GATE EC 2008 Q.1 - Q.20 carry one mark each. All the four entries of the 2×2 matrix $= \begin{bmatrix} p_{11} & p_{12} \\ p_{21} & p_{22} \end{bmatrix}$ are nonzero, and one of its eigenvalue is zero. Which of the following statements is true? **MCQ 1.1** (A) $p_{11}p_{12} - p_{12}p_{21} = 1$ (B) $p_{11}p_{22} - p_{12}p_{21} = -1$ (D) $p_{11}p_{22} + p_{12}p_{21} = 0$ (C) $p_{11}p_{22} - p_{12}p_{21} = 0$ The product of Eigen value is equal to the determinant of the matrix. Since one of **SOL 1.1** the Eigen value is zero, the product of Eigen value is zero, thus determinant of the matrix is zero. Thus $p_{11}p_{22} - p_{12}p_{21} = 0$ Hence (C) is correct answer. help The system of linear equations **MCQ 1.2** 4x + 2y = 72x + y = 6 has (A) a unique solution (B) no solution (C) an infinite number of solutions (D) exactly two distinct solutions **SOL 1.2** The given system is $\begin{bmatrix} 4 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ 6 \end{bmatrix}$ We have $A = \begin{bmatrix} 4 & 2 \\ 2 & 1 \end{bmatrix}$ $|A| = \begin{vmatrix} 4 & 2 \\ 2 & 1 \end{vmatrix} = 0$ and Rank of matrix $\rho(A) < 2$ $C = \begin{bmatrix} 4 & 2 & | & 7 \\ 2 & 1 & | & 6 \end{bmatrix}$ Now Rank of matrix $\rho(C) = 2$ Since $\rho(A) \neq \rho(C)$ there is no solution. Hence (B) is correct answer.

MCQ 1.3 The equation $\sin(z) = 10$ has

Page 2	GATE EC 2008	www.gatehelp.com	
	(A) no real or complex solution(B) exactly two distinct complex solutions(C) a unique solution(D) an infinite number of complex solutions		
SOL 1.3	$\sin z$ can have value between -1 to $+1$. Thus no solution. Hence (A) is correct solution.		
MCQ 1.4	For real values of x , the minimum value of the function $f(x) = \exp(x) + \exp(-x)$ is (A) 2 (B) 1 (C) 0.5 (D) 0		
SOL 1.4	Hence (A) is correct answer. We have $f(x) = e^x + e^{-x}$ For $x > 0$, $e^x > 1$ and $0 < e^{-x} < 1$ For $x < 0$, $0 < e^x < 1$ and $e^{-x} > 1$ Thus $f(x)$ have minimum values at $x = 0$ and that is $e^0 + e^{-x}$	$^{-0} = 2.$	
MCQ 1.5	Which of the following functions would have only odd pow- series expansion about the point $x = 0.2$ (A) $\sin(x^3)$ (B) $\sin(x^2)$ (C) $\cos(x^3)$ (D) $\cos(x^2)$	wers of x in its Taylor	
SOL 1.5	Hence (A) is correct answer. $\sin x = x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$ $\cos x = 1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$ Thus only $\sin(x^3)$ will have odd power of x .		
MCQ 1.6	Which of the following is a solution to the differential equat	ion $\frac{dx(t)}{dt} + 3x(t) = 0$?	
	(A) $x(t) = 3e^{-t}$ (B) $x(t) = 2e^{-3t}$ (C) $x(t) = -\frac{3}{2}t^2$ (D) $x(t) = 3t^2$		
SOL 1.6	Hence (B) is correct answer. We have $\frac{dx(t)}{dt} + 3x(t) = 0$ or $(D+3)x(t) = 0$ Since $m = -3$ $x(t) = Ce^{-3t}$ Thus only	y (B) may be solution	
MCQ 1.7	In the following graph, the number of trees (P) and trees	nber of cut-set (Ω) are	
	in the lone has graph, the humber of freed (1) and the hum		







There can be four possible tree of this graph which are as follows:



Hence (C) is correct option.

In the following circuit, the switch S is closed at t = 0. The rate of change of **MCQ 1.8** current $\frac{di}{dt}(0^+)$ is given by







Initially $i(0^{-}) = 0$ therefore due to inductor $i(0^{+}) = 0$. Thus all current I_s will flow in resistor R and voltage across resistor will be $I_s R_s$. The voltage across inductor will be equal to voltage across R_s as no current flow through R.





MCQ 1.12 Step responses of a set of three second-order underdamped systems all have the same percentage overshoot. Which of the following diagrams represents the poles of the three systems ?



SOL 1.12 Transfer function for the given pole zero plot is: $\frac{(s+Z_1)(s+Z_2)}{(s+P_1)(s+P_2)}$

> From the plot Re $(P_1 \text{ and } P_2) > (Z_1 \text{ and } Z_2)$ So, these are two lead compensator.

Hence both high pass filters and the system is high pass filter.

Page 6	GATE	EC 2008	www.gatehelp.com
	Hence (C) is correct option.		
MCQ 1.13	Which of the following is NOT as(A) Junction Capacitance(C) Depletion Capacitance	(B) Charge (D) Channe	-n junction ? e Storage Capacitance nel Length Modulations
SOL 1.13	Channel length modulation is no associated with MOSFET in whi the phenomenon called channel le Hence option (D) is correct.	ot associated with ich effective chann ength modulation.	a $p-n$ junction. It is being el length decreases, producing
MCQ 1.14	Which of the following is true?(A) A silicon wafer heavily doped(B) A silicon wafer lightly doped(C) A silicon wafer heavily doped(D) A silicon wafer lightly doped	l with boron is a p with boron is a p^+ l with arsenic is a p with arsenic is a p	p^+ substrate p^+ substrate p^+ substrate p^+ substrate
SOL 1.14	Trivalent impurities are used for n heavily doped with boron is a p^+ Hence option (A) is correct	making $p - type$ set substrate.	miconductors. So, Silicon wafer
MCQ 1.15	For a Hertz dipole antenna, the h (A) 360° (C) 90°	alf power beam wi (B) 180° (D) 45°	dth (HPBW) in the E -plane is
SOL 1.15	The beam-width of Hertizian dip Hence (C) is correct option	ole is 180° and its	half power beam-width is 90°.
MCQ 1.16	For static electric and magnetic which of the following represents (A) $\nabla \cdot E = 0$, $\nabla \times B = 0$ (C) $\nabla \times E = 0$, $\nabla \times B = 0$	fields in an inhom the correct form o (B) $\nabla \cdot E =$ (D) $\nabla \times E$	nogeneous source-free medium, f Maxwell's equations ? $0, \nabla B = 0$ $= 0, \nabla B = 0$
SOL 1.16	Maxwell equations $\nabla - \vec{B} = 0$ $\nabla \cdot \vec{E} = \rho/E$ $\nabla \times \vec{E} = -\vec{B}$ $\nabla \times \hat{H} = \vec{D} + \vec{J}$ For static electric magnetic fields $\nabla \cdot \vec{B} = 0$ $\nabla \cdot \vec{E} = \rho/E$ $\nabla \times \vec{E} = 0$ $\nabla \times \vec{E} = 0$ Hence (D) is correct option		

MCQ 1.17 In the following limiter circuit, an input voltage $V_i = 10 \sin 100\pi t$ is applied. Assume that the diode drop is 0.7 V when it is forward biased. When it is forward biased. The zener breakdown voltage is 6.8 V

The maximum and minimum values of the output voltage respectively are



Hence option (B) is correct. $g_m = \frac{\partial I_D}{\partial V_{GS}} = \frac{\partial}{\partial V_{GS}} K (V_{GS} - V_T)^2 = 2K (V_{GS} - V_T)$

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MCQ 1.20 Consider the amplitude modulated (AM) signal $A_c \cos \omega_c t + 2 \cos \omega_m t \cos \omega_c t$. For demodulating the signal using envelope detector, the minimum value of A_c should be

SOL 1.20 Hence (A) is correct option We have $x_{AM}(t) = A_c \cos \omega_c + 2 \cos \omega_m t \cos \omega_c t$

$$=A_C \Big(1 + \frac{2}{A_c} \cos \omega_m t\Big) \cos \omega_c t$$

For demodulation by envelope demodulator modulation index must be less than or equal to 1.

Thus

$$\frac{2}{A_c} \le 1$$
$$A_c \ge 2$$

Hence minimum value of $A_c = 2$

Q.21 to Q.75 carry two marks each

MCQ 1.21 The Thevenin equivalent impedance Z_{th} between the nodes P and Q in the following circuit is



Killing all current source and voltage sources we have,



$Z_{th} = 1$ or

Alternative :

Here at DC source capacitor act as open circuit and inductor act as short circuit. Thus we can directly calculate the venin Impedance as 1 Ω Hence (A) is correct option.

MCQ 1.22 The driving point impedance of the following network is given by 0.2sZ(

$$Z(s) = \frac{0.2s}{s^2 + 0.1s + 2}$$



The component values are

(A)
$$L = 5 \text{ H}, R = 0.5 \Omega, C = 0.1 \text{ F}$$

(B) $L = 0.1$
(C) $L = 5 \text{ H}, R = 2 \Omega, C = 0.1 \text{ F}$
Hence (D) is correct option

(B)
$$L = 0.1 \text{ H}, R = 0.5 \Omega, C = 5 \text{ F}$$

(D) $L = 0.1 \text{ H}, R = 2 \Omega, C = 5 \text{ F}$

SOL 1.22 Hence (D) is correct option.

$$Z(s) = R \left\| \frac{1}{sC} \right\| sL = \frac{s}{s^2 + \frac{s}{RC} + \frac{1}{LC}}$$

been given
$$Z(s) = \frac{0.2s}{s^2 + \frac{s}{RC} + \frac{1}{LC}}$$

We have

$$Z(s) = \frac{0.2s}{s^2 + 0.1s + 2}$$

Comparing with given we get

$$\frac{1}{C} = 0.2 \text{ or } C = 5 \text{ F}$$
$$\frac{1}{RC} = 0.1 \text{ or } R = 2 \Omega$$
$$\frac{1}{LC} = 2 \text{ or } L = 0.1 \text{ H}$$

MCQ 1.23 The circuit shown in the figure is used to charge the capacitor C alternately from two current sources as indicated. The switches S_1 and S_2 are mechanically coupled and connected as follows:

> For $2nT \le t \le (2n+1)T$, $(n = 0, 1, 2, ...) S_1$ to P_1 and S_2 to P_2 For $(2n+1) T \le t \le (2n+2) T$, $(n = 0, 1, 2, ...) S_1$ to Q_1 and S_2 to Q_2



Assume that the capacitor has zero initial charge. Given that u(t) is a unit step function, the voltage $v_c(t)$ across the capacitor is given by

(A)
$$\sum_{n=1}^{\infty} (-1)^n tu(t-nT)$$

(B) $u(t) + 2\sum_{n=1}^{\infty} (-1)^n u(t-nT)$
(C) $tu(t) + 2\sum_{n=1}^{\infty} (-1)^n u(t-nT)(t-nT)$
(D) $\sum_{n=1}^{\infty} [0.5 - e^{-(t-2nT)} + 0.5e^{-(t-2nT)} - T]$
Voltage across capacitor is

SOL 1.23

$$V_{c} = \frac{1}{C} \int_{0}^{t} i dt \quad \textbf{g.ate}$$

Here $C = 1$ F and $i = 1$ A. Therefore
 $V_{c} = \int_{0}^{t} dt$

For 0 < t < T, capacitor will be charged from 0 V $V_c = \int_0^t dt = t$

At $t = T, V_c = T$ Volts

For T < t < 2T, capacitor will be discharged from T volts as $V_c = T - \int_T^t dt = 2T - t$

At $t = 2T, V_c = 0$ volts For 2T < t < 3T, capacitor will be charged from 0 V $V_c = \int_{2T}^{t} dt = t - 2T$

At t = 3T, $V_c = T$ Volts For 3T < t < 4T, capacitor will be discharged from T Volts $V_c = T - \int_{3T}^{t} dt = 4T - t$

At t = 4T, $V_c = 0$ Volts For 4T < t < 5T, capacitor will be charged from 0 V $V_c = \int_{4T}^{t} dt = t - 4T$





Only option C satisfy this waveform. Hence (C) is correct option.

MCQ 1.24 The probability density function (pdf) of random variable is as shown below



The corresponding commutative distribution function CDF has the form



SOL 1.24 CDF is the integration of PDF. Plot in option (A) is the integration of plot given in question.

Hence (A) is correct option.

MCQ 1.25 The recursion relation to solve $x = e^{-x}$ using Newton - Raphson method is (A) $x_{n+1} = e^{-x_n}$ (B) $x_{n+1} = x_n - e^{-x_n}$ (C) $x_{n+1} = (1+x_n) \frac{e^{-x_n}}{1+e^{-x_n}}$ (D) $x_{n+1} = \frac{x_n^2 - e^{-x_n}(1-x_n) - 1}{x_n - e^{-x_n}}$

SOL 1.25 Hence (C) is correct answer. We have $x = e^{-x}$ or $f(x) = x - e^{-x}$ $f(x) = 1 + e^{-x}$

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The Newton-Raphson iterative formula is

$$x_{n+1} = x_n - \frac{f(x_n)}{f(x_n)}$$
Now $f(x_n) = x_n - e^{-x_n}$
 $f(x_n) = 1 + e^{-x_n}$
Thus $x_{n+1} = x_n - \frac{x_n - e^{-x_n}}{1 + e^{-x_n}} = \frac{(1+x_n)e^{-x_n}}{1 + e^{-x_n}}$

The residue of the function $f(z) = \frac{1}{(z+2)^2(z-2)^2}$ at z=2 is **MCQ 1.26** (A) $-\frac{1}{32}$ (B) $-\frac{1}{16}$ (C) 1 (D) $\frac{1}{32}$

(C)
$$\frac{16}{16}$$

SOL 1.26 Hence (A) is correct answer.

Res
$$f(z)_{z=a} = \frac{1}{(n-1)!} \frac{d^{n-1}}{dz^{n-1}} [(z-a)^n f(z)]_{z=a}$$

Here we have n = 2 and a = 2

Thus Res
$$f(z)_{z=2} = \frac{1}{(2-1)!} \frac{d}{dz} \left[(z-2)^2 \frac{1}{(z-2)^2(z+2)^2} \right]_{z=a}$$

= $\frac{d}{dz} \left[\frac{1}{(z+2)^2} \right]_{z=a} = \left[\frac{-2}{(z+2)^3} \right]_{z=a}$
= $-\frac{2}{64} = -\frac{1}{32}$

MCQ 1.27 Consider the matrix
$$P = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}$$
. The value of e^p is
(A) $\begin{bmatrix} 2e^{-2} - 3e^{-1} & e^{-1} - e^{-2} \\ 2e^{-2} - 2e^{-1} & 5e^{-2} - e^{-1} \end{bmatrix}$
(B) $\begin{bmatrix} e^{-1} + e^{-1} & 2e^{-2} - e^{-1} \\ 2e^{-1} - 4e^2 & 3e^{-1} + 2e^{-2} \end{bmatrix}$
(C) $\begin{bmatrix} 5e^{-2} - e^{-1} & 3e^{-1} - e^{-2} \\ 2e^{-2} - 6e^{-1} & 4e^{-2} + 6^{-1} \end{bmatrix}$
(D) $\begin{bmatrix} 2e^{-1} - e^{-2} & e^{-1} - e^{-2} \\ -2e^{-1} + 2e^{-2} - e^{-1} + 2e^{-2} \end{bmatrix}$
SOL 1.27 Hence (D) is correct answer.

1.27 Hence (D) is correct answer.

$$e^{P} = L^{-1}[(sI - A)^{-1}] = L^{-1} \left[\begin{pmatrix} s & 0 \\ 0 & s \end{pmatrix} - \begin{pmatrix} 0 & 1 \\ -2 & -3 \end{pmatrix} \right]^{-1} = L^{-1} \left(\begin{bmatrix} s & -1 \\ 2 & s + 3 \end{bmatrix}^{-1} \right)$$

$$= L^{-1} \left(\begin{bmatrix} \frac{s+3}{(s+1)(s+2)} & \frac{1}{(s+1)(s+2)} \\ \frac{-2}{(s+1)(s+2)} & \frac{1}{(s+1)(s+2)} \end{bmatrix} \right)$$

$$= \begin{bmatrix} 2e^{-1} - e^{-2} & e^{-1} - e^{-2} \\ -2e^{-1} + 2e^{-2} & -e^{-1} + 2e^{-2} \end{bmatrix}$$

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- **MCQ 1.28** In the Taylor series expansion of $\exp(x) + \sin(x)$ about the point $x = \pi$, the coefficient of $(x-\pi)^2$ is
 - (A) $\exp(\pi)$ (B) $0.5 \exp(\pi)$ (C) $\exp(\pi) + 1$ (D) $\exp(\pi) - 1$
- **SOL 1.28** Taylor series is given as

$$f(x) = f(a) + \frac{x-a}{1!}f(a) + \frac{(x-a)^2}{2!}f'(a) + \dots$$

For $x = \pi$ we have

 $f(x) = f(\pi) + \frac{x - \pi}{1!} f(\pi) + \frac{(x - \pi)^2}{2!} f'(x) \dots$ Thus

Now

Now
$$f(x) = e^{x} + \sin x$$
$$f(x) = e^{x} + \cos x$$
$$f'(x) = e^{x} - \sin x$$
$$f''(\pi) = e^{\pi} - \sin \pi = e^{\pi}$$
Thus the coefficient of $(x - \pi)^{2}$ is $\frac{f'(\pi)}{21}$

Hence (B) is correct answer.

 $P_x(x) = M \exp(-2|x|) - N \exp(-3|x|)$ is the probability density function for the **MCQ 1.29** real random variable X, over the entire x axis, M and N are both positive real numbers. The equation relating M and N is

(A)
$$M - \frac{2}{3}N = 1$$

(B) $2M + \frac{1}{3}N = 1$
(C) $M + N = 1$
(D) $M + N = 3$

- **SOL 1.29** Correct Option is ()
- The value of the integral of the function $q(x,y) = 4x^3 + 10y^4$ along the straight line **MCQ 1.30** segment from the point (0,0) to the point (1,2) in the x-y plane is (B) 35 (A) 33 (C) 40 (D) 56

The equation of straight line from (0,0) to (1,2) is y = 2x. **SOL 1.30** $q(x,y) = 4x^3 + 10y^4$ Now $q(x,2x) = 4x^3 + 160x^4$ or, $\operatorname{Now} \int_0^1 g(x, 2x) = \int_0^1 (4x^3 + 160x^4) \, dx$ $= [x^4 + 32x^5]_0^1 = 33$

Hence (A) is correct answer.

MCQ 1.31 A linear, time - invariant, causal continuous time system has a rational transfer function with simple poles at s = -2 and s = -4 and one simple zero at s = -1. Page 14

A unit step u(t) is applied at the input of the system. At steady state, the output has constant value of 1. The impulse response of this system is (A) $[\exp(-2t) + \exp(-4t)]u(t)$ (B) $[-4\exp(-2t) - 12\exp(-4t) - \exp(-t)]u(t)$

(C)
$$[-4\exp(-2t) + 12\exp(-4t)]u(t)$$

(D) $[-0.5\exp(-2t) + 1.5\exp(-4t)]u(t)$

$$\begin{aligned} \mathbf{x}(t) &= 0 \text{ for } \mathbf{x}(t) + 1 \text{ for } \mathbf{x}(t) \\ \text{Sol 1.31} \end{aligned} \qquad & \text{Hence (C) is correct answer.} \\ & G(s) &= \frac{K(s+1)}{(s+2)(s+4)}, \text{ and } R(s) = \frac{1}{s} \\ & C(s) &= G(s) R(s) = \frac{K(s+1)}{s(s+2)(s+4)} \\ &= \frac{K}{8s} + \frac{K}{4(s+2)} - \frac{3K}{8(s+4)} \\ & \text{Thus} \qquad c(t) &= K \Big[\frac{1}{8} + \frac{1}{4} e^{-2t} - \frac{3}{8} e^{-4t} \Big] u(t) \\ & \text{At steady-state} \\ & \text{Thus} \qquad \frac{K}{8} = 1 \text{ or } K = 8 \\ & \text{Then,} \qquad G(s) = \frac{8(s+1)}{(s+2)(s+4)} = \frac{1120}{(s+2)(s+4)} - \frac{4}{(s+2)} \\ & h(t) = L^{-1}G(s) = (-4e^{-2t} - 12e^{-4t}) u(t) \\ & \text{MCQ 1.32} \qquad \text{The signal } x(t) \text{ is described by} \\ & x(t) = \begin{cases} 1 & \text{for } -1 \leq t \leq +1 \\ 0 & \text{otherwise} \end{cases} \\ & \text{Two of the angular frequencies at which its Fourier transform becomes zero are} \\ & (A) \pi, 2\pi \qquad (B) 0.5\pi, 1.5\pi \\ & (C) 0, \pi \qquad (D) 2\pi, 2.5\pi \end{aligned}$$

$$= -j\omega [e^{-j\omega} - e^{j\omega}] = \frac{1}{-j\omega} (-2j\sin\omega)$$
$$= \frac{2\sin\omega}{\omega}$$

This is zero at $\omega = \pi$ and $\omega = 2\pi$

MCQ 1.33 A discrete time linear shift - invariant system has an impulse response h[n] with h[0] = 1, h[1] = -1, h[2] = 2, and zero otherwise. The system is given an input sequence x[n] with x[0] = x[2] = 1, and zero otherwise. The number of nonzero samples in the output sequence y[n], and the value of y[2] are respectively (A) 5, 2 (B) 6, 2

(C)
$$6, 1$$
 (D) $5, 3$

SOL 1.33 Hence (D) is correct answer.

Given
$$h(n) = [1, -1, 2]$$

 $x(n) = [1, 0, 1]$
 $y(n) = x(n)^* h(n)$
The length of $y[n]$ is
 $= L_1 + L_2 - 1 = 3 + 3 - 1 = 5$
 $y(n) = x(n)^* h(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k)$
 $y(2) = \sum_{k=-\infty}^{\infty} x(k) h(2-k)$
 $= x(0) h(2-0) + x(1) h(2-1) + x(2) h(2-2)$
 $= h(2) + 0 + h(0) = 1 + 2 = 3$

There are 5 non zero sample in output sequence and the value of y[2] is 3.

- **MCQ 1.34** Consider points P and Q in the x y plane, with P = (1,0) and Q = (0,1). The line integral $2\int_{P}^{Q} (xdx + ydy)$ along the semicircle with the line segment PQ as its diameter
 - (A) is -1
 - (B) is 0
 - (C) is 1
 - (D) depends on the direction (clockwise or anit-clockwise) of the semicircle
- **SOL 1.34** Hence (B) is correct answer.

$$I = 2 \int_{P}^{Q} (xdx + ydy)$$
$$= 2 \int_{P}^{Q} xdx + 2 \int_{P}^{Q} ydy$$
$$= 2 \int_{1}^{0} xdx + 2 \int_{0}^{1} ydy = 0$$

MCQ 1.35Let x(t) be the input and y(t) be the output of a continuous time system. Match
the system properties P1, P2 and P3 with system relations R1, R2, R3, R4
PropertiesRelationsP1 : Linear but NOT time - invariantR1 : $y(t) = t^2 x(t)$
P2 : Time - invariant but NOT linearR2 : y(t) = t |x(t)|

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- (A) (P1, R1), (P2, R3), (P3, R4) (B) (P1, R2), (P2, R3), (P3, R4)
- (C) (P1, R3), (P2, R1), (P3, R2)
- (D) (P1, R1), (P2, R2), (P3, R3)

R3 : y(t) = |x(t)|R4 : y(t) = x(t-5)

SOL 1.35 Mode function are not linear. Thus y(t) = |x(t)| is not linear but this functions is time invariant. Option (A) and (B) may be correct.

> The y(t) = t |x(t)| is not linear, thus option (B) is wrong and (a) is correct. We can see that

 R_1 : $y(t) = t^2 x(t)$ Linear and time variant. R_2 : y(t) = t |x(t)| Non linear and time variant. R_3 : y(t) = x|(t)| Non linear and time invariant R_4 : y(t) = x(t-5) Linear and time invariant Hence (B) is correct answer.

- A memory less source emits n symbols each with a probability p. The entropy of **MCQ 1.36** the source as a function of n
 - **G a i e** (B) decreases as $\log(\frac{1}{n})$ (D) increases as $n \log n$ (A) increases as $\log n$ (C) increases as n
 - help
- **SOL 1.36** The entropy is

$$H = \sum_{i=1}^{m} p_i \log_2 \frac{1}{p_i}$$
 bits

 $p_1 = p_2 = ... = p_n = \frac{1}{n}$

Since

$$H = \sum_{i=1}^{n} \frac{1}{n} \log n = \log n$$

Hence (A) is correct option.

MCQ 1.37 $\{x(n)\}\$ is a real - valued periodic sequence with a period N. x(n) and X(k) form N-point Discrete Fourier Transform (DFT) pairs. The DFT Y(k) of the sequence $y(n) = \frac{1}{N} \sum_{r=0}^{N-1} x(r) x(n+r)$ is (B) $\frac{1}{N} \sum_{n=1}^{N-1} X(r) X(k+r)$ (A) $|X(k)|^2$ (C) $\frac{1}{N} \sum_{r=1}^{N-1} X(r) X(k+r)$ (D) 0

SOL 1.37 Hence (A) is correct answer.
Given :
$$y(n) = \frac{1}{N} \sum_{r=0}^{N-1} x(r) x(n+r)$$

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It is Auto correlation. Hence $y(n) = r_{xx}(n) \xrightarrow{DFT} |X(k)|^2$

MCQ 1.38 Group I lists a set of four transfer functions. Group II gives a list of possible step response y(t). Match the step responses with the corresponding transfer functions.



$$G(s) = \frac{s+8}{s^2 + \alpha s - 4}$$

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where α is a parameter. Consider the standard negative unity feedback configuration as shown below



Which of the following statements is true?

- (A) The closed loop systems is never stable for any value of α
- (B) For some positive value of α , the closed loop system is stable, but not for all positive values.
- (C) For all positive values of α , the closed loop system is stable.
- (D) The closed loop system stable for all values of α , both positive and negative.



$$1 + G(s)H(s) = 0$$

$$1 + \frac{s+8}{s^2 + \alpha s - 4} = 0$$

or or $s^{2} + \alpha s - 4 + s + 8 = 0$ 1 C $s^{2} + (\alpha + 1)s + 4 = 0$

This will be stable if $(\alpha + 1) > 0 \rightarrow \alpha > -1$. Thus system is stable for all positive value of α .

MCQ 1.40 A signal flow graph of a system is given below



The set of equalities that corresponds to this signal flow graph is

$$(A) \quad \frac{d}{dt} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{bmatrix} \beta & -\gamma & 0 \\ \gamma & \alpha & 0 \\ -\alpha & \beta & 0 \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} + \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{pmatrix} u_1 \\ u_2 \end{pmatrix}$$
$$(B) \quad \frac{d}{dt} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{bmatrix} 0 & \alpha & \gamma \\ 0 & -\alpha & -\gamma \\ 0 & \beta & -\beta \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix} \begin{pmatrix} u_1 \\ u_2 \end{pmatrix}$$
$$(C) \quad \frac{d}{dt} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{bmatrix} -\alpha & \beta & 0 \\ -\beta & -\gamma & 0 \\ \alpha & \gamma & 0 \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix} \begin{pmatrix} u_1 \\ u_2 \end{pmatrix}$$

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(D)
$$\frac{d}{dt} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{bmatrix} -\alpha & 0 & \beta \\ \gamma & 0 & \alpha \\ -\beta & 0 & -\alpha \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix} \begin{pmatrix} u_1 \\ u_2 \end{pmatrix}$$



We labeled the given SFG as below :



From this SFG we have

$$\begin{aligned} \dot{x}_{1} &= -\gamma x_{1} + \beta x_{3} + \mu_{1} \\ \dot{x}_{2} &= \gamma x_{1} + \alpha x_{3} \\ \dot{x}_{3} &= -\beta x_{1} - \alpha x_{3} + u_{2} \\ x_{3} &= \begin{bmatrix} -\gamma & 0 & \beta \\ \gamma & 0 & \alpha \\ -\beta & 0 & -\alpha \end{bmatrix} \begin{bmatrix} x_{1} \\ x_{2} \\ x_{3} \end{bmatrix} + \begin{bmatrix} 0 & 1 \\ 0 & 0 \\ 1 & 0 \end{bmatrix} \begin{pmatrix} u_{1} \\ u_{2} \end{pmatrix} \end{aligned}$$
Thus

Hence (C) is correct option.

MCQ 1.41 The number of open right half plane of

$$G(s) = \frac{10}{s^5 + 2s^4 + 3s^3 + 6s^2 + 5s + 3}$$
(A) 0 (B) 1

SOL 1.41 The characteristic equation is

1+G(s)=0 or $s^5+2s^4+3s^3+6s^2+5s+3=0$ Substituting $s=\frac{1}{z}$ we have

$$3z^5 + 5z^4 + 6z^3 + 3z^2 + 2z + 1 = 0$$

The routh table is shown below. As there are tow sign change in first column, there are two RHS poles.

6

z^5	3	6	2
z^4	5	3	1
z^3	$\frac{21}{5}$	$\frac{7}{5}$	
z^2	$\frac{4}{3}$	3	
z^1	$-\frac{7}{4}$		
z^0	1		

Hence (C) is correct option.

MCQ 1.42 The magnitude of frequency responses of an underdamped second order system is 5 at 0 rad/sec and peaks to $\frac{10}{\sqrt{3}}$ at $5\sqrt{2}$ rad/sec. The transfer function of the system is

(A)
$$\frac{500}{s^2 + 10s + 100}$$
 (B) $\frac{375}{s^2 + 5s + 75}$
(C) $\frac{720}{s^2 + 12s + 144}$ (D) $\frac{1125}{s^2 + 25s + 225}$

SOL 1.42

For underdamped second order system the transfer function is

$$T(s) = \frac{K\omega_n^2}{s^2 + 2\xi\omega_n s + \omega_n^2}$$

It peaks at resonant frequency. Therefore $\omega_r = \omega_n \sqrt{1 - 2\xi^2}$ Resonant frequency and peak at this frequency

l

$$u_r = \frac{5}{2\xi\sqrt{1-\xi^2}}$$

We have $\omega_r = 5\sqrt{2}$, and $\mu_r = \frac{10}{\sqrt{3}}$. Only options (A) satisfy these values. $\omega_r = \frac{10}{\sqrt{3}}, \xi = \frac{1}{2}$ where $\omega_r = 10\sqrt{1-2(\frac{1}{4})} = 5\sqrt{2}$ and $\mu_r = \frac{5}{2\frac{1}{2}\sqrt{1-\frac{1}{4}}} = \frac{10}{\sqrt{3}}$ Hence

Hence satisfied

Hence (C) is correct option.

MCQ 1.43 Group I gives two possible choices for the impedance Z in the diagram. The circuit elements in Z satisfy the conditions $R_2 C_2 > R_1 C_1$. The transfer functions $\frac{V_0}{V_1}$ represents a kind of controller.



Match the impedances in Group I with the type of controllers in Group II



Since $R_2 C_2 > R_1 C_1$, it is lag compensator. Hence (B) is correct option.

MCQ 1.44 For the circuit shown in the following figure, transistor M1 and M2 are identical NMOS transistors. Assume the M2 is in saturation and the output is unloaded.



The current I_x is related to I_{bias} as (A) $I - I_x + I_z$

(A)
$$I_x = I_{bias} + I_s$$
 (D)
(C) $I_x = I_{bias} - \left(V_{DD} - \frac{V_{out}}{R_E}\right)$ (D)
By Current mirror,

SOL 1.44

$$I_x = \frac{\left(\frac{W}{L}\right)_2}{\left(\frac{W}{L}\right)_1} I_{bias}$$

Brought to you by: Nodia and Company PUBLISHING FOR GATE (B) $I_x = I_{bias}$ (D) $I_x = I_{bias} - I_s$ Since MOSFETs are identical, Thus $\left(\frac{W}{L}\right)_2 = \left(\frac{W}{L}\right)_2$ Hence $I_x = I_{bias}$ Hence (B) is correct option.

MCQ 1.45 The measured trans conductance g_m of an NMOS transistor operating in the linear region is plotted against the gate voltage V_G at a constant drain voltage V_D . Which of the following figures represents the expected dependence of g_m on V_G ?



Which is straight line.

MCQ 1.46 Consider the following circuit using an ideal OPAMP. The I-V characteristic of the diode is described by the relation $I = I_0 \left(e^{\frac{V}{V_i} - 1} \right)$ where $V_T = 25$ mV, $I_0 = 1\mu$ A and V is the voltage across the diode (taken as positive for forward bias). For an input voltage $V_i = -1$ V, the output voltage V_0 is



SOL 1.46 The circuit is using ideal OPAMP. The non inverting terminal of OPAMP is at ground, thus inverting terminal is also at virtual ground.



Thus current will flow from -ive terminal (0 Volt) to -1 Volt source. Thus the current I is

$$I = \frac{0 - (-1)}{100k} = \frac{1}{100k}$$

The current through diode is

 $I = I_0 \left(e^{\frac{V}{V_t}} - 1 \right)$ Now $V_T = 25$ mV and $I_0 = 1$ µA Thus $I = 10^{-6} \left[e^{\frac{V}{25 \times 10^{-3}}} - 1 \right] = \frac{1}{10^5}$ or V = 0.06 V

Now
$$V_0 = I \times 4k + V = \frac{1}{100k} \times 4k + 0.06 = 0.1 \text{ V}$$

Hence (B) is correct option.

MCQ 1.47 The OPAMP circuit shown above represents a



(A) high pass filter	(B) low pass filter
(C) band pass filter	(D) band reject filter

SOL 1.47 The circuit is using ideal OPAMP. The non inverting terminal of OPAMP is at ground, thus inverting terminal is also at virtual ground.



Page 24

Thus we can write

$$\frac{v_i}{R_1 + sL} = \frac{-v}{\frac{R_2}{sR_2C_2 + 1}}$$

or
$$\frac{v_0}{v_i} = -\frac{R_2}{(R_1 + sL)(sR_2C_2 + 1)}$$

and from this equation it may be easily seen that this is the standard form of T.F. of low pass filter

$$H(s) = \frac{K}{(R_1 + sL)(sR_2C_2 + 1)}$$

and form this equation it may be easily seen that this is the standard form of T.F. of low pass filter

$$H(s) = \frac{K}{as^2 + bs + b}$$

Hence (B) is correct option.

MCQ 1.48 Two identical NMOS transistors M1 and M2 are connected as shown below. V_{bias} is chosen so that both transistors are in saturation. The equivalent g_m of the pair is defied to be $\frac{\partial I_{out}}{\partial V_i}$ at constant V_{out}

The equivalent g_m of the pair is \blacksquare

$$V_{\text{bias}} \bullet \downarrow_{M_1} \bullet \downarrow_{M_2} \bullet$$

(A) the sum of individual g_m 's of the transistors

(B) the product of individual g_m 's of the transistors

- (C) nearly equal to the g_m of M1
- (D) nearly equal to $\frac{g_m}{g_0}$ of M2
- **SOL 1.48** The current in both transistor are equal. Thus g_m is decide by M_1 . Hence (C) is correct option.
- MCQ 1.49 An 8085 executes the following instructions 2710 LXI H, 30A0 H 2713 DAD H 2414 PCHL

All address and constants are in Hex. Let PC be the contents of the program counter and HL be the contents of the HL register pair just after executing PCHL. Which of the following statements is correct ?

(A)
$$\begin{array}{l} \mathrm{PC} = 2715\mathrm{H} \\ \mathrm{HL} = 30\mathrm{A0H} \end{array}$$
 (B)
$$\begin{array}{l} \mathrm{PC} = 30\mathrm{A0H} \\ \mathrm{HL} = 2715\mathrm{H} \end{array}$$

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- (C) $\begin{array}{l} PC = 6140 H \\ HL = 6140 H \end{array}$ (D) $\begin{array}{l} PC = 6140 H \\ HL = 2715 H \end{array}$
- SOL 1.492710H LXI H, 30A0H
2713H DAD H
2713H DAD H
2714H PCHL; Load 16 bit data 30A0 in HL pair
; 6140H \rightarrow HL
; Copy the contents 6140H of HL in PC
Thus after execution above instruction contests of PC and HL are same and that
is 6140H
Hence (C) is correct answer.
- **MCQ 1.50** An astable multivibrator circuit using IC 555 timer is shown below. Assume that the circuit is oscillating steadily.



The voltage V_c across the capacitor varies between (A) 3 V to 5 V (B) 3 V to 6 V (C) 3.6 V to 6 V (D) 3.6 V to 5 V

- **SOL 1.50** Correct Option is ()
- **MCQ 1.51** Silicon is doped with boron to a concentration of 4×10^{17} atoms cm³. Assume the intrinsic carrier concentration of silicon to be 1.5×10^{10} / cm³ and the value of kT/q to be 25 mV at 300 K. Compared to undopped silicon, the fermi level of doped silicon
 - (A) goes down by 0.31 eV
- (B) goes up by 0.13 eV

(D) goes up by 0.427 eV

(C) goes down by 0.427 eV

SOL 1.51 Hence option (C) is correct. $E_2 - E_1 = kT \ln \frac{N_A}{r}$

$$N_A = 4 \times 10^{17}$$

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$$n_i = 1.5 \times 10^{10}$$

 $E_2 - E_1 = 25 \times 10^{-3} e \ln \frac{4 \times 10^{17}}{1.5 \times 10^{10}} = 0.427 \text{ eV}$

Hence fermi level goes down by 0.427 eV as silicon is doped with boron.

MCQ 1.52 The cross section of a JFET is shown in the following figure. Let V_c be -2 V and let V_P be the initial pinch -off voltage. If the width W is doubled (with other geometrical parameters and doping levels remaining the same), then the ratio between the mutual trans conductances of the initial and the modified JFET is



OPMAP. Assume that the output of the OPAMP swings from +15 V to -15 V. The voltage at the non-inverting input switches between



SOL 1.53 Let the voltage at non inverting terminal be V_1 , then after applying KCL at non inverting terminal side we have

$$\frac{15 - V_1}{10} + \frac{V_0 - V_1}{10} = \frac{V_1 - (-15)}{10}$$

or
$$V_1 = \frac{V_0}{3}$$

If V_0 swings from -15 to +15 V then V_1 swings between -5 V to +5 V.
Hence (C) is correct option.

MCQ 1.54 The logic function implemented by the following circuit at the terminal OUT is



- (C) P OR Q (D) P AND Q
- **SOL 1.54** From the figure shown below it may be easily seen upper MOSFET are shorted and connected to V_{dd} thus OUT is 1 only when the node S is 0,



Since the lower MOSFETs are shorted to ground, node S is 0 only when input P

Page 28	GATE EC 2008	www.gatehelp.com
	and Q are 1. This is the function of AND gate. Hence (D) is correct answer.	
MCQ 1.55	 Consider the following assertions. S1 : For Zener effect to occur, a very abrupt junction is required. S2 : For quantum tunneling to occur, a very narrow energy barried. Which of the following is correct ? (A) Only S2 is true (B) S1 and S2 are both true but S2 is not a reason for S1 (C) S1 and S2 and are both true but S2 is not a reason for S1 (D) Both S1 and S2 are false 	er is required.
SOL 1.55	Hence option (A) is correct.	
MCQ 1.56	The two numbers represented in signed 2's complement form a and $Q = 11100110$. If Q is subtracted from P , the value obtain complement is (A) 1000001111 (B) 00000111 (D) 11111001	are $P + 11101101$ ned in signed 2's
SOL 1.56	MSB of both number are 11101101 = $(-19)_{10}$ and $11100110 = (-26)_{10}$ P - Q = (-19) - (-26) = 7 Thus 7 signed two's complements form is $(7)_{10} = 00000111$ Hence (B) is correct answer.	we get
MCQ 1.57	Which of the following Boolean Expressions correctly represent between P, Q, R and M_1 P Q Q Q Q Q Q Q Q Q Q	ents the relation
SOL 1.57	(A) $M_1 = (P \text{ OR } Q) \text{ XOR } R$ (B) $M_1 = (P \text{ AND } Q) X O C Q$ (C) $M_1 = (P \text{ NOR } Q) X \text{ OR } R$ (D) $M_1 = (P \text{ XOR } Q) X O C Q$ The circuit is as shown below	OR <i>R</i> DR <i>R</i>





Hence (D) is correct answer

MCQ 1.58 For the circuit shown in the following, $I_0 - I_3$ are inputs to the 4:1 multiplexers, R (MSB) and S are control bits.

The output Z can be represented by



(A) $PQ + P\overline{Q}S + \overline{QRS}$ (B) $P\overline{Q} + PQ\overline{R} + \overline{PQS}$ (C) $P\overline{QR} + \overline{P}QR + PARS + \overline{QRS}$ (D) $PQ\overline{R} + PQR\overline{S} + P\overline{QRS} + \overline{QRS}$

SOL 1.58 Hence (A) is correct answer. $Z = I_0 \overline{RS} + I_1 \overline{RS} + I_2 R\overline{S} + I_3 RS$ $= (P + \overline{Q}) \overline{RS} + P\overline{RS} + PQR\overline{S} + PRS$ $= P\overline{RS} + \overline{QRS} + P\overline{RS} + PQR\overline{S} + PRS$

The k – Map is as shown below

GATE EC 2008

 $Z = PQ + P\overline{Q}S + \overline{Q}\overline{R}S$

MCQ 1.59 For each of the positive edge-triggered J - K flip flop used in the following figure, the propagation delay is Δt .





Which of the following wave forms correctly represents the output at Q_1 ?

- (A) $\begin{array}{c} 1 \\ t_{1}+\Delta t \\ t_{1}+2\Delta t \\ \end{array}$ (B) $\begin{array}{c} 1 \\ t_{1}+2\Delta t \\ t_{1}+2\Delta t \\ \end{array}$ (C) $\begin{array}{c} 1 \\ t_{1}+2\Delta t \\ t_{1}+2\Delta t \\ \end{array}$ (D) $\begin{array}{c} 1 \\ t_{1}+\Delta t \\ \end{array}$
- **SOL 1.59** Since the input to both JK flip-flop is 11, the output will change every time with clock pulse. The input to clock is



The output Q_0 of first FF occurs after time ΔT and it is as shown below



The output Q_1 of second FF occurs after time ΔT when it gets input (i.e. after ΔT from t_1) and it is as shown below



Hence (B) is correct answer.

MCQ 1.60 For the circuit shown in the figure, D has a transition from 0 to 1 after CLK changes from 1 to 0. Assume gate delays to be negligible Which of the following statements is true

- (A) Q goes to 1 at the CLK transition and stays at 1
- (B) Q goes to 0 at the CLK transition and stays 0
- (C) Q goes to 1 at the CLK tradition and goes to 0 when D goes to 1
- (D) Q goes to 0 at the CLK transition and goes to 1 when D goes to 1



The truth table is shown below. When CLK make transition Q goes to 1 and when D goes to 1, Q goes to 0 Hence (A) is correct answer.

• Q

- MCQ 1.61A rectangular waveguide of internal dimensions (a = 4 cm and b = 3 cm) is to be
operated in TE_{11} mode. The minimum operating frequency is
(A) 6.25 GHz(B) 6.0 GHz(C) 5.0 GHz(D) 3.75 GHz
- **SOL 1.61** Cut-off Frequency is

$$f_c = \frac{c}{2} \sqrt{\left(\frac{m}{a}\right)^2 + \left(\frac{n}{b}\right)^2}$$

For TE_{11} mode,

$$f_c = \frac{3 \times 10^{10}}{2} \sqrt{\left(\frac{1}{4}\right)^2 + \left(\frac{1}{3}\right)^2} = 6.25 \text{ GHz}$$

Hence (A) is correct option.

MCQ 1.62 One end of a loss-less transmission line having the characteristic impedance of 75Ω and length of 1 cm is short-circuited. At 3 GHz, the input impedance at the other end of transmission line is

(A) 0	(B) Resistive
(C) C_{aba} a_{i} t_{i}	(D) Inductive

- (C) Capacitive (D) Inductive
- **SOL 1.62** Hence (D) is correct option.

$$Z_{in} = Z_o \frac{Z_L + iZ_o \tan{(\beta l)}}{Z_o + iZ_L \tan{(\beta l)}}$$

For $Z_L = 0, Z_{in} = iZ_o \tan(\beta l)$ The wavelength is

 $\lambda = \frac{c}{f} = \frac{3 \times 10^8}{3 \times 10^9} = 0.1 \text{ m or } 10 \text{ cm}$ $\beta l = \frac{2\pi}{\lambda} l = \frac{2\pi}{10} \times 1 = \frac{\pi}{5}$ $Z_{in} = iZ_o \tan \frac{\pi}{5} \textbf{G} \textbf{a} \textbf{l} \textbf{G}$

Thus

Thus Z_{in} is inductive because $Z_o \tan \frac{\pi}{5}$ is positive

- **MCQ 1.63** A uniform plane wave in the free space is normally incident on an infinitely thick dielectric slab (dielectric constant $\varepsilon = 9$). The magnitude of the reflection coefficient is
 - (A) 0 (B) 0.3 (D) 0.5
 - (C) 0.5 (D) 0.8
- **SOL 1.63** Hence (C) is correct option.

We have $\eta = \sqrt{\frac{\mu}{\varepsilon}}$

Reflection coefficient

$$\Gamma = \frac{\eta_2 - \eta_1}{\eta_2 + \eta_1}$$

Substituting values for η_1 and η_2 we have

$$\tau = \frac{\sqrt{\frac{\mu_o}{\varepsilon_o \varepsilon_r}} - \sqrt{\frac{\mu_o}{\varepsilon_o}}}{\sqrt{\frac{\mu_o}{\varepsilon_o \varepsilon_r}} + \sqrt{\frac{\mu_o}{\varepsilon_o}}} = \frac{1 - \sqrt{\varepsilon_r}}{1 + \sqrt{\varepsilon_r}} = \frac{1 - \sqrt{9}}{1 + \sqrt{9}}$$
 since $\varepsilon_r = 9$
$$= -0.5$$

- **MCQ 1.64** In the design of a single mode step index optical fibre close to upper cut-off, the single-mode operation is not preserved if
 - (A) radius as well as operating wavelength are halved

Page 33	GAT	'E EC 2008	www.gatehelp.com
	(B) radius as well as operating(C) radius is halved and operat(D) radius is doubled and operation	wavelength are doubled ing wavelength is doubled ating wavelength is halved	
SOL 1.64	In single mode optical fibre, the decreases Hence $r \propto \frac{1}{f}$	ne frequency of limiting mode	e increases as radius
	So. if radius is doubled, the free option (D) it is increased by tw Hence (C) is correct option.	equency of propagating mode o times.	gets halved, while in
MCQ 1.65	At 20 GHz, the gain of a parab (A) 15 dB (C) 35 dB	olic dish antenna of 1 meter a (B) 25 dB (D) 45 dB	nd 70% efficiency is
SOL 1.65	L 1.65 Hence (D) is correct option. $\lambda = \frac{c}{f} = \frac{3 \times 10^8}{20 \times 10^9} = \frac{3}{200}$		
	Gain $G_p = \eta \pi^2 \left(\frac{D}{\lambda}\right)^2 = 0.7$ = 44.87 dB	$\times \pi^2 \left(\frac{1}{\frac{3}{100}}\right)^2 = 30705.4$	
MCQ 1.66	Noise with double-sided power s through a RC low pass filter with the filter output is	spectral density on K over all ith 3 dB cut-off frequency of f	frequencies is passed f. The noise power at
	(A) K (C) $k\pi f_c$	(B) Kf_c (D) ∞	
SOL 1.66	Hence (C) is correct option. PSD of noise is $\frac{N_0}{2} = K$		(1)
	The 3-dB cut off frequency is $f_c = \frac{1}{2\pi RC}$		(2)
	Output noise power is $= \frac{N_0}{4RC} =$	$=\left(\frac{N_0}{2}\right)\frac{1}{2RC} = K\pi f_c$	
MCQ 1.67	Consider a Binary Symmetric C transmit a bit, say 1, we transmit the received sequence to represe the transmitted bit will be rece (A) $p^3 + 3p^2(1-p)$	Thannel (BSC) with probability it a sequence of three 1s. The result of the least two bits are 1. ived in error is (B) p^3	y of error being p . To receiver will interpret The probability that

Page 34		GATE EC 2008	www.gatehelp.com
	(C) $(1-p^3)$	(D) $p^3 + p^2(1-p)$	
SOL 1.67	At receiving end if we get to Let p be the probability of = Three zero $= {}^{3}C_{3}p^{3} + 3C$ $= p^{3} + p^{2}(1 - p^{3})$ Hence (D) is correct option	two zero or three zero then its er 1 bit error, the probability that p + two zero and single one $C_2 p^2 (1-p)$ p - p)	ror. transmitted bit error is
MCQ 1.68	Four messages band limited using Time Division Multi- transmission of this TDM s (A) W	to $W, W, 2W$ and $3W$ respective plexing (TDM). The minimum 1 signal is (B) $3W$	ly are to be multiplexed bandwidth required for
	$(C) \ b W$	$(\mathbf{D}) \ \mathbf{i} \ \mathbf{W}$	
JUL 1.00	$= \frac{1}{2} \text{ (sum of}$ $= \frac{1}{2} [2W + 2]$	W + 4W + 6W = 7W	
	Hence (D) is correct option	nate	
MCQ 1.69	Consider the frequency mo $10 \cos [2\pi \times 10^5 t + 5 \sin (2\pi \times 10^5 t)]$ with carrier frequency of 10 (A) 12.5 (C) 7.5	dulated signal $\langle 1500t \rangle + 7.5 \sin (2\pi \times 1000t)]$ \rangle^5 Hz. The modulation index is (B) 10 (D) 5	
SOL 1.69	Hence (B) is correct option We have $\theta_i = 2\pi 10^5 t + 5$ $\omega_i = \frac{d\theta_i}{dt} = 2\pi 10^5 + 10\pi 1$ Maximum frequency deviat $\Delta \omega_{\text{max}} = 2\pi (0 + 10\pi)$ Modulation index is $= \frac{\Delta f_{\text{max}}}{f_{\text{max}}}$	$\sin (2\pi 1500t) + 7.5 \sin (2\pi 1000t)$ $500 \cos (2\pi 1500t) + 15\pi 1000 \cos (2\pi 1500t) + 15\pi 1000 \cos (2\pi 1500t) + 15\pi 1000)$ $55 \times 1500 + 7.5 \times 1000)$ 00 $\frac{15000}{1500} = 10$	$2\pi 1000t$)
MCQ 1.70	The signal $\cos \omega_c t + 0.5 \cos (A)$ FM only (C) both AM and FM	$\omega_m t \sin \omega_c t$ is (B) AM only (D) neither AM n	or FM
SOI 4 70	Hence (C) is correct option	()	
55E 1./U	inche (C) is correct option		

Common Data for Questions 71, 72 and 73 :

A speed signal, band limited to 4 kHz and peak voltage varying between +5 V and -5 V, is sampled at the Nyquist rate. Each sample is quantized and represented by 8 bits.

MCQ 1.71 If the bits 0 and 1 are transmitted using bipolar pulses, the minimum bandwidth required for distortion free transmission is

(A) 64 kHz	(B) 32 kHz
(C) 8 kHz	(D) 4 kHz

SOL 1.71 Hence (B) is correct option.

 $f_m = 4 \text{ KHz}$ $f_s = 2f_m = 8 \text{ kHz}$ Bit Rate $R_b = nf_s = 8 \times 8 = 64 \text{ kbps}$ The minimum transmission bandwidth is

$$BW = \frac{R_b}{2} = 32 \text{ kHz}$$

- **MCQ 1.72** Assuming the signal to be uniformly distributed between its peak to peak value, the signal to noise ratio at the quantizer output is
- (A) 16 dB (C) 48 dB SOL 1.72 Hence (C) is correct option. $\left(\frac{S_0}{N_0}\right) = 1.76 + 6n \text{ dB}$ $= 1.76 + 6 \times 8 = 49.76 \text{ dB}$ We have n = 8
- MCQ 1.73 The number of quantization levels required to reduce the quantization noise by a factor of 4 wo
 (A) 1024
 (B) 512
 - $\begin{array}{c} (D) & 0.21 \\ (C) & 256 \\ (D) & 64 \\ \end{array}$
- **SOL 1.73** Hence (B) is correct option.

As Noise
$$\propto \frac{1}{L^2}$$

To reduce quantization noise by factor 4, quantization level must be two times i.e. 2L.

Now $L = 2^n = 2^8 = 256$ Thus 2L = 512

Common data for questions 74 & 75 :

The following series RLC circuit with zero conditions is excited by a unit impulse

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MCQ 1.74 For t > 0, the output voltage $v_C(t)$ is

(A)
$$\frac{2}{\sqrt{3}} \left(e^{\frac{-1}{2}t} - e^{\frac{\sqrt{3}}{2}t} \right)$$
 (B) $\frac{2}{\sqrt{3}} t e^{\frac{-1}{2}t}$
(C) $\frac{2}{\sqrt{3}} e^{\frac{-1}{2}t} \cos\left(\frac{\sqrt{3}}{2}t\right)$ (D) $\frac{2}{\sqrt{3}} e^{\frac{-1}{2}t} \sin\left(\frac{\sqrt{3}}{2}t\right)$

SOL 1.74

Writing in transform domain we have

$$\frac{V_c(s)}{V_s(s)} = \frac{\frac{1}{s}}{(\frac{1}{s} + s + 1)} = \frac{1}{(s^2 + s + 1)}$$
Since $V_s(t) = \delta(t) \rightarrow V_s(s) = 1$ and
 $V_c(s) = \frac{1}{(s^2 + s + 1)}$
or $V_c(s) = \frac{2}{\sqrt{3}} \left[\frac{\frac{\sqrt{3}}{2}}{(s + \frac{1}{2})^2 + \frac{3}{4}} \right]$
Taking inverse laplace transform we have
 $V_t = \frac{2}{\sqrt{3}} e^{-\frac{t}{2}} \sin\left(\frac{\sqrt{3}}{2}t\right)$

Hence (D) is correct option.

MCQ 1.75 For
$$t > 0$$
, the voltage across the resistor is
(A) $\frac{1}{\sqrt{3}} \left(e^{\frac{\sqrt{3}}{2}t} - e^{-\frac{1}{2}t} \right)$
(B) $e^{-\frac{1}{2}t} \left[\cos\left(\frac{\sqrt{3}}{2}t\right) - \frac{1}{\sqrt{3}} \sin\left(\frac{\sqrt{3}t}{2}t\right) \right]$
(C) $\frac{2}{\sqrt{3}} e^{-\frac{1}{2}t} \sin\left(\frac{\sqrt{3}t}{2}t\right)$
(D) $\frac{2}{\sqrt{3}} e^{-\frac{1}{2}t} \cos\left(\frac{\sqrt{3}}{2}t\right)$
Let voltage across resistor be v_R
 $\frac{V_R(s)}{V_S(s)} = \frac{1}{(\frac{1}{s} + s + 1)} = \frac{s}{(s^2 + s + 1)}$
Since $v_s = \delta(t) \rightarrow V_s(s) = 1$ we get

$$V_R(s) = \frac{s}{(s^2 + s + 1)} = \frac{s}{(s + \frac{1}{2})^2 + \frac{3}{4}}$$

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or

$$= \frac{(s+\frac{1}{2})}{(s+\frac{1}{2})^2 + \frac{3}{4}} - \frac{\frac{1}{2}}{(s+\frac{1}{2})^2 + \frac{3}{4}}$$
$$v_R(t) = e^{-\frac{1}{2}} \cos \frac{\sqrt{3}}{2} t - \frac{1}{2} \times \frac{2}{\sqrt{3}} e^{-\frac{1}{2}} \sin \frac{\sqrt{3}}{2} t$$
$$= e^{-\frac{t}{2}} \left[\cos \frac{\sqrt{3}}{2} t - \frac{1}{\sqrt{3}} \sin \frac{\sqrt{3}}{2} t \right]$$

Hence (B) is correct option.

Linked Answer Questions : Q. 76 to Q.85 carry two marks each.

Statement for linked Answers Questions 76 & 77:

A two-port network shown below is excited by external DC source. The voltage and the current are measured with voltmeters V_1 , V_2 and ammeters. A_1 , A_2 (all assumed to be ideal), as indicated

$$\begin{array}{c} \mathbf{A} = \underbrace{\mathbf{A}}_{1} + \underbrace{\mathbf{A}}_{1} + \underbrace{\mathbf{A}}_{2} + \underbrace{$$

Thus z-parameter matrix is

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$$\begin{bmatrix} z_{11} & z_{12} \\ z_{21} & z_{22} \end{bmatrix} = \begin{bmatrix} 1.5 & 4.5 \\ 1.5 & 1.5 \end{bmatrix}$$
Hence (C) is correct option.
MCQ 1.77 The *h*-parameter matrix for this network is
(A) $\begin{bmatrix} -3 & 3 \\ -1 & 0.67 \end{bmatrix}$ (B) $\begin{bmatrix} -3 & -1 \\ 3 & 0.67 \end{bmatrix}$
(C) $\begin{bmatrix} 3 & 3 \\ 1 & 0.67 \end{bmatrix}$ (D) $\begin{bmatrix} 3 & 1 \\ -3 & -0.67 \end{bmatrix}$
SOL 1.77 From the problem statement we have
 $h_{12} = \frac{v_1}{v_2} \Big|_{i_0=0} = \frac{4.5}{1.5} = 3$
 $h_{22} = \frac{i_2}{v_2} \Big|_{i_0=0} = \frac{1}{1.5} = 0.67$
From *z* matrix, we have
 $v_1 = z_{11}i_1 + z_{12}i_2$
 $v_2 = z_{21}i_1 + z_{22}i_2$
If $v_2 = 0$
Then $\frac{i_2}{i_1} = \frac{-z_{21}}{-z_{22}} = \frac{-1.5}{1.5} = -1 = h_{21}$
or $i_2 = -i_1$
Putting in equation for v_1 , we get
 $v_1 = (z_{11} - z_{12})i_1$
 $\frac{v_1}{i_1} \Big|_{v_2=0} = h_{11} = z_{11} - z_{12} = 1.5 - 4.5 = -3$
Hence *h* -parameter will be

$$\begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} = \begin{bmatrix} -3 & 3 \\ -1 & 0.67 \end{bmatrix}$$

Hence (A) is correct option.

Statement for Linked Answer Question 78 and 79:

In the following network, the switch is closed at $t = 0^{-}$ and the sampling starts from t = 0. The sampling frequency is 10 Hz.



MCQ 1.78The samples x(n), n = (0, 1, 2, ...) are given by
(A) $5(1 - e^{-0.05n})$
(C) $5(1 - e^{-5n})$ (B) $5e^{-0.05n}$
(D) $5e^{-5n}$

SOL 1.78 Current through resistor (i.e. capacitor) is

$$I = I(0^{+}) e^{-t/RC}$$
Here, $I(0^{+}) = \frac{V}{R} = \frac{5}{200k} = 25\mu A$
 $RC = 200k \times 10\mu = 2 \sec$
 $I = 25e^{-\frac{t}{2}}\mu A$
 $= V_R \times R = 5e^{-\frac{t}{2}} V$
Here the voltages across the resistor is input to sampler at frequency of 10 Hz. Thus
 $x(n) = 5e^{\frac{-n}{2\times 10}} = 5e^{-0.05n}$ For $t > 0$
Hence (B) is correct answer.

MCQ 1.79 The expression and the region of convergence of the z-transform of the sampled signal are

(A)
$$\frac{5z}{z-e^5}$$
, $|z| < e^{-5}$
(B) $\frac{5z}{z-e^{-0.05}}$, $|z| < e^{-0.05}$
(C) $\frac{5z}{z-e^{-0.05}}$, $|z| > e^{-0.05}$
Hence (C) is correct answer.
Since $x(n) = 5e^{-0.05n}u(n)$ is a causal signal
Its z transform is
 $X(z) = 5\left[\frac{1}{1-e^{-0.05}z^{-1}}\right] = \frac{5z}{z-e^{-0.05}}$
Its ROC is $|e^{-0.05}z^{-1}| > 1 \rightarrow |z| > e^{-0.05}$

Statement for Linked Answer Questions 80 and 81:

In the following transistor circuit, $V_{BE} = 0.7$ V, $r_3 = 25$ mV/ I_E , and β and all the capacitances are very large



MCQ 1.80 The value of DC current I_E is

SOL 1.79

SOL 1.80

For the given DC values the Thevenin equivalent circuit is as follows



The thevenin resistance and voltage are

$$V_{TH} = \frac{10}{10 + 20} \times 9 = 3 \text{ V}$$

and total $R_{TH} = \frac{10 \text{k} \times 20 \text{k}}{10 \text{k} + 20 \text{k}} = 6.67 \text{ k}\Omega$

Since β is very large, therefore I_B is small and can be ignored Thus $I_E = \frac{V_{TH} - V_{BE}}{R_E} = \frac{3 - 0.7}{2.3k} \mathbf{\overline{c}}^1 \text{ mA}$ Hence (A) is correct option.

MCQ 1.81The mid-band voltage gain of the amplifier is approximately
(A) -180
(C) -90(B) -120
(D) -60

SOL 1.81 The small signal model is shown in fig below

Brought to you by: <u>Nodia and Company</u> PUBLISHING FOR GATE Hence (D) is correct option.

Statement For Linked Answer Question 82 & 83:

In the following circuit, the comparators output is logic "1" if $V_1 > V_2$ and is logic "0" otherwise. The D/A conversion is done as per the relation $V_{DAC} = \sum_{n=0}^{3} 2^{n-1} b_n$ Volts, where b_3

(MSB), b_1, b_2 and b_0 (LSB) are the counter outputs. The counter starts from the clear state.



SOL 1.82 Hence (D) is correct answer. We have

$$V_{DAC} = \sum_{n=0}^{3} 2^{n-1} b_n = 2^{-1} b_0 + 2^0 b_1 + 2^1 b_2 + 2^2 b_3$$

or
$$V_{DAC} = 0.5 b_0 + b_1 + 2 b_2 + 4 b_3$$

The counter outputs will increase by 1 from 0000 till $V_{th} > V_{DAC}$. The output of counter and V_{DAC} is as shown below

Clock	$b_3 b_3 b_2 b_0$	V_{DAC}
1	0001	0
2	0010	0.5
3	0011	1
4	0100	1.5
5	0101	2

SOL 1.84

6	0110	2.5
7	0111	3
8	1000	3.5
9	1001	4
10	1010	4.5
11	1011	5
12	1100	5.5
13	1101	6
14	1110	6.5

and when $V_{ADC} = 6.5$ V (at 1101), the output of AND is zero and the counter stops. The stable output of LED display is 13.

MCQ 1.83 The magnitude of the error between V_{DAC} and V_{in} at steady state in volts is (A) 0.2

(A) 0.2
(C) 0.5
SOL 1.83 Hence (B) is correct answer.
The
$$V_{ADC} - V_{in}$$
 at steady state is
 $= 6.5 - 6.2 = 0.3V$ (D) 1.0

Statement for Linked Answer Question 84 & 85 :

The impulse response h(t) of linear time - invariant continuous time system is given by $h(t) = \exp(-2t) u(t)$, where u(t) denotes the unit step function.

MCQ 1.84 The frequency response $H(\omega)$ of this system in terms of angular frequency ω , is given by $H(\omega)$

(A)
$$\frac{1}{1+j2\omega}$$

(B) $\frac{\sin \omega}{\omega}$
(C) $\frac{1}{2+j\omega}$
(D) $\frac{j\omega}{2+j\omega}$
Hence (C) is correct answer.

$$h(t) = e^{-2t} u(t)$$

$$H(j\omega) = \int_{-\infty}^{\infty} h(t) e^{-j\omega t} dt$$

$$= \int_{0}^{\infty} e^{-2t} e^{-j\omega t} dt = \int_{0}^{\infty} e^{-(2+j\omega)t} dt = \frac{1}{(2+j\omega)}$$

MCQ 1.85 The output of this system, to the sinusoidal input $x(t) = 2\cos 2t$ for all time t, is (A) 0 (B) $2^{-0.25}\cos(2t - 0.125\pi)$

(C)
$$2^{-0.5}\cos(2t - 0.125\pi)$$
 (D) $2^{-0.5}\cos(2t - 0.25\pi)$

SOL 1.85 Hence (D) is correct answer. U(x,y) = 1

$$H(j\omega) = \frac{1}{(2+j\omega)}$$

The phase response at $\omega = 2$ rad/sec is

$$\angle H(j\omega) = -\tan^{-1}\frac{\omega}{2} = -\tan^{-1}\frac{2}{2} = -\frac{\pi}{4} = -0.25\pi$$

Magnitude respone at $\omega = 2$ rad/sec is

1

$$|H(j\omega)| = \sqrt{\frac{1}{2^2 + w^2}} = \frac{1}{2\sqrt{2}}$$

Input is $x(t) = 2\cos(2t)$

Output i

$$= \frac{1}{2\sqrt{2}} \times 2\cos(2t - 0.25\pi)$$
$$= \frac{1}{\sqrt{2}}\cos[2t - 0.25\pi]$$

Answer Sheet									
1.	(C)	19.	(B)	37.	(A)	55.	(A)	73.	(B)
2.	(B)	20.	(A)	38.	(D)	56.	(B)	74.	(D)
3.	(A)	21.	(A)	39.	(C) C	57.	(D)	75.	(B)
4.	(A)	22.	(D)	40.	(C)	58.	(A)	76.	(C)
5.	(A)	23.	(C)	41.	(C)	59.	(B)	77.	(A)
6.	(B)	24.	(A)	42.	(C)	60.	(A)	78.	(B)
7.	(C)	25.	(C)	43.	(B)	61.	(A)	79.	(C)
8.	(B)	26.	(A)	44.	(B)	62.	(D)	80.	(A)
9.	(C)	27.	(D)	45.	(C)	63.	(C)	81.	(D)
10.	(D)	28.	(B)	46.	(B)	64.	(C)	82.	(D)
11.	(C)	29.	(*)	47.	(B)	65.	(D)	83.	(B)
12.	(C)	30.	(A)	48.	(C)	66.	(C)	84.	(C)
13.	(D)	31.	(C)	49.	(C)	67.	(D)	85.	(D)
14.	(A)	32.	(A)	50.	(*)	68.	(D)		
15.	(C)	33.	(D)	51.	(C)	69.	(B)		
16.	(D)	34.	(B)	52.	(C)	70	(C)		
17.	(C)	35.	(B)	53.	(C)	71	(B)		
18.	(D)	36.	(A)	54.	(D)	72	(C)		

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