

Pre-foundation Career Care Programmes (PCCP) Division

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1. Given : AB is diameter  $\angle CAB = 30^{\circ}$ To find ∠PCA construction : Join OC sol : ∴ In ∆AOC as AO = OC $\therefore \angle OAC = \angle OCA = 30^{\circ}$  $\angle OCP = 90^{\circ}$  [Radius make an angle of 90° with tangent at point of contact]  $\therefore \angle PCA + \angle OCA = 90^{\circ}$  $\therefore \angle PCA + 30^\circ = 90^\circ$  $\therefore \angle PCA = 60^{\circ}$ 2. k + 9, 2k - 1 and 2k + 7 are in A.P.  $\therefore a_2 - a_1 = a_3 - a_2$ [where a<sub>1</sub>, a<sub>2</sub> and a<sub>3</sub> are the 1<sup>st</sup>, 2<sup>nd</sup> and 3<sup>rd</sup> term of the A.P.] 2k - 1 - k - 9 = 2k + 7 - 2k + 1k - 10 = 8k = 18 3. In ∆ABC  $\cos 60^\circ = \frac{BC}{AC}$  $\frac{1}{2} = \frac{2.5}{AC}$ 2.5  $AC = 2.5 \times 2$ AC = 5 m: length of the ladder is 5 m 4. We have to draw a card from 52 playing cards so the total event of drawing a card is = 52 and the event of getting red card and queen is = 26 + 2 = 28Acc to question The probability of getting  $= P(\overline{A}) = 1 - P(A)$ neither red card nor a queen  $= P(\overline{A}) = 1 - \frac{28}{52} = \frac{6}{13}$ Let -5,  $\alpha$  be the roots of  $2x^2 + px - 15 = 0$ 5. so sum of roots =  $-5 + \alpha = -\frac{P}{2}$ and product of roots =  $-5 \times \alpha = \frac{-15}{2}$  $\therefore \alpha = \frac{3}{2}$ If  $\alpha = 3/2$  then P = 7and  $P(x^2 + x) + k = 0$  have equal roots so D = 0 $\Rightarrow P^2 - 4Pk = 0$  $\Rightarrow P(P - 4k) = 0$ P = 0 & P - 4k = 0so 4k = p $k = \frac{P}{4} = \frac{7}{4}$ lesonance® SOLUTION\_10th CBSE(BOARD)\_SUMMATIVE ASSESSMENT-II\_MATHS\_PAGE #1

6. 
$$x_{1} = \frac{(2 \times 7) + (1 \times 2)}{2 + 1}$$

$$x_{1} = \frac{-14 + 2}{3} = \frac{-12}{3} = -4$$

$$y_{1} = \frac{(2 \times 4) + (1 \times -2)}{2 + 1} = \frac{8 - 2}{3} = \frac{6}{3} = 2$$

$$(x, y) = (-4, 2) \text{ coordinates of } Q.$$

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$$(x, y) =$$

angle isosceles triangle.

a and d respectively.

 $a_4 = a + (4-1) d = 0$  $a_4 = a + 3d = 0$ a + 3d = 0∴ a =–3d ..... (1)

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equal

 $a_{25} = a + (25-1) d$  $a_{25} = a + 24 d$ By equation .....(1)  $a_{25} = -3d + 24d$  $a_{25} = 21 d$  $a_{11}^{-1} = a + (11-1) d$  $a_{11} = a + 10d$ By equation .....(1)  $a_{11} = -3d + 10d$  $\therefore a_{11} = 7d$ multiply both sides by 3  $3a_{11} = 21d$  $\therefore$   $3a_{11} = a_{25}$  Hence proved 10. In ∆OTP OT = r, OP = 2r [Given]  $\angle$  OTP = 90° [radius is perpendicular to tangent at the pair of contact] Let  $\angle TPO = \theta$  $\therefore \sin\theta = \frac{OT}{OP} = \frac{r}{2r} = \frac{1}{2}$ C.  $\therefore \theta = 30^{\circ}$  $\therefore$  In  $\triangle$ TOP  $\angle$ TOP = 60° [By angle sum property]  $\angle$  TOP =  $\angle$  SOP [As  $\triangle$ 's are congruent]  $\therefore \angle$  SOP is also 60°  $\therefore \angle \text{TOS} = 120^\circ \text{ In } \triangle \text{OTS} \text{ as } \text{OT} = \text{OS} \therefore [\angle \text{OST} = \angle \text{OTS}]$  $\angle \text{OTS} + \angle \text{OST} + \angle \text{SOT} = 180 \Rightarrow 2 \angle \text{OST} + 120 = 180^{\circ}$  $\therefore \angle \text{OTS} + \angle \text{OST} = 30^{\circ}$  $AB^2 = BC^2 + AC^2$ 11.  $\Rightarrow$  169 = BC<sup>2</sup> + 144  $25 = BC^{2}$ BC = 513cm Area of shaded region = Area of semicircle – Area of ∆ABC  $=\frac{\pi r^2}{2}-\frac{1}{2} \times BC \times AC$ B  $= \frac{1}{2} [3.14 \times \frac{13}{2} \times \frac{13}{2}] - (5 \times 12)$  $=\frac{1}{2}(132.665-60)$ = 36.3325 cm<sup>2</sup> 2.8 m 12. Total CSA of tent  $= 2\pi rh + \pi rl$  $= \frac{22}{7} \left[ \left( 2 \times \frac{3}{2} \times 2.1 \right) + \left( \frac{3}{2} \times 1.4 \right) \right]$  $\Rightarrow \frac{22}{7} \times 10.5 = 33 \text{ m}^2$ 2.1 m Total CSA oftent = 33 m<sup>2</sup> 1 m<sup>2</sup> cost  $\rightarrow$  Rs. 500  $33 \text{ m}^2 \text{ cost} \rightarrow \text{Rs.} 500 \times 33 = 16500 \text{ Rs}$ So total cost of canvas needed to make the text is Rs 16500 3 m

13. Given : Coordinates of P(x,y)P(x,y)A(a + b, b - a)B(a - b, a + b)To prove = bx = ayAccording to question PA = PB $(PA)^2 = (PB)^2$ A(a + b, b - a)B(a - b, a + b)so accoding to distance formula  $[x - (a + b)]^2 + [y - (b - a)]^2 = [(x - (a - b)]^2 + [y - (a + b)]^2$  $(a + b)^2 - 2(a + b)x + (b - a)^2 - 2(b - a)y = (a - b)^2 - 2(a - b)x + (a + b)^2 - 2(a + b)y$ 2[(a + b)x + (b - a)y] = 2[(a - b)x + (a + b)y](a + b)x + (b - a)y = (a - b)x + (a + b)y(a + b)x - (a - b)x = (a + b)y - (b - a)y(a + b - a + b)x = (a + b - b + a)y2bx = 2aybx = ay hence prove



14.

Shaded area = Area of larger major sector - area of smaller major sector

$$= \pi (14)^2 \times \frac{40}{360} - \pi (7)^2 \left(\frac{40}{360}\right)$$

$$= \pi \times \frac{40}{360} (14^2 - 7^2)$$

$$= \frac{22}{7} \times \frac{1}{9} (147) = 51.3 \text{ cm}^2$$
15. 
$$\frac{\frac{n}{2} [2a_1 + (n-1)d_1]}{\frac{n}{2} [2a_2 + (n-1)d_2]} = \frac{7n+1}{4n+27}$$

$$\frac{2a_1 + (n-1)d_1}{2a_2 + (n-1)d_2} = \frac{7n+1}{4n+27}$$

$$\frac{a_1 + \frac{(n-1)}{2}d_1}{a_2 + \frac{(n-1)}{2}d_2} = \frac{7n+1}{4n+27} \quad ..(1)$$
Put  $\frac{n-1}{2} = m-1$ 

$$n-1 = 2m-2$$

$$n = 2m-2 + 1$$

$$= 2m-1$$

$$\frac{a_1 + (m-1)d_1}{a_2 + (m-1)d_2} = \frac{7(2m-1)+1}{4(2m-1)+27}$$

$$= \frac{14m-7+1}{8m-4+27} = \frac{14m-6}{8m+23}$$



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16. Let 
$$x - 2 = t$$
  

$$\frac{1}{t(t+1)} + \frac{1}{t(t-1)} = \frac{2}{3}$$

$$= \frac{t-1+t+1}{t(t+1)(t-1)} = \frac{2}{3}$$

$$3t = t (t+1) (t-1)$$

$$3t = t(t^{2} - 1)$$

$$3t = t^{3} - t$$

$$t^{3} - 4t = 0$$

$$t (t^{2} - 4) = 0$$

$$t = 0 \quad t^{2} - 4 = 0$$

$$t = \pm \sqrt{4}$$

$$t = \pm 2$$

$$x - 2 = 0 \qquad \& x - 2 = \pm 2$$

$$x = 2 \qquad x = 0, 4$$

**17.** Volume of cone =  $\frac{1}{3}\pi r^2h$ 

$$= \frac{1}{3} \times \frac{22}{7} \times 5 \times 5 \times 24$$

Volume of cone = volume of cylinder

$$\frac{1}{3} \times \frac{22}{7} \times 5 \times 5 \times 24 = \frac{22}{7} \times 10 \times 10 \times h$$
  
h = 2 cm

18. The rise in the level of water will be due to the volume of sphere

$$\therefore \frac{4}{3} \pi (6)^3 = \pi x^2 \times 3\frac{5}{9}$$
$$\frac{4}{3} \times 6 \times 6 \times 6 = x^2 \times \frac{32}{9}$$
$$x = 9$$

$$\therefore$$
 diameter = 2x = 18 cm

19.

Let x be distance of cliff from man and h + 10 be height of hill which is required. In right triangle ACB,



....(i)

...(ii)

In right triangle BCD,

$$\tan 30^\circ = \frac{\text{CD}}{\text{BC}} = \frac{10}{\text{x}} \implies$$

$$x = 10 \sqrt{3}$$

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 $\frac{1}{\sqrt{3}} = \frac{10}{x}$ 

 $\Rightarrow$ 

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From (i) & (ii)  $\frac{h}{\sqrt{3}} = 10 \sqrt{3}$ h = 30 m  $\Rightarrow$ :. Height of cliff = h + 10 = 30 + 10 = 40 m. Distance of ship from cliff = x =  $10\sqrt{3}$  m = 10 (1.732) = 17.32 m 20. Sample space while tossing 3 coins S = {HHH, HHT, HTH, HTT, THH, THT, TTH, TTT} (i) Favourable cases = {HHT, HTH, THH}  $P(exactly 2 heads) = \frac{Number of favourable outcomes}{Number of total outcomes} = \frac{3}{8}$ (ii) Favourable cases = {HHH, HHT, HTH, THH} P(at least 2 heads) =  $\frac{4}{8} = \frac{1}{2}$ (iii) favourable cases = {HTT, THT, TTH, TTT} P (at least 2 tails) =  $\frac{4}{8} = \frac{1}{2}$ 21. Given r = 2.8 ; h = 3.5 m (ht. of cone)  $h_1 = 2.1 \text{ m}$  $\therefore$  I =  $\sqrt{r^2 + (h_1)^2}$  = 3.5 m Area of convas required per tent = [CSA of cone + CSA of cylinder]  $=\pi rl + 2\pi rh$  $= \pi r [3.5 + 7]$  $=\frac{22}{7}\times\frac{28}{10}\times\frac{105}{10}=\frac{462}{5}$ m<sup>2</sup> cost of canvas per tent = Rs.  $\frac{462}{5} \times 120$  = Rs. 11088 Total cost of 1500 tents = Rs.  $11088 \times 1500$ Amount shared by each schoo; = Rs.  $\frac{11088 \times 1500}{50}$  = Rs. 332640 22. Given : AP and AQ are two tangents drawn from a point A to a circle C (O, r). To prove : AP = AQ. Construction : Join OP, OQ and OA. **Proof :** In  $\triangle AOQ$  and  $\triangle APO$ ∠OQA =∠OPA «esonance»

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[Tangent at any point of a circle is perp. to radius through the point of contact] AO = AO [Common]



Steps of constructions are as follows

(1) Draw a circle of radius 4 cm

(2) Let O be its centre and P be any external point such that OP = 8 cm

(3) Join OP and then taking OP as diameter draw a circle intersecting the given circle at two points A and B. Join AP and BP.

(4) Hence, AP and BP are the required tangents



24.

23.

Let AO'= OX'= XO = r  $\therefore$  Radius is always perpendicular to tangent,  $\therefore \angle ACO = 90^{\circ}$ In  $\triangle ADO$  and  $\triangle ACO$   $\angle DAO' = \angle CAO$  [Common]  $\angle ADO' = \angle ACO$  [each 90°]  $\therefore$  By AA similarity criteria  $\triangle ADO' \sim \triangle ACO$ 

$$\Rightarrow \frac{\mathrm{DO'}}{\mathrm{CO}} = \frac{\mathrm{AO'}}{\mathrm{AO}} = \frac{\mathrm{r}}{\mathrm{3r}} = \frac{1}{3}$$

25. We have

$$\frac{1}{x+1} + \frac{2}{x+2} = \frac{4}{x+4}$$

$$\Rightarrow \frac{x+2+2(x+1)}{x^2+3x+2} = \frac{4}{x+4}$$
$$\Rightarrow (3x+4) (x+4) = 4(x^2+3x+2)$$
$$\Rightarrow 3x^2+16x+16 = 4x^2+12x+8$$
$$\Rightarrow x^2-4x-8 = 0$$

Using quadratic formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{4 \pm \sqrt{16 + 32}}{2} = \frac{4 \pm 4\sqrt{3}}{2}$$
$$x = 2 + 2\sqrt{3} \text{ or } 2 - 2\sqrt{3}$$

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Coordinates of D =  $\frac{2(4) + (1)}{2+1}$ 28.  $= \frac{8+1}{3} = \frac{9}{3} = 3 = \frac{2(6) + (1)(5)}{2+1}$ Coordinates of D =  $(3, \frac{17}{3})$ Coordinates of E =  $\frac{2(4) + (1)(7)}{2+1} = \frac{8+7}{3} = \frac{15}{3} = 5$  $\frac{2(6)+1(2)}{2+1} = \frac{12+2}{3} = \frac{14}{3}$ area  $\Delta(ADE) = \frac{1}{2} \left[ 4 \frac{17}{3} - \frac{14}{3} + 3(\frac{14}{3} - 6) + 5(6 - \frac{17}{3}) \right]$  $= \frac{1}{2} \left[ 4 \times 1 + 3 \frac{(-4)}{3} + 5 \times \frac{1}{3} \right]$  $=\frac{1}{2}\times\frac{5}{3}=\frac{5}{6}$ area ∆ABC  $= \frac{1}{2} \left[ 4(5-2) + 1 (2-6) + 7 (6-5) \right]$  $=\frac{1}{2}[4 \times 3 + 1 \times -4 + 7 \times 1]$  $=\frac{1}{2}[12-4+7]=\frac{15}{2}$  $\Rightarrow \frac{\text{area } \triangle ABC}{\text{area } \triangle ADE} = \frac{\frac{2}{5}}{\frac{5}{6}} = 9$  $\therefore$  area  $\triangle ABC = 9$  area ( $\triangle ADE$ ) 29. Total no. of events 16  $\{1 \times 1, 1 \times 4, 4 \times 9, 1 \times 16\}$  $2 \times 1, 2 \times 4, 2 \times 9, 2 \times 16$  $3 \times 1, 3 \times 4, 3 \times 9, 3 \times 16$  $4 \times 1$ ,  $4 \times 4$ ,  $4 \times 9$ ,  $4 \times 16$ } Events when product is less than 16 = 8  $\{1 \times 1, 1 \times 4, 1 \times 9, 2 \times 1, 2 \times 4, 3 \times 1, 3 \times 4, 4 \times 1\}$ events when product is less than 16  $\therefore$  Probability that sproduct of x & y is less than 16 = Total no. of events  $=\frac{8}{16}=\frac{1}{2}$ /<sub>0</sub>0 30. O r 'esonance® SOLUTION\_10th CBSE(BOARD)\_SUMMATIVE ASSESSMENT-II\_MATHS\_PAGE #9 Educating for better tomorrow

(i) length of sector  $\widehat{CA} = \pi r \frac{\theta}{180}$ In ∆OAB  $\tan \theta = \frac{AB}{OA}$  $AB = r \tan \theta$ Now, sec  $\theta = \frac{BO}{r}$  so, BO = r sec  $\theta$ length of CO = rSo length of BC = OB - OC= r sec  $\theta$  – r So perimeter =  $\widehat{AC}$  + AB + BC  $= \pi r \frac{\theta}{180} + r \tan \theta + r \sec \theta - r$ = r [tan  $\theta$  + sec  $\theta$  +  $\frac{\pi\theta}{180}$  -1] Speed of boat in still water = 24 km/hr Let the speed of stream be 'x' Upstream = Speed of boat = 24 - x $\frac{\text{Distance}}{\text{speed}} = \frac{32}{24 - x}$ Tupstream = Downstream Speed of boat = 24 + x $T_{downstream} = \frac{distance}{speed} = \frac{32}{24 + x}$ ATP  $T_{upstream} - T_{downstream} = 1$  $\frac{32}{24-x} - \frac{32}{24+x} = 1$ 

31.

 $24 - x \qquad 24 + x$   $32 \left[ \frac{24 + x - (24 - x)}{(24 - x)(24 + x)} \right] = 1$   $32 \left[ 24 + x - 24 + x \right] = (24 - x) (24 + x)$   $64x = (24)^2 - x^2$   $x^2 + 64x - 576 = 0$   $x^2 + 72x - 8x - 576 = 0$  x (x + 72) - 8(x + 72) = 0 (x - 8) (x + 72) = 0 x = 8, -72∴ speed of stream = 8 km/hr

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