

FIRST YEAR HIGHER SECONDARY SAMPLE QUESTION PAPER 2023

PART III

MATHEMATICS(COMMERCE)

Time : 2 Hours

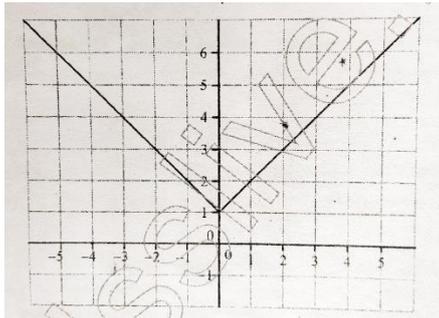
Maximum : 60Scores

Cool off Time : 15 Minutes

Answer any six questions from 1 to 8 .Each carries 3 marks .

1. If $U = \{1,2,3,4,5,6,7,8,9\}$; $A = \{2,4,6,8\}$ $B = \{2,3,5,7\}$, Verify $(A \cup B)' = A' \cap B'$ (3)

2. Graph of the function $f: R \rightarrow R$ is given below:



a) Write the value of $f(2)$ (1)

b) Write the range of $f(x)$ (1)

c) Identify the function and choose the correct answer. (1)

i) $f(x) = |x + 1|$ ii) $f(x) = |x - 1|$ iii) $f(x) = |x| + 1$ iv) $f(x) = |x| - 1$

3. Express the complex number $\frac{2-i}{(1+2i)}$ in the form $a+ib$. (3)

4. (a) Represent the inequality $x > -3$ on a number line. (1)

(b) Solve the inequality $3(2 - x) \geq 2(1 - x)$ (2)

5. (a) If ${}^n C_9 = {}^n C_8$, then $n =$ ----- (1)

(b) If $\frac{1}{6!} + \frac{1}{7!} = \frac{x}{8!}$, then x is _____ (2)

6. Let S and S' foci of the ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$ Let P be a point on the ellipse, then

(i) $PS + PS' =$ _____ (1)

(ii) Find the coordinates of S and S' (2)

7. Find the derivative of $\sin x$ from the first principle. (3)

8. Two dice are thrown at random . Find the probability of

(i) getting a doublet (1)

(ii) getting sum of the numbers on the dice 8 (2)

Answer any six questions from 9 to 16 .Each carries 4 marks .

9. (a) $A = \{2,3\}$ $B = \{1,3,5\}$ then the number of relations from A to B is _____ (1)
- (b) R is a relation defined on the set $A = \{1,2,3,4, \dots, 14\}$. $R = \{(x,y) / 3x - y = 0, x,y \in A\}$
- Write the domain, co-domain and range (3)
10. (a) Prove that $\frac{\sin 5x - 2\sin 3x + \sin x}{\cos 5x - \cos x} = \tan x$ (3)
- (b) $\frac{2\pi}{3}$ radian = _____ degree (1)
- i) 60 ii) 150 iii) 120 iv) 180
11. (a) Find the value of n if ${}^{(n-1)}P_3 = 5 \cdot {}^{(n+1)}P_3$ (2)
- (b) Find the number of arrangements of the letters of the word INDEPENDENCE. (2)
12. Find the co-ordinates of the foci, the vertices, the length of transverse axis, conjugate axis, the eccentricity and the latus rectum of the hyperbola $\frac{x^2}{16} - \frac{y^2}{9} = 1$ (4)
13. (a) $\lim_{x \rightarrow a} \frac{x^n - a^n}{x - a} = \dots\dots\dots$ (1)
- (b) Find the derivative of $\frac{x + \cos x}{\tan x}$ (3)
14. Consider the following data : 6,8,10,12,14,16,18,20,22,24 .Find its mean deviation about mean. (4)
15. (a) ${}^nC_0 - {}^nC_1 + {}^nC_2 - {}^nC_3 + \dots + (-1)^n {}^nC_n = \dots\dots\dots$ (1)
- i) 2^n ii) 0 iii) 2^{n-1} iv) 2
- (b) Expand $(x + \frac{1}{x})^5$ (3)
16. (a) The coordinates of points in the XY plane are of the form _____ (1)
- (b) Consider the triangle with vertices A(0,7,-10); B(1,6,-6) and C(4,9,-6) .Prove that the triangle is right angled (3)

Answer any 3 questions from 17 to 20 .Each carries 6 marks .

17. (a) The 6th term of the GP $\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \dots\dots\dots$ is _____ (2)
- (b) The sum of first three terms of a G.P is $\frac{13}{12}$ and their product is -1 .
- Find the common ratio and the terms. (4)
18. (a) Find the equation of the line joining (-2,6) and (4,8) . (2)
- (b) If the angle between two lines is $\frac{\pi}{4}$ and slope of one of the lines is $\frac{1}{2}$, find the slope of the other line. (4)
19. (a) If A and B are mutually exclusive and exhaustive events then $P(A) + P(B) = \dots\dots\dots$ (1)
- (b) In a class of 60 students, 30 opted for NCC, 32 opted for NSS and 24 opted for both NCC and NSS . If one of these students is selected at random, find the probability that :

