

ONLINE MATHS CLASS - X - 16 (27 / 07 /2021)

2 . CIRCLES – CLASS - 4

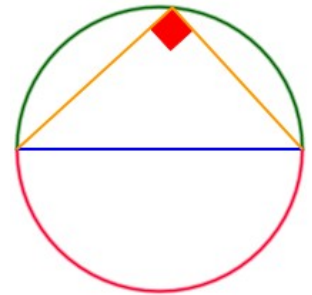
What did we study in the last class ?

- If we join the ends of a diameter of a circle to a point on the circle , we get a right angle .
- Angle in a semicircle is right
- If a pair of lines drawn from the ends of a diameter of a circle are perpendicular to each other , then they meet on the circle .

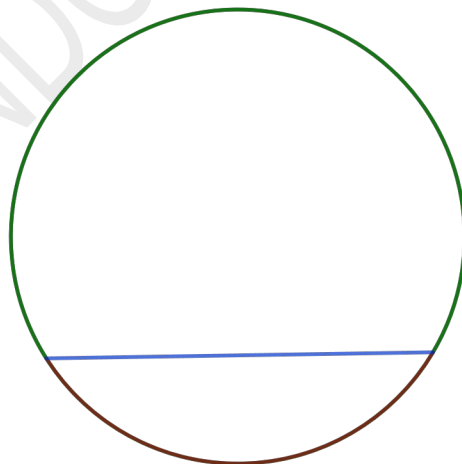
Activity 1

If we draw a diameter of a circle , it will cut the circle into two equal parts (semicircles)

We have already learned that the angle formed by joining the ends of the chord to a point on this parts of the circle is right .



What happens if we draw a chord other than a diameter ?



Does this chord (not a diameter) bisect the circle ?

No . A chord other than a diameter divides a circle into a larger and a smaller parts .

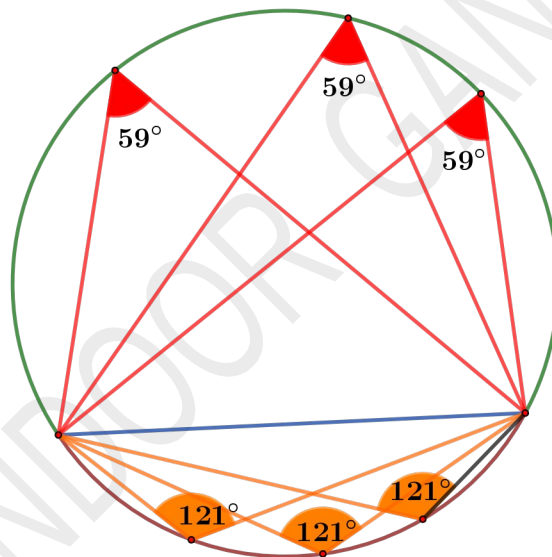
Activity 2

Are there any peculiarity among the angles formed by joining the ends of a chord (not a diameter) to the points on the larger and smaller parts of the circle ?

Draw a circle of radius 5 cm . Draw a chord (not a diameter) on it . This chord will divide the circle into two non equal parts . Mark three points on the larger part of the circle obtained and join the ends of the chord to these points . Three angle are obtained .

Measure these angles .

Similarly mark three points on the smaller part of the circle obtained and join the ends of the chord to these points . Three angle are obtained . Measure these angles .



Findings

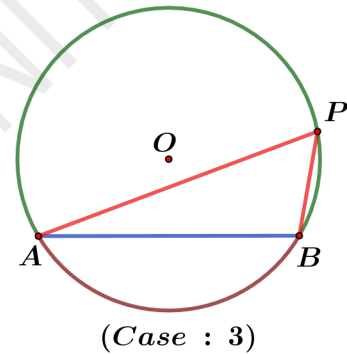
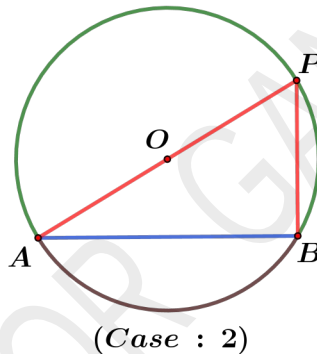
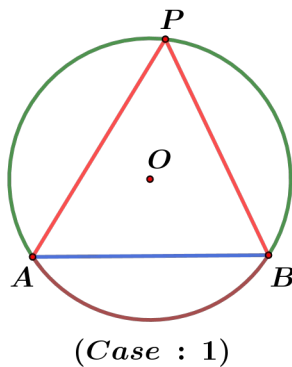
- A chord divides a circle into two parts .
- A chord other than a diameter divides the circle into two non equal parts .
- Three angles formed by the ends of a non diametrical chord to the points on the larger part of the circle are equal .
- Three angles formed by the ends of a non diametrical chord to the points on the smaller part of the circle are equal .

- Three angles formed by the ends of a chord other than a diameter to the points on the larger part of the circle are not equal to the angles formed by the ends of a chord other than a diameter to the points on the smaller part of the circle .

Activity 3

Are the angles formed by the ends of a chord other than a diameter to the points on the smaller part of the circle are equal ? . Let's discuss .

Draw a circle centred at O . Draw a chord AB (not a diameter) . Mark a point P on the larger part of the circle made by the chord AB . Join the ends of the chord to the point P . The following situations may arise .



Case1 : The lines AP and BP may on the either side of the centre .

Case 2 : The line AP may pass through the centre .

Case 3 : The lines AP and BP may on the same side of the centre .

What is the value of $\angle APB$ in all these situations ? Let's discuss .

Case 1 (AP and BP are on the either side of the centre)

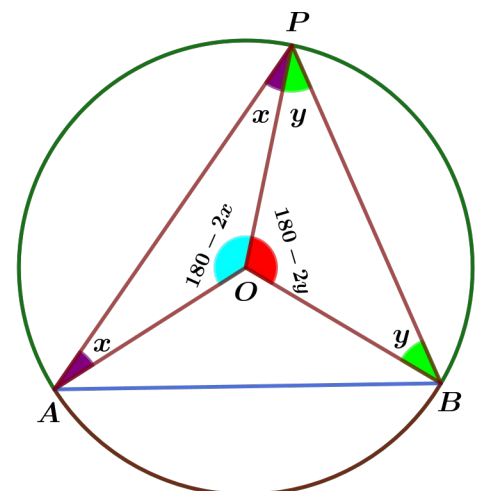
Draw the lines OA , OB and OP .

$$OA = OB = OP \quad (\text{Radii of a circle are equal})$$

$\triangle AOP$ is an isosceles triangle . ($OA = OP$)

$$\angle OAP = \angle OPA = x^\circ$$

$$\implies \angle AOP = (180 - 2x)^\circ \quad (\text{Sum of the angles of a}$$



triangle is 180°)

BOP is an isosceles triangle . ($OB = OP$)

$$\angle OBP = \angle OPB = y^\circ$$

$$\implies \angle BOP = (180 - 2y)^\circ$$

$$\angle AOB = 360 - (180 - 2x + 180 - 2y) \quad (\text{Angle around a point is } 360^\circ)$$

$$= 360 - (180 + 180 - 2x - 2y)$$

$$= 360 - (360 - 2x - 2y)$$

$$= 360 - 360 + 2x + 2y = 2x + 2y$$

$$= 2(x + y) = 2x \angle APB$$

Findings (Case 1)

- $\angle AOB = 2 \times \angle APB \implies \angle APB = \frac{1}{2} \times \angle AOB$
- The angle formed by joining the ends of a chord to a point on the larger part of the circle is half the angle made by joining the ends of the chord to the centre of the circle .
- Since the angle formed by joining the ends of the chord to the centre of the circle is always a constant , the angle formed by joining the ends of a chord to the points on the larger part of the circle are equal .

Case 2 (The line AP passes through the centre of the circle)

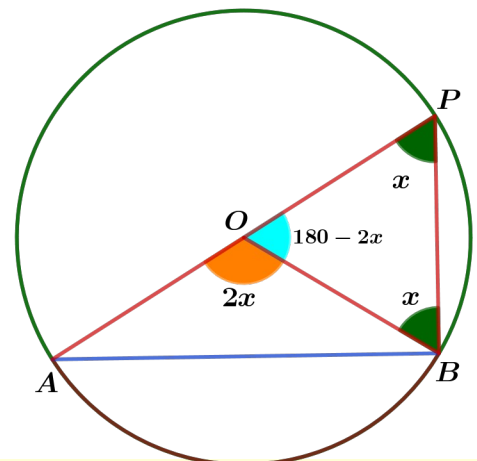
Draw the line OB .

$$OA = OB = OP \quad (\text{Radii of a circle are equal})$$

BOP is an isosceles triangle . ($OB = OP$)

$$\angle OBP = \angle OPB = x^\circ \implies \angle BOP = (180 - 2x)^\circ$$

(Sum of the angles of a triangle is 180°)



$$\angle AOB = 180 - (180 - 2x) = 180 - 180 + 2x = 2x^\circ \quad (\text{linear pair})$$

That is , $\angle AOB = 2x \angle APB$

Findings (Case 2)

- $\angle AOB = 2 \times \angle APB \implies \angle APB = \frac{1}{2} \times \angle AOB$
- The angle formed by joining the ends of a chord to a point on the larger part of the circle is half the angle made by joining the ends of the chord to the centre of the circle .
- Since the angle formed by joining the ends of the chord to the centre of the circle is always a constant , the angle formed by joining the ends of a chord to the points on the larger part of the circle are equal .

Case 3 (AP and BP are on the same side of the centre)

Draw the lines OA, OB and OP .

$$OA = OB = OP \quad (\text{Radii of a circle are equal})$$

AOP is an isosceles triangle . ($OA=OP$)

$$\angle OAP = \angle OPA = x^\circ$$

$$\implies \angle AOP = (180 - 2x)^\circ$$

BOP is an isosceles triangle . ($OB = OP$)

$$\angle OBP = \angle OPB = y^\circ$$

$$\implies \angle BOP = (180 - 2y)^\circ \quad (\text{Sum of the angles of a triangle is } 180^\circ)$$

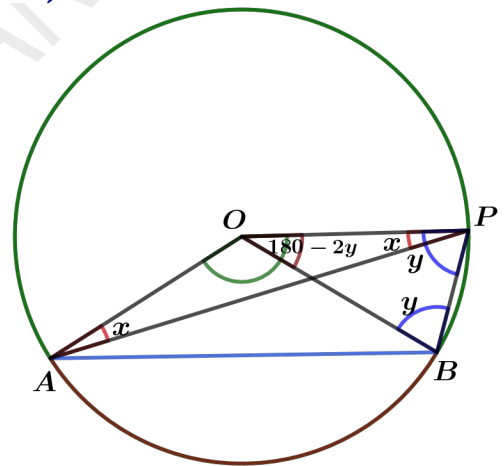
$$\angle APB = (y - x)^\circ$$

$$\angle AOB = \angle AOP - \angle BOP$$

$$= 180 - 2x - (180 - 2y)$$

$$= 180 - 2x - 180 + 2y$$

$$= 180 - 180 + 2y - 2x = 2y - 2x = 2(y - x) = 2x \angle APB$$



Findings (Case 3)

- $\angle AOB = 2 \times \angle APB \implies \angle APB = \frac{1}{2} \times \angle AOB$
- The angle formed by joining the ends of a chord to a point on the larger part of the circle is half the angle made by joining the ends of the chord to the centre of the circle .
- Since the angle formed by joining the ends of the chord to the centre of the circle is always a constant , the angle formed by joining the ends of a chord to the points on the larger part of the circle are equal .

Conclusion

If we joining the ends of a chord other than a diameter to any point on the larger part of the circle , we get an angle which is half the size of the angle , we get by joining them to the centre of the circle .

Assignment .

What is the relation among the angles formed by joining the ends of a chord other than a diameter to the points on the larger and smaller parts of the circle ?