

○ **2 . Circles - Class 9** ○

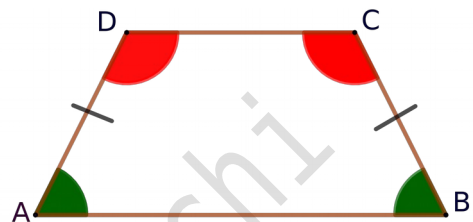
To view class

Assignment Answer

Since ABCD is an isosceles trapezium

AD = BC and also

AB is parallel to DC .



We have to prove $\angle A + \angle C = 180^\circ$ & $\angle B + \angle D = 180^\circ$

Since ABCD is an isosceles trapezium,

$$\angle A = \angle B \quad \dots\dots\dots (1)$$

Since AB // DC

$$\angle A + \angle D = 180^\circ \quad \dots\dots\dots (2) \quad (\text{Co-interior angles are supplementary})$$

From (1) & (2) we have

$$\angle B + \angle D = 180^\circ$$

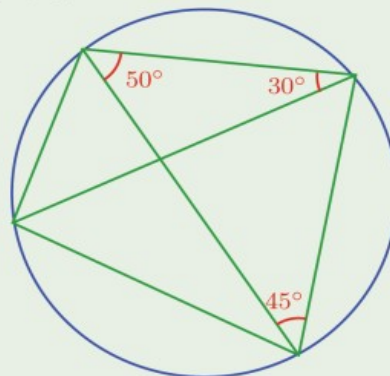
Also, $\angle A + \angle C = 180^\circ$

Since the opposite angles are supplementary , ABCD is cyclic.

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Q1)

Calculate the angles of the quadrilateral in the picture and also the angles between their diagonals:



Ans) Given , $\angle BDC = 50^\circ$

So , $\angle BAC = 50^\circ$

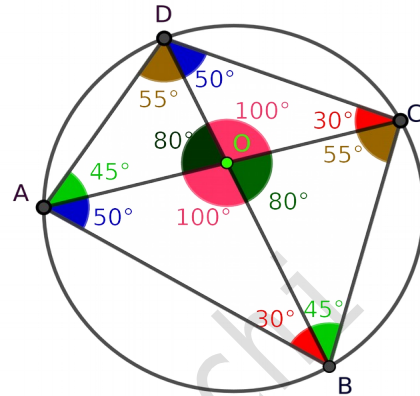
Given , $\angle ACD = 30^\circ$

So, $\angle ABD = 30^\circ$

Given , $\angle CBD = 45^\circ$

So, $\angle CAD = 45^\circ$

All angles made by an arc on the alternate arc are equal



Consider $\triangle ABC$,

$$\angle ACB = 180^\circ - (50^\circ + 75^\circ) = 180^\circ - 125^\circ = 55^\circ$$

So $\angle ADB = 55^\circ$

Consider $\triangle AOD$, $\angle AOD = 180^\circ - (55^\circ + 45^\circ) = 180^\circ - 100^\circ = 80^\circ$

$$\angle DOC = 180^\circ - 80^\circ = 100^\circ \text{ (Linear pair)}$$

$$\angle AOD = \angle BOC = 80^\circ \text{ (opposite angles)}$$

$$\angle DOC = \angle AOB = 100^\circ \text{ (opposite angles)}$$

\therefore Angles of the quadrilateral are

$$\angle A = 45^\circ + 50^\circ = 95^\circ$$

$$\angle B = 30^\circ + 45^\circ = 75^\circ$$

$$\angle C = 55^\circ + 30^\circ = 85^\circ$$

$$\angle D = 50^\circ + 55^\circ = 105^\circ$$

Angles between diagonals are

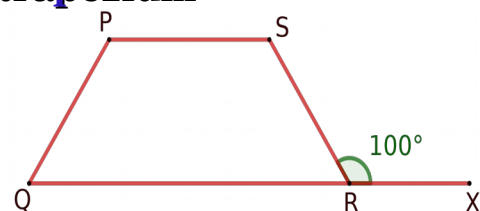
$$\angle AOD = \angle BOC = 80^\circ$$

$$\angle DOC = \angle AOB = 100^\circ$$

Assignment

Q1) In the figure PQRS is an isosceles trapezium and QR is extended to X .

If $\angle SRX = 100^\circ$,
find all angles of PQRS ?



Q2) Prove that any non- isosceles trapezium is not cyclic ?

