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ANNUAL EVALUATION 2021-22

CLASS: 9 MATHEMATICS

1)

$\triangle ABC$, $\triangle ABD$, $\triangle ABE$ have equal area

$$2) a) \frac{1}{10} + \frac{2}{100} + \frac{3}{1000} = 0.1 + 0.02 + 0.003$$
$$= 0.123$$

$$b) 0.125 = \frac{1}{10} + \frac{2}{100} + \frac{5}{1000}$$

3) b) Here $BD = \sqrt{2}$

$$a) \text{Area of Square } BDEF = (\sqrt{2})^2$$
$$= 2 \text{ m}^2$$

$$4) \text{Here } \frac{AB}{BC} = \frac{PQ}{QR}$$

$$\frac{2}{3} = \frac{6}{QR}$$

$$\therefore QR = 6 \times \frac{3}{2}$$
$$= \underline{\underline{9 \text{ cm}}}$$

$$\text{Also, } \frac{BC}{CD} = \frac{QR}{RS}$$

$$\frac{3}{4} = \frac{9}{RS}$$

$$\therefore RS = 9 \times \frac{4}{3} = \underline{\underline{12 \text{ cm}}}$$

5) a) Perimeter = $4 \times \text{Side}$
 $= \underline{4a}$

b) Constant of proportionality = 4

6) a) We have, $BD:DC = AB:AC$
 $= 8:12$
 $= \underline{\underline{2:3}}$

b) We have,
 $\text{area}(\triangle ABD) : \text{area}(\triangle ADC) = BD:DC$
 $= \underline{\underline{2:3}}$

8) one table + one chair = 4000
 one table + 3 chairs = 6000

\therefore Cost of 2 chairs = $6000 - 4000$
 $= 2000$

\therefore Cost of 1 chair = $\frac{2000}{2}$
 $= \underline{\underline{1000 \text{ rupees}}}$

Since cost of one table + one chair = 4000

\therefore Cost of one table = $4000 - 1000$
 $= \underline{\underline{3000 \text{ rupees}}}$

7) Since smaller side = x

a) Longer side = $10 + x$

b) Perimeter of that larger rectangle = $4 \times \text{side}$
 $= 4(10 + x)$

9) a) Since perpendicular drawn from centre to a chord bisects the chord

$$\text{Since } PQ = 8\text{ cm}, PC = \frac{1}{2} \times 8 = 4\text{ cm}$$

b) OC bisects the longest chord AB

$$\text{also, } \angle AOC = \angle BOC$$

$$AP + PC = CQ + BQ$$

$$\therefore AP = BQ \quad (\because PC = CQ)$$

10) a) The line segment joining any 2 sides of a triangle is parallel to the third side and its length is equal to the half of the third side.

$$\therefore PR = \frac{1}{2} \times BC$$

$$= \frac{1}{2} \times 6$$

$$= \underline{\underline{3\text{ cm}}}$$

b) Perimeter of $\triangle PQR = \frac{1}{2} \times$ Perimeter of $\triangle ABC$

$$= \frac{1}{2} \times 18$$

$$= \underline{\underline{9\text{ cm}}}$$

11) a) $AC = 6, PR = 3$

$\therefore AC$ is 2 times PR

b) Here $\triangle ABC \sim \triangle RQP$

$$\therefore \frac{AB}{RQ} = \frac{BC}{QP} = \frac{AC}{RP}$$

$$\frac{8}{RQ} = \frac{4}{QP} = \frac{6}{3}$$

$$\therefore \frac{8}{RQ} = \frac{6}{3} \quad \therefore RQ = 8 \times \frac{1}{2} = 4$$

$$QP = \frac{1}{2} \times BC = \frac{1}{2} \times 6 = 3$$

12) radius (r) = 5 cm

$$\therefore \text{Perimeter} = 2\pi r$$

$$= 2\pi \times 5$$

$$= 10\pi$$

$$\approx 10 \times 3.14$$

$$\approx \underline{\underline{31.4 \text{ cm}}}$$

$$\text{Area} = \pi r^2$$

$$= \pi \times 5^2$$

$$= 25\pi$$

$$\approx 25 \times 3.14$$

$$\approx 78.5$$

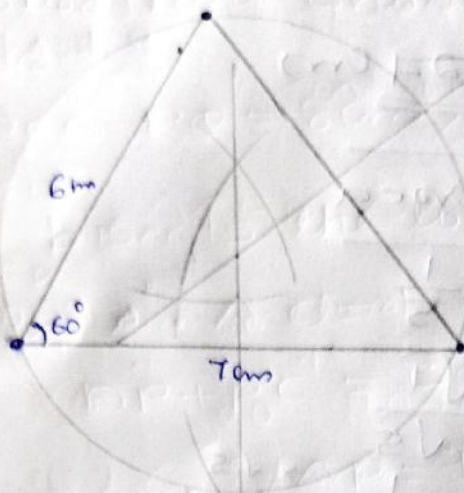
$$\approx \underline{\underline{78.5 \text{ cm}^2}}$$

13) a) Distance = 7 - 3

$$= \underline{\underline{4 \text{ units}}}$$

$$\text{b) mid point} = \frac{3+7}{2} = \frac{10}{2} = \underline{\underline{5}}$$

14)



15) Let the numbers be x, y

Given, $5x + 2y = 20 \rightarrow \textcircled{1} \times 3$

$2x + 6y = 34 \rightarrow \textcircled{2}$

$15x + 6y = 60 \rightarrow \textcircled{3}$

$\textcircled{3} - \textcircled{2} \Rightarrow 13x = 26$

$x = \frac{26}{13}$

$x = 2$

Substitute $x = 2$ in $\textcircled{1}$

$5(2) + 2y = 20$

$10 + 2y = 20$

$2y = 20 - 10$

$2y = 10$

$y = \frac{10}{2} = 5$

Two numbers are 2, 5

16)

$$\begin{aligned} \text{a) Side} &= \sqrt{5} \text{ cm} \\ &= \sqrt{5} \\ &\approx \underline{\underline{2.24 \text{ cm}}} \end{aligned}$$

$$\begin{aligned} \text{b) Side} &= \sqrt{\frac{1}{5}} \\ &= \sqrt{\frac{1}{5}} \\ &= \frac{\sqrt{1}}{\sqrt{5}} \\ &= \frac{1}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} \\ &= \frac{\sqrt{5}}{5} \\ &\approx \frac{2.24}{5} \\ &\approx \underline{\underline{0.448 \text{ cm}}} \end{aligned}$$

17)

$$\begin{aligned} \frac{1}{3} &= \frac{1}{10} \times \frac{10}{3} \\ &= \frac{1}{10} \left[3 + \frac{1}{3} \right] \\ &= \frac{3}{10} + \frac{1}{30} \end{aligned}$$

$$\frac{1}{3} - \frac{3}{10} = \frac{1}{30} \rightarrow \textcircled{1}$$

Similarly

$$\frac{1}{3} - \frac{33}{100} = \frac{1}{300} \rightarrow \textcircled{2}$$

$$\frac{1}{3} - \frac{333}{1000} = \frac{1}{3000} \rightarrow \textcircled{3}$$

$$\therefore a) \frac{1}{3} \approx \frac{3}{10}$$

$$\frac{1}{3} \approx \frac{33}{100}$$

$$\frac{1}{3} \approx \frac{333}{1000}$$

$$b) \frac{1}{3} = 0.3333 \dots$$

18)

a) Centroid divides each median in the ratio 2:1

$$\therefore AG:GD = 2:1$$

b) Also $BG:GE = 2:1$

$$\text{Since } GE = 3 \text{ cm} \therefore BG = 2 \times 3 = \underline{\underline{6 \text{ cm}}}$$

c) median divides triangle into 2 triangles of equal area.

$$\therefore \text{area of } \triangle ABD = \frac{1}{2} \times 60 = \underline{\underline{30 \text{ cm}^2}}$$

19)

a) Since $\triangle ABC \sim \triangle PQR$

$$\text{So we have } AB:PQ = AD:PS$$

$$10:20 = 8:PS$$

$$\therefore PS = \underline{\underline{16 \text{ cm}}}$$

D) Here Scale factor = 2
(K)

$$\begin{aligned}\therefore \text{Area of } \Delta PQR &= K^2 \times \text{area of } \Delta ABC \\ &= 2^2 \times 48 \\ &= 4 \times 48 \\ &= \underline{\underline{192 \text{ cm}^2}}\end{aligned}$$

20)

a) Given $2\pi r = 12\pi$
 $\therefore r = \underline{\underline{6 \text{ cm}}}$

$$\begin{aligned}\text{Area} &= \pi r^2 \\ &= \pi \times 6^2 \\ &= \underline{\underline{36\pi \text{ cm}^2}}\end{aligned}$$

b) Arc length = $2\pi r \times \frac{\alpha}{360}$
 $= 12\pi \times \frac{120}{360}$
 $= \underline{\underline{4\pi \text{ cm}}}$

21)

a) Given $|x| = 3 \therefore x = +3, -3$

b) $|x-1| = 3 \therefore x-1 = +3$ or $x-1 = -3$

$$\begin{array}{l|l} x = 3+1 & x = -3+1 \\ = \underline{\underline{4}} & = \underline{\underline{-2}} \end{array}$$

c) $|x-1| = |x-3|$

$$\therefore x = \frac{1+3}{2} = \frac{4}{2} = \underline{\underline{2}}$$

22) Given $l = 50\text{ cm}$, $b = 30\text{ cm}$, $h = 40\text{ cm}$

$$T.S.A = 2(lb + bh + lh)$$

$$= 2(50 \times 30 + 30 \times 40 + 50 \times 40)$$

$$= 2(1500 + 1200 + 2000)$$

$$= 2 \times 4700$$

$$= \underline{\underline{9400\text{ cm}^2}}$$

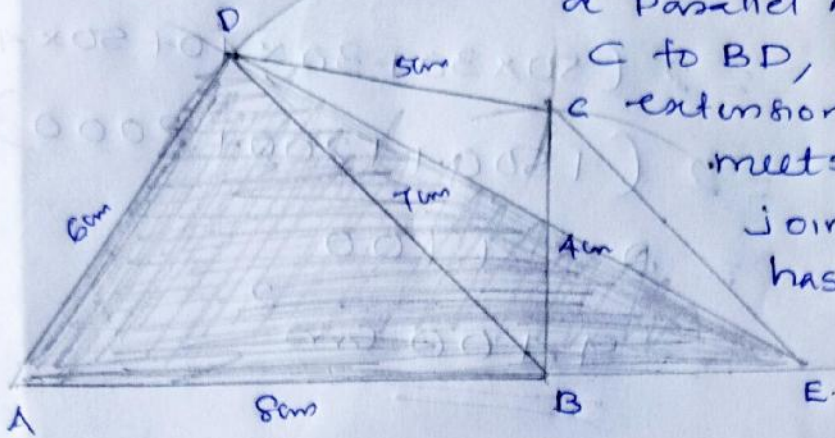
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Daily wages	Number	Total daily wages
500	3	$500 \times 3 = 1500$
600	7	$600 \times 7 = 4200$
700	10	$700 \times 10 = 7000$
900	8	$900 \times 8 = 7200$
1000	2	$1000 \times 2 = 2000$
TOTAL	30	21900

$$\text{Average daily wages} = \frac{21900}{30}$$

$$= \underline{\underline{730\text{ rupees}}}$$

24)



Draw the quad. ABCD
draw one diagonal BD
Extend AB, draw
a parallel line from
C to BD, so that the
extension of AB
meets it at E.

Joint DE, DAED
has the same area
as that of
quad. ABCD.

25) $\sqrt{32} = \sqrt{16 \times 2} = \sqrt{16} \times \sqrt{2} = \underline{4\sqrt{2}}$

a) $\sqrt{50} = \sqrt{25 \times 2} = \sqrt{25} \times \sqrt{2} = \underline{5\sqrt{2}}$

b) $\sqrt{50} + \sqrt{32} = 5\sqrt{2} + 4\sqrt{2} = \underline{9\sqrt{2}}$

c) $\sqrt{50} - \sqrt{32} = 5\sqrt{2} - 4\sqrt{2} = \underline{\sqrt{2}}$

26)

a) From ΔOCB ,

$$BC = \sqrt{5^2 - 3^2}$$

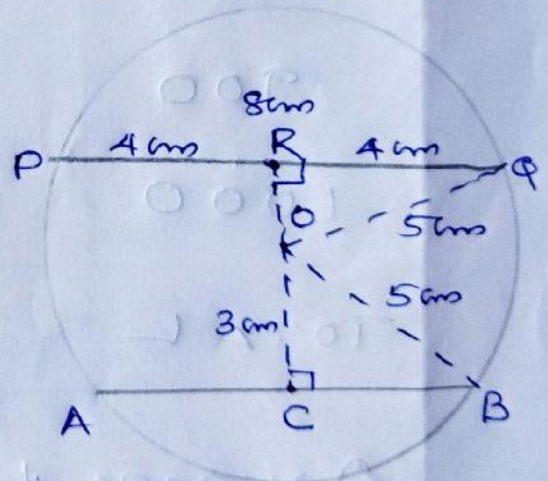
$$= \sqrt{25 - 9}$$

$$= \sqrt{16}$$

$$= 4 \text{ cm}$$

$AB = 4 \times 2 = \underline{8 \text{ cm}}$

b) From ΔORQ , $OR = \sqrt{5^2 - 4^2} = \sqrt{25 - 16}$
 $= \sqrt{9} = \underline{3 \text{ cm}}$



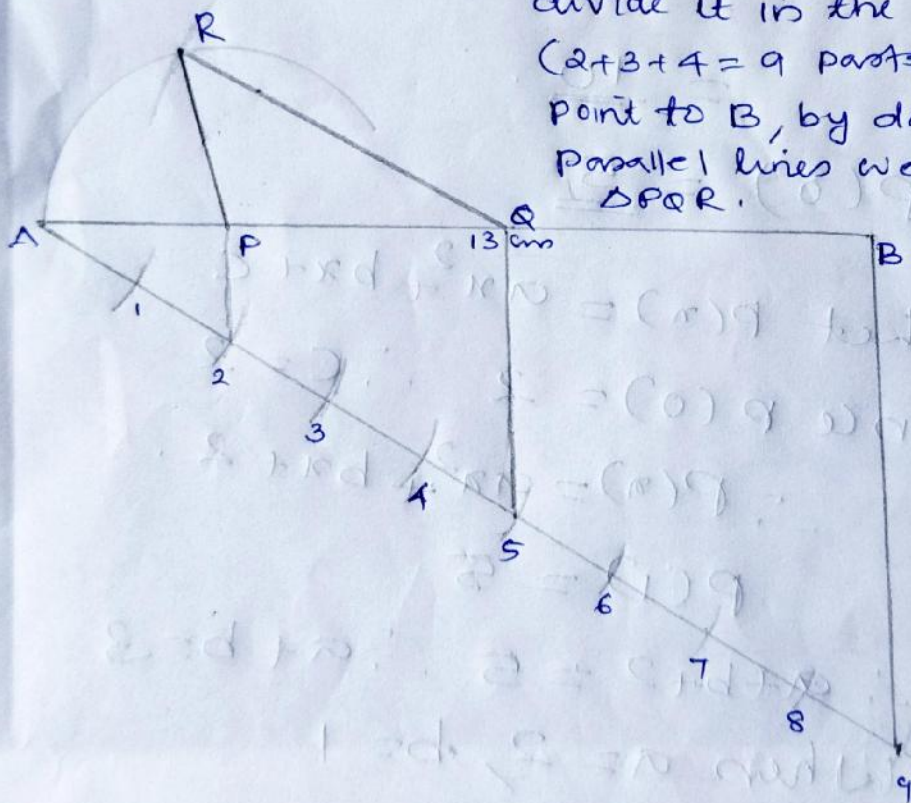
Distance of PQ from the Centre
 = 3 cm

c) Distance b/w AB & PQ
 = 3 + 3
 = 6 cm

[Here AB and PQ are of same length so they are equal distance from the Centre. In that way also we can solve this problem]

27)

First draw AB = 13 cm
 draw a slanted ray Ax
 divide it in the ratio 2:3:4
 (2+3+4 = 9 parts) join 9th
 point to B, by drawing the
 parallel lines we can complete
 ΔPQR.



$$28) d_1 : d_2 = r_1 : r_2$$

$$a) = \underline{\underline{3 : 4}}$$

$$b) P_1 : P_2 = r_1 : r_2$$

$$= \underline{\underline{3 : 4}}$$

$$c) A_1 : A_2 = r_1^2 : r_2^2$$

$$= \underline{\underline{9 : 16}}$$

$$29) P(x) = 2x^2 + 3x + 5$$

$$a) P(1) = 2(1)^2 + 3(1) + 5$$

$$= 2 + 3 + 5$$

$$= \underline{\underline{10}}$$

$$P(0) = \underline{\underline{5}}$$

$$b) \text{ Let } P(x) = ax^2 + bx + c$$

$$\text{ Since } P(0) = 2 \quad \therefore c = 2$$

$$\therefore P(x) = ax^2 + bx + 2$$

$$P(1) = 5$$

$$\therefore a + b + 2 = 5 \quad \therefore a + b = 3$$

$$\therefore \text{ When } a = 2, b = 1$$

$$\therefore P(x) = \underline{\underline{2x^2 + x + 2}}$$

$$V = \pi r^2 h.$$

$$= \pi \times 1 \times 1 \times 2$$

$$= \underline{\underline{2\pi \text{ m}^3}}$$

$$= 2\pi \times 1000 \text{ litres}$$

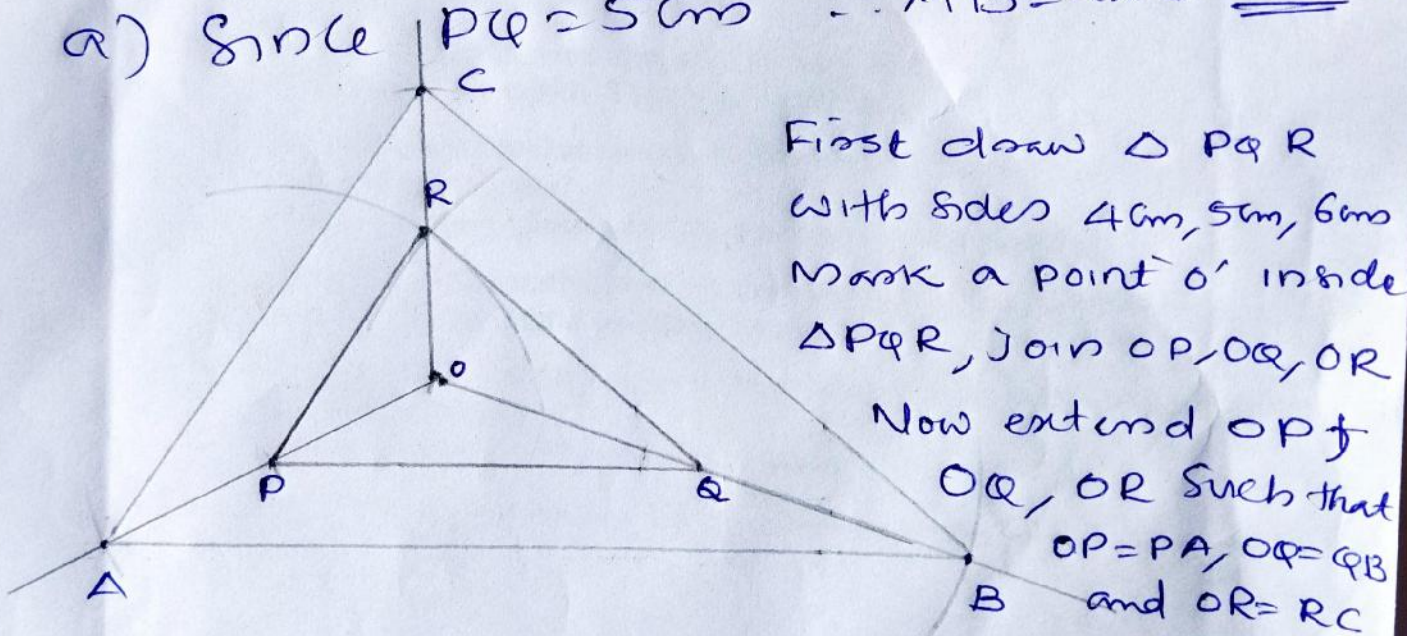
$$= 2000\pi \text{ litres}$$

$$\approx 2000 \times 3.14$$

$$\approx \underline{\underline{6280 \text{ litres.}}}$$

31) Here ratio of sides = $r_1 : r_2 = 1 : 2$

a) Since $PQ = 5 \text{ cm}$ $\therefore AB = 2 \times 5 = \underline{\underline{10 \text{ cm}}}$



First draw ΔPQR
with sides 4cm, 5cm, 6cm
Mark a point 'o' inside
 ΔPQR , Join OP, OQ, OR

Now extend OP to
 A , OQ to B , OR to C such that
 $OP = PA, OQ = QB$
and $OR = RC$

In that way we can compute the ΔABC .

32)

a) $3 \times 3 \times 3 = 3^3 = 27$

b) 3^4 times

c) 3 times

d) 3^5

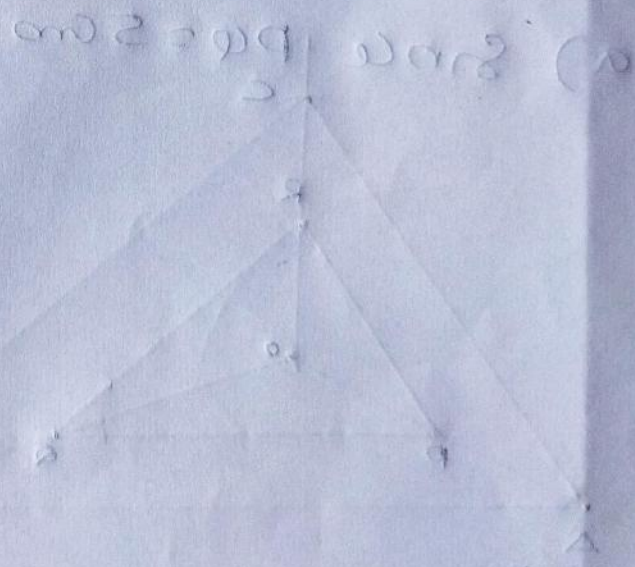
e) 3^{10}

f) 3^n

∴ Area of triangle = $\frac{1}{2} \times \text{base} \times \text{height}$

∴ Area of triangle = $\frac{1}{2} \times 8 \times 2 = 8 \text{ cm}^2$

First draw a line
with base 8 cm
Now a point is marked
at a height of 2 cm
Now connect the
corners of the
triangle to the
point at the
height of 2 cm



∴ Area of triangle = $\frac{1}{2} \times 8 \times 2 = 8 \text{ cm}^2$