of equal sides to the midpoint of its opposite side of an isosceles triangle is perpendicular to that side)

Area of the triangle ABC = $\frac{1}{2} \times AB \times h = \frac{1}{2} \times 10 \times 5 = 25 \text{ sq. cm}$

45 In the figure $\angle PRQ = 60^\circ$, $\angle QSR = 30^\circ$,

$$\angle RPS = 40^\circ$$

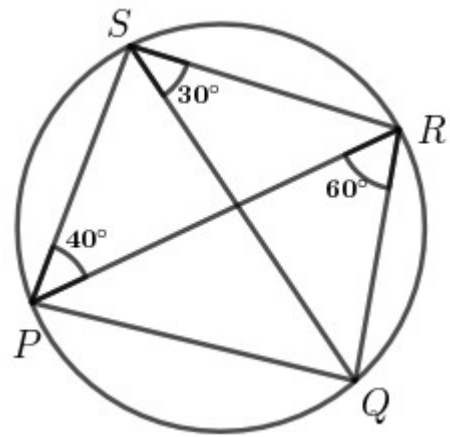
a) What is the measure of $\angle PSQ$?

b) What is the measure of $\angle QPR$?

c) What is the measure of $\angle SQR$?

d) What is the measure of $\angle PQS$?

e) What is the measure of $\angle PRS$?



Answer .

a) $\angle PSQ = 60^\circ$ (All angles made by an arc on the alternate arc are equal)

b) $\angle QPR = 30^\circ$

c) $\angle SQR = 40^\circ$

d) $\angle PQS = 50^\circ$ ($\angle PSR = 60 + 30 = 90^\circ \rightarrow \angle PQR = 90^\circ$

The opposite angles of a cyclic quadrilateral are supplementary)

e) $\angle PRS = 50^\circ$ ($\angle QPS = 30 + 40 = 70^\circ \rightarrow \angle QRS = 110^\circ$)