

# SSLC Model Examination March 2021

## Mathematics - English Version. Detailed Solutions with Questions.

*Prepared by Dr. V. S. RaveendraNath.*

---

### Question. 1

What is the common difference of the arithmetic sequence 4, 10, 16, ... ?  
[4, 5, 6, 10]

### Solution.

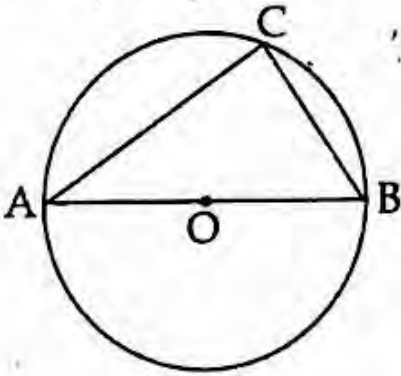
Given sequence = 4, 10, 16, .....

$$\begin{aligned}\text{Common difference} &= x_2 - x_1 \\ &= 10 - 4 = 6.\end{aligned}$$

.....drvsvr

## Question. 2.

In the figure O is the centre of the circle. Write the measure of  $\angle ACB$ .  
[ $30^\circ$ ,  $60^\circ$ ,  $90^\circ$ ,  $100^\circ$ ]



**Solution.**

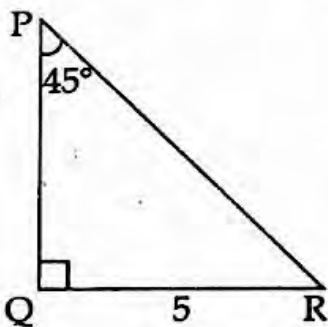
$$\angle ACB = 90^\circ \text{ (Angle in semi circle).}$$

.....drvsvr

## Question. 3.

In triangle PQR,  $\angle Q = 90^\circ$ ,  $\angle P = 45^\circ$ ,  $QR = 5$  centimetres. What is the length of PR ?

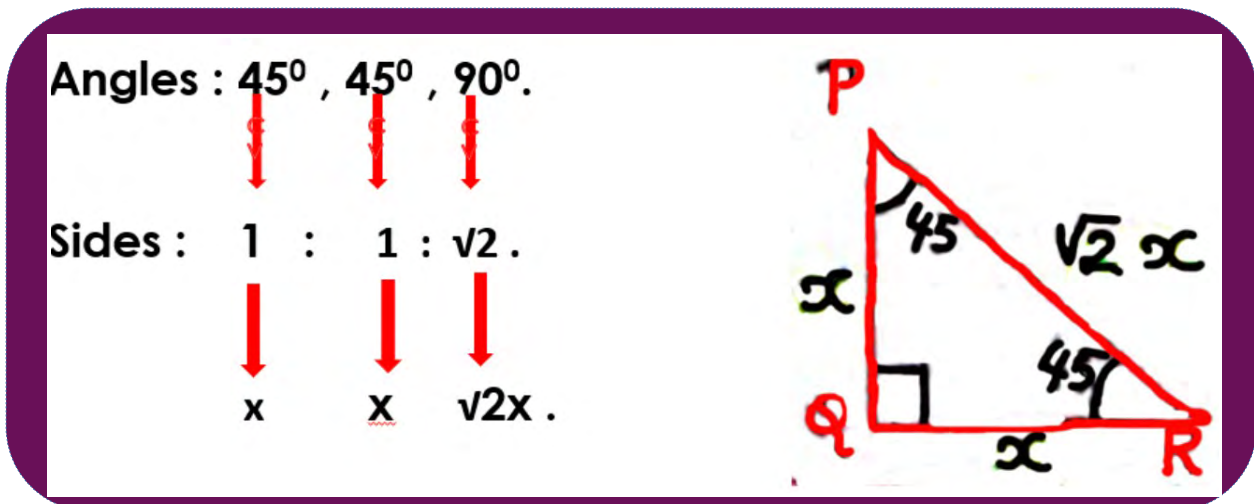
$$\left[ 10\sqrt{2}, 5\sqrt{2}, 10, \frac{5}{\sqrt{2}} \right]$$



## Solution.

$\triangle PQR$  be rt. isosceles triangle

$$\therefore \angle P = \angle R = 45^\circ .$$



$$PR = x\sqrt{2} = 5\sqrt{2}$$

.....drvsvr

## Question. 4.

Which of the following is a point on the x-axis ?

$[(3, 0), (0, 3), (-3, 2), (0, -2)]$

## Solution.

$(3, 0)$ . [ $y = 0$  becomes x axis)

.....drvsvr

## Question. 5.

Which of the following is the midpoint of the line joining (6, 2) and (12, 2) ?  
[(8, 2), (10, 2), (2, 8), (9, 2)]

### Solution.

$x_1, y_1$   $x_2, y_2$

Given points = (6, 2) (12, 2)

$$\begin{aligned} \text{Mid point} &= \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) \\ &= \left( \frac{6 + 12}{2}, \frac{2 + 2}{2} \right) \\ &= \left( \frac{18}{2}, \frac{4}{2} \right) = (9, 2). \end{aligned}$$

.....drvsr

## Question. 6.

Algebraic form of an arithmetic sequence is  $3n + 2$ .

(a) What is its first term ?

(b) Find its 10<sup>th</sup> term.

### Solution.

Given  $x_n = 3n + 2$

(a). Put  $n = 1$ , get the first term

ie., first term =  $3 \times 1 + 2 = 5$ .

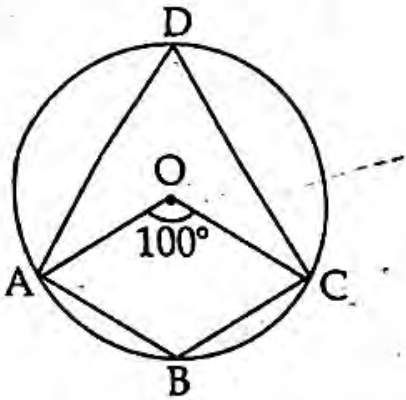
(b) 10<sup>th</sup> term ; put  $n = 10$

ie.,  $3 \times 10 + 2 = 32$ .

.....drvsr.

## Question. 7.

A, B, C and D are points on the circle with centre O.  $\angle AOC = 100^\circ$ .



- (a) What is the measure of  $\angle ADC$  ?  
(b) Find  $\angle ABC$ .

## Solution.

Given  $\angle AOC = 100^\circ$  .

a). Measure of  $\angle ADC = \frac{1}{2} \times 100$   
 $= 50^\circ$  .

b)  $\angle ABC = 180 - 50 = 130^\circ$  .

[ ABCD be a cyclic quadrilateral]

.....drvsvr

## Question. 8.

One is asked to say a natural number from 1 to 20.

- (a) What is the probability of it being an even number ?
- (b) What is the probability of it being a multiple of 5 ?

### Solution.

**a)** Given natural numbers 1 to 20.

Total numbers  $n(N) = 20$ .

From this even numbers

$= 2, 4, 6, 8, 10, 12, 14, 16, 18, 20$

ie.,  $n(F) = 10$ .

Hence the probability =  $n(F) / n(N)$

$$= \frac{10}{20} = \frac{1}{2} .$$

**b)** Multiple of 5 are 5, 10, 15, 20.

ie.,  $n(F) = 4$

$$\begin{aligned} \text{Hence the probability} &= \frac{n(F)}{n(N)} \\ &= \frac{4}{20} = \frac{1}{5} \end{aligned}$$

.....drvsr

## Question. 9.

Write the second degree polynomial  $x^2 - 16$  as the product of two first degree polynomials.

### Solution.

Given polynomial =  $x^2 - 16$

The first degree polynomial

$$= (x + 4)(x - 4) .$$

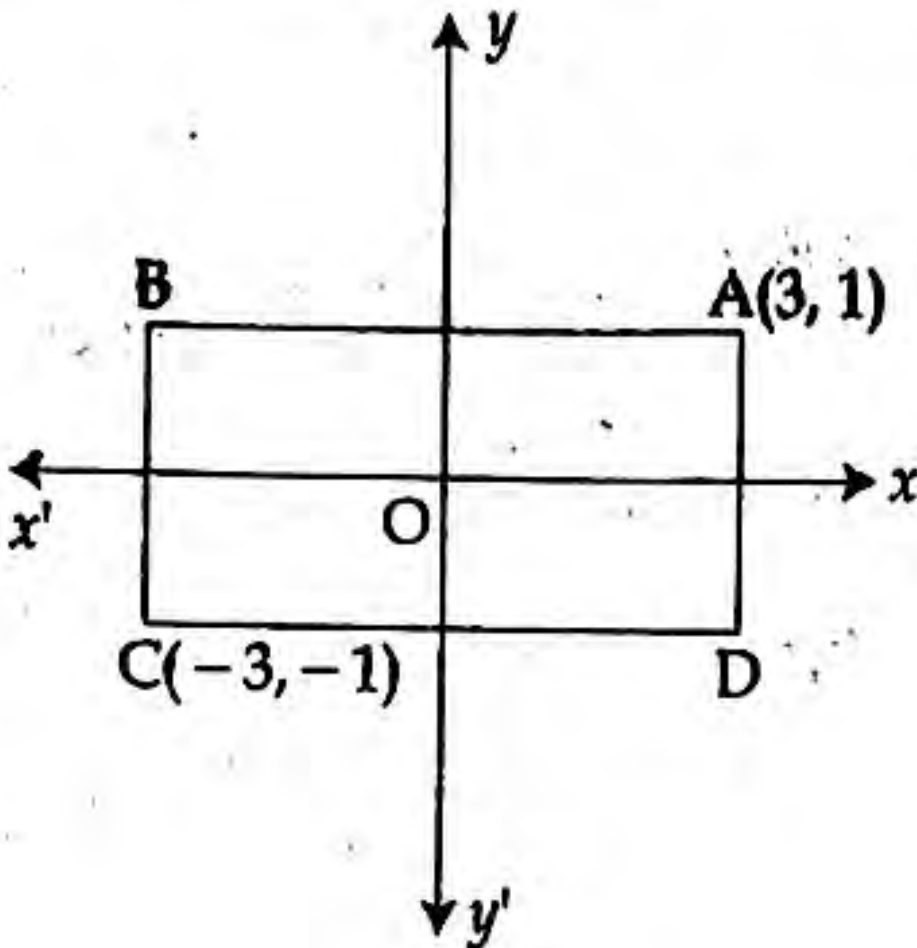
$$[ \because (a+b)(a-b) = a^2 - b^2 ]$$

.....drvsr.



### Question. 10.

In the figure the sides of the rectangle ABCD are parallel to the axes. Two of its vertices are  $A(3,1)$  and  $C(-3, -1)$ . Write the coordinates of B and D.



## Solution.

From the figure we can directly observed that

**B(+3, 1) and D(3, -1).**

.....drvsn

## Question. 11.

The 5<sup>th</sup> term of an arithmetic sequence is 20 and the 8<sup>th</sup> term is 32

- (a) What is the common difference of this sequence ?
- (b) Find its 11<sup>th</sup> term.

## Solution.

Given, 5<sup>th</sup> term of an AP is 20 and 8<sup>th</sup> term is 32.

**a)**

Here we know that , term difference is proportional to position difference, and the constant of proportionality is the common

difference ie.,  $\frac{X_m - X_n}{m - n} = d$

$$\text{ie., } \frac{32-20}{8-5} = \frac{12}{3} = 4.$$

b). Given 5<sup>th</sup> term = 20.

$$\text{ie., } f + 4d = 20.$$

$$f + 4 \times 4 = 20$$

$$f = 20 - 16 = 4.$$

Hence 11<sup>th</sup> term =  $f + 10d$

$$= 4 + 10 \times 4$$

$$= 44.$$

.....drvsvr

## Question. 12.

$x$  is a natural number.

- (a) What number should be added to  $x^2 + 2x$  to get a perfect square
- (b) If  $x^2 + 2x = 15$ . Find the natural number represented by  $x$ .

## Solution.

Given  $x$  is a natural number.

a) 1 is added to  $x^2 + 2x$  get a perfect square

[ $\because x^2 + 2x + 1$  be  $(a + b)^2$  form]

b) Given  $x^2 + 2x = 15$

[by square completion method or factorization method or quadratic method]

$$x^2 + 2x + 1 = 15 + 1$$

$$(x + 1)^2 = 16.$$

$$x + 1 = \sqrt{16} = 4.$$

$$x = 4 - 1 = 3.$$

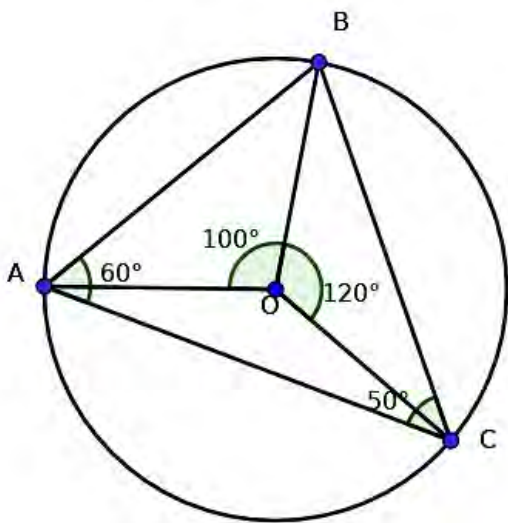
$\therefore$  the natural number representd by  $x = 3$ .

.....drvsvr

## Question. 13.

The vertices of a triangle are points on a circle of radius 3 centimetres. If two angles of this triangle are  $50^\circ$  and  $60^\circ$ , draw the triangle.

### Solution.



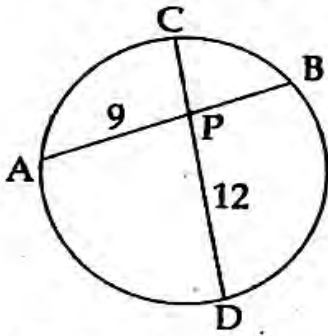
### Construction:

Draw a circle with radius 3cm O as the center. Draw OB and make an  $\angle AOB = 100^\circ$  ( $2 \times 50 = 100$ ).make an  $\angle BOC = 120^\circ$  .( $2 \times 60 = 120$ ) and join AB,BC and AC.

.....drvsvr

## Question. 14.

The chords AB and CD intersect at P. AB = 17 centimetres, PA = 9 centimetres, PD = 12 centimetres.



- (a) What is the length of PB ?
- (b) Find the length of PC.

### Solution.

Given, AB = 17cm, PA = 9cm,  
PD = 12cm.

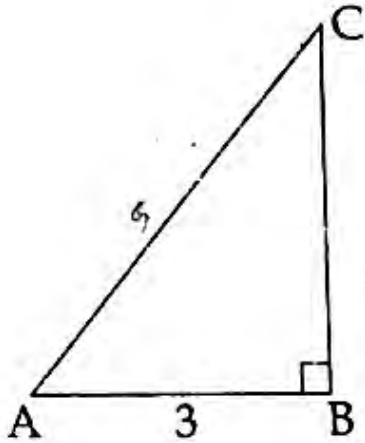
a) Length of PB = AB - PA  
 $= 17 - 9 = 8\text{cm}$

b) We know that  $PA \times PB = PC \times PD$   
ie.,  $9 \times 8 = PC \times 12$   
 $PC = 72/12 = 6\text{ cm.}$

.....drvsvr

## Question. 15.

In triangle ABC,  $\angle B = 90^\circ$ ,  $AB = 3$  centimetres,  $\cos A = \frac{3}{5}$ .



- (a) What is the length of AC?
- (b) Find  $\sin A$ .

## Solution.

Given  $\triangle ABC$  is a rt. triangle

$$AB = 3, \cos A = \frac{3}{5} .$$

$$a) \cos A = \frac{\text{Adj}}{\text{Hpy}} = \frac{AB}{AC} = \frac{3}{5}$$

ie.,  $AC = 5$ .

b) Here  $AB = 3$ ,  $AC = 5$

$\Delta ABC$  is a rt. triangle

By Pythagoras,

$$BC^2 = AC^2 - AB^2$$

$$= 5^2 - 3^2 = 25 - 9 = 16$$

$$\therefore BC = \sqrt{16} = 4.$$

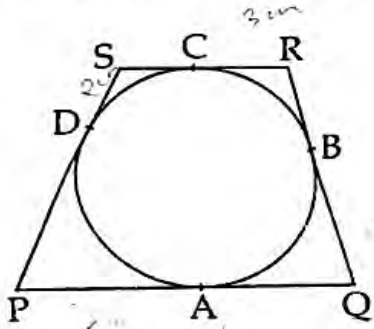
$$\sin A = \frac{\text{Opp}}{\text{Hpy}} = \frac{BC}{AC} = \frac{4}{5}.$$

.....drvsvr



## Question. 16.

In the figure, the circle touches the sides of the quadrilateral PQRS at A, B, C and D. PA = 5 centimetres, QB = 4 centimetres, RC = 3 centimetres, SD = 2 centimetres.



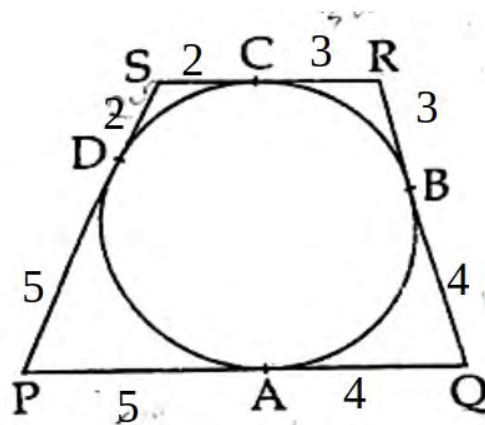
- What is the length of PD ?
- Find the perimeter of the quadrilateral PQRS.

## Solution.

Given  $PA = 5\text{cm}$ ,  $QB = 4\text{cm}$ ,  
 $RC = 3\text{cm}$ ,  $SD = 2\text{cm}$ .

a) The length of  $PD = PA = 5\text{cm}$   
[ length of same tangent]

b).



From the figure perimeter

$$= PA + AQ + QB + BR + RC + CS + SD + DP$$

$$= 5 + 4 + 4 + 3 + 3 + 2 + 2 + 5 = 28\text{cm.}$$

.....drvsvr

## Question. 17.

The base radius and slant height of a cone are 6 centimetres and 10 centimetres respectively.

(a) What is its height?

(b) Find its volume.

## Solution

Given,  $r = 6\text{cm}$ ,  $l = 10\text{cm}$ .

$$\begin{aligned} \text{a) Height} &= \sqrt{l^2 - r^2} = \sqrt{10^2 - 6^2} \\ &= \sqrt{100 - 36} = \sqrt{64} \\ &= 8\text{cm.} \end{aligned}$$

$$\text{b). Volume} = \frac{1}{3} \times \pi r^2 h$$

$$= \frac{1}{3} \times \pi \times 6^2 \times 8 = 96\pi \text{ cm}^3$$

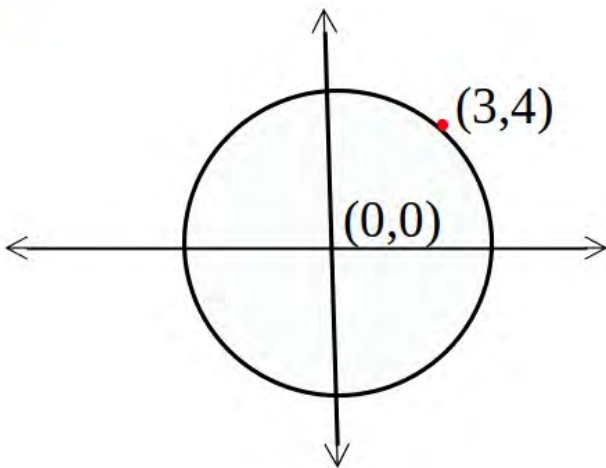
.....drvsvr

## Question. 18.

(3, 4) is a point on a circle with centre at the origin.

- Find its radius.
- Write the coordinates of the points where the circle cuts the x-axis.

## Solution.



Equation of the circle  $x^2 + y^2 = r^2$

$$\text{radius} = \sqrt{3^2 + 4^2}$$

$$= \sqrt{9 + 16} = \sqrt{25}$$

$$= 5.$$

Coordinates be (5,0) or (-5,0)

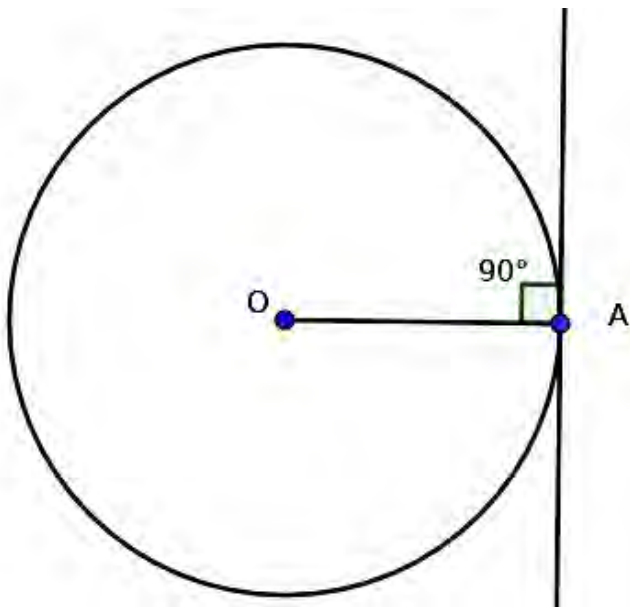
.....drvsvr

## Question. 19.

Draw a circle of radius 3 centimetres. Mark a point A on the circle and draw tangent through A.

**Solution.**

**Construction.**



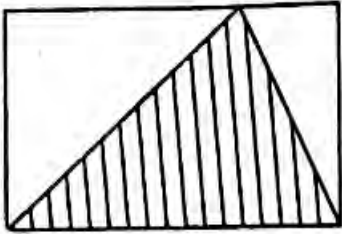
Draw a circle with a radius 3cm O as its center. Draw OA line and draw perpendicular to

OA through A.

.....drvsvr

## Question. 20.

In the figure, the area of the rectangle is 40 square centimetres.



- (a) What is the area of the shaded triangle ?
- (b) If a dot is put in the figure without looking into it. What is the probability of it being inside the shaded triangle ?

### Solution.

Given, the area of the rectangle  
 $= 40 \text{ cm}^2$ .

a) Area of the shaded triangle

$$= \frac{1}{2} \times 40 = 20 \text{ cm}^2$$

b) Probability =

$$\frac{\text{area of the shaded region}}{\text{Total area of the rectangle}}$$

$$= \frac{20}{40} = \frac{1}{2} .$$

.....drvsvr

## Question. 21.

The 10<sup>th</sup> term of an arithmetic sequence is 20 and its 20<sup>th</sup> term is 10.

- (a) What is its common difference ?
- (b) What is its 30<sup>th</sup> term ?
- (c) Which is the first negative term of this sequence ?

## Solution.

$$\begin{aligned} \text{Given, } 10^{\text{th}} \text{ term} &= 20, \\ 20^{\text{th}} \text{ term} &= 10. \end{aligned}$$

Here we know that , term difference is proportional to position difference, and the constant of proportionality is the common

difference ie.,  $\frac{X_m - X_n}{m - n} = d$

$$\text{a) ie., } d = \frac{10 - 20}{20 - 10} = \frac{-10}{10} = -1.$$

b). Given 10<sup>th</sup> term - 20

$$\text{ie., } f + 9d = 20$$

$$f + 9 \times -1 = 20$$

$$f = 20 + 9 = 29$$

Hence the 30<sup>th</sup> term =  $f + 29d$

$$= 29 + 29 \times -1 = 0$$

c). Here 30<sup>th</sup> term is 0

$\therefore$  the 31<sup>st</sup> term be -1.

.....drvsn

## Question. 22.

✓ 1, 3, 5, ..... is an arithmetic sequence.

- What is its 20<sup>th</sup> term ?
- Find the sum of first 20 terms of this sequence.
- What is the sum of first 20 terms of the arithmetic sequence 6, 8, 10, ... ?

## Solution.

Give sequence 1, 3, 5,.....

$$f = 1; d = 3 - 1 = 2.$$

$$\begin{aligned} \text{a) } 20^{\text{th}} \text{ term} &= f + 19d \\ &= 1 + 19 \times 2 = 39. \end{aligned}$$

$$\begin{aligned} \text{b) } \text{Sum of 1}^{\text{st}} 20 \text{ term} &= n^2 \\ &= 20^2 = 400. \end{aligned}$$

c). Given sequence 6, 8, 10,.....

$$f = 6, d = 8 - 6 = 2.$$

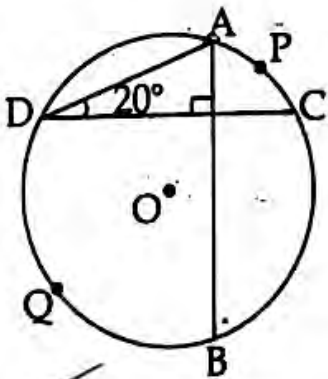
$$\begin{aligned} x_{20} &= f + 19d = 6 + 19 \times 2 \\ &= 44. (\text{ } x_n) \end{aligned}$$

$$\begin{aligned} \text{Sum} &= \frac{n}{2} (x_1 + x_n) \\ &= \frac{20}{2} (6 + 44) = 500. \end{aligned}$$



## Question. 23.

In the figure, O is the centre of the circle. AB and CD are two perpendicular chords.  $\angle D = 20^\circ$ .



- Write the measure of  $\angle A$ .
- What is the central angle of arc BQD?
- What is the central angle of arc APC?

## Solution.

a) Measuremet of  $\angle A$

$$= 180 - (90 + 20) = 70^\circ$$

b). Center angle of arc BQD

$$= 2 \times \angle A = 2 \times 70 = 140^\circ .$$

c) Center angle of arc BAPC

$$= 2 \times \angle D = 2 \times 20 = 40^\circ .$$

.....drvsr

## Question. 24.

- (a) Perimeter of a rectangle is 40 centimetres. Write a pair of numbers that can be the measures of its sides.
- (b) Perimeter of a rectangle is 40 centimetres and its area is 84 square centimetres. Find the lengths of its sides.

## Solution.

a) Given perimeter = 40cm.

$$\text{ie., } 2(l+b) = 40$$

$$l + b = 40/2 = 20.$$

Here we can write so many pair of numbers . Only we get the sum of two numbers becomes 20

such as 13,7; 11,9; 15,5; and so on.

b) Perimeter = 40cm

$$\text{Area} = 84 \text{ cm}^2 .$$

$$\text{ie., } 2(l+b) = 40$$

$$l + b = 40/2 = 20.$$

Let length be 'x' ,

breadth 20- x

$$\text{Area} = 84$$

$$\text{ie., } l \times b = 84$$

$$x(20 + x) = 84$$

$$20x - x^2 = 84$$

$$x^2 - 20x = -84 \quad (\text{apply square completion method})$$

$$x^2 - 20x + 100 = -84 + 100$$

$$(x - 10)^2 = 16$$

$$x - 10 = \sqrt{16} = 4$$

$$x = 4 + 10 = 14.$$

Hence length = 14 cm

breadth =  $20 - 14 = 6$ cm.

.....drvsvr

## Question. 25.

A box contains 6 black beads and 4 white beads. Another box contains 5 black beads and 3 white beads. If we take one bead from each box without looking :

- (a) What is the total number of pairs ?
- (b) What is the probability that both are black ?
- (c) Find the probability of one being black and the other being white.

## Solution.

	Box - 1	Box - 2
Black beads	6	5
White beads	4	3
Total	10	8

a) Total number of pairs

$$= m \times n = 10 \times 8 = 80.$$

**b)** Total number of both black

$$= m \times n = 6 \times 5 = 30.$$

$$\text{Probability} = n(F)/n(N) = 30/80 \\ = 3/8.$$

**c)** Probability being one black and one being white

$$= \frac{4 \times 5}{80} + \frac{6 \times 3}{80} = \frac{20}{80} + \frac{18}{80}$$

$$= \frac{38}{80} = \frac{19}{40} .$$

.....drvsvr

## Question. 26.

(a)  $P(x) = x^2 - 5x + 10$ . What number is  $P(2)$  ?

(b) Write  $P(x) - P(2)$  as the product of two first degree polynomials.

## Solution.

a) Given  $P(x) = x^2 - 5x + 10$

$$P(2) = 2^2 - 5 \times 2 + 10 = 4 .$$

b)  $P(x) - P(2) = x^2 - 5x + 10 - 4$   
 $= x^2 - 5x + 6$  [factorize]  
 $= (x - 3)(x - 2)$

.....drvsvr

## Question. 27.

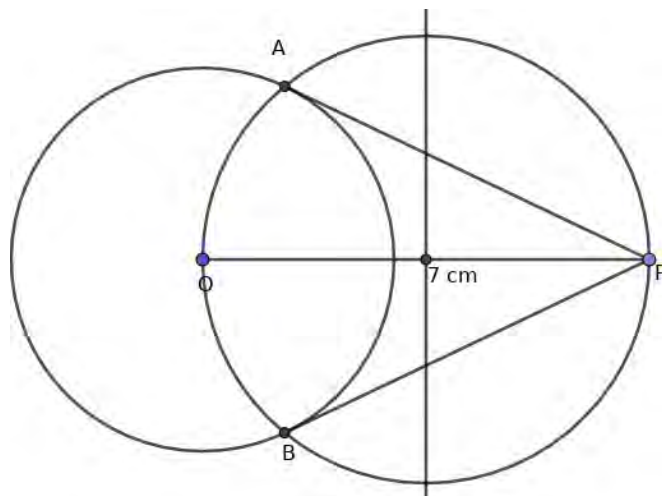
- (a) Draw a circle of radius 3 centimetres.  
(b) Mark a point P at a distance of 7 centimetres from its centre.  
(c) Draw tangents from P to this circle.

## Solution.

a)

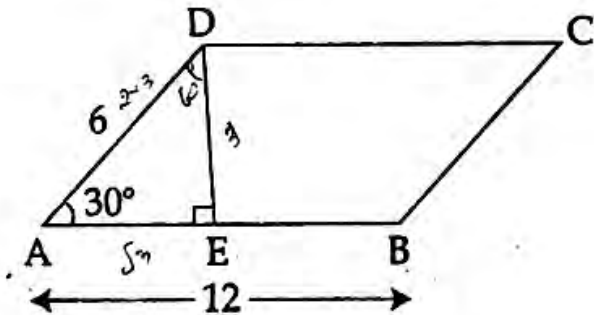
b)

c)



## Question. 28.

In the figure, ABCD is a parallelogram,  $\angle A = 30^\circ$ ,  $AB = 12$  centimetres,  $AD = 6$  centimetres.



- Find the length of DE.
- Find the area of the parallelogram ABCD.

## Solution.

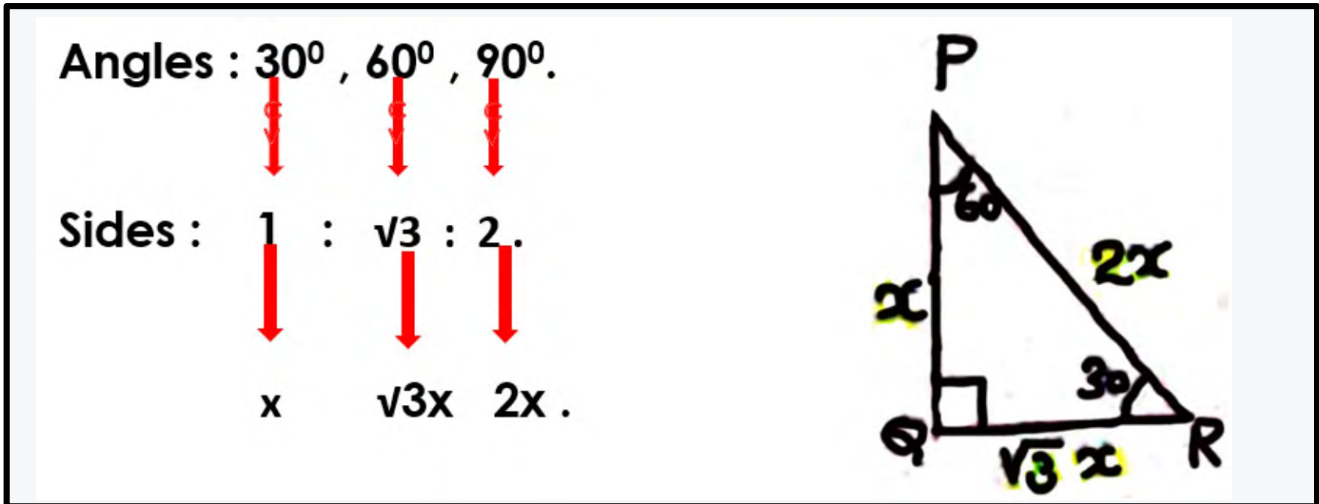
Given  $AB = 12\text{cm}$ ,  $AD = 6\text{cm}$ ,  $\angle A = 30^\circ$ .

$\triangle AED$  be a rt. Triangle.

$30^\circ, 60^\circ, 90^\circ$ .

$1 : \sqrt{3} : 2$

[ see the question figure ]



a) Length of DE = x = 3cm.

b) Area of ABCD = bh  
 = 12 × 3 = 36cm<sup>2</sup>.

.....drvsvr

## Question. 29.

The marks got by 6 students in an examination are given below.

26, 21, 32, 38, 45, 48

- Find the mean of the marks.
- What is the median mark ?



## Solution.

Given data

$$= 26, 21, 32, 38, 45, 48.$$

a) Mean = Sum / N

$$= 26 + 21 + 32 + 38 + 45 + 48 / 6$$

$$= 210 / 6 = 35.$$

b). Median

Arrange the data in ascending order

ie., 21, 26, **32, 38**, 45, 48 .

$$\frac{32 + 38}{2} = \frac{70}{2} = 35.$$

.....drvsn

## Question. 30.

1. A circle with centre at the origin cuts the  $y$ -axis at the point  $(0, 5)$ .
- Write the coordinates of other two points on this circle.
  - What is the radius of this circle ?
  - Verify whether the point  $(4, 4)$  lies on this circle.

### Solution.

a) Other points

$$(0, -5), (5, 0), (-5, 0)$$

b) Radius = 5.

c) Find the distance between the points  $(4, 4)$  and  $(0, 0)$

$$\begin{aligned}\sqrt{x^2 + y^2} &= \sqrt{4^2 + 4^2} = \sqrt{16 + 16} \\ &= \sqrt{32}\end{aligned}$$

we can see that  $\sqrt{32}$  is greater than the radius 5.

Hence the the point is not lies on the circle.

.....drvsvr

### Question. 31.

Look at the following number pattern.

		1		3	
	2	3	4	5	
5	6	7	8	9	
----- 16					
-----					

- (a) Write the next line of this pattern.
- (b) Write the sequence of last numbers in each line.
- (c) What will be the last number in the 9<sup>th</sup> line ?
- (d) Write the first and last numbers of the 10<sup>th</sup> line.

## Solution.

a) Next lines of this pattern

10 11 12 3 14 15 16.

b) Last number in each line

1 , 4, 9 , 16 ,25 ,.....

c) Number in the 9<sup>th</sup> line

$$9^2 = 81.$$

d) First number of 10<sup>th</sup> line = 82.

[∵ 9<sup>th</sup> line number = 81]

Last number of 10<sup>th</sup> line

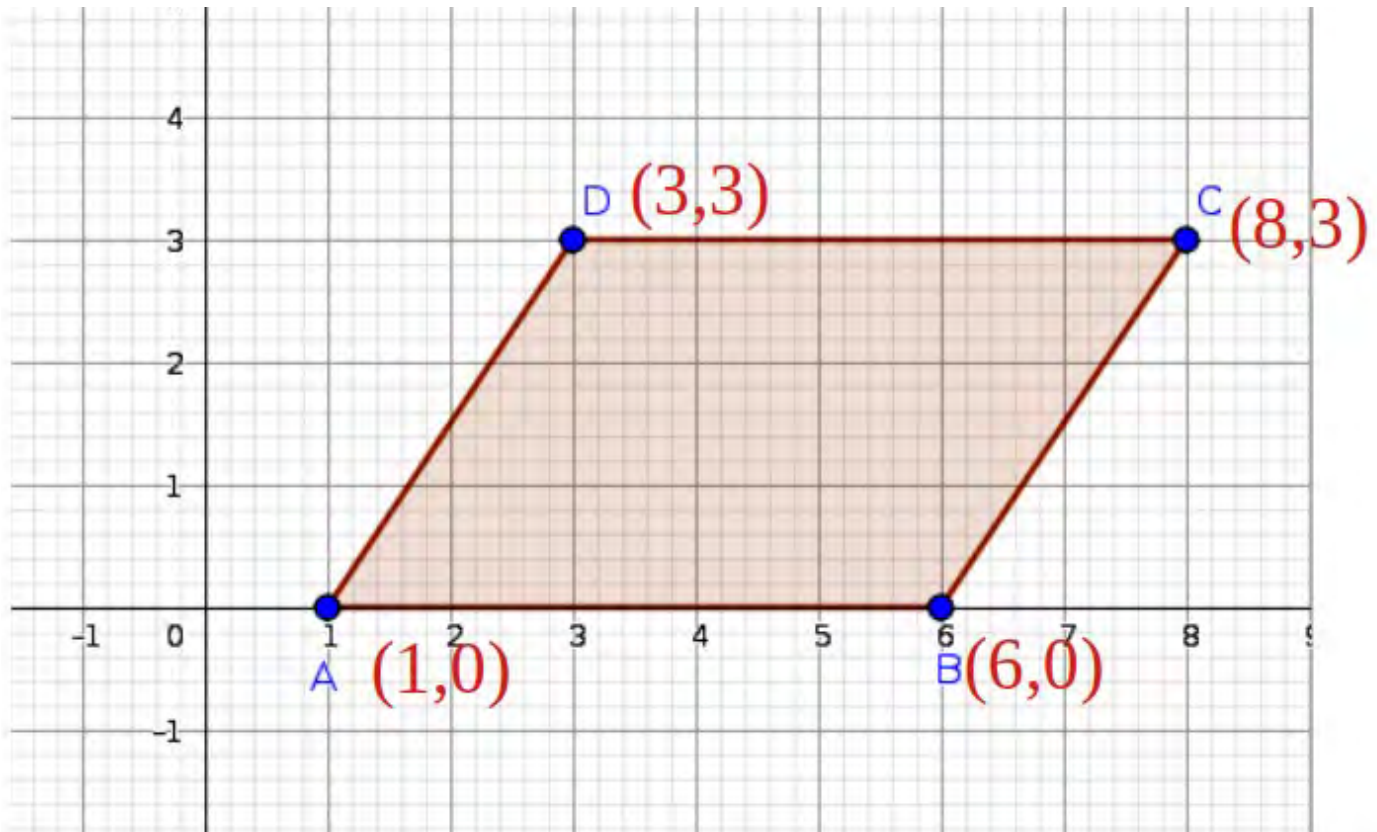
$$= 10^2 = 100.$$

.....drvsvr

## Question. 32.

- (a) Draw the  $x, y$  axes and mark the points A(1, 0), B(6, 0), C(8, 3), D(3, 3).
- (b) Write the most suitable name for quadrilateral ABCD.
- (c) Find its area.

## Solution.



b) ABCD be a Parallelogram.

c) Area = bh

$$= 5 \times 3 = 15 \text{ sq. unit}$$

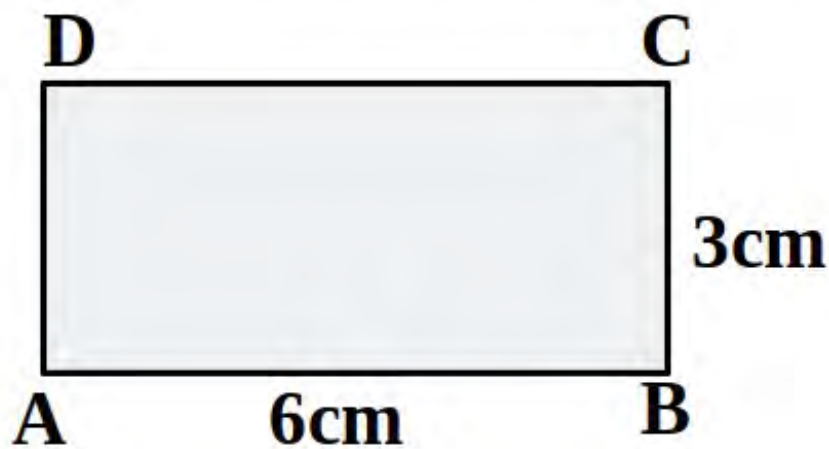
.....drvsvr

## Question. 33.

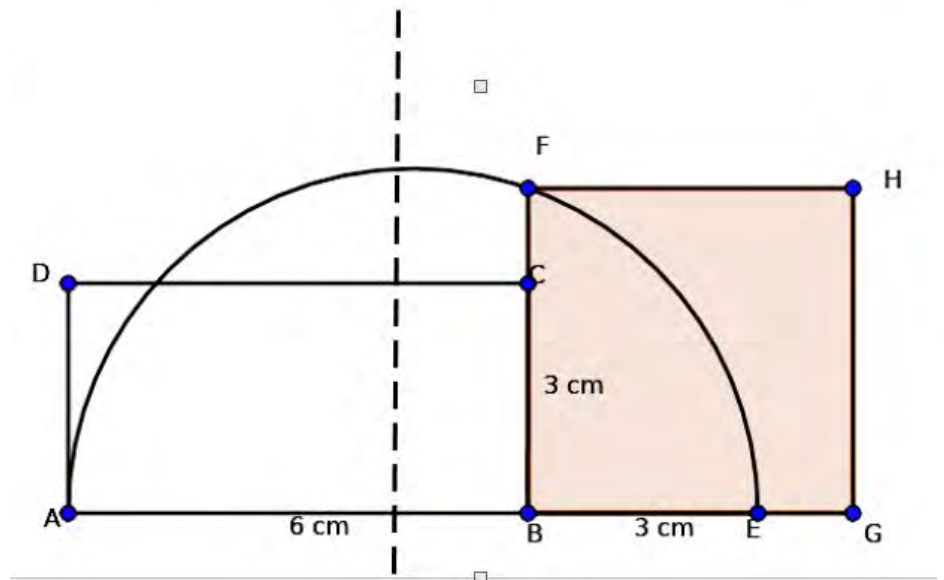
- b. (a) Draw a rectangle of sides 6 centimetres and 3 centimetres.  
(b) Draw a square of same area.

### Solution.

a)



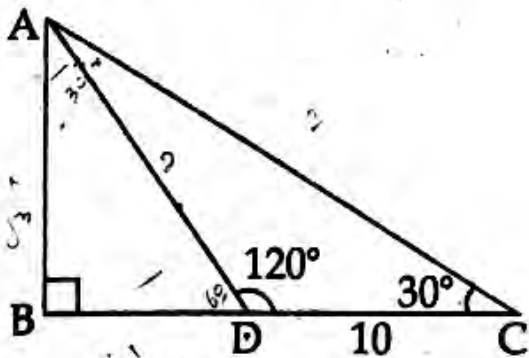
b)



.....drvsr

## Question. 34.

In triangle ABC,  $\angle B = 90^\circ$ ,  $\angle C = 30^\circ$ ,  $\angle ADC = 120^\circ$ . Also  $DC = 10$  centimetres.



- What is  $\angle DAC$ ?
- What is the length of AD?
- Find  $\angle ADB$ .
- Find the lengths of BD and AC.

### Solution.

Given,  $\angle B = 90^\circ$ ,  $\angle ADC = 120^\circ$

$DC = 10\text{cm}$ ,  $\angle C = 30^\circ$ .

**a)** In  $\triangle ADC$ ,  $\angle A = 180 - (120 + 30) = 30^\circ$ .

In  $\triangle ABC$ ,

$$\angle A = 180 - (90 + 30 + 30) = 30^\circ.$$

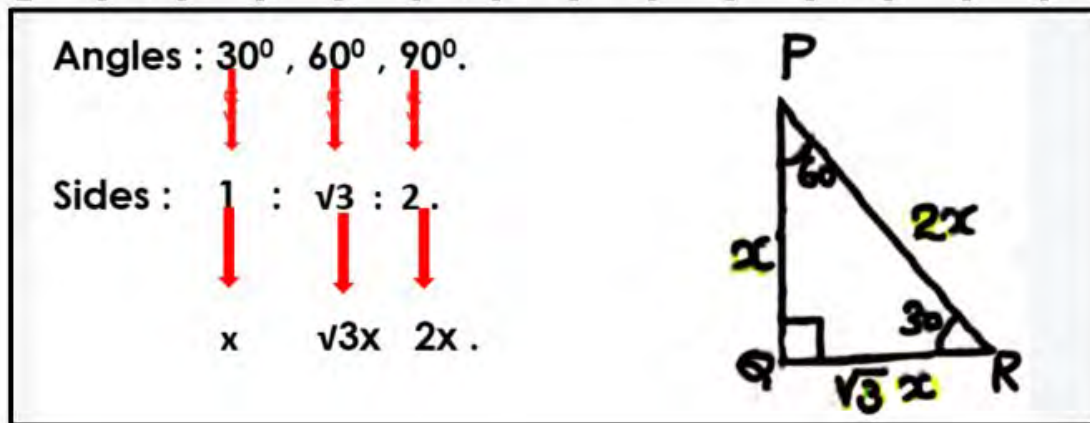
$$\therefore \angle DAC = 30^\circ.$$



$\triangle ABD$  be a rt. triangle,  
 $30^\circ, 60^\circ, 90^\circ$ .

$1 : \sqrt{3} : 2$

[ see the question figure]



$$BD = 10/2 = 5\text{cm};(x)$$

$$BC = 5 + 10 = 15\text{cm}$$

$$AB = x\sqrt{3} = 5\sqrt{3}$$

**b).**  $AD = 2x = 10\text{cm}$

**c).** Length of  $BD = 5\text{cm}$ .

In rt. triangle  $ABC$

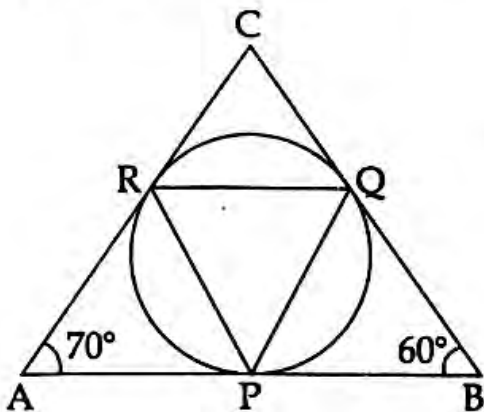


$$\begin{aligned}
 \text{Length of } AC &= \sqrt{AB^2 + BC^2} \\
 &= \sqrt{5\sqrt{3^2 + 15^2}} = \sqrt{75 + 225} \\
 &= \sqrt{300} = 10\sqrt{3} \text{ cm.}
 \end{aligned}$$

.....drvsvr

## Question. 35.

In the figure, the circle touches the sides of triangle ABC, at P, Q and R.  $\angle A = 70^\circ$ ,  $\angle B = 60^\circ$ .



- What is the measure of  $\angle BPQ$ ?
- What is  $\angle PRQ$ ?
- Find the measures of other two angles of triangle PQR.

## Solution.

Given,  $\angle A = 70^\circ$ ,  $\angle B = 60^\circ$ .

a) Measurement of  $\angle BPQ = 60^\circ$ .

b)  $\angle PRQ = 60^\circ$  .

c) Other two angles are

$$\angle PQR = 55^\circ \text{ and}$$
$$\angle QPR = 65^\circ$$

.....drvsvr

### Question. 36.

The sum of first 31 terms of an arithmetic sequence is 620.

- (a) What is its 16<sup>th</sup> term ?
- (b) What is the sum of 15<sup>th</sup> and 17<sup>th</sup> terms ?
- (c) Find the sum of first and 31<sup>st</sup> terms.

### Solution.

Given, sum of the first 31<sup>st</sup> term = 620.

a)  $16^{\text{th}}$  term ( $x_{16}$ ) =  $\text{Sum}/N$

$$= 620/31 = 20.$$

b) Sum of the 15<sup>th</sup> and 17<sup>th</sup> term

$$= 2 \times x_{16} = 2 \times 20 = 40..$$

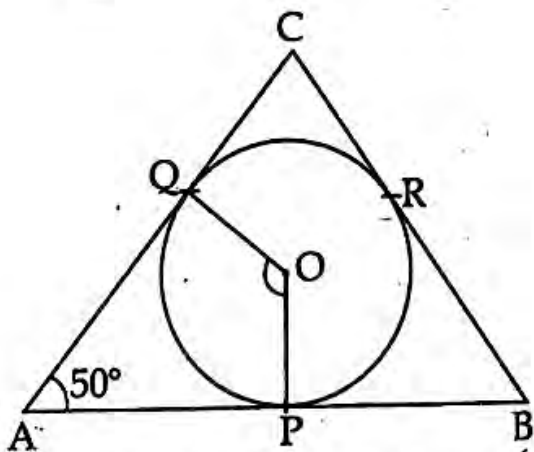
c). Sum of first and 31<sup>st</sup> term

$$x_1 + x_{31} = 40.$$

.....drvsvr

## Question. 37.

The circle touches the sides of triangle ABC at P, Q and R,  $\angle A = 50^\circ$ . What is  $\angle POQ$  ?

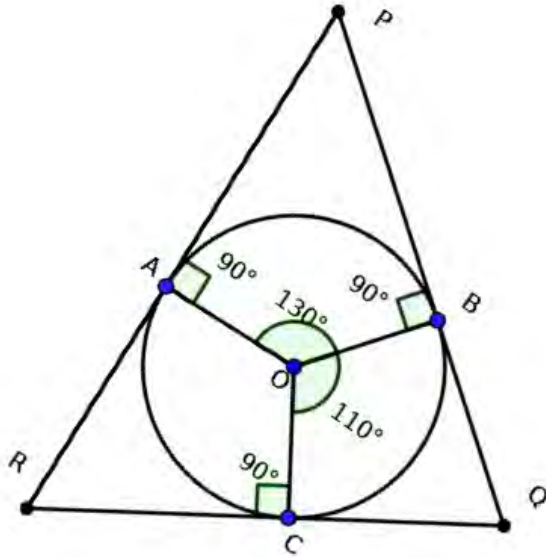


Draw a circle of radius 2 centimetres. Draw the triangle with two angles  $50^\circ$  and  $70^\circ$  and all its sides as tangents to this circle.

**Solution .**

$$a) \angle POQ = 180 - 50 = 130^\circ .$$

b)



### Construction

Draw a circle with radius 3cm O as the center. Makes an angle  $AOB = 130$  ( $180 - 50$ ). And also

makes  $\angle BOC = 110$  ( $180 - 70$ ).

Draw tangents through A, B and C.

.....drvsvr

## Question. 38.

The diameters of two spheres are in the ratio 2 : 3.

- (a) What is the ratio of their radii ?
- (b) Find the ratio of their surface areas.
- (c) If the surface area of the first sphere is  $16\pi$  square centimetres. Find the surface area of the second sphere.

## Solution .

Given, the ratio of diameter  
= 2 : 3.

a) Ratio of radius also be **2:3.**

b). Ratio of surface area

$$\begin{aligned} & 3\pi r^2 : 3\pi r^2 \\ &= 4\pi \times 2^2 : 4\pi \times 3^2 \\ &= \mathbf{4:9.} \end{aligned}$$

c) TSA of the first sphere =  $16\pi$

TSA of the second sphere =

$$16\pi \times \frac{9}{4} = 36\pi \text{ cm}^3 .$$

.....drvsr

## Question. 39.

The following table shows the students in a class sorted according to their heights.

Height (centimetres)	Number of Students
130 - 140	9
140 - 150	10
150 - 160	10
160 - 170	9
170 - 180	7
Total	45

a

19

29

38

45

- (a) If the students are arranged in the increasing order of their heights, student at what position will be in the middle ?
- (b) What is assumed to be the height of the 20<sup>th</sup> student ?
- (c) Find the median height.

## Solution .

Height	Frequency	cf
130-140	9	9
140-150	10	19 (F)
150-160 (Median class)	10 (f)	29 $\frac{N}{2}$
160-170	9	38
170-180	7	45
Total	45	

a) Position of the child with

$$\text{median height} = \frac{n+1}{2}$$

$$= \frac{45+1}{2} = 23.$$

b) The assumed height of the 20<sup>th</sup> student

$$\frac{N}{2} = \frac{45}{2} = 22.5.,$$

Median class 150-160 ,

$$l_1 = 150$$

$$C = 10, F = 19, f = 10.$$

The assumed height of the

$$20^{\text{th}} \text{ student} = \frac{150+151}{2}$$

$$= \frac{301}{2} = 150.5.$$



$$\text{c) Median height } l_1 + \frac{\left(\frac{N}{2} - F\right) C}{f}$$

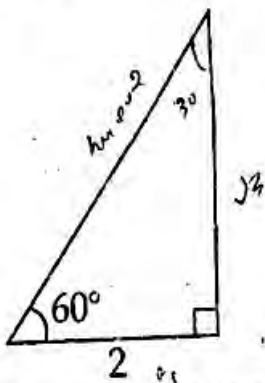
$$= 150 + \frac{22.5 - 19}{10} \times 10$$

$$= 150 + 3.5 = 153.5 \text{ cm.}$$

.....drvsvr

## Question. 40.

- (a) The figure shows a ladder leaning against a wall. It makes an angle  $60^\circ$  with the floor. The foot of the ladder is 2 metres away from the wall. Find the length of the ladder.



- (b) If the same ladder is kept such that the angle with the floor is  $30^\circ$ , how high will its top be from the floor? How far is the foot of the ladder from the wall?

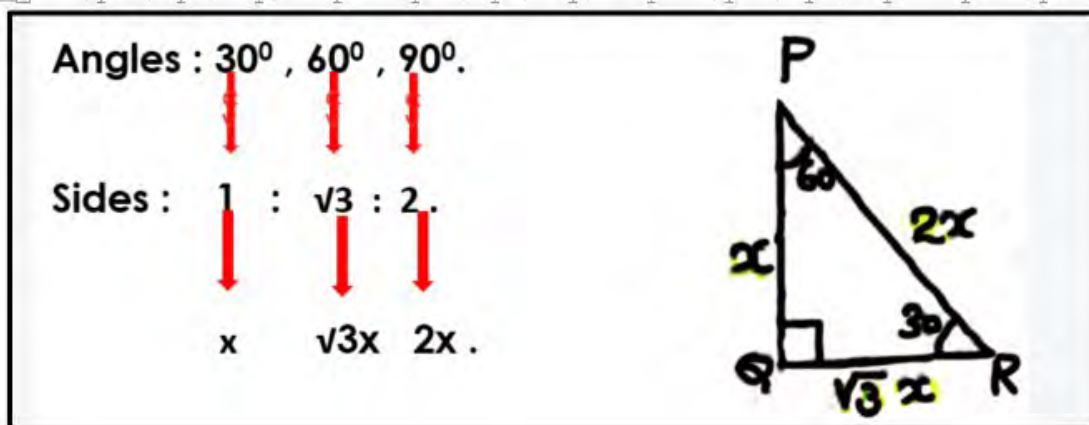
## Solution .

Given triangle be a rt. triangle.

ie.,  $30^\circ$  ,  $60^\circ$  ,  $90^\circ$  .

$1 : \sqrt{3} : 2$

[ see the question figure]



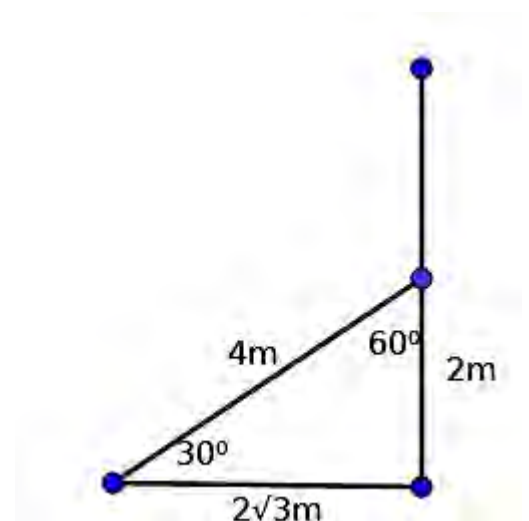
a) Length of the laser

$$= 2 \times 2 = 4\text{m.}$$

b). Height =  $2\text{m}$ .

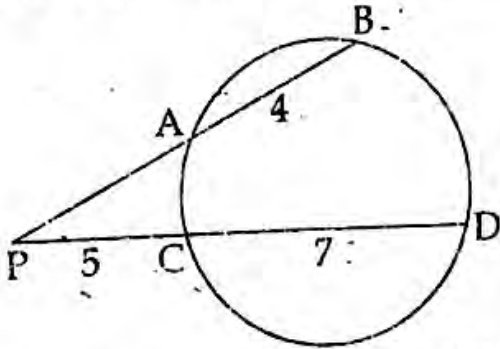
Distance =  $2\sqrt{3}\text{m}$ .

.....drvsvr



## Question. 41.

In the figure, the chords AB and CD are extended to meet at P. AB = 4 centimetres, PC = 5 centimetres, CD = 7 centimetres.



- What is the length of PD ?
- If the length of PA is taken as  $x$ , then what is the length of PB ?
- Form a second degree equation in  $x$  and find the length of PA.

## Solution

a) Length of PD = PC + CD  
 $= 5 + 7 = 12.$

b) By given condition  
 $PB = x + 4.$

c) We know that  
 $PA \times PB = PC \times PD$   
ie.,  $x(x + 4) = 5 \times 12$

$$x^2 + 4x = 60$$

( using square completion method)

$$x^2 + 4x + 4 = 60 + 4$$

$$(x + 2)^2 = 64$$

$$x + 2 = \sqrt{64} = 8$$

$$x = 8 - 2 = 6 \text{ cm}$$

$$PA = 6 \text{ cm.}$$

.....drvsvr

## Question. 42.

The coordinates of the end points of a diameter of a circle are (3, 4) and (-3, -4).

- Write the coordinates of the centre of the circle.
- What is the radius of the circle ?
- Write the equation of this circle.

## Solution.

a). Center of the circle

Find the mid point

$$\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} = \frac{3-3}{2}, \frac{4+4}{2}$$
$$= (0,0).$$

b). Radius of the circle= distance between (0,0) and (3,4)

$$= \sqrt{3^2+4^2} = \sqrt{9+16}$$
$$= \sqrt{25} = 5.$$

c). Equation of the circle

$$x^2 + y^2 = r^2$$

$$x^2 + y^2 = 5^2$$

$$x^2 + y^2 = 25.$$

.....drvsvr

## Question. 43.

The base radius and height of a cylindrical block of wood are 8 centimetres and 15 centimetres. A cone of maximum size is carved out of this.

- (a) What are the radius and height of the cone?
- (b) Find its slant height.
- (c) Find the curved surface area of this cone.

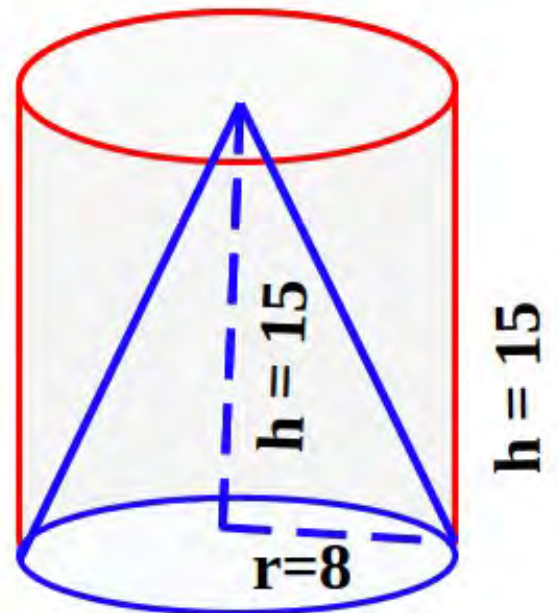
### Solution.

Radius = 8cm; height = 15cm.

a) Radius = 8cm  
Height = 15cm

b) Slant height

$$\begin{aligned}l &= \sqrt{h^2 + r^2} \\&= \sqrt{15^2 + 8^2} \\&= \sqrt{225 + 64} = \sqrt{289} = 17\text{cm}\end{aligned}$$

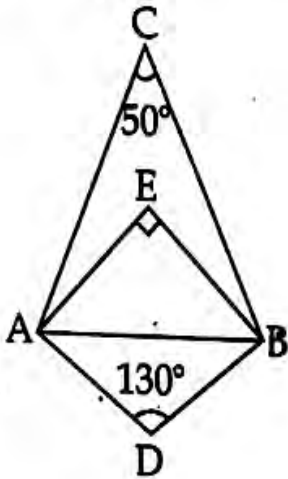


c). CSA of the cone =  $\pi r l$ .  
 $= \pi \times 8 \times 17 = 136\pi \text{cm}^2$ .

.....drvsvr

### Question. 44.

In the figure,  $\angle AEB = 90^\circ$ ,  $\angle C = 50^\circ$ ,  $\angle D = 130^\circ$ .



- If a circle is drawn with AB as diameter, where is the position of E?  
 (Outside the circle ; on the circle ; inside the circle)
- Write the positions of the points C and D with respect to this circle.
- Is it possible to draw a circle through the four points A, B, C and D? Why?

## Solution.

Given,  $\angle AEB = 90^\circ$ ,  $\angle C = 50^\circ$

$\angle D = 130^\circ$ .

a) E On the circle.

[ $\because 90^\circ$  semicircle]

b) D inside the circle [ $\because > 90$ ]

C out side the circle. [ $\because < 90$ ]

c) Yes,

ABCD be cyclic quadrilateral

.....drvsvr



## Question. 45.

Read the following mathematical concept and answer the questions that follow.

Let us examine the natural numbers, which are powers of 2.

Powers of 2	Digit in the ones place
$2^1 = 2$	2
$2^2 = 4$	4
$2^3 = 8$	8
$2^4 = 16$	6
$2^5 = 32$	2
$2^6 = 64$	4
$2^7 = 128$	8
$2^8 = 256$	6

- (a) Which of the following cannot be the digit in the ones place of a power of 2 ?  
[2, 3, 4, 6]
- (b) Which of the following is the ones place digit in  $2^9$  ?  
[2, 3, 4, 6]
- (c) What is the ones place digit in  $2^{100}$  ?  
[2, 4, 6, 8]
- (d) The ones place digit of  $2^n$  is 6. Then the number n can be :  
[12, 13, 14, 15]
- (e)  $m + n = 26$ , then what is the ones place digit of  $2^m \times 2^n$  ?  
[2, 8, 4, 6]

**Solution.**

- a) 3                      b) 2 ,                      c) 6 ,  
d) 12                      e) 4 .

.....drvsr

**SSLC Model Examination March  
2021**

**Mathematics - English Version.**

**Detailed Solutions with Questions.**

*Prepared by Dr. V. S. RaveendraNath.*

.....