

RRV GIRLS HIGHER SECONDARY SCHOOL, KILIMANOOR
SECOND YEAR HIGHER SECONDARY PRE MODEL EXAMINATION – 2023
MATHEMATICS (SCIENCE)

Time: 2 Hours

Cool-Off time : 15 mnt

Maximum Score : 60

Answer any 6 questions from 1 to 8. Each carries 3 scores. (6 x 3 = 18)

1. (a) The maximum number of ordered pairs to form a non-zero reflexive relation on a set of 4 elements (1)
(i) 2^4 (ii) 4 (iii) 2 (iv) 8
(b) Show that the relation R in the set {1, 2, 3} given by $R = \{(1,1), (2,2), (3,3), (1,3), (3,2)\}$ is reflexive but not symmetric nor transitive (2)

2. (a) If $\begin{bmatrix} x & 0 \\ 1 & y \end{bmatrix} = \begin{bmatrix} -2 & 0 \\ 1 & 5 \end{bmatrix}$
Find the value of x and y. (1)
(b) If $A = \begin{bmatrix} 1 & 2 \\ -1 & 3 \\ 0 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 3 & 4 & -1 \\ 2 & 1 & 3 \end{bmatrix}$
Find A-B. (2)

3. (a) The value of $\begin{vmatrix} x & x-1 \\ x+1 & x \end{vmatrix}$ is _____. (1)
(b) Find the value of λ if $A = \begin{bmatrix} \lambda & 1 \\ 6 & 3 \end{bmatrix}$ is singular (2)

4. Find the value of k, so that the function $f(x) = \begin{cases} kx^2, & \text{If } x \geq 1 \\ 4, & \text{If } x < 1 \end{cases}$
Is continuous at $x=1$ (3)

5. Find $\frac{dy}{dx}$ if $x^y = y^x$ (3)

6. Consider two vectors $\vec{a} = \hat{i} - \hat{j} + \hat{k}$
And $\vec{b} = \hat{i} + \hat{j} - \hat{k}$
(i) Find $|\vec{a}|$ and $|\vec{b}|$ (1)
(ii) Find $\vec{a} \cdot \vec{b}$ (1)
(iii) Find the angle between \vec{a} & \vec{b} (1)

7. Find the cartesian equation of the line which passes through the point $(-2, 4, -5)$ and is parallel to the line.

$$\frac{x + 3}{3} = \frac{y - 4}{-5} = \frac{z + 8}{6} \quad (3)$$

8. (a) If $P(A) = 0.4$, $P(B) = k$ and $P(A \cup B) = 0.7$ find k if A and B are independent events. (1)

- (b) If A and B are two events such that $P(A) = \frac{1}{4}$, $P(B) = \frac{1}{2}$ and $P(A \cap B) = \frac{1}{8}$
Find $P(\text{not } A \text{ and not } B)$ (2)

Answer any 6 questions from 9 to 16. Each carries 4 scores. (6 x 4 = 24)

9. (a) A function $f: A \rightarrow B$, where $A = \{1, 2, 3\}$ and $B = \{4, 5, 6\}$ defined by $f = \{(1,6), (2,4), (3, 5)\}$ then f is

- (i) One – one (ii) onto (iii) bijection (iv) neither one-one
not onto (1)

- (ii) Show that the modulus function given by $f(x) = |x|$ is neither one-one
nor onto. (3)

10. (a) $\sin^{-1} \sin \frac{2\pi}{3} = \underline{\hspace{2cm}}$

- (i) $\frac{2\pi}{3}$ (ii) $\frac{\pi}{4}$ (iii) $\frac{\pi}{2}$ (iv) $\frac{\pi}{3}$ (1)

- (ii) Write the value of $\tan^{-1} [2 \sin (2 \cos^{-1} \sqrt{3}/2)]$ (3)

11. If $A = \begin{bmatrix} 3 & 3 & -1 \\ -2 & -2 & 1 \\ -4 & -5 & 2 \end{bmatrix}$

- (i) Find $A + A^1$ and $A - A^1$ (2)

- (ii) Express A as the sum of a symmetric and a skew-symmetric matrix. (2)

12. (a) Find the area of the curve $y^2 = x$ and the line $x=4$ and the x -axis in first quadrant. (1)

- (b) Find the area of the region bounded by the curve $x^2 + y^2 = 9$ (3)

13. (a) The degree of the differential equation $x^4 \frac{d^2y}{dx^2} = 1 + \left(\frac{dy}{dx}\right)^3$ is

(i) 1 (ii) 4 (iii) 3 (iv) 2 (1)

(b) Find the general solution of the differential equation $y \log y \, dx - x \, dy = 0$ (3)

14. Consider two vectors $\vec{a} = 2\hat{l} + 3\hat{j} + 4\hat{k}$ and $\vec{b} = -\hat{j} - 2\hat{k}$

(i) Find $\vec{a} \times \vec{b}$ and $|\vec{a} \times \vec{b}|$ (2)

(ii) Find the unit vector perpendicular to the vectors \vec{a} and \vec{b} . (1)

(iii) Find the area of the parallelogram whose adjacent sides are \vec{a} and \vec{b} . (1)

15. Find the shortest distance between the lines

$$\vec{r} = (\hat{l} + 2\hat{j} + \hat{k}) + \lambda (\hat{l} - \hat{j} + \hat{k})$$

and $\vec{r} = (2\hat{l} - \hat{j} - \hat{k}) + \lambda (2\hat{l} + \hat{j} + 2\hat{k})$ (4)

16. A man is known to speak truth 3 out of 4 times. He throws a die and reports that it is a six. Find the probability that it is actually a six. (4)

Answer any 3 questions from 17 to 20. Each carries 6 scores (3 x 6 = 18)

17. Consider the linear equations

$$x - y + z = 4$$

$$2x + y - 3z = 0$$

$$x + y + z = 2$$

(i) Write the above equation as a matrix equation. (1)

(ii) Solve the system using matrix method. (5)

18. (a) $f(x)$ is a strictly increasing function if $f'(x)$ is _____

(i) Zero (ii) Negative (iii) positive (iv) None. (1)

(b) Find the intervals in which the function $f(x) = x^2 - 4x + 6$ is strictly decreasing. (2)

(c) Show that of all rectangles with a given area, the square has the least perimeter. (3)

19. Evaluate

(a) $\int \frac{x}{(x+1)(x+2)} dx$ (2)

(b) $\int \log x dx$ (1)

(c) $\int_0^{\pi/2} \frac{\sin^4 x}{\sin^4 x + \cos^4 x} dx$ (3)

20. Consider the *LPP*

Maximise $Z = 3x + 2y$ subject to

$$x + 2y \leq 10$$

$$3x + y \geq 15$$

$$x, y \geq 0$$

(a) Draw its feasible region (3)

(b) Find the corner points of the feasible region. (2)

(c) Find the maximum value of z (1)

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