

Self Evaluation

Mathematics Test 3

2 score

1 hour

25 scores

1) In the polynomial $p(x) = ax^3 + bx^2 + cx + d$, $a + b = -7$, $c + d = 7$ then which of the following is always a factor of $p(x)$?

- (a) $x - 1$ (b) $x + 1$ (c) $x + 2$ (d) $x - 2$

1 score

2) In triangle ABC if $A(0, 0)$, $B(6, 0)$, $C(0, 8)$ then

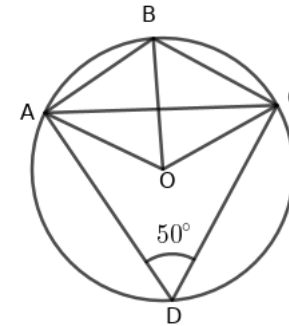
- a) What is the mid point of the side BC ?
- b) What is the radius of the circle passing through the vertices?

2 score

3) The radius and height of a cone are equal. Slant height is 12 cm

- a) What is the radius ?
- b) Find the curved surface area of the cone

4) In the figure O is the centre of the circle. $AB = BC$, $\angle ADC = 50^\circ$



- a) What is the measure of $\angle AOC$?
- b) What is the measure of $\angle ABC$?
- c) What is the measure of $\angle BAC$, $\angle BCA$?

3 score

5) 97, 94, 91 \dots എന്ന സമാന്തരശ്രേണി പരിഗണിക്കുക

- a) What is the common difference ?
- b) Write the algebraic form of this sequence?
- c) Which is the first negative term of this sequence?

3 score

6) Sum of the area of two squares is 116sq.cm . The difference between the perimeters is 24.

- If the side of the small square is x then what is the side of the big square?
- Form a second degree equation.
- Calculate the side of the squares .

4 score

7) One side of a triangle is 6cm. Angle at the ends of this side are $40^\circ, 60^\circ$.

- Draw the triangle.
- Construct the circle which touches its sides.

5 score

8) A child standing in the bank of a river observes the top of a tree on the other side of the river at an angle of elevation 60° . When moves 20metre back the top of the tree is found at the angle 30° .

- Draw a rough diagram
- Calculate the height of the tree.
- Calculate the width of the river.

5 score

SJ Self Evaluation Series

Answers

- $\star a + b + c + d = -7 + 7 = 0$. That is $p(1) = 0$
 $\star x - 1$ is always a factor
- Triangle ABC is a right triangle $\angle A = 90^\circ$

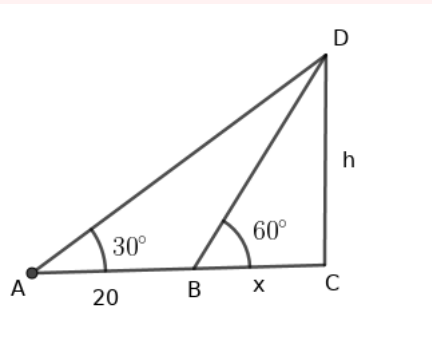
 - Mid point of BC is $(\frac{0+6}{2}, \frac{8+0}{2}) = (3, 4)$
 - $BC = \sqrt{6^2 + 8^2} = 10$.
 Radius of the circumcircle 5
- h, r, l form a
 $45^\circ - 45^\circ - 90^\circ$ triangle

 - $r = \frac{12}{\sqrt{2}} = 6\sqrt{2}\text{cm}$
 - $\pi r l = 72\sqrt{2}\pi\text{sq.cm}$
- $\angle AOC = 100^\circ$
 - $\angle ABC = 180 - 50 = 130^\circ$
 - $\angle BAC = \angle BCA = \frac{180-130}{2} = 25^\circ$
- $d = 94 - 97 = -3$
 - $x_n = dn + (f - d) = -3n + (97 - -3) = -3n + 100$
 - $-3n + 100 < 0 \rightarrow -3n < -100$
 $3n > 100, n > \frac{100}{3}$
 $n > 33.33, n = 34$

$$x_{34} = -3 \times 34 + 100 = -2$$

First negative term is -2

- 6) a) If the larger side is y , $4y - 4x = 24$, $y - x = 6$, $y = x + 6$
- b) $x^2 + (x+6)^2 = 116$, $x^2 + x^2 + 12x + 6^2 = 116$
 $2x^2 + 12x + 36 = 116$, $x^2 + 6x = 40$
- c) $x^2 + 6x + 9 = 49$, $(x+3)^2 = 49$, $x+3 = 7$, -7
 $x = 7 - 3 = 4$. sides are $x = 4\text{cm}$, $y = 6 + 4 = 10\text{ cm}$
- 7) ★ Draw a triangle using the given measurements
 ★ Draw the bisectors of two angles. They intersect at a point.
 ★ Draw perpendicular from this point to the side .
 Take the intersecting point of the angle bisectors as the centre and perpendicular distance to the side as diameter , draw the circle.
- 8) a) Draw figure



b) Triangle BCD is a $30^\circ - 60^\circ - 90^\circ$ triangle .

$$BC = x, h = \sqrt{3}x$$

Triangle ACD is a $30^\circ - 60^\circ - 90^\circ$ triangle .

$$20 + x = \sqrt{3}h = \sqrt{3} \times \sqrt{3}x$$

$$20 + x = 3x, 20 = 2x, x = 10\text{metre}$$

c) Height of the tree = $\sqrt{3}x = 10\sqrt{3}\text{metre}$

d) Width of the river 10metre