

**R.K ACADEMY SULUR- CBE****FULL PORTION 3**

Date : 04-Mar-20

10th Standard

**Maths**Reg.No. :      

**instructions: 1) Check the question paper for fairness of printing. If there is any lack of fairness, inform the Hall supervisor immediately. 2) Use black or blue ink to write and underline and pencil to draw diagrams.**

Time : 03:00:00 Hrs

Total Marks : 100

14 x 1 = 14

Note: This question paper contains four parts.

Note: i) Answer all questions.

ii) Choose the most suitable answer from the given four alternatives and write the option code with the corresponding answer iii) Each question carries 1 mark.

- 1) (b) (2, -1)
- 2) (d) 11
- 3) (a)  $\frac{8}{27}$
- 4) (a) straight line
- 5) (a) (i) and (ii) only
- 6) (c) 2 equal halves
- 7) (b) 4 cm
- 8) (d) 4 cm
- 9) (c)  $l_2$  and  $l_4$  are perpendicular

10)

(d)  $-\frac{7}{2}$

11)

(b)  $\frac{b}{3}$

12)

(a)  $\frac{2}{3}$

13)

(c)  $\frac{8\pi h^2}{9}$  sq. units

14)

(b)  $\frac{p}{p+q+r}$

ANSWER THE FOLLOWING ( Q. NO 28 IS COMPULSORY )

10 x 2 = 20

15)

$$f(x) = 2x + 5, x \neq 0. \frac{f(x+2) - f(2)}{x}$$

$$f(1) = 2 \times 1 + 5 = 7$$

$$f(2) = 2 \times 2 + 5 = 9$$

$$f(3) = 2 \times 3 + 5 = 11$$

When  $x=1$ 

$$\frac{f(x+2) - f(2)}{x}$$

$$f(x) = 2x + 5 \Rightarrow f(x + 2)$$

$$2(x + 2) + 5$$

$$2x + 4 + 5 = 2x + 9$$

$$2(2) + 5 = 4 + 5 = 9$$

$$\therefore \frac{f(x+2)-f(2)}{x} = \frac{2x+9-9}{x} = \frac{2x}{x} = 2$$

16)

$$f(x) = x-6, g(x)=x^2$$

$$f \circ g(x) = f(g(x)) = f(x^2) = x^2 - 6 \quad \dots\dots(1)$$

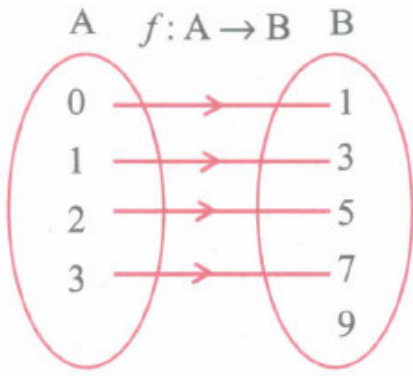
$$g \circ f(x) = g(f(x)) = g(x-6) = (x-6)^2 = x^2 + 36 - 12x = x^2 - 12x + 36 \quad \dots(2)$$

$$(1) \neq (2)$$

$$\therefore f \circ g(x) \neq g \circ f(x)$$

17)

An arrow diagram



18)

Let Senthil's house number be x.

It is given that  $1 + 2 + 3 + \dots + (x - 1) = (x + 1) + (x + 2) + \dots + 49$

$$1 + 2 + 3 + \dots + (x - 1) = [1 + 2 + 3 + \dots + 49] - [1 + 2 + 3 + \dots + x]$$

$$\frac{x-1}{2} [1 + (x - 1)] = \frac{49}{2} [1 + 49] - \frac{x}{2} [1 + x]$$

$$\frac{x(x-1)}{2} = \frac{49 \times 50}{2} - \frac{x(x+1)}{2}$$

$$x^2 - x = 2450 - x^2 - x \Rightarrow 2x^2 = 2450$$

$$x^2 = 1225 \text{ gives } x = 35$$

Therefore, Senthil's house number is 35.

19)

$$13 + 23 + 33 + \dots + 163 = \left[ \frac{16 \times (16+1)}{2} \right]^2 = (136)^2 = 18496$$

20)

$$\begin{aligned} & \frac{1}{x^2-5x+6} + \frac{1}{x^2-3x+2} - \frac{1}{x^2-8x+15} \\ &= \frac{1}{(x-2)(x-3)} + \frac{1}{(x-2)(x-1)} - \frac{1}{(x-5)(x-3)} \\ &= \frac{(x-1)(x-5) + (x-3)(x-5) - (x-1)(x-2)}{(x-1)(x-2)(x-3)(x-5)} \\ &= \frac{(x-1)(x-2)(x-3)(x-5)}{x^2-11x+18} = \frac{(x-9)(x-2)}{(x-1)(x-2)(x-3)(x-5)} \\ &= \frac{x-9}{(x-1)(x-3)(x-5)} \end{aligned}$$

21)

$$\begin{aligned} A^T &= \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \\ A \cdot A^T &= \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \\ &= \begin{pmatrix} \cos^2\theta + \sin^2\theta & -\cos\theta\sin\theta + \cos\theta\sin\theta \\ -\sin\theta\cos\theta + \cos\theta\sin\theta & \sin^2\theta + \cos^2\theta \end{pmatrix} \\ &= \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} = I \end{aligned}$$

Hence proved.

22)

$$\frac{(k-12)}{a}x^2 + \frac{2(k-12)}{b}x + \frac{2}{c} = 0$$

$$D^2 = b^2 - 4ac = (2(k-12))^2 - 4(k-12)(2)$$

$$= 4(k-12)[(k-12) - 2]$$

$$= 4(k-12)(k-14)$$

The given equation will have equal roots, if  $D = 0$

$$\Rightarrow 4(k-12)(k-14) = 0$$

$$k - 12 = 0 \text{ or } k - 14 = 0$$

$$k = 12, 14$$

23)

In  $\triangle ABC$ ,  $AD$  is the bisector of  $\angle A$

Therefore by Angle Bisector of  $\angle A$

$$\frac{AB}{AC} = \frac{BD}{DC}$$

$$\frac{10}{14} = \frac{x}{6-x} \text{ gives } \frac{5}{7} = \frac{x}{6-x}$$

$$\text{so, } 12x = 30 \text{ we get, } x = \frac{30}{12} = 2.5 \text{ cm.}$$

24)

If  $a$  and  $b$  are the intercepts then  $a + b = 7$  or  $b = 7 - a$

By intercept form  $\frac{x}{a} + \frac{y}{b} = 1 \dots (1)$

$$\text{We have } \frac{x}{a} + \frac{y}{7-a} = 1$$

As this line passes through the point  $(-3, 8)$ , we have

$$\frac{-3}{a} + \frac{8}{7-a} = 1 \text{ gives } -3(7-a) + 8a = a(7-a)$$

$$21 + 3a + 8a = 7a - a^2$$

$$\text{So, } a^2 + 4a - 21 = 0$$

$$\text{Solving this equation } (a-3)(a+7) = 0$$

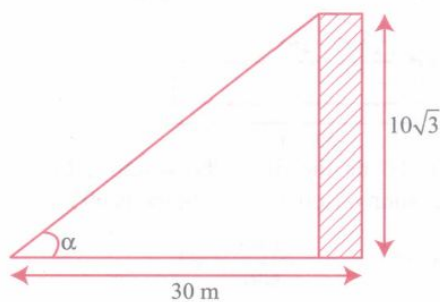
$$a = 3 \text{ or } a = -7$$

Since  $a$  is positive, we have  $a = 3$  and  $b = 7 - a = 7 - 3 = 4$ .

$$\text{Hence } \frac{x}{3} + \frac{y}{4} = 1$$

Therefore,  $4x + 3y - 12 = 0$  is the required equation.

25)



Angle of elevation of the top of the tower from a point 30 m away is  $\alpha$

$$\tan \alpha = \frac{\text{opp. side}}{\text{adj. side}} = \frac{10\sqrt{3}}{30} = \frac{1}{\sqrt{3}}$$

$$\therefore \alpha = \tan^{-1} \left( \frac{1}{\sqrt{3}} \right) = 30^\circ$$

26)

27)

Let  $r$  and  $h$  be the radius and height of the cone respectively.

Given that, volume of the cone =  $11088 \text{ cm}^3$

$$\frac{1}{3} \pi r^2 h = 11088$$

$$\frac{1}{3} \times \frac{22}{7} \times r^2 \times 24 = 11088$$

$$r^2 = 441$$

Therefore, radius of the cone  $r = 21$  cm

28)

Sample space

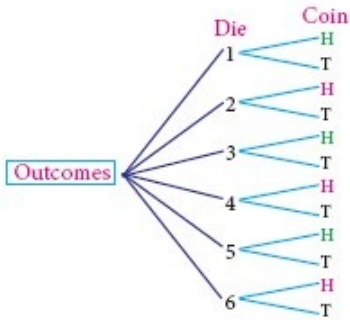
$$S = \{1H, 1T, 2H, 2T, 3H, 3T, 4H, 4T, 5H, 5T, 6H, 6T\};$$

$$n(S) = 12$$

Let A be the event of getting an odd number and a head.

$$A = \{1H, 3H, 5H\}; n(A) = 3$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{3}{12} = \frac{1}{4}$$

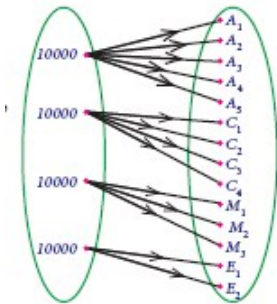


ANSWER THE FOLLOWING ( Q. NO 42 IS COMPULSORY )

10 x 5 = 50

29)

- {(10000, A<sub>1</sub>), (10000, A<sub>2</sub>), (10000, A<sub>3</sub>),
- (10000, A<sub>4</sub>), (10000, A<sub>5</sub>), (25000, C<sub>1</sub>),
- (25000, C<sub>2</sub>), (25000, C<sub>3</sub>), (25000, C<sub>4</sub>),
- (50000, M<sub>1</sub>), (50000, M<sub>2</sub>), (50000, M<sub>3</sub>),
- (100000, E<sub>1</sub>), (100000, E<sub>2</sub>)}



30)

$$gff(x) = g[f\{f(x)\}] \text{ (This means "g of f of f of x")}$$

$$= g[f(3x+1)] = g[3(x+1)+1] = g(9x+4)$$

$$g(9x+4) = [(9x+4)+3] = 9x+7$$

$$fgg(x) = f[g\{g(x)\}] \text{ (This means "f of g of g of x")}$$

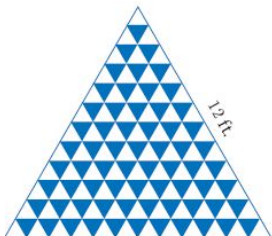
$$= f[g(x+3)] = f[(x+3)+3] = f(x+6)$$

$$f(x+6) = [3(x+6)+1] = 3x+19$$

These two quantities being equal, we get  $9x + 7 = 3x + 19$ . Solving this equation we obtain  $x=2$ .

31)

Since the mosaic is in the shape of an equilateral triangle of 12 ft, and the tile is in the shape of an equilateral triangle of 12 inch (1 ft) there will be 12 rows in the mosaic.



From the figure, it is clear that number of white tiles in each row are 1, 2, 3, 4, ..., 12 which clearly forms an Arithmetic Progression

Similarly the number of blue tiles in each row are 0, 1, 2, 3, ..., 11 which is also an Arithmetic Progression.

$$\text{Number of white tiles} = 1 + 2 + 3 + \dots + 12 = \frac{12}{2}[1 + 12] = 78$$

$$\text{Number of blue tiles} = 0 + 1 + 2 + 3 + \dots + 11 = \frac{12}{2}[0 + 11] = 66$$

$$\text{The total number of tiles in the mosaic} = 78 + 66 = 144$$

32)

Let the two A.Ps be

$$AP_1 = a_1 + a_1 + d, a_1 + 2d, \dots$$

$$AP_2 = a_2, a_2 + d, a_2 + 2d, \dots$$

In  $AP_1$  we have  $a_1 = 2$

In  $AP_2$  we have  $a_2 = 7$

$$t_{10} \text{ in } AP_1 = a_1 + 9d = 2 + 9d \dots (1)$$

$$t_{10} \text{ in } AP_2 = a_2 + 9d = 7 + 9d \dots (2)$$

The difference between their 10th terms

$$= (1) - (2) = 2 + 9d - 7 - 9d$$

$$= -5 \dots (I)$$

$$t_{21} \text{ in } AP_1 = a_1 + 20d = 2 + 20d \dots (3)$$

$$t_{21} \text{ in } AP_2 = a_2 + 20d = 7 + 20d \dots (4)$$

The difference between their 21st terms is (3) ... (4)

$$= 2 + 20d - 7 - 20d$$

$$= -5 \dots (II)$$

$$I = II$$

Hence it is proved

33)

$$\text{Squaring both sides } (\sqrt{y+1} + \sqrt{2y-5})^2 = 3^2$$

$$y+1+2y-5+2(\sqrt{y+1} + \sqrt{2y-5})=9$$

$$3y-4-9=-2\sqrt{y+1} + \sqrt{2y-5}$$

Again squaring both sides

$$(3y-13)^2(-2\sqrt{y+1} + \sqrt{2y-5})^2$$

$$9y^2-78y+169=4(y+1)(2y-5)$$

$$9y^2-78y+169=4(2y^2+2y-5y-5)$$

$$9y^2-78y+169=8y^2+8y-20y-20$$

$$9y^2-78y+169-8y^2+12y+20=0$$

$$y^2-66y+189=0$$

$$y^2-63-3y+189=0$$

$$y(y-63)-3(y-63)=0$$

$$(y-63)(y-3)=0$$

$$y=63,3$$

34)

$$\text{Let } \frac{1}{x} = p, \frac{1}{y} = q, \frac{1}{z} = r$$

The given equations are written as

$$\frac{p}{2} + \frac{q}{4} - \frac{r}{3} = \frac{1}{4}$$

$$p = \frac{q}{3}$$

$$p - \frac{q}{5} + 4r = 2 \frac{2}{15} = \frac{32}{15}$$

By simplifying we get,

$$6p + 3q - 4r = 3 \dots (1)$$

$$3p = q \dots (2)$$

$$15p - 3q + 60r = 32 \dots (3)$$

Substituting (2) in (1) and (3) we get,

$$15p - 4r = 3 \dots\dots(4)$$

$$6p + 60r = 32 \text{ reduces to } 3p + 30r = 16 \dots\dots\dots (5)$$

Solving (4) and (5),

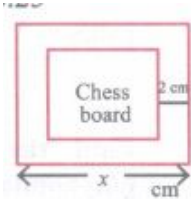
$$\begin{array}{r} 15p - 4r = 3 \\ 15p + 150r = 80 \quad (-) \\ \hline -154r = -77 \end{array} \text{ we get, } r = \frac{1}{2}$$

Substituting  $r = \frac{1}{2}$  in (4) we get,  $15p - 2 = 3$  gives,  $p = \frac{1}{3}$

From (2),  $q = 3p$  we get  $q = 1$

Therefore,  $x = \frac{1}{p} = 3, y = \frac{1}{q} = 1, z = \frac{1}{r} = 2$ . That is,  $x = 3, y = 1, z = 2$ .

35)



Let the length of the side of the chess board be  $x$  cm Then

$$\text{Area of } 64 \text{ squares} = (x - 4)^2$$

$$(x - 4)^2 = 64 \times 6.25$$

$$\Rightarrow x^2 - 8x + 16 = 400$$

$$\Rightarrow x^2 - 8x - 384 = 0$$

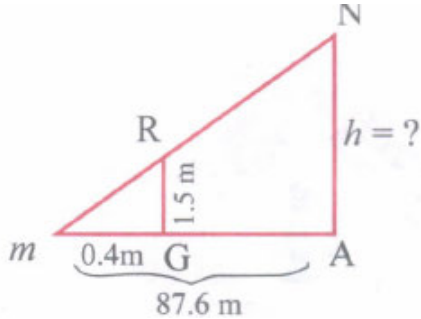
$$\Rightarrow x^2 - 24x + 16x - 384 = 0$$

$$\Rightarrow (x - 24)(x + 16) = 0$$

$$\Rightarrow x = 24 \text{ cm.}$$

36)

In the picture  $\triangle MLN, \triangle MGR$  are similar triangles.



$$\frac{GR}{LN} = \frac{MG}{ML}$$

$$\frac{1.5}{h} = \frac{0.4}{87.6}$$

$$0.4 \times h = 87.6 \times 1.5$$

$$\frac{4}{10} \times h = \frac{876}{10} \times \frac{15}{10}$$

$$= \frac{657}{2} = 328.5m$$

$\therefore$  Height of the lamppost is 328.5m

37)

Statement :

In a right angle triangle, the square on the hypotenuse is equal to the sum of the squares on the other two sides

Given :

$$\triangle ABC, \angle A = 90^\circ$$

To prove :

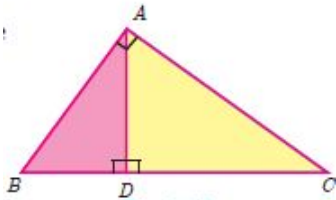


Fig. 4.46

$$AB^2 + AC^2 = BC^2$$

Construction : Draw  $AD \perp BC$

No.	Statement	Reason
1	Compare $\triangle ABC$ and $\triangle ABD$ $\angle B$ is common $\angle BAC = \angle BDA = 90^\circ$ Therefore, $\triangle ABC \sim \triangle ABD$ $\frac{AB}{BD} = \frac{BC}{AB}$ $AB^2 = BC \times BD \dots (1)$	Given $\angle BAC = 90^\circ$ and by construction $\angle BDA = 90^\circ$
2..	Compare $\triangle ABC$ and $\triangle ADC$ $\angle C$ is common $\angle BAC = \angle ADC = 90^\circ$ Therefore, $\triangle ABC \sim \triangle ADC$ $\frac{BC}{AC} = \frac{AC}{DC}$ $AC^2 = BC \times DC \dots (2)$	Given $\angle BAC = 90^\circ$ and by construction $\angle CDA = 90^\circ$ By AA similarity

Adding 1) and (2) we get

$$AB^2 + AC^2 = BC \times BD + BC \times DC$$

$$= BC(BD + DC) = BC \times BC$$

$$AB^2 + AC^2 = BC^2 .$$

Hence the theorem is proved.

38)

$$980 \text{ L@ Rs. } 14/\text{L}$$

$$1220 \text{ L@ Rs. } 16/\text{L}$$

$$\frac{17-16}{x-1220} = \frac{16-14}{1220} - 980$$

$$\Rightarrow \frac{1}{x-1220} = \frac{2}{240}$$

$$\Rightarrow x-1220=120$$

$$\Rightarrow x=1340$$

He can sell 1340 L@ Rs. 17L.

39)

$$a^2 = \frac{(1+\sin\theta)^2}{\cos^2\theta} = \frac{1+\sin^2\theta+2\sin\theta}{\cos^2\theta}$$

$$\therefore a^2 - 1 = \frac{\sin^2\theta+2\sin\theta+1-\cos^2\theta}{\cos^2\theta}$$

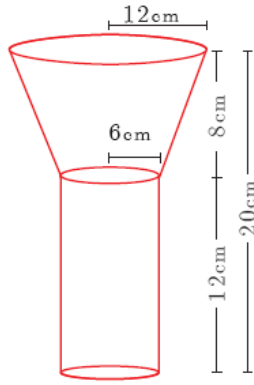
$$a^2 + 1 = \frac{\sin^2\theta+2\sin\theta+1+\cos^2\theta}{\cos^2\theta}$$

$$\therefore \text{L.H.S} = \frac{a^2-1}{a^2+1} = \frac{2\sin\theta+2\sin\theta}{2\sin\theta+2}$$

$$= \frac{\cancel{2} \sin \theta (\cancel{\sin \theta + 1})}{\cancel{2} (\cancel{\sin \theta + 1})}$$

$$= \sin \theta = \text{R.H.S}$$

40)



Let  $R, r$  be the top and bottom radii of the frustum.

Let  $h_1, h_2$  be the heights of the frustum and cylinder respectively

Given that,  $R = 12 \text{ cm}, r = 6 \text{ cm}, h_2 = 12 \text{ cm}$

Now,  $h_1 = 20 - 12 = 8 \text{ cm}$

Here, Slant height of the frustum  $l = \sqrt{(R - r)^2 + h_1^2} \text{ units}$

$$= \sqrt{36 + 64}$$

$$l = 10 \text{ cm}$$

Outer surface area  $= 2\pi r h_2 + \pi(R + r) l \text{ sq. units}$

$$= \pi[2r h_2 + (R + r)l]$$

$$= \pi[(2 \times 6 \times 12) + (12 + 6) \times 10]$$

$$= \pi[144 + 180]$$

$$= \frac{22}{7} \times 324 = 1018.28$$

Therefore, outer surface area of the funnel is  $1018.28 \text{ cm}^2$ .

41)

Volume of a cylinder  $= \pi r^2 h$

Volume of a cone  $= \frac{1}{3} \pi r^2 h$

Volume of a sphere  $= \frac{4}{3} \pi r^3$

Their ratio  $V_1 : V_2 : V_3$

$$\pi r^2 h : \frac{1}{3} \pi r^2 h : \frac{4}{3} \pi r^3$$

$$h : \frac{h}{3} : \frac{4r}{3}$$

$$3h : h : 4r$$

$$3h : h : 2(2r) \quad (\text{where } 2r = h)$$

$$\therefore V_1 : V_2 : V_3 = 3 : 1 : 2$$

42)

Time Taken X	Mid Value $x_i$	No. of Students $f_i$	$d_i = x_i - C$	$d_i = \frac{x_i - A}{C}$	$f_i x_i$	$f_i d_i^2$	$f_i d_i^3$
8.5-9.5	9	6	-2	-2	-12	4	24
9.5-10.5	10	8	-1	-1	-8	1	8
10.5-11.5	11	17	0	0	0	0	0
11.5-12.5	12	10	1	1	10	1	10
12.5-13.5	13	9	2	2	18	4	36
		N=50				8	78

Standard deviation

$$\sigma = c \times \sqrt{\frac{\sum f_i d_i^2}{N} - \left(\frac{\sum f_i d_i}{N}\right)^2}$$

$$= 1 \times \sqrt{\frac{78}{50} - \left(\frac{8}{50}\right)^2}$$

$$= 1 \times \sqrt{1.56 - (0.16)^2}$$



$$= 1 \times \sqrt{1.56 - -0.0256} = 1 \times \sqrt{1.534}$$

$$= 1 \times 1.213$$

$$= 1.2$$

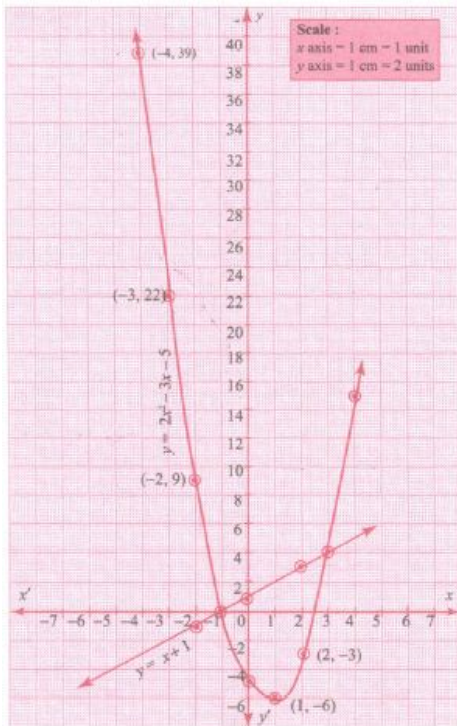
ANSWER THE FOLLOWING

2x 8 = 16

43) a)

x	-4	-3	-2	-1	0	1	2	3	4
x <sup>2</sup>	16	9	4	1	0	1	4	9	16
-2x <sup>2</sup>	32	18	8	2	0	2	8	18	32
-3x	12	9	6	3	0	-3	-6	-9	-12
-5	-5	-5	-5	-5	-5	-5	-5	-5	-5
y=x <sup>2</sup> -3x-5	39	22	9	0	-5	-6	-3	4	15

Draw the parabola using the points (-4, 39), (-3, 22), (-2, 9), (-1, 0), (0, -5), (1, -6), (2, -3), (3, 4), (4, 15).



To solve  $2x^2 - 4x - 6 = 0$ , subtract it from  $y = 2x^2 - 3x - 5$

$$y = 2x^2 - 3x - 5 \text{ is a straight line}$$

$$0 = 2x^2 - 4x - 6$$

$$\begin{array}{r} 2x^2 - 4x - 6 \\ - (2x^2 - 3x - 5) \\ \hline x - 1 \end{array}$$

$$y = x + 1$$

x	-2	0	2
y	-1	1	3

Draw a straight line using the points (-2, -1), (0, 1), (2, 3). The points of intersection of the parabola and the straight line forms the roots of the equation.

The x-coordinates of the points of intersection forms the solution set.

∴ Solution {-1, 3}

(OR)

b)

$$x^2 - 6x + 9 = 0$$

$$\text{Let } y = X^2 - 6x + 9$$

Step 1:

x	-4	-3	-2	-1	0	1	2	3	4
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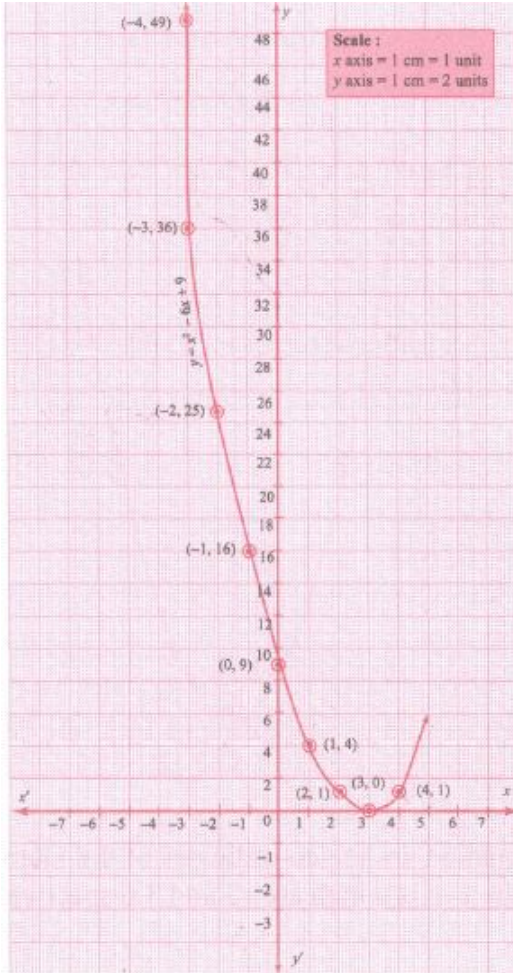
$x^2$	16	9	4	1	0	1	4	9	16
$-6x$	24	18	12	6	0	-6	-12	-18	-24
9	9	9	9	9	9	9	9	9	9
$y=x^2-6x+9$	49	36	25	16	9	4	1	0	1

Step 2:

Points to be plotted: (-4, 49), (-3, 36), (-2, 25), (-1, 16), (0, 9), (1, 4), (2, 1), (3, 0), (4, 1)

Step 3:

Draw the parabola and mark the co-ordinates of the intersecting points



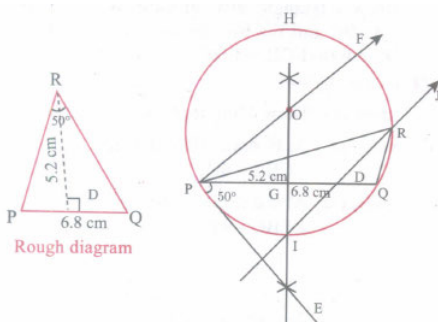
Step 4:

The point of intersection of the parabola with x axis is (3, 0)

Since there is only one point of intersection with the x-axis, the quadratic equation has real and equal roots.

∴ Solution (3, 3)

44) a)



Construction:

Steps (1) Draw a line segment PQ = 6.8 cm

Steps (2) At P, draw PE such that  $\angle QPE = 50^\circ$

Steps (3) At P, draw PF such that  $\angle FPE = 90^\circ$

Steps (4) Draw  $\perp'$  bisector to PQ, which intersects PF at O.

Steps (5) With O as centre and OP as radius draw a circle.

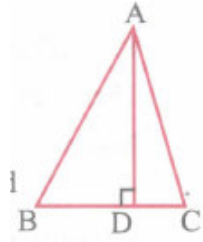
Steps (6) From P mark an arc of 5.2 cm on PQ at D.

Steps (7) The  $\perp'$  bisector intersects the circle at I. Join ID.

Steps (8) ID produced meets the circle at R. Now join PR & QR.  $\triangle PQR$  is the required triangle

**(OR)**

b)



We have  $DB = 3 CD$ .

$$BC = BD + DC$$

$$BC = 3CD + CD$$

$$BC = 4CD$$

$$CD = \frac{1}{4}BC$$

$$CD = \frac{1}{4}BC$$

$$BD = 3CD = \frac{3}{4}BC$$

Since  $\triangle ABD$  is a right triangle (i) right angled . at D.

$$AB^2 = AD^2 + BD^2$$

By  $\triangle ACD$  is a right triangle right angled at D

$$AC^2 = AD^2 + CD^2$$

Subtracting equation (iii) from equation (ii), we got

$$AB^2 - AC^2 = BD^2 - CD^2$$

$$\Rightarrow AB^2 - AC^2 = \left(\frac{3}{4}BC\right)^2 - \left(\frac{1}{4}BC\right)^2$$

$$\left(\text{from } CD = \frac{1}{4}BC, BD = \frac{3}{4}BC\right)$$

$$(i) \Rightarrow AB^2 - AC^2 = \frac{9}{16}BC^2 - \frac{1}{16}BC^2$$

$$\Rightarrow AB^2 - AC^2 = \frac{1}{2}BC^2$$

$$\Rightarrow AB^2 - AC^2 = \frac{1}{2}BC^2$$

$$\Rightarrow 2(AB^2 - AC^2) = BC^2$$

$$\Rightarrow 2AB^2 = 2AC^2 + BC^2$$

**R.K ACADEMY SULUR- CBE****FULL PORTION 3**

10th Standard

Date 16-Feb-20

Maths

Reg.No. :      

**instructions: 1) Check the question paper for fairness of printing. If there is any lack of fairness,inform the Hall supervisor immediately. 2)Use black or blue ink to write and underline and pencil to draw diagrams.**

Exam Time : 03:00:00 Hrs

Total Marks : 100

Note: This question paper contains four parts.

14 x 1 = 14

Note:i)Answer all questions.

ii) Choose the most suitable answer from the given four alternatives

and write the option code with the corresponding answer iii)Each

question carries 1 mark.

1) If  $g = \{(1,1), (2,3), (3,5), (4,7)\}$  is a function given by  $g(x) = \alpha x + \beta$  then the values of  $\alpha$  and  $\beta$  are

- (a) (-1,2) (b) (2,-1) (c) (-1,-2) (d) (1,2)

2) Given  $F_1 = 1, F_2 = 3$  and  $F_n = F_{n-1} + F_{n-2}$  then  $F_5$  is

- (a) 3 (b) 5 (c) 8 (d) 11

3) Sum of infinite terms of G.P is 12 and the first term is 8.what is the fourth term of the G.P?

- (a)  $\frac{8}{27}$  (b)  $\frac{4}{27}$  (c)  $\frac{8}{20}$  (d)  $\frac{1}{3}$

4) Graph of a linear polynomial is a

- (a) straight line (b) circle (c) parabola (d) hyperbola

5)

If  $A = \begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{pmatrix}$ ,  $B = \begin{pmatrix} 1 & 0 \\ 2 & -1 \\ 0 & 2 \end{pmatrix}$  and  $C = \begin{pmatrix} 0 & 1 \\ -2 & 5 \end{pmatrix}$ , Which of the following statements are correct?

(i)  $AB + C = \begin{pmatrix} 5 & 5 \\ 5 & 5 \end{pmatrix}$

(ii)  $BC = \begin{pmatrix} 0 & 1 \\ 2 & -3 \\ -4 & 10 \end{pmatrix}$

(iii)  $BA + C = \begin{pmatrix} 2 & 5 \\ 3 & 0 \end{pmatrix}$

(iv)  $(AB)C = \begin{pmatrix} -8 & 20 \\ -8 & 13 \end{pmatrix}$

- (a) (i) and (ii) only (b) (ii) and (iii) only (c) (iii) and (iv) only (d) all of these

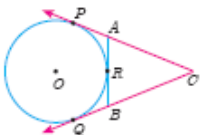
6) Axis of symmetry in the term of vertical line separates parabola into:

- (a) 3 equal halves (b) 5 equal halves (c) 2 equal halves (d) 4 equal halves

7) In a  $\triangle ABC$ , AD is the bisector  $\angle BAC$ .If  $AB=5\text{cm}$  and  $DC=8\text{cm}$ . The length of the side AC is

- (a) 6 cm (b) 4 cm (c) 3 cm (d) 8 cm

8) In figure CP and CQ are tangents to a circle with centre at O. ARB is another tangent touching the circle at R. If  $CP=11\text{ cm}$  and  $BC = 7\text{ cm}$ , then the length of BR is



- (a) 6 cm                                      (b) 5 cm                                      (c) 8 cm                                      (d) 4 cm

9) Consider four straight lines

(i)  $l_1 : 3y = 4x + 5$

(ii)  $l_2 : 4y = 3x - 1$

(iii)  $l_3 : 4y + 3x = 7$

(iv)  $l_4 : 4x + 3y = 2$

Which of the following statement is true?

- (a)  $l_1$  and  $l_2$  are perpendicular (b)  $l_1$  and  $l_4$  are parallel (c)  $l_2$  and  $l_4$  are perpendicular (d)  $l_2$  and  $l_3$  are parallel

10) Find the value of 'a' if the lines  $7y=ax+4$  and  $2y=3-x$  are parallel

- (a)  $\frac{7}{2}$                                       (b)  $-\frac{2}{7}$                                       (c)  $\frac{2}{7}$                                       (d)  $-\frac{7}{2}$

11) The electric pole subtends an angle of  $30^\circ$  at a point on the same level as its foot. At a second point 'b' metres above the first, the depression of the foot of the tower is  $60^\circ$ . The height of the tower (in metres) is equal to

- (a)  $\sqrt{3} b$                                       (b)  $\frac{b}{3}$                                       (c)  $\frac{b}{2}$                                       (d)  $\frac{b}{\sqrt{3}}$

12) If  $4 \tan\theta=3$ , then  $\left(\frac{4\sin\theta-\cos\theta}{4\sin\theta+\cos\theta}\right)$  is equal to

- (a)  $\frac{2}{3}$                                       (b)  $\frac{1}{3}$                                       (c)  $\frac{1}{2}$                                       (d)  $\frac{3}{4}$

13) The total surface area of a cylinder whose radius is  $\frac{1}{3}$  of its height is

- (a)  $\frac{9\pi h^2}{8}$  sq.units                                      (b)  $24\pi h^2$  sq.units                                      (c)  $\frac{8\pi h^2}{9}$  sq.units                                      (d)  $\frac{56\pi h^2}{9}$  sq.units

14) The probability a red marble selected at random from a jar containing p red, q blue and r green marbles is

- (a)  $\frac{q}{p+q+r}$                                       (b)  $\frac{p}{p+q+r}$                                       (c)  $\frac{p+q}{p+q+r}$                                       (d)  $\frac{p+r}{p+q+r}$

ANSWER THE FOLLOWING ( Q. NO 28 IS COMPULSORY )

10 x 2 = 20

15) Let  $f(x)=2x+5$ . If  $x \neq 0$  then find  $\frac{f(x+2)-f(2)}{x}$ .

16) Using the functions f and g given below, find f o g and g o f. Check whether f o g = g o f.

$$f(x) = x-6, g(x)=x^2$$

17) Let  $A = \{0, 1, 2, 3\}$  and  $B = \{1, 3, 5, 7, 9\}$  be two sets. Let  $f: A \rightarrow B$  be a function given by  $f(x) = 2x + 1$ . Represent this function as an arrow .

18) The houses of a street are numbered from 1 to 49. Senthil's house is numbered such that the sum of numbers of the houses prior to Senthil's house is equal to the sum of numbers of the houses following Senthil's house. Find Senthil's house number?

19) Find the sum of

$$1^3+2^3+3^3+\dots+16^3$$

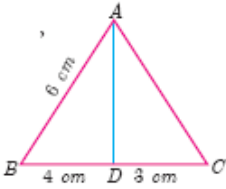
20) Simplify  $\frac{1}{x^2-5x+6} + \frac{1}{x^2-3x+2} - \frac{1}{x^2-8x+15}$

21) If  $A = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}$  prove that  $AA^T = I$ .

22) Find the values of k for which the following equation has equal roots.

$$(k - 12)r + 2(k - 12)x + 2 = 0$$

23) In the figure, AD is the bisector of  $\angle A$ . If  $BD = 4$  cm,  $DC = 3$  cm and  $AB = 6$  cm, find AC.



- 24) A line makes positive intercepts on coordinate axes whose sum is 7 and it passes through  $(-3, 8)$ . Find its equation
- 25) Find the angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of a tower of height  $10\sqrt{3}$  m
- 26) A ladder 15 metres long just reaches the top of a vertical wall. If the ladder makes an angle of  $60^\circ$  with the wall, find the height of the wall.
- 27) The volume of a solid right circular cone is  $11088 \text{ cm}^3$ . If its height is 24 cm then find the radius of the cone.
- 28) A die is rolled and a coin is tossed simultaneously. Find the probability that the die shows an odd number and the coin shows a head

ANSWER THE FOLLOWING ( Q. NO 42 IS COMPULSORY )

10 x 5 = 50

- 29) A company has four categories of employees given by Assistants (A), Clerks (C), Managers (M) and an Executive Officer (E). The company provide Rs.10,000, Rs.25,000, Rs.50,000 and Rs.1,00,000 as salaries to the people who work in the categories A, C, M and E respectively. If  $A_1, A_2, A_3, A_4$  and  $A_5$  were Assistants;  $C_1, C_2, C_3, C_4$  were Clerks;  $M_1, M_2, M_3$  were managers and  $E_1, E_2$  were Executive officers and if the relation R is defined by  $xRy$ , where x is the salary given to person y, express the relation R through an ordered pair and an arrow diagram.
- 30) Find x if  $gff(x) = fgg(x)$ , given  $f(x) = 3x+1$  and  $g(x)=x+3$ .
- 31) A mosaic is designed in the shape of an equilateral triangle, 12 ft on each side. Each tile in the mosaic is in the shape of an equilateral triangle of 12 inch side. The tiles are alternate in colour as shown in the figure. Find the number of tiles of each colour and total number of tiles in the mosaic.
- 32) Two A.P.'s have the same common difference. The first term of one A.P. is 2 and that of the other is 7. Show that the difference between their 10<sup>th</sup> terms is the same as the difference between their 21<sup>st</sup> terms, which is the same as the difference between any two corresponding terms.
- 33) Solve  $\sqrt{y+1} + \sqrt{2y-5} = 3$
- 34) Solve:  $\frac{1}{2x} + \frac{1}{4y} - \frac{1}{3z} = \frac{1}{4}$ ;  $\frac{1}{x} = \frac{1}{3y}$ ;  $\frac{1}{x} - \frac{1}{5y} + \frac{4}{z} = 2\frac{2}{15}$
- 35) A chess board contains 64 equal squares and the area of each square is  $625 \text{ cm}^2$ , A border round the board is 2 cm wide.
- 36) A girl looks the reflection of the top of the lamp post on the mirror which is 66 m away from the foot of the lamppost. The girl whose height is 12.5 m is standing 2.5 m away from the mirror. Assuming the mirror is placed on the ground facing the sky and the girl, mirror and the lamppost are in a same line, find the height of the lamp post.
- 37) Pythagoras Theorem?
- 38) The owner of a milk store finds that, he can sell 980 litres of milk each week at Rs.14 / litre and 1220 litres of milk each week at Rs. 16 / litre. Assuming a linear relationship between selling price and demand, how many litres could he sell weekly at Rs. 17 / litre?
- 39) if  $\frac{\cos\theta}{1+\sin\theta} = \frac{1}{a}$ , then prove that  $\frac{a^2-1}{a^2+1} = \sin\theta$
- 40) A funnel consists of a frustum of a cone attached to a cylindrical portion 12 cm long attached at the bottom. If the total height be 20 cm, diameter of the cylindrical portion be 12 cm and the diameter of the top of the funnel be 24 cm. Find the outer surface area of the funnel.

- 41) What is the ratio of the volume of a cylinder, a cone, and a sphere. If each has the same diameter and same height?
- 42) The time taken by 50 students to complete a 100 meter race are given below. Find its standard deviation.

Time taken(sec)	8 5-9.5	9.5-10.5	10.5-11.5	11.5-12.5	12.5-13 5
Number of students	6	8	17	10	9

ANSWER THE FOLLOWING

2x 8 = 16

- 43) a) Draw the graph of  $y = 2x^2 - 3x - 5$  and hence solve  $2x^2 - 4x - 6 = 0$

(OR)

- b) Graph the following quadratic equations and state their nature of solutions.

$$x^2 - 6x + 9 = 0$$

- 44) a) Draw  $\angle PQR$  such that  $PQ = 6.8$  cm, vertical angle is  $50^\circ$  and the bisector of the vertical angle meets the base at D where  $PD = 5.2$  cm.

(OR)

- b) The perpendicular from A on side BC at a  $\triangle ABC$  intersects BC at D such that  $DB = 3 CD$ . Prove that  $2AB^2 = 2AC^2 + BC^2$

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9944844528

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