

Assignment

- Represent the complex number $z = -1 - i$

in polar form

Ans) $z = -1 - i$

$$|z| = \sqrt{(-1)^2 + (-1)^2} = \sqrt{2}$$

$$\tan \phi = \left| \frac{y}{x} \right| = \left| \frac{-1}{-1} \right| = \left| \frac{-1}{-1} \right| = 1 = \tan 45^\circ$$

$$= \frac{\pi}{4}$$

$$\text{So, argument} = \frac{\pi}{4} - \pi = \frac{-3\pi}{4}$$

$$z = r (\cos \theta + i \sin \theta)$$

$$= \sqrt{2} \left[\cos \left(\frac{-3\pi}{4} \right) + i \sin \left(\frac{-3\pi}{4} \right) \right]$$

2) Consider the complex number $z = \frac{1+i}{1-i}$

- i. Express z in the form $a + ib$
- ii. Find the modulus and argument of z
- iii. Represent z in the polar form

Solution

$$\begin{aligned} \text{i. } z &= \frac{1+i}{1-i} = \frac{(1+i)(1+i)}{(1-i)(1+i)} \\ &= \frac{1+i+i+i^2}{1-i^2} = \frac{1+2i-1}{1+1} = \frac{2i}{2} = i = 0+i \end{aligned}$$

$$\text{ii. } z = 0 + i$$

$$r = |z| = \sqrt{0^2 + 1^2} = 1$$

\therefore Modulus of $z = 1$

z represents the point $(0, 1)$, lies on the positive imaginary axis.

Hence the argument is $\frac{\pi}{2}$.

\therefore Modulus of $z = 1$ and Argument of $z = \frac{\pi}{2}$

iii. \therefore The polar form of z is $1 \left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2} \right)$