

(d) passing through the point (0,11)

12) The slope of the line joining (12, 3), (4, a) is $\frac{1}{8}$. The value of 'a' is

(a) 1 (b) 4 (c) -5 (d) 2

13) (2, 1) is the point of intersection of two lines.

(a) x - y - 3 = 0; 3x - y - 7 = 0 (b) x + y = 3; 3x + y = 7 (c) 3x + y = 3; x + y = 7(d) x + 3y - 3 = 0; x - y - 7 = 014) The value of is $sin^2\theta + \frac{1}{1+tan^{2}\theta}$ equal to (a) $tan^2\theta$ (b) 1 (c) $cot^2\theta$ (d) 0 PART - B Answer any 10 questions Question No. 28 is compulsay 15) Find f o g and g o f when f(x) = 2x + 1 and $g(x) = x^2 - 2$ 16) Check whether the following sequences are in A.P. or not? x + 2, 2x + 3, 3x + 4, 17) Find he 19th term of an A.P. -11, -15, -19,.... 18) Find the first term of a G.P. in which S₆ = 4095 and r = 4 19) If the difference between the roots of the equation $x^2 - 13x + k = 0$ is 17. find k

20) If a, β are the roots of the equation $3x^2 + 7x - 2 = 0$, find the values of $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$

21) If a and β are the roots of $x^2 + 7x + 10 = 0$ find the values of $a^2 + \beta^2$

22) QA and PB are perpendiculars to AB. If AO = 10 cm, BO = 6 cm and PB = 9 cm. Find AQ.



23) Find the equation of a line through the given pair of points $(2, \frac{2}{3})$ and $(\frac{-1}{2}, 2)$

24) Show that the straight lines x - 2y + 3 = 0 and 6x + 3y + 8 = 0 are perpendicular.

25) What is the inclination of a line whose slope is 1

26) Show that the given vertices form a right angled triangle and check whether its satisfies Pythagoras theorem L(0, 5), M(9,12) and N(3,14)

 $14 \times 5 = 70$

27) prove that
$$\sqrt{\frac{1+\cos\theta}{1-\cos\theta}} = \operatorname{cosec} \theta + \cot\theta$$

28) prove the following identities

$$\sqrt{rac{1+sin heta}{1-sin heta}}+\sqrt{rac{1+sin heta}{1-sin heta}}=2sec heta$$

Answer any 10 questions. Question No. 42 is compulsay

29) If the function f: $R \rightarrow R$ defined by

$$f(x) = \begin{cases} 2x + 7, x < -2 \\ x^2 - 2, -2 \le x < 3 \\ 3x - 2, x \ge 3 \end{cases}$$
(i) f(4)
(ii) f(-2)
(iii) f(4) + 2f(1)
(iv) $\frac{f(1) - 3f(4)}{f(-2)}$

30) Find the sum to n terms of the series 5 + 55 + 555 + ...

31) Find the GCD of the polynomials $x^3 + x^2 - x + 2$ and $2x^3 - 5x^2 + 5x - 3$.

- 32) Find the square root of the following expressions $16x^2 + 9y^2 - 24xy + 24x - 18y + 9$
- 33) Find the square root of the expression $\frac{4x^2}{y^2} + \frac{20x}{y} + 13 \frac{30y}{x} + \frac{9y^2}{x^2}$
- 34) The roots of the equation $x^2 + 6x 4 = 0$ are a, β . Find the quadratic equation whose roots are

 α^2 and β^2

- 35) In trapezium ABCD, AB || DC, E and F are points on non-parallel sides AD and BC respectively, such that EF || AB. Show that AE $\frac{AE}{ED} = \frac{BF}{FC}$
- 36) In the figure, find the area of triangle AGF



- 37) If the points A(2, 2), B(-2, -3), C(1, -3) and D(x, y) form a parallelogram then find the value of x and y.
- 38) Find the equation of the median and altitude of Δ ABC through A where the vertices are A(6,

2), B(-5,-1) and C(1, 9)

- 39) Prove that $\sin^2 A\cos^2 B + \cos^2 A\sin^2 B + \cos^2 A\cos^2 B + \sin^2 A\sin^2 B=1$
- 40) if $\cos\theta + \sin\theta = \sqrt{2} \cos\theta$, then prove that $\cos\theta \sin\theta = \sqrt{2} \sin\theta$
- 41) If $\frac{\cos\alpha}{\cos\beta}$ = m and $\frac{\cos\alpha}{\sin\beta}$ = n, then prove that (m² + n²) cos² β = n²

42) if
$$\frac{\cos\theta}{1+\sin\theta} = \frac{1}{a}$$
, then prove that $\frac{a^2-1}{a^2+1} = \sin\theta$

Answer any one from 43 & 44 and any one from 45 & 46.

43) Varshika drew 6 circles with different sizes. Draw a graph for the relationship between the diameter and circumference of each circle as shown in the table and use it to find the circumference of a circle when its diameter is 6 cm.

Diameter (\mathbf{x}) cm	1	2	3	4	5
Circumference (\mathbf{y}) cm	3.1	6.2	9.3	12.4	15.5

- 44) A bus is travelling at a uniform speed of 50 km/hr. Draw the distance-time graph and hence find
 - (i) the constant of variation
 - (ii) how far will it travel in $\frac{1}{2}$
 - (iii) the time required to cover a distance of 300 km from the graph.
- 45) Construct a triangle similar to a given triangle PQR with its sides equal to $\frac{3}{5}$ of the corresponding sides of the triangle PQR (scale factor $\frac{3}{5} < 1$)
- 46) Construct a \triangle PQR which the base PQ = 4.5 cm, \angle R = 35° and the median RG R to PG is 6 cm



 $4 \times 8 = 32$

விளையாட்டுத்துறையும், கணிதத்துறையும் ஒன்று விடா முயற்சி+கடின பயிற்சி= வெற்றி HINDU HIGHER SECONDARY SCHOOL, ALWARTHIRUNAGARAI. 1() TIRUCHENDUR EDUCATION DISTRICT. Date : 08-Sep-22 **OUARTERLY MODEL EXAM 2022-2023** Maths Reg.No. : Time: 03:00:00 Hrs Total Marks : 100 PART - A $14 \times 1 = 14$ 1) (d) {0,1,2} 2) (a) Always true 3) (c) 1 4) (a) 0 5) (d) A is larger than B by 1 6) (b) 5 7) (c) -120, 100 8) (b) G.P 9) (c) $\angle B = \angle D$ 10) (a) 25:4 11) (b) parallel to Y axis 12) (d) 2 13) (b) x + y = 3; 3x + y = 714) (b) 1 PART - B $14 \times 2 = 28$ Answer any 10 quest ons. Question No. 28 is compulsay 15) $f(x) = 2x + 1, q(x) = x^2 - 2$ $f \circ q(x) = f(q(x)) = f(x^2 - 2) = 2(x^2 - 2) + 1 = 2x^2 - 3$ $g \circ f(x) = g(f(x)) = g(2x + 1) = (2x + 1)^2 - 2 = 4x^2 + 4x - 1$ Thus fog = $2x^2$ - 3, g of = $4x^2$ + 4x 1 From the above, we see that f og \neq g of 16) To check that the given sequence is in A.P., it is enough to check if the differences between the consecutive terms are equal or not. $t_2 - t_1 = (2x + 3) - (x - 2) = x + 1$

 $t_3 - t_1 = (3x + 4) - (2x + 3) = x + 1$ $t_2 - t_1 = t_3 - t_2$ Thus, the differences between consecutive terms are equal.

Hence the sequence x + 2, 2x + 3, 3x + 4,.... is in A.P

Given the A.P. - 11, - 15, - 19,.... Here First term a = -11Common difference $d = t_2 - t_1 = -15 - (-11)$ = -15 + 11 d = -4 n^{th} term of an A.P. is $t_n = a + (n - 1)d$ 19^{th} term $(t_{19}) = -11 + (19 - 1) (-4)$ = -11 + 18 (-4) = -11 + (-72) = -8319th term of -11, -15, -19, ... is - 83.

18)

Common ratio = 4 > 1, sum of first 6 terms S₆ = 4095 Hence , S₆ = $\frac{a(r^n-1)}{r-1}$ = 4095 Since, r = 4, $\frac{a(4^6-1)}{4-1}$ = 4095 gives a x $\frac{4095}{3}$ = 4095 First term a = 3.

19)

 $x^2 - 13x + k = 0$ here, a = 1, b = -13, c = kLet a, β be the roots of the equation. Then $a + \beta = \frac{-b}{a} = \frac{-(-13)}{1} = 13$ (1) also $a - \beta = 17$ (2) (1) + (2) we get, 2a = 30 gives a = 15Therefore, $15 + \beta = 13$ (from (1)) gives $\beta = -2$ But, $a\beta = \frac{c}{a} = \frac{k}{1}$ gives $15 \times (-2) = k$ we get, k = -30

20)

$$3x^{2} + 7x - 2 = 0 \text{ here, } a = 3, b = 7, c = -2$$

since, a, β are the roots of the equation
$$a + \beta = \frac{-b}{a} = \frac{-7}{3}, a\beta = \frac{c}{a} = \frac{-2}{3}$$
$$\frac{\alpha}{\beta} + \frac{\beta}{\alpha} = \frac{\alpha^{2} + \beta^{2}}{\alpha\beta} = \frac{(\alpha + \beta)^{2} - 2\alpha\beta}{\alpha\beta} = \frac{\left(\frac{-7}{3}\right)^{2} - 2\left(\frac{-2}{3}\right)}{\frac{-2}{3}} = \frac{-61}{6}$$

 $x^{2} + 7x + 10$ here, a = -1, b = 7, c = 10 if a and β are roots of the equation then, $a + β = \frac{-b}{a} = \frac{-7}{1} = -7$; $aβ = \frac{c}{a} = \frac{10}{1} = 10$ $a^{2} + β^{2} = (a + β)^{2} - 2aβ = (-7)^{2} - 2 \times 10 = 29$

22)

 $\Delta AOQ \text{ and } \Delta BOP, \angle OAQ = \angle OBP = 90^{0}$ $\angle AOQ = \angle BOP \text{ (Vertically opposite angles)}$ Therefore, by AA Criterion of similarity, $\Delta AOQ \sim \Delta BOP$ $\frac{AO}{BO} = \frac{OQ}{OP} = \frac{AQ}{BP}$ $\frac{10}{6} = \frac{AQ}{9} \text{ gives } AQ = \frac{10 \times 9}{6} = 15cm$ 23)

Given points $\left(2,\frac{2}{3}\right)$ and $\left(-\frac{1}{2},-2\right)$ Equation of the line passing through (x_1, y_1) and (x_1, y_1) $rac{y-y_1}{y_2-y_1}=rac{x-x_1}{x_2-x_1}$ $rac{y-rac{2}{3}}{-2-rac{2}{3}}=rac{x-2}{-rac{1}{2}-2}$ $\frac{3y-2}{-6-2} = \frac{2x-4}{-1-4}$ -5(3y - 2) = -8(2x - 4)-15y+10 = -16x + 3216x - 15y - 22 = 024) Show of the straight lines x - 2y + 3 = 0 is $m_1 = \frac{-1}{-2} = \frac{1}{2}$ Slope of the straight line 6x + 3y + 8 = 0 is $m_2 = \frac{-6}{3} = -2$ Now, $m_1 \ge m_2 = \frac{1}{2} \ge (-2) = -1$ Hence, the two straight lines are perpendicular 25) Slope 'm' = 1 $\tan\theta = 1 = \tan 45^{\circ}$ $\theta = 45^0$ 26) L (0, 9), M (9,12) and N (3, 14) Slope of a line = $\frac{y_1 - y_2}{x_1 - x_2}$ Slope of LM = $\frac{5 - 12}{0 - 9} = \frac{-7}{-9} = \frac{7}{9}$ Slope of MN = $\frac{12 - 14}{9 - 3} = \frac{-2}{6} = \frac{-1}{3}$ Slope of LN = $\frac{5 - 14}{0 - 3} = \frac{-9}{-3} = 3$ (Slope of MN) x (slope of LN) = $\left(-\frac{1}{3}\right) \times 3 = -1$ MN is perpendicular to LN. Hence, the given vertices form a right angled triangle Distance formula = $\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ $LM = \sqrt{(0-9)^2 + (5-12)^2} = \sqrt{81+49} = \sqrt{130}$ $LM^2 = 130$ $MN = \sqrt{(9-3)^2 + (12-14)^2} = \sqrt{36+4} = \sqrt{40}$ $MN^2 = 40$ $LN = \sqrt{(0-3)^2 + (5-14)^2} = \sqrt{9+81} = \sqrt{90}$ $LN^{2} = 90$ $LN^2 + MN^2 = LM^2$ Hence, the Pythagoras theorem is satisfied. 27) $\sqrt{\frac{1+\cos\theta}{1-\cos\theta}} = \sqrt{\frac{1+\cos\theta}{1-\cos\theta}} \times \frac{1+\cos\theta}{1+\cos\theta}$ [multiply numerator and denominator by the conjugate of 1 -COSA1

$$= \sqrt{\frac{(1+\cos\theta)^2}{(1-\cos\theta)^2}} = \frac{1+\cos\theta}{\sqrt{\sin^2\theta}} \text{ [since } \sin_2\theta + \cos_2\theta = 1\text{]}$$
$$= \frac{1+\cos\theta}{\sin\theta} = \csc\theta + \cot\theta$$

$$egin{aligned} &\sqrt{rac{1+\sin heta}{1-\sin heta}} = \sec heta + an heta \ \mathbf{LHS} = \sqrt{rac{1+\sin heta}{1-\sin heta}} \ &= \sqrt{rac{1+\sin heta}{1-\sin heta}} imes rac{1-\sin heta}{1-\sin heta} \end{aligned}$$

[Multiplying the Numerator and denominator by $\sqrt{1-\sin\theta}$]

$$= \sqrt{\frac{1^2 - \sin^2 \theta}{(1 - \sin \theta)^2}} \quad [\because (a + b)(a - b) = a^2 - b^2]$$

$$= \sqrt{\frac{\cos^2 \theta}{(1 - \sin \theta)^2}} \quad [\because 1 - \sin^2 \theta = \cos^2 \theta]$$

$$= \frac{\cos \theta}{1 - \sin \theta}$$

$$= \frac{\cos \theta}{1 - \sin \theta} \times \frac{1 + \sin \theta}{1 + \sin \theta}$$
[Multiplying Numerator and denominator by $1 + \sin \theta$]

$$= \frac{\cos \theta (1+\sin \theta)}{1^2 - \sin^2 \theta} = \frac{\cos \theta (1+\sin \theta)}{\cos^2 \theta}$$

[:: $(a+b)(a-b) = a^2 - b^2$] $[1 - \sin^2 \theta = \cos^2 \theta]$
= $\frac{1+\sin \theta}{\cos \theta} = \frac{1}{\cos \theta} + \frac{\sin \theta}{\cos \theta}$
= $\sec \theta + \tan \theta = \text{RHS}$

PART - C

Answer any 10 questions. Question No. 42 is compulsay

29)

The function f is defined by three values in intervals I, II, III as shown by the side.

For a given value of x = a, find out the interval at which the point a is located, there after find

 $14 \times 5 = 70$

f(a) using the particular value defined in that interval.

(i) First, we see that, x = 4 lie in the third interval.

Therefore, f(x) = 3x - 2; f(4) = 3(4) = 10

(ii) x = -2 lies in the second interval

Therefore,
$$f(x) = x^2 - 2$$
; $f(-2) = (-2)^2 - 2 = 2$

(iii) From (i), f(4) =10.

To find f(1) first we see that x = 1 lies in the second interval.

Therefore, $f(x) = x^2 - 2 \Rightarrow f(1) = 1^2 - 2 = -1$

So, f(4) + 2f(1) = 10 + 2(-1) = 8

(iv) We know that f(1) = -1 and f(4) = 10

For finding f(-3), we see that x = -3, lies in the first interval.

Therefore, f(x) = 2x + 7; thus, f(-3) = 2(-3) + 7 = 1Hence, $\frac{f(1)-3f(4)}{f(-3)} = \frac{-2-3(10)}{1} = -31$ $\frac{1}{X'-6} + \frac{1}{-5} + \frac{1}{-4} + \frac{1}{-3} + \frac{1}{-2} + \frac{1}{-1} + \frac{1}{-2} + \frac{1}{-3} + \frac{1}{-5} + \frac{1}{-$

30)

The series is neither Arithmetic nor Geometric series. So it can be split into two series and then find the sum.

$$5 + 55 + 555 + \dots + n \text{ terms} = 5 [1 + 11 + 111 + \dots n \text{ terms}]$$

= $\frac{5}{9} [9 + 99 + 999 + \dots + n \text{ terms}]$
= $\frac{5}{9} [(10 - 1) + (100 - 1) + (1000 - 1) + \dots + n \text{ terms}]$
= $\frac{5}{9} [10 + 100 + 1000 + \dots + n \text{ terms}) - n]$
= $\frac{5}{9} [\frac{10(10^n - 1)}{(10 - 1)} - n] = \frac{50(10^n - 1)}{81} = \frac{5n}{9}$

31)

Let
$$f(x) = 2x^3 - 5x^2 + 5x - 3$$
 and $g(x) = x^3 + x^2 - x + 2$

$$x^{3} + x^{2} - x + 2 \boxed{2x^{3} - 5x^{2} + 5x - 3}_{2x^{3} + 2x^{2} - 2x + 4} (-)$$
$$\boxed{-7x^{2} + 7x - 7}_{= -7(x^{2} - x + 1)}$$

 $-7(x^2 - x + 1) \neq 0$, note that -7 is not a divisor of g(x)

Now dividing, $g(x) = x^3 + x^2 - x + 2$ by the new remainder $x^2 - x + 1$ (leaving the constant factor), we get

$$\begin{array}{c}
x + 2 \\
x^{2} - x + 1 \\
x^{3} + x^{2} - x + 2 \\
x^{3} - x^{2} + x \\
2x^{2} - 2x + 2 \\
2x^{2} - 2x + 2 \\
0
\end{array} (-)$$

Here, we get zero remainder

Therefore, GCD $(2x^3 - 5x^2 + 5x - 3, x^3 + x^2 - x + 2) = x^2 - x + 1$.

32)

$$\sqrt{16x^2 + 9y^2 - 24xy + 24x - 18y + 9}$$

= $\sqrt{(4x)^2 + (-3y)^2 + (3)^2 + 2(4x)(-3y) + 2(-3y)(3) + 2(4x)(3)}$
= $\sqrt{(4x + -3y + 3)^2} = |4x - 3y + 3|$

33)

$$\frac{\frac{2x}{y} + 5 - \frac{3y}{x}}{\frac{2x}{y}} = \frac{\frac{4x^2}{y^2} + \frac{20x}{y} + 13 - \frac{30y}{x} + \frac{9y^2}{x^2}}{\frac{4x^2}{y^2}} = \left(-\right)$$

$$\frac{\frac{4x}{y} + 5}{\frac{\frac{20x}{y} + 13}{\frac{20x}{y} + 25}} = \left(-\right)$$

$$\frac{\frac{4x}{y} + 10 - \frac{3y}{x}}{\frac{-12 - \frac{30y}{x} + \frac{9y^2}{x^2}}{0}} = \left(-\right)$$
Hence $\sqrt{\frac{4x^2}{y^2} + \frac{20x}{y} + 13 - \frac{30y}{x} + \frac{9y^2}{x^2}}{0}} = \left(\frac{2x}{y} + 5 - \frac{3y}{x}\right)$
34)

If the roots are given, the quadratic equation is X^2 - (sum of the roots) x + product the roots =0. For the given equation.

$$x^{2} - 6x - 4 = 0$$

 $α + β = -6$
 $αβ = -4$
 $α^{2} + β^{2} = (α + β)^{2} - 2αβ$
 $= (-6)^{2} - 2(-4) = 36 + 8 = 44$
 $α^{2}β^{2} = (αβ)^{2} = (-4)2 = 16$
∴ The requird equation = $x^{2} - 44x + 16 = 0$

35)



G ven: ABCD is a trapezium in which DC II AB and EF II AB To prove that $\frac{AE}{ED} = \frac{BF}{FC}$ Construction : join AC meeting EF at G Proof: In ADC, we have EG II DC $\Rightarrow \frac{AE}{ED} = \frac{AG}{GC}$ [By thales theorem](1) In ABC , we have $\frac{AG}{GC} = \frac{BF}{FC}$ [Bv thales theorem](2) From (1) and (2), we get $\frac{AE}{ED} = \frac{BF}{FC}$

36)

Area of triangle AGF

Vertices A (- 5,3), G (- 4.5,0.5) and F (- 2,3). Area of triangle = $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ sq. units = $\frac{1}{2}[-5(0.5 - 3) - 4.5(3 - 3) - 2(3 - 0.5)]$ = $\frac{1}{2}[12.5 - 5] = \frac{7.5}{2} = 3.75$ sq. units 37)

Given points A (2, 2), B (- 2,- 3), C (1, - 3) and D (x, y)

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Slope of a line = \frac{y_1 - y_2}{x_1 - x_2}
Slope of AB = \frac{2+3}{2+2} = \frac{5}{4}
Slope of BC = \frac{-3+3}{-2-1} = 0
Slope of CD = -\frac{-3-y}{1-x}
Slope of AD = \frac{2-y}{2-x}
     Since, the points form a parallelogram
    AB is parallel to CD and BC is parallel to AD
     Slope of AB = Slope of CD
     \frac{5}{4} = \frac{-3-y}{1-x}
    5(1 - x) = 4(-3 - y)
     5 - 5x = -12 - 4y
    5x - 4y = 17
    Slope of BC = Slope of AD
    0 = rac{2-y}{2-x}
    2 - y = 0
    y = 2
    Substituting in (1)
    5x - 4(2) = 17
    5x = 17 + 8 = 25
    x = \frac{25}{5} = 5
    x = 5, y = 2
38)
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Given vertices are A (6, 2), B (- 5, - 1) and C (1, 9) Median through A : Let D be the mid point of BC Mid point of BC $= D\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$ $= D\left(\frac{-5+1}{2}, \frac{-1+9}{2}\right)$ = D(-2, 4)Now AD is the median. Equation of AD $\frac{y-y_1}{y_2-y_1} = \frac{x-x_1}{x_2-x_1}$ $\frac{\frac{y-2}{4-2}}{\frac{y-2}{2}} = \frac{x-6}{-2-6}$ $\frac{y-2}{2} = \frac{x-6}{-8}$ -4y + 8 = x - 6x + 4y - 14 = 0Altitude through A Altitude is passing through 'A and perpendicular to BC. Now, Slope of BC = $\frac{y_1 - y_2}{x_1 - x_2} = \frac{-1 - 9}{-5 - 1} = \frac{-10}{-6} = \frac{5}{3}$ Slope of Altitude = $-\frac{3}{5}$ Equation of the altitude which is passing through A (6,2) and having slope $-\frac{3}{5}$ is $y - y_1 = m(x - x_1)$ $y-2 = -\frac{3}{5}(x-6)$ 5y-10 = -3x + 183x + 5y - 28 = 039) $sin^2 Acos^2 B + cos^2 Asin^2 B + cos^2 A + cos^2 B + sin^2 Asin^2 B$ = sin² Acos² B + sin² Asin² B + cos² A + cos² B + sin²Asin² B $= \sin^2 A(\cos^2 B + \sin^2 B) + \cos^2 A(\sin^2 B + \cos^2 B)$ $= \sin^2 A(1) + \cos^2 A(1)$ (since $\sin^2 B + \cos^2 B = 1$) = sin² A + cos² A = 1 40)

Now, $\cos\theta + \sin\theta = \sqrt{2} \cos\theta$ Squaring both sides, $(\cos\theta + \sin\theta)^2 = (\sqrt{2} \cos\theta)^2$ $\cos^2\theta + \sin^2\theta + 2\sin\theta\cos\theta = 2\cos^2\theta$ $2\cos^2\theta - \cos^2\theta - \sin^2\theta = 2\sin\theta\cos\theta$ $\cos^2\theta - \sin^2\theta = 2\sin\theta\cos\theta$ $(\cos\theta + \sin\theta)(\cos\theta + \sin\theta) = 2\sin\theta\cos\theta$ $\cos\theta - \sin\theta = \frac{2\sin\theta\cos\theta}{\cos\theta + \sin\theta} = \frac{2\sin\theta\cos\theta}{\sqrt{2}\cos\theta}$ [since $\cos\theta + \sin\theta = \sqrt{2} \cos\theta$] $= \sqrt{2} \cos\theta$ Therefore $\cos\theta - \sin\theta = \sqrt{2} \cos\theta$

41)

Given

$$\begin{aligned} \frac{\cos \alpha}{\cos \beta} &= m\\ \frac{\cos \alpha}{\sin \beta} &= n\\ \text{LHS} &= \left(m^2 + n^2\right)\cos^2 \beta\\ &= \left(\frac{\cos^2 \alpha}{\cos^2 \beta} + \frac{\cos^2 \alpha}{\sin^2 \beta}\right)\cos^2 \beta\\ &= \frac{\left(\cos^2 \alpha \sin^2 \beta + \cos^2 \alpha \cos^2 \beta\right)}{\cos^2 \beta \sin^2 \beta}\cos^2 \beta\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\cos^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &= \frac{\cos^2 \alpha (\sin^2 \beta + \cos^2 \beta)}{\sin^2 \beta}\\ &=$$

Given
$$\frac{\cos \theta}{1+\sin \theta} = \frac{1}{a}$$

 $\therefore a = \frac{1+\sin \theta}{\cos \theta}$
LHS $= \frac{a^2-1}{a^2+1}$
 $= \frac{\left(\frac{1+\sin \theta}{\cos \theta}\right)^2 - 1}{\left(\frac{1+\sin \theta}{\cos \theta}\right)^2 + 1}$
 $= \frac{\frac{1^2+\sin^2 \theta + 2\sin \theta}{\cos^2 \theta} - 1}{\frac{1^2+\sin^2 \theta + 2\sin \theta}{\cos^2 \theta}}$
 $= \frac{\frac{1+\sin^2 \theta + 2\sin \theta - \cos^2 \theta}{\cos^2 \theta}}{\frac{1+\sin^2 \theta + 2\sin \theta}{\cos^2 \theta}} \times \frac{\cos^2 \theta}{1+(\sin^2 \theta + \cos^2 \theta) + 2\sin \theta}$
 $= \frac{\sin^2 \theta + \sin^2 \theta + 2\sin \theta}{1+1+2\sin \theta}$
 $= \frac{2\sin^2 \theta + 2\sin \theta}{2+2\sin \theta}$
 $= \frac{2\sin^2 \theta + 2\sin \theta}{2+2\sin \theta}$
 $= \frac{2\sin \theta(\sin \theta + 1)}{2(1+\sin \theta)}$
 $= \sin \theta = RHS$

Answer any one from 43 & 44 and any one from 45 & 46.

 $4 \times 8 = 32$

43)



From the table, we found that as x increses, y also increases. Thus the variation is a direct variation.

Let y = kx, where k is a constant of proportionality.

From the given values, we have

 $k = rac{3.1}{1} = rac{6.2}{2} = rac{9.3}{3} = rac{12.4}{4} = \ldots = 3.1$

When you plot the points (1, 3.1) (2, 6.2) (3, 9.3), (4, 12.4), (5, 15.5), you find the relation y = (3.1)x forms a straight-line graph.

Clearly, from the graph, when diameter is 6 cm, its circumference is 18.6 cm.

44)



Let x be the time taken in minutes and y be the distance travelled in km

$\begin{array}{ c c }\hline \text{Time taken } \mathbf{x} \text{ (in minutes)} \end{array}$	60	120	180	240
Distance \mathbf{y} (in km)	50	100	150	200

(i) Observe that as time increases, the distance travelled also increases. Therefore, the variation is a direct variation. It is of the form y = kx.

Constant of variation

 $k = \frac{y}{x} = \frac{50}{60} = \frac{100}{120} = \frac{150}{180} = \frac{200}{240} = \frac{5}{6}$

Hence, the relation may be given as

 $y = kx \Rightarrow y = rac{5}{6}x$

(ii) From the graph, $y=rac{5x}{6},$ if x = 90 , then $y=rac{5}{6} imes 90=75~{
m km}$

The distance travelled for $1\frac{1}{2}$ hours (i.e.,) 90 minutes is 75 km.

(iii) From the graph, $y = \frac{5x}{6}$, if y = 300 then $x = \frac{6y}{5} = \frac{6}{5} \times 300 = 360$ minutes (or) 6 hours.

The time taken to cover 300 km is 360 minutes, that is 6 hours.

Given a triangle PQR we are required to construct another triangle whose sides are $\frac{3}{5}$ of the corresponding sides of the triangle PQR.



Steps of construction

1.Construct a riangle PQR with any measurement

2. Draw a ray QX making an acute angle with QR on the side opposite to vertex P.

3. Locate 5 (the greater of 3 and 5 in $\frac{3}{5}$) points.

 $Q_1Q_2,\,Q_3,\,Q_4$ and Q_5 on QX so that QQ_1 = Q_1Q_2 = Q $\,Q_3$ = Q_4Q_5

4. Join Q₅R and draw a line through Q₃ (the third point, 3 being smaller of 3 and 5 in $\frac{3}{5}$) parallael to Q₅R to intersect QR at R

5 Draw line through R' pa allel to the line RP to intersect QP at P'.

Then, $\triangle P'QR'$ is the required triangle each of whose sides is three fifths of the corresponding sides of \triangle PQR.

46)



Construction:

Step (1) Draw a line segment PQ = 4.5 cm

Step (2) At P, draw PE such that $\angle QPE = 35^{0}$

Step (3) At P, draw PF such that $\angle EPF = 90^{\circ}$

Step (4) Draw \perp bisector to PQ which intersects PF at O.

Step (5) With O centre OP as raidus draw a circle.

Step (6) From G, marked arcs of radius 6 cm on the circle marked them as R and S.

Step (7) foined PR and RQ. Then \triangle PQR is the required triangle

Step (8) \triangle PQS is the required triangle

