

Assignment AnswersT.B Page 53

Q1)

a) Join OA

Since $OA = OB$ & $OC = OA$, ΔOAB & ΔOAC are isosceles trianglesGiven $\angle OBA = 20^\circ$, Given $\angle OCA = 30^\circ$

$$\therefore \angle OAB = 20^\circ$$

$$\therefore \angle OAC = 30^\circ$$

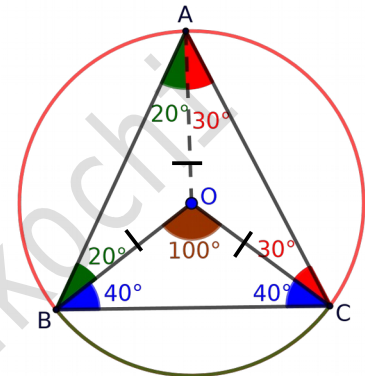
$$\angle BAC = \angle OAB + \angle OAC$$

$$= 20^\circ + 30^\circ = 50^\circ$$

$$\angle BOC = 2 \times 50^\circ = 100^\circ$$

Since $OB = OC$, ΔOBC is an isosceles triangle.

$$\therefore \angle OBC = \angle OCB = \frac{180^\circ - 100^\circ}{2} = \frac{80^\circ}{2} = 40^\circ$$

Angles of ΔABC are $\angle A = 50^\circ$, $\angle B = 60^\circ$, $\angle C = 70^\circ$ Angles of ΔOBC are $\angle OBC = 40^\circ$, $\angle OCB = 40^\circ$, $\angle BOC = 100^\circ$ 

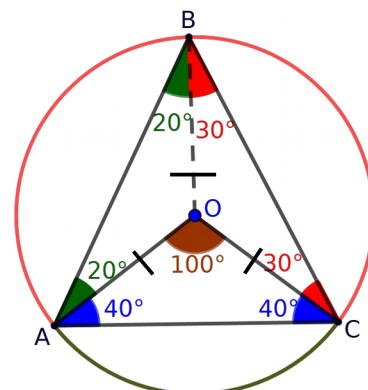
b)

 ΔOAC is an isosceles triangle.Given $\angle OAC = 40^\circ$

$$\therefore \angle OCA = 40^\circ$$

$$\angle AOC = 180^\circ - 80^\circ = 100^\circ$$

$$\therefore \angle ABC = \frac{100^\circ}{2} = 50^\circ$$



Join OB, ΔOBC is an isosceles triangle

So $\angle OCB = \angle OBC = 30^\circ$

$\therefore \angle OBA = 50^\circ - 30^\circ = 20^\circ$

ΔOBA is an isosceles triangle, So $\angle OAB = 20^\circ$

Angles of ΔABC are $\angle A = 60^\circ$, $\angle B = 50^\circ$, $\angle C = 70^\circ$

Angles of ΔOBC are $\angle OBC = 30^\circ$, $\angle OCA = 30^\circ$, $\angle BOC = 180^\circ - 60^\circ = 120^\circ$

c) Given $\angle BOC = 70^\circ$

ΔOBC is an isosceles triangle

$$\begin{aligned} \angle OBC = \angle OCB &= \frac{180^\circ - 70^\circ}{2} \\ &= \frac{110^\circ}{2} = 55^\circ \end{aligned}$$

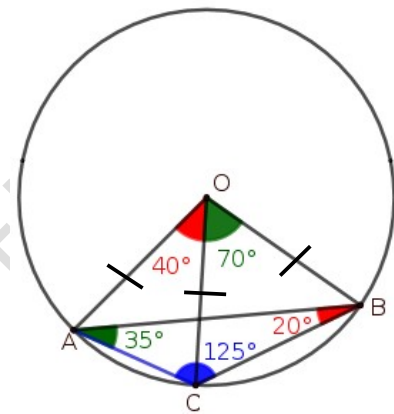
Angles of ΔOBC are $\angle OBC = 55^\circ$,
 $\angle BOC = 70^\circ$, $\angle OCB = 55^\circ$

Since $\angle AOC = 40^\circ$, $\angle ABC = \frac{40^\circ}{2} = 20^\circ$

Since $\angle BOC = 70^\circ$, $\angle BAC = \frac{70^\circ}{2} = 35^\circ$

$\angle ACB = 180^\circ - (20^\circ + 35^\circ) = 180^\circ - 55^\circ = 125^\circ$

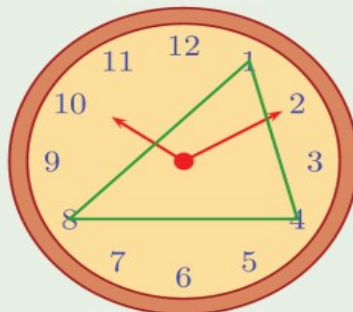
Angles of ΔABC are 125° , 20° , 35°



T B Page 53

Q2)

The numbers 1, 4, 8 on a clock's face are joined to make a triangle.



Calculate the angles of this triangle.

How many equilateral triangles can we make by joining numbers on the clock's face?

Ans)

a) In a clock's face

$$60 \text{ minute} = 360^\circ$$

$$1 \text{ minute} = \frac{360^\circ}{60} = 6^\circ$$

$$5 \text{ minute} = 30^\circ$$

$$\angle BOC = 4 \times 30^\circ = 120^\circ$$

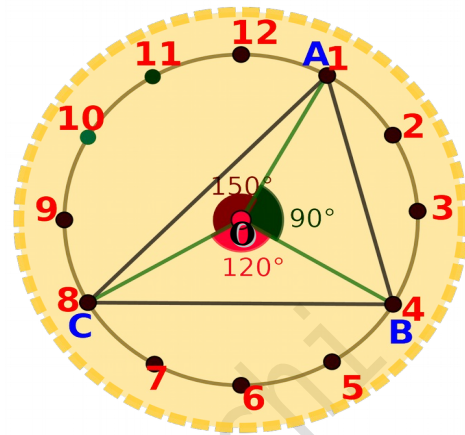
$$\therefore \angle A = \frac{120^\circ}{2} = 60^\circ$$

$$\angle AOC = 5 \times 30^\circ = 150^\circ$$

$$\therefore \angle B = \frac{150^\circ}{2} = 75^\circ$$

$$\angle AOB = 3 \times 30^\circ = 90^\circ$$

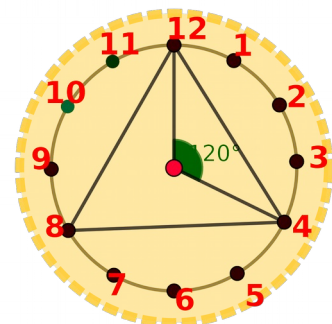
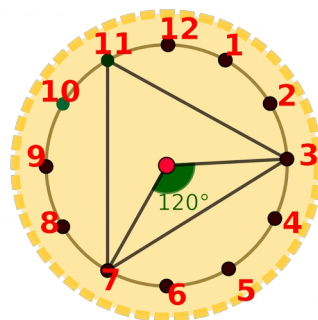
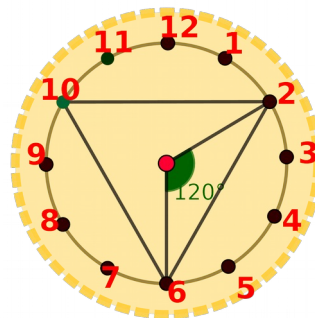
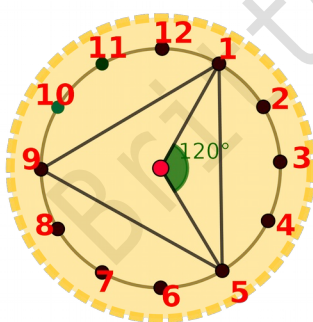
$$\therefore \angle C = \frac{90^\circ}{2} = 45^\circ$$



b)

We can make 4 equilateral triangles by joining the numbers on the clock

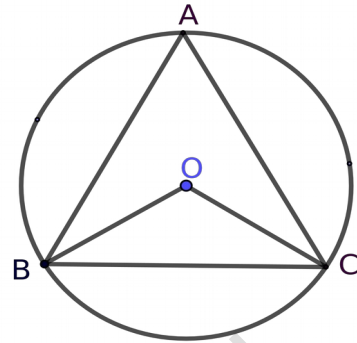
(1, 5, 9), (2, 6, 10), (3, 7, 11), (4, 8, 12)



Assignment

Q) In the figure O is the centre of the circle and ABC is an equilateral triangle.

Find $\angle BAC$ and $\angle ABO$.

**T.B Page 54**

- (5) In the picture, O is the centre of the circle and A, B, C , are points on it. Prove that $\angle OAC + \angle ABC = 90^\circ$.

