

END-TERM EXAMINATION  
SECOND SEMESTER [MCA] – MAY-JUNE 2006  
THEORY OF COMPUTATION

MCA-104  
Time: 3 Hours  
Marks: 60

Q. 1

- (a) Draw a finite automata that accepts sets of strings composed of zeros and ones which end with string 00.
- (b) Define an inherently ambiguous language. Give an example of such language.
- (c) Give a recursive formula for addition of two positive numbers using initial functions like zero, identify and successor functions. Hence show that addition of two positive numbers is computable.
- (d) Show that if M1 is a Moore machine then there exists a corresponding Mealy machine.
- (e) Draw a NFA with three states that accepts  $L = \{a^n : n \geq 1\} \cup \{b^k a^m : k \geq 0, m \geq 0\}$ .  
(4 x 5 = 20)

Q. 2

- (a) Show that the set of all strings in  $\{0, 1\}$  such that every third symbol is the same as the first symbol is a regular language.
- (b) Construct a context free grammar for the language  $L = \{w \mid w \in \{0, 1\}^*, |w| \text{ is odd and } w \text{ contains } 0 \text{ in the middle of the string}\}$ .  
(5, 5)

Q. 3 Convert the following Context Free Grammar into GNF.

$S \rightarrow bA$   
 $S \rightarrow aB$   
 $A \rightarrow bAA$   
 $A \rightarrow aS$   
 $A \rightarrow a$   
 $B \rightarrow aBB$   
 $B \rightarrow bS$   
 $B \rightarrow b'$

Q. 4

(a) Draw a Push Down Automata with minimum number of pushdown stores of the language  $\{wcwR \mid w \in \{0, 1\}^*\}$ . Here  $wR$  is reverse string of  $w$ .

(b) Give a matrix grammar for the above language. (7, 3)

Q. 5

(a) Define a Turing machine. Draw a Turing Machine that adds two positive integers.

(b) State and prove the pumping lemma for CFL. (5, 5)

Q. 6

(a) Define Derivation Tree. Is it possible to draw a derivation tree for a string derived from context sensitive grammar? Give reasons for your answer. (5, 5)

(b) Let '10011010011' is a symbol sequence. Apply the following prioritized Markov rules to convert the sequence such that all symbols following the pattern '1101' should be '0'.

(1)  $a0 \rightarrow 0a$

(2)  $a1 \rightarrow 0a$

(3)  $a \rightarrow$

(4)  $1101 \rightarrow 1101a$

(5)  $\rightarrow$

Q. 7 Write short notes on any two of the following:- (5, 5)

(a) L –System of grammar

(b) Partial recursive function

(c) Unsolvable class or problem.