

**Plus One Higher Secondary Examination 2021**

**Mathematics**

**Answer key**

**Prepared by**

**Academic Council**

*Mathematics Association Kollam*

1. (i)  $A = \{1,2,3,4,5\}$

(ii)  $A \cap B = \{1,2\}$

(iii)  $A - B = \{3,4,5\}$

2.  $t_1 = 105, t_n = 995, d = 5$

$$n = \frac{t_n - t_1}{d} + 1 = \frac{995 - 105}{5} + 1 = 179$$

$$S_n = \frac{n}{2}(a + t_n) = \frac{179}{2}(105 + 995) = 98450$$

3.  $(2x + 3)^5$

$$\begin{aligned} &= {}^5C_0 (2x)^5 + {}^5C_1 (2x)^4 \cdot 3 + {}^5C_2 (2x)^3 \cdot 3^2 + {}^5C_3 (2x)^2 \cdot 3^3 + {}^5C_4 (2x) \cdot 3^4 + {}^5C_5 \cdot 3^5 \\ &= 32x^5 + 240x^4 + 720x^3 + 1080x^2 + 810x + 243 \end{aligned}$$

4. LHL =  $\lim_{x \rightarrow 0^-} 2x + 3 = 2 \cdot 0 + 3 = 3$

RHL =  $\lim_{x \rightarrow 0^+} 3(x + 1) = 3(0 + 1) = 3$

Since LHL = RHL,  $\lim_{x \rightarrow 0} \begin{cases} 2x + 3; & x \leq 0 \\ 3(x + 1); & x \geq 0 \end{cases} = 3$

5.  $n(H) = 250, n(E) = 200, n(H \cup E) = 400$

No. people who speak Hindi and English =  $n(H \cap E)$

$$n(H \cup E) = n(H) + n(E) - n(H \cap E)$$

$$400 = 250 + 200 - n(H \cap E)$$

$$n(H \cap E) = 250 + 200 - 400 = 50$$

6. Given line is  $2x + 3y - 6 = 0$

$$A = 2, B = 3, C = -6$$

$$\text{Slope} = \frac{-A}{B} = \frac{-2}{3}$$

$$\text{y-intercept} = \frac{-C}{B} = 2$$

7. Given Parabola is  $y^2 = 12x$

$$4a = 12, a = 3$$

$$(i) \text{Focus} = (a, 0) = (3, 0)$$

$$(ii) \text{Equation of Directrix is } x = -a \text{ or } x = -3 \text{ or } x + 3 = 0$$

$$(iii) \text{Length of latus rectum} = 4a = 12$$

8. (i) YZ Plane

$$\begin{aligned} (ii) \text{Distance} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2} \\ &= \sqrt{(2 - (-3))^2 + (4 - 7)^2 + (-1 - 2)^2} \\ &= \sqrt{25 + 9 + 9} = \sqrt{43} \end{aligned}$$

9.  $P(n) : 7^n - 3^n$  is divisible by 4

$P(1) : 7^1 - 3^1$  is divisible by 4

4 is divisible by 4

$P(1)$  is true

$P(k) : 7^k - 3^k$  is divisible by 4

Assume that  $P(k)$  is true

$$7^k - 3^k = 4m$$

$$7^k = 4m + 3^k$$

P(k+1):  $7^{k+1} - 3^{k+1}$  is divisible by 4

We have to prove that p(k+1) is true

$$\begin{aligned}7^{k+1} - 3^{k+1} &= 7^k \cdot 7^1 - 3^k \cdot 3^1 \\ &= 7(4m + 3^k) - 3 \cdot 3^k \\ &= 28m + 7 \cdot 3^k - 3 \cdot 3^k \\ &= 28m + 4 \cdot 3^k \\ &= 4(7m + 3^k)\end{aligned}$$

$7^{k+1} - 3^{k+1}$  is divisible by 4

P(k+1) is true.

Hence by P.M.I then result is true for all natural number n

**10.(i)** General Term  $T_{r+1} = {}^n C_r a^{n-r} b^r$   
 $= {}^{12} C_r x^{12-r} (-2y)^r$

**(ii)** Put  $r=3$ , 4<sup>th</sup> Term,  $T_4 = {}^{12} C_3 x^{12-3} (-2y)^3 = -1760 x^9 y^3$

**11.** Let the ratio be k:1

The Z co-ordinate of XY plane = 0

$$\frac{k(-8) + 1(10)}{k+1} = 0$$

$$8k = 10$$

$$k = \frac{5}{4}$$

Ratio=5:4

**12. (i)** It is false that every natural number is greater than zero

**(ii)** Converse : If a number  $n$  is even, then  $n^2$  is even

Contra positive: If a number  $n$  is not even, then  $n^2$  is not even

**13. (i)** 8

**(ii)**  $\{1,2\}, \{2,3\}, \{1,3\}$

**(iii)**  $A' = \{4,5,6\}$

**14. (i)**  $x+1 = 3$

$$x = 2$$

$$y-2 = 1$$

$$y = 3$$

**(ii)**  $A \times B = \{(1,3), (1,4), (2,3), (2,4), (3,3), (3,4)\}$

**15. (i)**  $\sin x = -\frac{\sqrt{3}}{2}$

$$\tan x = \sqrt{3}$$

**(ii)**  $\sin^2 \frac{2\pi}{6} + \cos^2 \frac{\pi}{3} = \left(\frac{1}{2}\right)^2 + \left(\frac{1}{2}\right)^2 = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$

**16.**  $1 + 3 + 3^2 + \dots + 3^{n-1} = \frac{3^n - 1}{2}$

$P(n) : 1 + 3 + 3^2 + \dots + 3^{n-1} = \frac{3^n - 1}{2}$

$P(1) : 1 = \frac{3^1 - 1}{2}$

$$1 = 1$$

P(1) is true

$$P(k) : 1 + 3 + 3^2 + \dots + 3^{k-1} = \frac{3^k - 1}{2}$$

Assume that p(k) is true

$$P(k+1) : 1 + 3 + 3^2 + \dots + 3^{k+1-1} = \frac{3^{k+1} - 1}{2}$$

We have to prove that p(k+1) is true

L.H.S

$$1 + 3 + 3^2 + \dots + 3^k$$

$$= [1 + 3 + 3^2 + \dots + 3^{k-1}] + 3^k$$

$$= \frac{3^k - 1}{2} + 3^k$$

$$= \frac{3^k - 1 + 2 \cdot 3^k}{2}$$

$$= \frac{3 \cdot 3^k - 1}{2} = \frac{3^{k+1} - 1}{2} = \text{RHS}$$

P(k+1) is true.

Hence by P.M.I then result is true for all natural number n

**17. (i)** i

**(ii)**  $3(7+i7) + i(7+i7)$

$$= 21 + 21i + 7i + 7i^2$$

$$= 21 + 28i - 7$$

$$= 14 + 28i$$

$$18. r = \sqrt{1^2 + \sqrt{3}^2} = \sqrt{1 + 3} = \sqrt{4} = 2$$

$$\tan \alpha = \left| \frac{b}{a} \right| = \sqrt{3}$$

$$\alpha = \frac{\pi}{3}$$

Complex number lies in first quadrant

$$\theta = \frac{\pi}{3}$$

$$1 + i\sqrt{3} = 2\left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}\right)$$

19. (i) 10

(ii)  ${}^{21}C_2 = 210$

20. (i) Number of 3 digit numbers can be formed using 5 digits =  $5 P_3$

$$= 5 \times 4 \times 3 = 60$$

(ii) Required number of permutations =  $\frac{9!}{4! 2!}$

$$= 7560$$

21. Slope of the line,  $m = \frac{-A}{B} = \frac{-1}{-7} = \frac{1}{7}$

Slope of the perpendicular line = -7

Equation of the perpendicular line is  $(y - y_1) = m(x - x_1)$

$$\text{ie, } y - (-3) = (-7)(x - 2)$$

$$y + 3 = -7x + 14$$

$$7x + y = 11$$

**22. (i)**  $a=5, c=4$

$$c^2 = a^2 - b^2$$

$$4^2 = 5^2 - b^2$$

$$16 = 25 - b^2$$

$$b=3$$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

$$\frac{x^2}{5^2} + \frac{y^2}{3^2} = 1$$

**(ii)**  $e = \frac{c}{a} = \frac{4}{5}$

**23.(i)**  $y = x(x^2 + 2x + 1)$

$$= x^3 + 2x^2 + x$$

$$\frac{dy}{dx} = 3x^2 + 4x + 1$$

**(ii)**  $y = \frac{x+1}{x}$

$$\frac{dy}{dx} = \frac{x \times \frac{d(x+1)}{dx} - (x+1) \times \frac{d(x)}{dx}}{(x)^2} = \frac{x \cdot 1 - (x+1) \cdot 1}{x^2} = \frac{-1}{x^2}$$

**24.** Assume that  $\sqrt{5}$  is rational

$$\sqrt{5} = \frac{p}{q}, \text{ where } p \text{ and } q \text{ do not have a common factor}$$

$$P = \sqrt{5} q$$

$$P^2 = 5 q^2$$

$P^2$  is a multiple of 5

$P$  is a multiple of 5

$$P = 5m$$

$$(5m)^2 = 5 q^2$$



$$25 m^2 = 5 q^2$$

$$q^2 = 5 m^2$$

$q^2$  is a multiple of 5

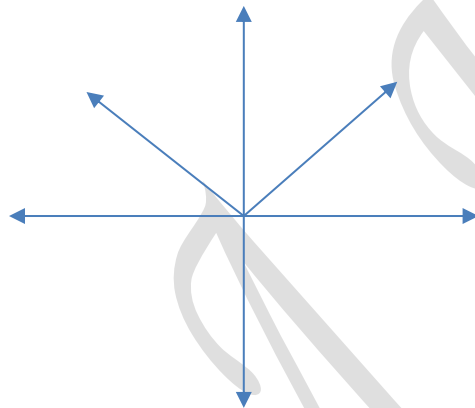
$q$  is a multiple of 5

$P$  and  $q$  have a common factor 5, which is a contradiction

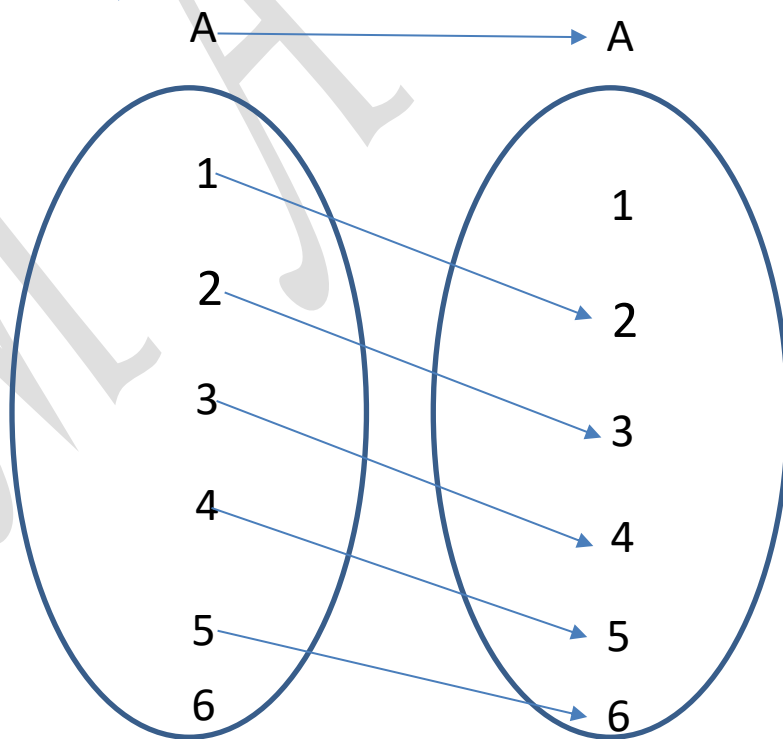
Our assumption is wrong

$\sqrt{5}$  is irrational

25. (i)



(ii) (a)



(b) domain =  $\{1,2,3,4,5\}$

26. (i)  $\sin 75^\circ$

$$= \sin (45^\circ + 30^\circ)$$

$$= \sin 45^\circ \cos 30^\circ + \cos 45^\circ \sin 30^\circ$$

$$= \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2}$$

$$= \frac{\sqrt{3}}{2\sqrt{2}} + \frac{1}{2\sqrt{2}}$$

$$= \frac{\sqrt{3}+1}{2\sqrt{2}}$$

(ii)  $\frac{\sin 5x + \sin 3x}{\cos 5x + \cos 3x} = \tan 4x$

$$\frac{\sin 5x + \sin 3x}{\cos 5x + \cos 3x} = \frac{2 \sin \frac{5x+3x}{2} \cos \frac{5x-3x}{2}}{2 \cos \frac{5x+3x}{2} \cos \frac{5x-3x}{2}}$$

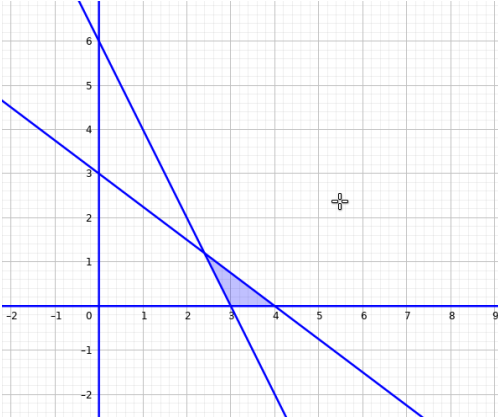
$$= \frac{\sin 4x \cos x}{\cos 4x \cos x} = \frac{\sin 4x}{\cos 4x} = \tan 4x$$

27.  $2x + y = 6$

x	0	3
y	6	0

$$3x + 4y = 12$$

x	0	4
y	3	0



28. (i)  $a = 5, r = 5$

$$a_{12} = a r^{11}$$

$$= 5 \cdot 5^{11}$$

$$= 5^{12}$$

(ii)  $8 + 88 + 888 + \dots$  to  $n$  terms

$$= 8[1 + 11 + 111 + \dots \text{ to } n \text{ terms}]$$

$$= \frac{8}{9}[9 + 99 + 999 + \dots \text{ to } n \text{ terms}]$$

$$= \frac{8}{9}[(10-1) + (100-1) + (1000-1) + \dots \text{ to } n \text{ terms}]$$

$$= \frac{8}{9}[(10 + 100 + 1000 + \dots \text{ to } n \text{ terms}) - (1 + 1 + 1 + \dots \text{ to } n \text{ terms})]$$

$$= \frac{8}{9} \left[ 10 \left( \frac{10^n - 1}{10 - 1} \right) - n \right]$$

29.

$x_i$	$f_i$	$xif_i$	$(x_i - \bar{x})^2$	$f_i(x_i - \bar{x})^2$
35	3	105	729	2187
45	7	315	289	2023
55	12	660	49	588
65	15	975	9	135
75	8	600	169	1352
85	3	255	529	1587
95	2	190	1089	2178
	<b>N=50</b>	<b>3100</b>		<b>10050</b>

(i) Mean,  $\bar{x} = \frac{\sum x_i f_i}{N} = \frac{3100}{50} = 62$

(ii) Variance =  $\frac{\sum f_i(x_i - \bar{x})^2}{N} = \frac{10050}{50} = 201$

(iii) Standard deviation =  $\sqrt{\text{variance}} = \sqrt{201}$

30. (i) Sample space,  $S = \{HH, HT, TH, TT\}$

The Event,  $E = \{HT, TH, TT\}$

$$P(E) = \frac{3}{4}$$

(ii) a)  $P(E \cup F) = P(E) + P(F) - P(E \cap F)$

$$= \frac{1}{4} + \frac{1}{2} - \frac{1}{8} = \frac{5}{8}$$

b)  $P(E' \cap F') = P(E \cup F)'$

$$= 1 - P(E \cup F)$$

$$= 1 - \frac{5}{8} = \frac{3}{8}$$

---