## DISTRICT INSTITUTE OF EDUCATION AND TRAINING, PALAKKAD SSLC PRE-MODEL EXAMINATION 2023

MATHEMATICS-STD. X
MAX.MARK :80

## Answer any three questions from question numbers 1 to 4. Each question carries 2 marks .

1) a) Write an arithmetic sequence of common differene 3 .
b) What is the difference between the tenth and fifteenth terms of this sequence?
2)Write $x^{2}-1 / 4$ as the product first degree polynomials.
3)Find the coordinates of the point which divides the line joining the points $A(2,5)$ and $B(8,8)$ in the ratio $1: 2$.
2) In a circle, chords $A B$ and $C D$ intersect in $P$.

If $A B=10, A P=4, C P=8$
a) Find $A P \times P B$
b) Find the lenghth of PD.

Answer any 4 questions from question numbers 5 to 10 . Each question carries 3 marks.
5) (a)If the median of the numbers $17,13,18,15, x, 10,9$ is $x$, find the value of $x$.
(b) If the value of $x$ is 16 ,find the median.
6) In the figure
$A B=10 \mathrm{~cm}, C E=13 \mathrm{~cm}, P F=12 \mathrm{~cm}$
a) Name the figure which can be formed by folding this along the base edges.
b)What is the slant height?
c)what will be the height?

7) The diagonal of a rectangle is 12 cm long. The angle it makes with one side is $35^{\circ}$. Find the perimeter of the rectangle.
$\left[\sin 35^{\circ}=0.57, \cos 35^{\circ}=0.82\right]$
8) In the figure $A B$ is the diameter of the semicircle and $C D=8 \mathrm{~cm}$. The lenghth of $B C$ is 12 cm less than the lenghth of $A C$
a)If $A C=x$, what is the lenghth of $B C$ ?
b) What is the radius of the semicircle?
9) In the figure PC is a tangent to the circle
a) Find $<$ PCA
b) Find < CBA
c) Find $<B C A$

10) In an arithmetic sequence the $5^{\text {th }}$ and $10^{\text {th }}$ terms are 30 and 55 respetively.
a) What is the common difference?
b) Write the sequence.
c) Find the $100^{\text {th }}$ term of this sequence.

## Answer any 8 questions from question numbers 11 to 21. Each question carries 4 marks.

11) If $p(x)=x^{2}-4 x+4$
a) Prove that $(x-2)$ is a factor of $p(x)$.
b) Find the solution of the equation $p(x)=0$
12) a) Draw a circle with centre at origin and radius 4 cm .
b)Draw a radius $O P$ making an angle $45^{\circ}$ with the X -axis and draw a tangent at P .
c) Find the coordinates of the points $A$ and $B$ where the tangent intersects the axes.
d) Find the length of $A B$.
13) A solid figure is formed by attaching a hemisphere of radius 9c.m. with the base of a cone of same radius. The total height of the solid figure is 21 cm .
a) What is the height of the cone?
b) What is the volume of the solid figure?
14) A man observes the top of a tower at an angle of elevation $60^{\circ}$ from a point at a fixed distane from the foot of the tower. Then he observes the tower from a point 10 m. vertically above the previous position at an angle of elevation $45^{\circ}$.
a) Draw a rough sketh.
b) Find the height of the tower and the distance of the man from the tower.
15) The sum of a number and its reciproal is $13 / 6$. Which is the number?
16) a) In the figure triangle $A B C$ is equilqteral.If one side of $A B C$ is ' $a$ 'units, find its area.
b) If a dot is put in the figure with eyes closed, what is the probability that it is in the incircle?

17) In the figure the circle touches the three sides of right triangle $C D E . C D=6 \mathrm{~cm}$, $D E=8 \mathrm{~cm}, D E=10 \mathrm{~cm}$.

If the length of DK is ' $x$ '
a) Write the length of LD in terms of ' $x$ '.
b)What is the lenghth of LC ?

c) Write the lenghth of CE in terms of $x$.Find the lenghths of all other lines.
d) What is the radius of the incircle?
18) Find the sum
a) $1+2+3+\ldots+10$
b) $2+4+6+\ldots+20$
c) $3+6+9+\ldots+30$
d) $6+12+18+\ldots+60$
19)


In the figure $A B C D$ is a squre of side $8 \mathrm{~cm} ., \mathrm{O}$ is the origin.

The axes are drawn through the midpoints of the sides of $A B C D$.
a) Find the coordinates of the vertices of ABCD.
b)Find the coordinates of the points where the sides $A D$ and $B C$ cuts the $X$-axis.
c)Find the slope of diagonal BD.
20) a) In the figure, $O$ is the incentre.

If $\angle \mathrm{POQ}=122^{\circ}$ what is the measure of $\angle \mathrm{A}$ ?
b) Draw a triangle with two angles $100^{\circ}, 67^{\circ}$ and with radius of the incircle 3 cm .
21) The algebraic form of an arithmetic sequence is

$4 n+3$.
a) What is the first term?
b) What is the common difference ?
c)What is the difference between the $10^{\text {th }}$ and $20^{\text {th }}$ terms of this sequence?
d) Can the difference between any two terms of this sequence be 363 ?

Give reason.
22) $A B C D E$ is a regular pentagon. The tangents at $A$ and $B$ intersectat $P$.
a) Find the measure of $<E$.
b) Find the measure of $<\mathrm{ADE}$.
c) Find the measurs of $<$ PAB and $<$ PBA
d) Find the measure of $<\mathrm{APB}$

23) The monthly consumption of electricity of 75 households in a locality are given below.

| Monthly consumption | Number of houses |
| :--- | :--- |
| $65-85$ | 4 |
| $85-105$ | 5 |
| $105-125$ | 13 |
| $125-145$ | 20 |
| $145-165$ | 14 |
| $165-185$ | 8 |
| $185-205$ | 4 |
| $205-225$ | 7 |
|  | 75 |

a)In which class is the maximum consumption?
b)Which is the median class?
c)Find the median.
24) a) Write the sequence of odd numbersgreater than 1 .
b)What is the algebraic form of the above sequence ?
c)What is the algebraic form of the arithmetic sequence $\frac{3}{6}, \frac{5}{6}, \frac{7}{6} \ldots \ldots \ldots \ldots$ ?
d)Prove that no natural number is a term of this sequene.
25) Two cones are made of sectors with central angles $216^{\circ}$ and $288^{\circ}$ and radius 10 cm .each.
a) Find the radii of the two cones.
b) Find their heights.
c) Find the ratio between their volumes.
26) In triangle $A B C, A B=6$ c.m., $<A=60^{\circ},<B=50^{\circ}$. Draw triangle $A B C$ and draw its incircle. Measure the radius of the incircle.
27)In $\triangle A B C \quad A(-2,0), B(3,0)$ and area of the triangle is $15 \mathrm{~cm}^{2}$.
a) What is the length of $A B$ ?

b) What is the height of the triangle?
c) Write the coordinates of $C$.
d) Draw the coordinate axes and mark the points $A, B, C$ and join them to form $\triangle A B C$.
28) In10 A there are 20 boys and 24 girls. In 10B there are 22
boys and 18 girls. If one student is selected from each class
a)What is the possible number of pairs ?
b)What is the probability that both are girls?
c)What is the probability that both are boys?
d)What is the probability that atleast one is a girl?
29) In a right triangle one perpendicular side is 7c.m longer than the other. Hypotenuse is 9.c.m. more than the shortest side.
a)If the length of the shortest side is $x$, express the lengths of the other two sides in terms of $x$.
b)What is the relation between the three sides of a right triangle ?
c)Find the lengths of the three sides of this right triangle.

