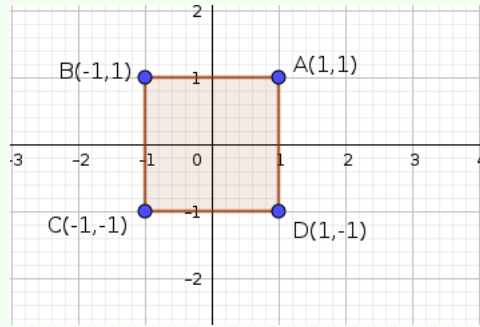


## Session 66 | Co ordinates 1 | Worksheet 66

1) Draw coordinate axes

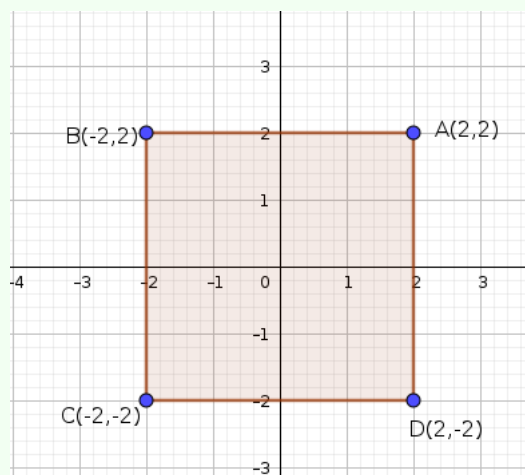
- Mark the points  $A(1, 1)$ ,  $B(-1, 1)$ ,  $C(-1, -1)$ ,  $D(1, -1)$
- Complete the quadrilateral  $ABCD$  and suggest a suitable name to it
- Find the perimeter of  $ABCD$
- Calculate the area of  $ABCD$



- Figure is given above
- $ABCD$  is a square
- One side is 2 unit. Perimeter is  $4 \times 2 = 8$
- Area  $2 \times 2 = 4$  sq.unit

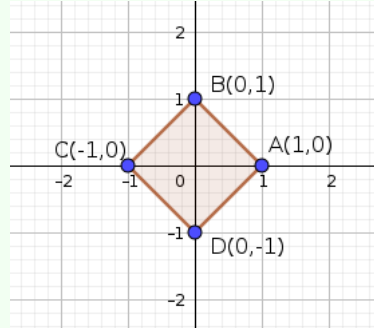
2) Draw coordinate axes

- Mark the points  $A(2, 2)$ ,  $B(-2, 2)$ ,  $C(-2, -2)$  and  $D(2, -2)$
- Suggest a suitable name to  $ABCD$
- Find the perimeter of  $ABCD$
- Calculate the area of  $ABCD$



- Figure is given above
- Square
- One side is 4 unit. Perimeter is  $4 \times 4 = 16$
- Area  $4 \times 4 = 16$  sq.unit

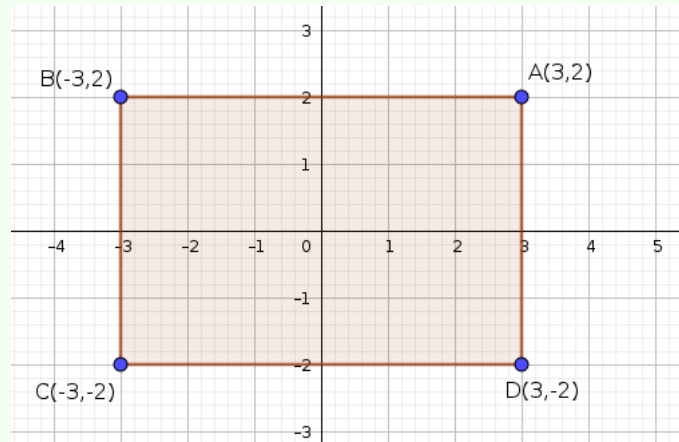
- Mark the points  $A(1, 0)$ ,  $B(0, -1)$ ,  $C(-1, 0)$ ,  $D(0, -1)$
- Suggest a suitable name to  $ABCD$
- Find the perimeter of  $ABCD$
- Calculate the area of  $ABCD$



- Figure is given above
- Square
- One side is  $\sqrt{2}$ . Perimeter is  $4\sqrt{2}$
- Area  $\sqrt{2} \times \sqrt{2} = 2$

- 4) The vertices of  $ABCD$  are  $A(3, 2)$ ,  $B(-3, 2)$ ,  $C(-3, -2)$ ,  $D(3, -2)$

- Draw coordinate axes and mark the points
- Find the length of sides?
- Calculate perimeter and area of  $ABCD$
- What is the length of its diagonal



- Diagram is given above
- $AB = CD = 6$ ,  $AD = BC = 4$
- Perimeter =  $2(6 + 4) = 20$ , Area =  $6 \times 4 = 24$
- Diagonal =  $\sqrt{6^2 + 4^2} = \sqrt{52}$

- 5) Choose the correct answer

- Which of the following is a point on  $x$  axis  
 (a)  $(0, 6)$     (b)  $(-3, 6)$     (c)  $(-3, 0)$     (d)  $(1, 1)$

b) What is the radius of the circle with centre  $(0, 0)$  and passing through  $(1, 1)$ ?

3

(a)  $\sqrt{2}$     (b)  $\sqrt{3}$     (c)  $\sqrt{5}$     (d) 1

c) What is the distance between the points  $(-7, 3)$  and  $(10, 3)$

(a) 17    (b) 10    (c) 8    (d) 11

a)  $(-3, 0)$

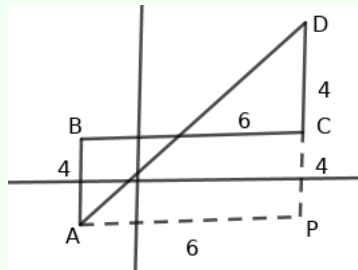
b)  $\sqrt{2}$

c)  $\sqrt{17}$

1

## Session 67 | Co ordinates 2 | Worksheet 67

- 1) Draw coordinate axes and mark  $A(-2, -2)$ 
  - a) Write the coordinates of  $B$  which is 4 unit away parallel to  $y$  axis in the upward direction.
  - b) Write the coordinates of  $C$  which is 6 unit in the right of  $B$  parallel to  $x$  axis
  - c) Write the coordinates of  $D$  which is 4 unit above  $C$  on the line parallel to  $y$  axis
  - d) What is the distance between  $A$  and  $D$ ?



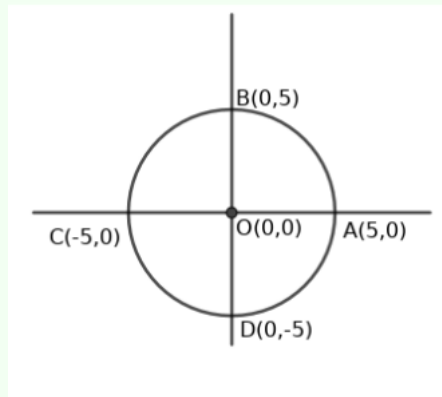
- a)  $B(-2, -2 + 4) = B(-2, 2)$
- b)  $C(-2 + 6, 2) = C(4, 2)$
- c)  $D(4, 2 + 4) = D(4, 6)$
- d)  $AD = \sqrt{AP^2 + PD^2} = \sqrt{6^2 + 8^2} = 10$

- 2)  $A(1, 1), B(-3, 1), C(-3, -4), D(1, -4)$  are the coordintes of the vertices of a rectangle.
  - a) What is the length of the side  $AB$ ?
  - b) What is the length of the side  $AD$ ?
  - c) Calcualte the perimetre and area of the rectangle.

- a)  $AB = |1 - (-3)| = 4$
- b)  $AD = |1 - (-4)| = 5$
- c) Perimetre =  $2(4 + 5) = 18$   
Area =  $4 \times 5 = 20$

3) There is a circle with centre at the origin . The circle passes through  $(5, 0)$  <sup>2</sup>

- What is the radius of the circle?
- What are the coordinates of the points where the circle cut the axes?
- Is  $(3, 4)$  a point on the circle? How can we realize it?



- 5
- $A(5, 0), B(0, 5), C(-5, 0), D(0, -5)$
- The distance from origin to the point  $(3, 4)$  is  $= \sqrt{3^2 + 4^2} = 5$ , the radius of the circle. This point is on this circle.

4) The vertices of a right triangle are  $A(1, 1), B(4, 1), C(1, 5)$ .

- Name the vertex at which  $90^\circ$  angle is taken
- What is the length of perpendicular sides?
- What is the length of its hypotenuse?
- What is the radius of its circumcircle?

- $A(1, 1)$
- $AB = |4 - 1| = 3, AC = |5 - 1| = 4$
- $BC = \sqrt{3^2 + 4^2} = 5$
- Circumradius  $= \frac{5}{2} = 2.5$

## Session 68 | Coordinates 3 | Worksheet 68

1) In  $\triangle ABC$ ,  $A(1, 3)$ ,  $B(7, 3)$ ,  $C(4, 11)$  are the vertices

- What is the length of  $AB$ ?
- What is the altitude to  $AB$ ?
- Calculate the area of  $\triangle ABC$

- $AB = |7 - 1| = 6$
- $h = |11 - 3| = 8$
- Area =  $\frac{1}{2} \times 6 \times 8 = 24$  sq.cm

2)  $\triangle ABC$  is an equilateral triangle. Side  $AB$  coincides  $x$  axis. If  $A(-1, 0)$ ,  $B(5, 0)$  then

- What is the length of  $AB$ ?
- What is the altitude of the triangle?
- What are the coordinate pairs of  $C$ ?

- $AB = |5 - (-1)| = 6$
- Altitude =  $3\sqrt{3}$
- $C(2, 3\sqrt{3})$ ,  $C(2, -3\sqrt{3})$

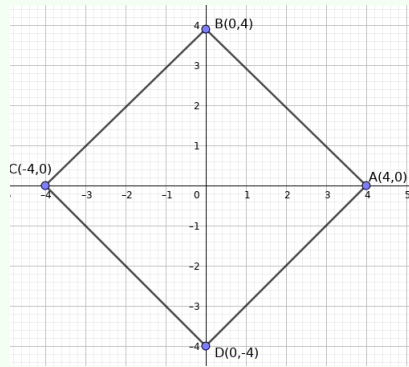
3) Three vertices of  $ABCD$  are  $A(0, 0)$ ,  $B(8, 0)$ ,  $C(8, 4)$

- Write the coordinates of  $D$
- Find the perimeter of the rectangle.
- Calculate the area of the rectangle.

- $D(0, 4)$
- $AB = CD = 8$ ,  $BC = AD = 4$   
Perimetre =  $2(8 + 4) = 24$
- Area =  $8 \times 4 = 32$  sq.unit

4)  $A(4, 0)$ ,  $B(0, 4)$ ,  $C(-4, 0)$ ,  $D(0, -4)$  are the vertices of a quadrilateral

- Suggest a suitable name to  $ABCD$
- Find the length of a side?
- Calculate the area and perimeter



- a) Square
- b)  $4\sqrt{2}$
- c) Area  $(4\sqrt{2})^2 = 32$  sq.unit, Perimetre  $= 4 \times 4\sqrt{2} = 16\sqrt{2}$

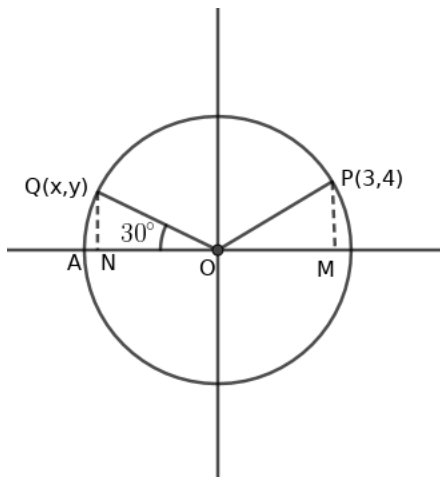
5) In triangle  $ABC$ ,  $A(1, 2)$ ,  $B(7, 2)$  are two vertices.

- a) What is the length of the side  $AB$
- b) In triangle  $ABC$ ,  $\angle A = 90^\circ$ . Write a pair of coordinates of  $C$
- c) What is the length of side  $AC$ ?
- d) Calculate the area of the triangle.

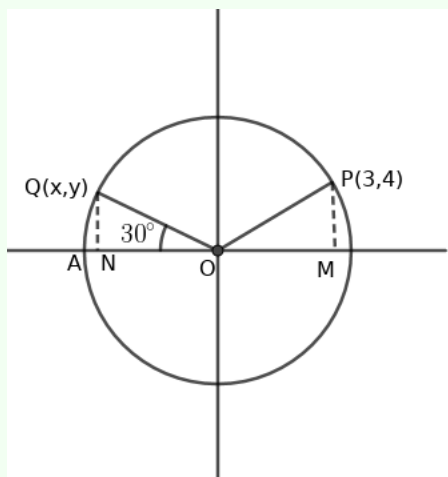
- a)  $AB = |7 - 1| = 6$
- b)  $C(1, 5)$  or any other pair with  $x$  coordinate 1
- c) If  $C(1, 5)$ ,  $AC = |5 - 2| = 3$
- d) In the right triangle  $ABC$  with  $A(1, 2)$ ,  $B(7, 2)$  and  $C(1, 5)$   
Area  $= \frac{1}{2} \times 6 \times 3 = 9$  sq.unit

## Session 69 | Coordinates 4 | Worksheet 69

- 1)  $P(3, 4)$  is a point in a circle with centre at the origin.  
 $Q(x, y)$  is another point on this circle,  $\angle AOQ = 30^\circ$  then



- What is the radius of this circle?
- What are the points where the circle cut the axes ?
- Write the coordinates of  $Q$
- Write the coordinates of three more points on this circle.

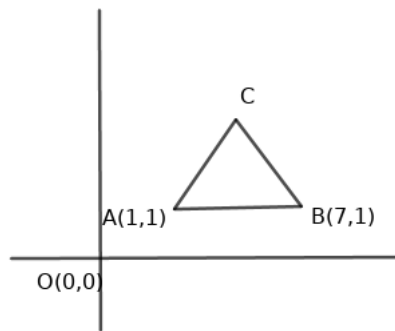


- $OP = \sqrt{OM^2 + PM^2} = \sqrt{3^2 + 4^2} = 5$
- $(5, 0), (0, 5), (-5, 0), (0, -5)$
- $\triangle ONQ$  is a  $30^\circ - 60^\circ - 90^\circ$  triangle  
 $OQ = 5, \therefore QN = \frac{5}{2}, ON = \frac{5}{2}\sqrt{3}$   
 $Q(-\frac{5}{2}\sqrt{3}, \frac{5}{2})$
- $(-3, 4), (-3, -4), (3, -4)$

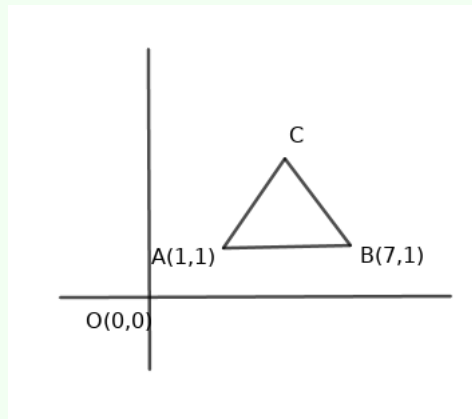


2)  $ABC$  is an equilateral triangle. If  $A(1, 1)$ ,  $B(7, 1)$  then

2

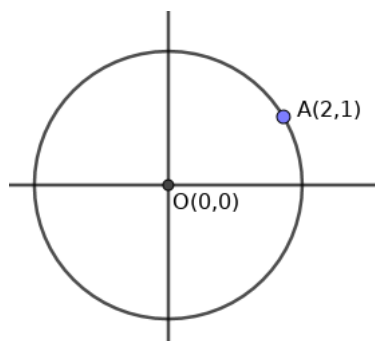


- What is the length of one side?
- What is the altitude of this triangle?
- Write the coordinates of  $C$
- Calculate the area of the triangle.

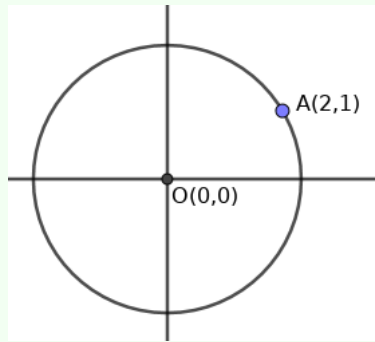


- $AB = |7 - 1| = 6$
- $3\sqrt{3}$
- $C(1 + 3, 1 + 3\sqrt{3})$
- Area =  $\frac{1}{2} \times 6 \times 3\sqrt{3} = 9\sqrt{3}$

3)  $(2, 1)$  is a point on the circle with centre at the origin.

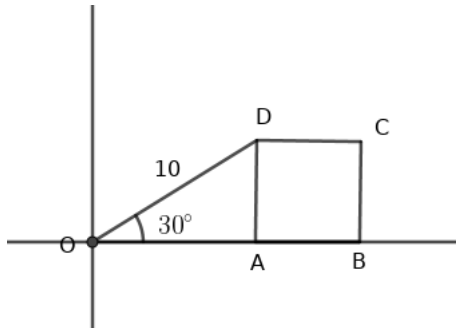


- What is the radius of the circle?
- What are the points where the circle cut the axes?
- Write the coordinates of 7 more points on this circle.



- a) Radius  $\sqrt{1^2 + 2^2} = \sqrt{5}$
- b)  $(\sqrt{5}, 0), (0, \sqrt{5}), (-\sqrt{5}, 0), (0, -\sqrt{5})$
- c)  $(-1, 2), (-1, -2), (1, -2), (2, 1), (-2, 1), (-2, -1), (2, -1)$

4) In the figure  $ABCD$  is a square.  $OD = 10, \angle AOD = 30^\circ$ .



- a) Write the coordinates of  $A$
- b) What is the length of one side of the square?
- c) Write the coordinates of the vertices of the square.

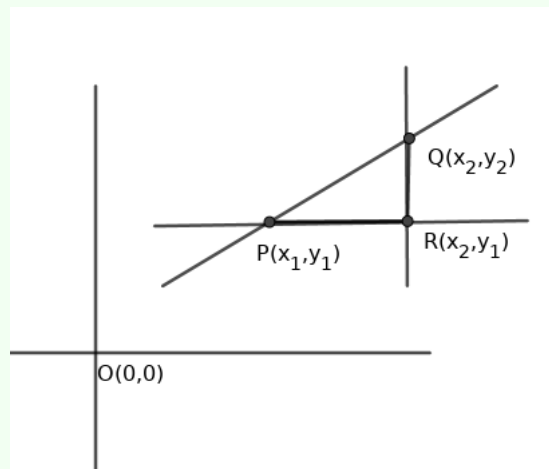
- a)  $OA = 5\sqrt{3}$   
 $A(5\sqrt{3}, 0)$
- b)  $AD = 5$ , Side is 5 unit
- c)  $A(5\sqrt{3}, 0), B(5 + 5\sqrt{3}, 0), C(5 + 5\sqrt{3}, 5), D(5\sqrt{3}, 5)$

## Session 70 | Coordinates 5 | Worksheet 70

1) Complete the following activities

- a) Draw coordinate axes and mark the points  $P(x_1, y_1), Q(x_2, y_2)$
- b) Draw a line through  $P$  parallel to  $x$  axes, a line passing through  $Q$  parallel to  $y$  axis
- c) Mark the intersecting point as  $R$
- d) Calculate the length  $PR$  and  $QR$
- e) Prove that  $PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

a),b),c) see the figure



- d)  $PR = |x_2 - x_1|, QR = |y_2 - y_1|$
- e)  $PQ^2 = PR^2 + QR^2, PQ^2 = |x_2 - x_1|^2 + |y_2 - y_1|^2$   
 Note  $|a|^2 = a^2$   
 $PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

2) Using the distance formula calculate the following.

- a) The distance between  $P(-6, 7)$  and  $Q(-1, -5)$
- b) What is the distance from origin to  $(-5, 12)$
- c) Find the distance between  $P(-7, -3)$  and  $Q(-5, -11)$

- a)  $PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$   
 $PQ = \sqrt{(-1 - (-6))^2 + (-5 - 7)^2}$   
 $PQ = \sqrt{5^2 + (-12)^2} = \sqrt{169} = 13$
- b)  $O(0, 0), A(-5, 12)$   
 $OA = \sqrt{(-5 - 0)^2 + (12 - 0)^2} = \sqrt{25 + 144} = \sqrt{169} = 13$
- c)  $PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$   
 $PQ = \sqrt{(-5 - (-7))^2 + (-11 - (-3))^2} = \sqrt{2^2 + 8^2} = \sqrt{68}$

3) The distance between  $A(2, y)$  and  $B(-4, 3)$  is 10 unit

- a) Form an equation using the distance formula
- b) What are the real numbers suitable for  $y$ ?
- c) Write the coordinates of these points .

$$\begin{aligned}
 \text{a) } AB &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
 10 &= \sqrt{(-4 - 2)^2 + (3 - y)^2} \\
 \text{b) Squaring on both sides } 10^2 &= (-6)^2 + (3 - y)^2 \\
 100 - 36 &= (3 - y)^2 \\
 (3 - y)^2 &= 64, 3 - y = \pm\sqrt{64} = \pm 8 \\
 \text{If } 3 - y = 8, y &= -5. \text{ If } 3 - y = -8, y = 11 \\
 \text{c) } A(2, 11), B(-4, 3) \\
 A(2, -5), B(-4, 3)
 \end{aligned}$$

4) Consider the points  $A(1, -1), B(5, 2), C(9, 5)$

- Find the distance  $AB, BC$  and  $AC$
- Prove that these points are on a line.
- What is the mid point of  $AC$ ?

$$\begin{aligned}
 \text{a) } AB &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}, AB = \sqrt{(5 - 1)^2 + (2 - (-1))^2} = \sqrt{16 + 9} = 5 \\
 BC &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}, BC = \sqrt{(9 - 5)^2 + (5 - 2)^2} = \sqrt{16 + 9} = 5 \\
 AC &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}, AC = \sqrt{(9 - 1)^2 + (5 - (-1))^2} = \sqrt{64 + 36} = 10 \\
 \text{b) } AB + BC &= 10, AC = 10 \rightarrow AB + BC = AC \\
 A, B, C &\text{ are on a line} \\
 \text{c) } AB = 5, BC = 5. &\text{ Therefore } B \text{ is the mid point of } AC
 \end{aligned}$$

5) Choose the correct answer

- What is the perimeter of the triangle having vertices  $(1, 1), (4, 1)$  and  $(1, 5)$   
 (a) 12    (b) 10    (c) 20    (d) 17
- What is the radius of the circle with end points of the diameter are  $(-1, 7)$  and  $(7, 7)$   
 (a) 5    (b) 4    (c) 2    (d) 7
- What is the altitude to the side  $AB$  in the triangle with vertices  $A(1, 1), B(6, 1), C(3, 7)$   
 (a) 6    (b) 4    (c) 2    (d) 6

- 12
- 4
- 6

## Session 71 | Coordinates 6 | Worksheet 71

1) The distance from a point  $P$  on  $x$  axis to  $A(7, 6)$  and  $B(-3, 4)$  are equal

- a) What is the  $y$  coordinate of  $P$
- b) Form an equation using the distance formula.
- c) Write the coordinates of  $P$
- d) Find the sides of  $\triangle ABP$ .

a) 0

b) Distance from  $P(x, 0)$  to  $A(7, 6)$  is  $= \sqrt{(x-7)^2 + (0-6)^2}$   
 Distance from  $P(x, 0)$  to  $B(-3, 4)$  is  $= \sqrt{(x-(-3))^2 + (0-4)^2}$

c) Since  $PA = PB$  then  $\sqrt{(x-7)^2 + (0-6)^2} = \sqrt{(x-(-3))^2 + (0-4)^2}$   
 squaring on both sides ,  
 $(x-7)^2 + 36 = (x+3)^2 + 16$ ,  $x^2 - 14x + 49 + 36 = x^2 + 6x + 9 + 16$   
 $x = 3$ ,  $P(3, 0)$  ,

d)  $PA = \sqrt{(7-3)^2 + (6-0)^2} = \sqrt{4^2 + 6^2} = \sqrt{52}$   
 $PB = \sqrt{52}$  ,  $AB = \sqrt{(7-(-3))^2 + (6-4)^2} = \sqrt{104}$   
 Since  $PA^2 + PB^2 = AB^2$  , we can say ,this is an isosceles right angled triangle.

2) Consider the points  $A(4, 2)$ ,  $B(7, 5)$ ,  $C(9, 7)$

- a) Find the distances  $AB$ ,  $BC$  and  $AC$
- b) Can we construct  $\triangle ABC$  ? why?
- c) Write the property of these points.

a)  $AB = \sqrt{(7-4)^2 + (5-2)^2} = \sqrt{3^2 + 3^2} = \sqrt{18} = 3\sqrt{2}$   
 $BC = \sqrt{(9-7)^2 + (7-5)^2} = \sqrt{2^2 + 2^2} = \sqrt{8} = 2\sqrt{2}$   
 $AC = \sqrt{(9-4)^2 + (7-2)^2} = \sqrt{5^2 + 5^2} = \sqrt{50} = 5\sqrt{2}$

b) The sum of two sides is not greater than the third side. Triangle cannot be constructed.

c)  $AB + BC = AC$ . So, the points are on a line.

3) Consider the points  $A(0, 1)$ ,  $B(1, 4)$ ,  $C(4, 3)$ ,  $D(3, 0)$

- a) Find the sides of  $ABCD$
- b) Find the length of diagonals.
- c) Suggest a suitable name to this quadrilateral.

a)  $AB = \sqrt{(1-0)^2 + (4-1)^2} = \sqrt{10}$   
 $BC = \sqrt{(4-1)^2 + (3-4)^2} = \sqrt{3^2 + (-1)^2} = \sqrt{10}$   
 $CD = \sqrt{(3-4)^2 + (0-3)^2} = \sqrt{(-1)^2 + (-3)^2} = \sqrt{10}$   
 $AD = \sqrt{(0-3)^2 + (1-0)^2} = \sqrt{(-3)^2 + 1^2} = \sqrt{10}$

b)  $AC = \sqrt{(4-0)^2 + (3-1)^2} = \sqrt{4^2 + 2^2} = \sqrt{20}$   
 $BD = \sqrt{(3-1)^2 + (0-4)^2} = \sqrt{2^2 + (-4)^2} = \sqrt{4+16} = \sqrt{20}$

c) Sides are equal. Diagonals are equal . $ABCD$  is a square .

4) Consider the points  $A(2, -2), B(14, 10), C(11, 13), D(-1, 1)$

2

- Find the sides of  $ABCD$
- Find the length of the diagonals.
- Suggest a suitable name to this quadrilateral.

$$\begin{aligned} \text{a) } AB &= \sqrt{(14-2)^2 + (10-(-2))^2} = \sqrt{12^2 + 12^2} = 12\sqrt{2} \\ BC &= \sqrt{(11-14)^2 + (13-10)^2} = \sqrt{(-3)^2 + 3^2} = 3\sqrt{2} \\ CD &= \sqrt{(-1-11)^2 + (1-13)^2} = \sqrt{(-12)^2 + (-12)^2} = 12\sqrt{2} \\ AD &= \sqrt{(2-(-1))^2 + (-2-1)^2} = \sqrt{3^2 + (-3)^2} = 3\sqrt{2} \\ \text{b) } AC &= \sqrt{(11-2)^2 + (13-(-2))^2} = \sqrt{9^2 + 15^2} = \sqrt{306} \\ BD &= \sqrt{(14-(-1))^2 + (10-1)^2} = \sqrt{15^2 + 9^2} = \sqrt{306} \\ \text{c) } AB &= CD, BC = AD \text{ opposite Sides are equal.} \\ AC &= BD \text{ Diagonals are equal. } ABCD \text{ is a rectangle.} \end{aligned}$$

5) Answer the following questions.

a) What is the diameter of the circumcircle of the triangle with vertices  $(0, 0), (1, 0), (0, 1)$

- (a) 1      (b) 2      (c)  $\sqrt{2}$       (d)  $\sqrt{3}$

b) What is the altitude of the triangle with vertices  $A(1, 1)B(3, 1)$  and  $C(5, 4)$

- (a) 1      (b) 2      (c) 3      (d)  $\sqrt{3}$

c) What is the fourth vertex of the parallelogram having a pair of opposite vertices are  $(1, 3), (4, 4)$  and other vertex is  $(3, 3)$

- (a)  $(2, 4)$       (b)  $(4, 2)$       (c)  $(1, 1)$       (d)  $(2, 2)$

- a)  $\sqrt{2}$   
b) 3  
c)  $(2, 4)$

1

## Session 72 | Coordinates 7 | Worksheet 72

- 1) Consider the points  $A(2, 3), B(3, 4), C(5, 6), D(4, 5)$
- Calculate the  $AB$  and  $CD$
  - Calculate  $AD$  and  $BC$
  - Find the length of diagonals  $AC$  and  $BD$
  - Suggest a suitable name to  $ABCD$ .

a)  $AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$   
 $AB = \sqrt{(3 - 2)^2 + (4 - 3)^2} = \sqrt{2}$   
 $CD = \sqrt{(4 - 5)^2 + (5 - 6)^2} = \sqrt{2}$

b)  $AD = \sqrt{(4 - 2)^2 + (5 - 3)^2} = \sqrt{8} = 2\sqrt{2}$   
 $BC = \sqrt{(5 - 3)^2 + (6 - 4)^2} = \sqrt{8} = 2\sqrt{2}$

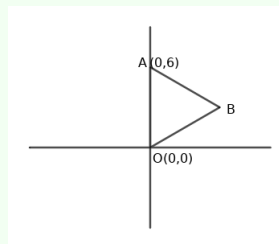
c)  $AC = \sqrt{(5 - 2)^2 + (6 - 3)^2} = \sqrt{18} = 3\sqrt{2}$   
 $BD = \sqrt{(4 - 3)^2 + (5 - 4)^2} = \sqrt{2}$

d)  $AB = CD, AD = BC$  opposite sides are equal  
 $AC \neq BD$  diagonals are not equal.  $ABCD$  is a parallelogram.

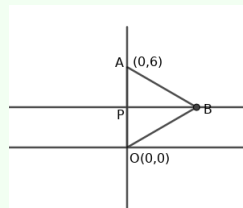
- 2)  $\triangle OAB$  is an equilateral triangle. If  $O(0, 0), A(0, 6)$  then

- Draw a rough diagram
- Find the length of one side.
- Write a pair of coordinates of  $B$
- How many equilateral triangles are there satisfying this condition.

- a) Look at the picture



- b)  $OA = |6 - 0| = 6$
- c) Mid point of  $OA$  is  $P(0, 3)$   
 $\triangle BAP$  is a  $30^\circ - 60^\circ - 90^\circ$  triangle.  $PA = 3, PB = 3\sqrt{3}$



Coordinates of  $B$  are  $B(3\sqrt{3}, 3)$

- d) Two equilateral triangles are possible. Triangle with vertices  $O(0, 0), B(0, 6), C(3\sqrt{3}, 3)$  and triangle with vertices  $O(0, 0), B(0, 6), C(-3\sqrt{3}, 3)$

3) Vertices of a triangle are  $A(8, 6), B(8, -2), C(2, -2)$

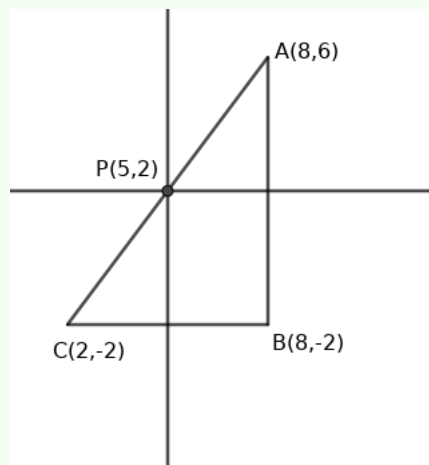
2

- Find the centre of its circumcircle.
- What is the radius of the circumcircle.

$$\begin{aligned} \text{a) Let } P(x, y) \text{ be the circumcentre. } PA &= \sqrt{(x-8)^2 + (y-6)^2}, \quad PB = \sqrt{(x-8)^2 + (y+2)^2}, \quad PC = \sqrt{(x-2)^2 + (y+2)^2} \\ PA &= PB = PC \\ \therefore PA^2 &= PB^2 = PC^2 \\ (x-8)^2 + (y-6)^2 &= (x-8)^2 + (y+2)^2 \\ x^2 + y^2 - 16x - 12y + 100 &= x^2 + y^2 - 16x + 4y + 68, \quad 16y = 32, \quad y = 2 \\ PB^2 &= PC^2, \quad (x-8)^2 + (y+2)^2 = (x-2)^2 + (y+2)^2, \quad 12x = 60, \quad x = 5 \\ P &(5, 2) \end{aligned}$$

$$\text{b) Radius} = \sqrt{(5-8)^2 + (2-6)^2} = 5$$

See the picture.



4)  $A(-3, 0), B(1, -3), C(4, 1)$  are the vertices of a triangle.

- Find the length of its sides
- Prove that  $\triangle ABC$  is an isosceles right triangle.
- calculate the area of this triangle.

$$\begin{aligned} \text{a) } AB &= \sqrt{(1 - -3)^2 + (-3 - 0)^2} = \sqrt{4^2 + (-3)^2} = 5 \\ BC &= \sqrt{(4 - 1)^2 + (1 + 3)^2} = 5 \\ AC &= 5\sqrt{2} \\ \text{b) } AB &= BC \text{ This is an isosceles triangle. } AB^2 + BC^2 = 25 + 25 = 50, \quad AC^2 = (5\sqrt{2})^2 = 50 \\ AB^2 + BC^2 &= AC^2 \\ \text{This is a right triangle . Isosceles right triangle.} \\ \text{c) Area} &= \frac{1}{2} \times 5 \times 5 = \frac{25}{2} \end{aligned}$$

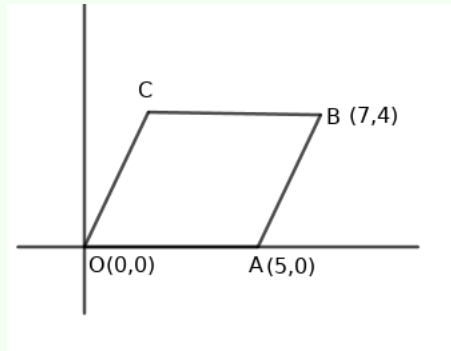


## Session 73 | Coordinates 8 | Worksheet 73

1)  $OABC$  is a parallelogram. If  $O(0, 0)$ ,  $A(5, 0)$ ,  $B(7, 4)$  then

- Draw a rough diagram
- Write the coordinates of  $C$
- Calculate the area of the parallelogram.

a) Look at the picture



- Side  $OA$  is parallel to  $BC$ . Therefore the difference of  $x$  coordinates of  $O, A$  is same as the difference of  $x$  coordinates of  $B$  and  $C$   
Similarly in the case of  $y$  coordinates  
 $C(7 - 5, 4) = C(2, 4)$
- Area =  $5 \times 4 = 20$

2) In the trapezium  $ABCD$ ,  $A(8, 5)$ ,  $B(-8, 5)$ ,  $C(-5, -3)$ ,  $D(5, -3)$  then

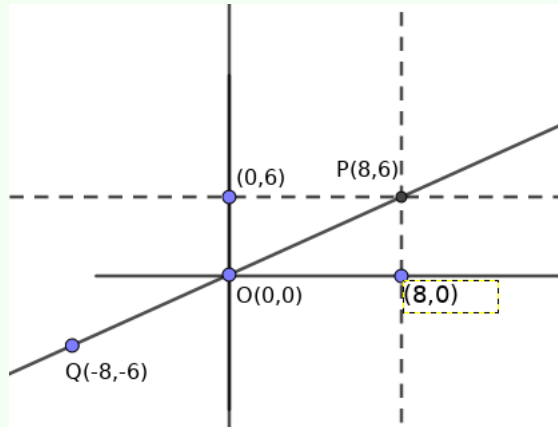
- Find the length of parallel sides
- What is the distance between parallel sides?
- Calculate the area of the trapezium

- $y$  coordinates of  $A$  and  $B$  are equal. Line  $AB$  is parallel to  $x$  axis.  $y$  coordinates of  $C$  and  $D$  are equal.  $CD$  is parallel to  $x$ .  
That is  $AB$  is parallel to  $CD$ .  $AB = |8 - (-8)| = 16$ ,  $CD = |5 - (-5)| = 10$
- Distance between  $AB$  and  $CD$  is  $|5 - (-3)| = 8$
- Area =  $\frac{1}{2} \times 8(16 + 10) = 4 \times 26 = 104$

3) Draw a line parallel to  $x$  axis passing through  $(0, 6)$ . Draw another line parallel to  $y$  axis passing through  $(8, 0)$ .

- Find the coordinates of the intersecting point  $P$
- What is the distance from origin to  $P$ .
- Write the coordinates of one more point on this line other than origin.

a)  $P(8, 6)$  Look at the picture



b)  $OP = \sqrt{8^2 + 6^2} = 10$

c)  $Q(-8, -6)$

4)  $ABC$  is an equilateral triangle. If  $A(3, 2)$ ,  $B(7, 2)$  then

- Find the length of its sides.
- What is the altitude of the triangle?
- Find the suitable coordinate pairs of  $C$
- Calculate the area of the triangle.

a)  $AB = |7 - 3| = 4$

b) Altitude =  $2\sqrt{3}$

c)  $C(3 + 2, 2 + 2\sqrt{3})$  or  $C(3 + 2, -(2\sqrt{3} - 2))$   
 $(5, 2 + 2\sqrt{3})$  or  $(5, 2 - 2\sqrt{3})$

d) Area =  $\frac{1}{2} \times 4 \times 2\sqrt{3} = 4\sqrt{3}$

5)  $P(2, -1)$ ,  $Q(3, 4)$ ,  $R(-2, 3)$ ,  $S(-3, -2)$  are the vertices of a quadrilateral.

- Find the length of sides .
- What is the length of its diagonals?
- Suggest a suitable name to this quadrilateral.
- Calculate the area .

a)  $PQ = \sqrt{(3-2)^2 + (4+1)^2} = \sqrt{26}$   
 $QR = \sqrt{(-2-3)^2 + (3-4)^2} = \sqrt{26}$   
 $RS = \sqrt{(-3+2)^2 + (-2-3)^2} = \sqrt{26}$   
 $SP = \sqrt{(-3-2)^2 + (-2+1)^2} = \sqrt{26}$

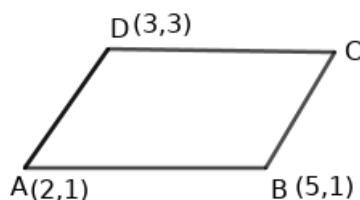
b) Diagonals  $PR = \sqrt{(-2-2)^2 + (3+1)^2} = 4\sqrt{2}$   
 $QS = \sqrt{(-3-3)^2 + (-2-4)^2} = 6\sqrt{2}$

c)  $PQ = QR = RS = SP$   
 $PR \neq QS$  .This is a rhombus

d) Area =  $\frac{1}{2} \times d_1 \times d_2 = 24$  sq.unit

## Session 74 | Coordinates 9 | Worksheet 74

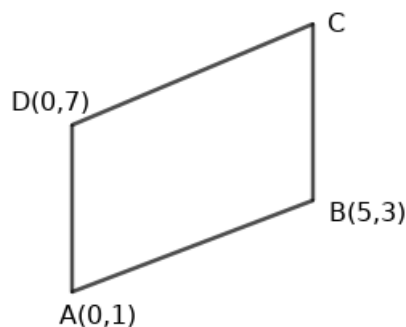
1) In the figure  $ABCD$  is a parallelogram. If  $A(2, 1)$ ,  $B(5, 1)$ ,  $D(3, 3)$  then



- Write the coordinates of  $C$
- Find the length of side  $AB$  and the distance between the parallel sides  $AB$  and  $CD$
- Calculate the area of the parallelogram.

- $AB$  is parallel to  $CD$   
The change in the  $x$  coordinates of  $A$  and  $B$  is same as the change in the  $x$  coordinates of  $C$  and  $D$ .  
Change in the  $y$  coordinates of  $A$  and  $B$  is same as the change in the  $y$  coordinates of  $C$  and  $D$   
 $C(3 + 3, 3) = C(6, 3)$
- $AB = |5 - 2| = 3$   
Distance between the parallel sides  $= |3 - 1| = 2$
- Area  $= 3 \times 2 = 6$

2) In the parallelogram  $ABCD$ , if  $A(0, 1)$ ,  $B(5, 3)$ ,  $D(0, 7)$  then



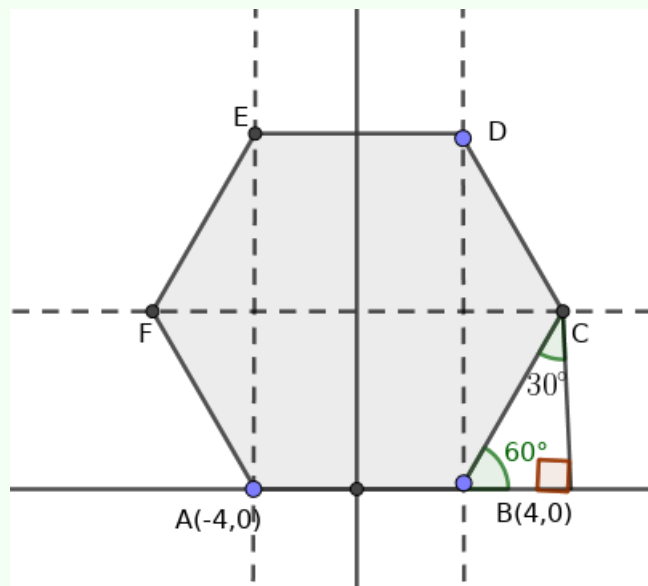
- Write the coordinates of  $C$
- What is the distance between the sides  $AD$  and  $BC$
- Calculate the area of the parallelogram

- a)  $AD$  is parallel to  $BC$   
 The difference in the  $x$  coordinates of  $A$  and  $D$  is same as that of  $B$  and  $C$ . It is zero.  
 The difference in the  $y$  coordinates of  $A$  and  $D$  is same as that of  $B$  and  $C$ . It is 6.  
 $C(5, 3 + 6) = C(5, 9)$
- b) Distance  $= |5 - 0| = 5$
- c) Area  $= 6 \times 5 = 30$

3)  $ABCDEF$  is a regular hexagon. If  $A(-4, 0), B(4, 0)$  then

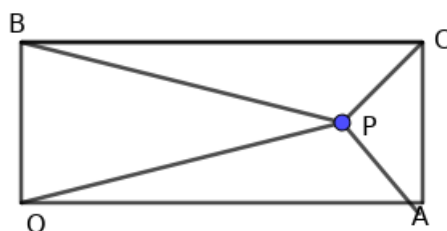
- Draw the diagram
- Find the length of one side
- Write the coordinates of other vertices
- Calculate the area of the hexagon.

a) see the picture



- b)  $AB = |4 - (-4)| = 8$
- c)  $\triangle BPC$  is a  $30^\circ - 60^\circ - 90^\circ$  triangle. (Mark P in the figure. It is the foot of the perpendicular from  $C$  to  $x$  axis)  
 $BC = 8, BP = 4, PC = 4\sqrt{3}$   
 $C(8, 4\sqrt{3}), F(-8, 4\sqrt{3}), D(4, 8\sqrt{3}), E(-4, 8\sqrt{3})$

4)  $OACB$  is a rectangle.



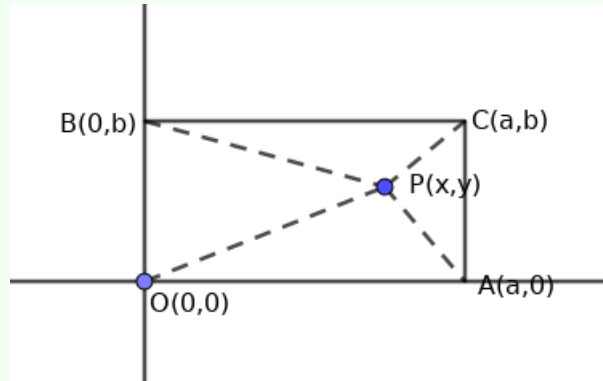
a) Draw coordinate axes with  $O$  as the origin

3

b) If  $a$  is the length and  $b$  is the breadth, write the coordinates of the vertices

c) If  $P$  is a point inside the rectangle then prove that  $PA^2 + PC^2 = PB^2 + PD^2$ .

a,b) see the picture



$$\begin{aligned} \text{c) } OP^2 + CP^2 &= x^2 + y^2 + (x - a)^2 + (y - b)^2 \\ &= 2x^2 + 2y^2 - 2ax - 2by + a^2 + b^2 \\ PA^2 + PB^2 &= (x - a)^2 + y^2 + (x - a)^2 + (y - b)^2 \\ &= 2x^2 + 2y^2 - 2ax - 2by + a^2 + b^2 \\ OP^2 + CP^2 &= PA^2 + PB^2 \end{aligned}$$

1

# Evaluation

1

## Mathematics X

Scores 25

Times 1 hour

### Choose the correct answer. 1 mark each

1) Which of the following is a point on  $x$  axis

- (a)  $(7, 0)$     (b)  $(0, 7)$     (c)  $(7, 7)$     (d)  $(0, -7)$

Answers

Ans :  $(7, 0)$

2) The line parallel to  $x$  axis passing through  $(0, 3)$  and parallel to  $y$  axis passing through  $(3, 0)$  intersect at  $P$ . What is the distance from origin to  $P$ ?

- (a)  $3\sqrt{3}$     (b)  $3\sqrt{2}$     (c) 3    (d)  $\sqrt{3}$

Answers

Ans :  $3\sqrt{2}$

3) What is the distance between the points  $(-3, 2)$  and  $(3, 2)$

- (a) 4    (b) 7    (c) 6    (d) 5

Answers

Ans : 6

### Questions from 4 to 5 carries 2 mark each

4) The vertices of a square are  $(3, 0)$ ,  $(0, 3)$ ,  $(-3, 0)$ ,  $(0, -3)$

- a) What is the length of a side ?  
b) Find the area of the square.

Answers

a)  $3\sqrt{2}$

b) Area =  $(3\sqrt{2})^2 = 9 \times 2 = 18$

5)  $A(8, 6)$  is a point on a circle with center at the origin.

- a) What is the radius of this circle?  
b) What are the points at which the circle cut the axes?

**Answers**

a) Radius =  $\sqrt{8^2 + 6^2} = \sqrt{100} = 10$

b)  $(10, 0), (0, 10), (-10, 0), (0, -10)$

**Questions from 6 to 8 carries 3 each**6) Consider the points  $A(7, 6)$  and  $B(-3, 4)$ 

- a) If  $P(x, y)$  is a point on  $x$  axis then what is  $y$ ?
- b) If  $PA = PB$  then write the equation using the co-ordinates
- c) Find the coordinates of the point  $P$  on  $x$  axis equidistant from  $A$  and  $B$

**Answers**

a)  $y = 0$

$$\begin{aligned} \text{b) } \sqrt{(x-7)^2 + (0-6)^2} &= \sqrt{(x-(-3))^2 + (0-4)^2} \\ (x-7)^2 + 36 &= (x+3)^2 + 16 \\ x^2 - 14x + 49 + 36 &= x^2 + 6x + 9 + 16 \end{aligned}$$

c) Simplifying  $20x = 60, x = 3$ . The point on  $x$  axis is  $P(3, 0)$

7) In triangle  $ABC$ ,  $A(-3, 2), B(5, 2)$  and  $C(2, 7)$ 

- a) What is the length of the side  $AB$ ?
- b) What is the altitude to  $AB$ ?
- c) Calculate the area of  $\triangle ABC$

**Answers**

a)  $AB = |5 - (-3)| = 8$

b) Altitude is  $|7 - 2| = 5$

c) Area =  $\frac{1}{2} \times 8 \times 5 = 20$

8) Consider the points  $A(1, -1), B(5, 2), C(9, 5)$ 

- a) Find the distance  $AB$  and  $BC$
- b) Find the distance  $AC$
- c) Are the points  $A, B, C$  on a line?

**Answers**

a)  $AB = \sqrt{(5-1)^2 + (2+1)^2} = 5, BC = \sqrt{(9-5)^2 + (5-2)^2} = 5$

b)  $AC = \sqrt{(9-1)^2 + (5+1)^2} = 10$

c)  $AC = AB + BC$ . The points are on a line

**Question 9 carries 4 score**

3

- 9)  $A(0, 1), B(1, 4), C(4, 3)$  and  $D(3, 0)$  are the vertices of a quadrilateral
- Find the length of its sides
  - Calculate the length of diagonals
  - Suggest a suitable name to this quadrilateral

**Answers**

$$\begin{aligned} \text{a) } AB &= \sqrt{(1-0)^2 + (4-1)^2} = \sqrt{10} \\ BC &= \sqrt{(4-1)^2 + (3-4)^2} = \sqrt{10} \\ CD &= \sqrt{(3-4)^2 + (0-3)^2} = \sqrt{10} \\ AD &= \sqrt{(3-0)^2 + (0-1)^2} = \sqrt{10} \end{aligned}$$

$$\begin{aligned} \text{b) } AC &= \sqrt{(4-0)^2 + (3-1)^2} = \sqrt{25} = 5 \\ BD &= \sqrt{(3-1)^2 + (0-4)^2} = \sqrt{25} = 5 \end{aligned}$$

c) Sides are equal . Diagonals are equal. It is a square

**Question 10 carries 5 marks**

- 10) The trigonometric table given in the text book gives sin measure , cos measure and tan measure of angles from 0 to 90 degree.

It can be noted that sin measure increases from 0 to 1 as the angle increases from 0 to 90°.

cos measures decreases from 1 to 0 as the angle increases from 0 to 90°.

If the sum of two angles is 90° then sin of one angle is equal to cos of other angle.  $\sin 90^\circ = \cos 0^\circ = 1$  and  $\sin 0^\circ = \cos 90^\circ = 0$ .

Also, the maximum value of sin and cos is 1

- If  $\sin A = \cos A$  then what is  $A$ ?
- If  $\sin X = \cos Y$  then what is  $X + Y$ ?
- $\sin A + \sin B + \sin C = 3$  then what is  $\cos A + \cos B + \cos C$ ?
- What is the product  $\cos 1^\circ \times \cos 2^\circ \times \cos 3^\circ \times \dots \times \cos 90^\circ$ ?

**Answers**

a)  $45^\circ$

b)  $90^\circ$

c) 0

d) 0

1