Reg. No. : $\qquad$
Name : $\qquad$

## SECOND YEAR HIGHER SECONDARY EXAMINATION, MARCH - 2024

Part - III
STATISTICS
Maximum : 60 Scores

## General Instructions to Candidates:

- There is a 'Cool-off time' of 15 minutes in addition to the writing time.
- Use the 'Cool-off time' to get familiar with questions and to plan your answers.
- Read questions carefully before answering.
- Read the instructions carefully.
- Calculations, figures and graphs should be shown in the answer sheet itself.
- Malayalam version of the questions is also provided.
- Give equations wherever necessary.
- Electronic devices except non-programmable calculators are not allowed in the Examination Hall.


## 






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Answer any 6 questions from 1 to 7. Each carries 1 score.

1. The maximum value of coefficient of correlation is
(a) 0
(b) 1
(c) -1
(d) 2
2. The time taken by a student to reach the school is an example of $\qquad$ variable.
(a) qualitative
(b) discrete
(c) continuous
(d) normal
3. The ratio of two independent chi-square variables is $\qquad$ .
(a) Normal
(b) t-statistic
(c) Chi-square statistic
(d) F-statistic
4. An estimator, $t$ is said to be an unbiased estimator for the parameter ' $\theta$ ' if $E(t)=$ $\qquad$ .
(a) $\theta$
(b) 0
(c) 1
(d) t
5. $\quad 1-\mathrm{p}($ type II Error $)=$ $\qquad$ .
(a) $\alpha$
(b) $\beta$
(c) Power of a test
(d) Level of significance
6. The test statistic used in ANOVA is $\qquad$ .
(a) z
(b) t
(c) $\chi^{2}$
(d) F
7. The sale of cotton clothes in summer is associated with $\qquad$ component of time series.
(a) Secular trend
(b) Seasonal variation
(c) Cyclical variation
(d) Irregular variation

Answer any 10 questions from 8 to 19. Each carries 2 scores.
8. Write a short note on positive correlation and negative correlation between variables.
9. In a regression analysis the following results are obtained :

$$
\mathrm{b}_{\mathrm{y} x}=0.23, \mathrm{r}=0.45, \quad \sigma_{x}=10
$$

Find the standard deviation of $y$.
10. Find the derivative of the following function :

$$
y=x^{2}+3 x+4
$$

## 


$(6 \times 1=6)$
 $\qquad$

（a） 0
（b） 1
（c）-1
（d） 2
 $\qquad$ வேカியறிலிா உக்ஃกே வงஸ゙．
（a）கைフロிடロถிவூ
（b）wl（พุ

（d）ตேวฉิอ๐
 $\qquad$

（a）ாேงฉิอณை
（b）t－గ్నত్రীగ్గிゃ


 வกめளிைெிிஜ் $\mathrm{E}(\mathrm{t})=$ $\qquad$ （ேூயிகிெஸை๐．
（a）$\theta$
（b） 0
（c） 1
（d） t
 $\qquad$ ．
（a）$\alpha$
（b）$\beta$
（c）வரிகஅツ கษロー
（d）గัชิமகைைை
 $\qquad$ ®ேஸ゙．
（a） z
（b） t
（c）$\chi^{2}$
（d） F
 $\qquad$



（c）ปつがめ エリリー

 2 セサை
$(10 \times 2=20)$




$$
\mathrm{b}_{\mathrm{y} x}=0.23, \mathrm{r}=0.45, \quad \sigma_{x}=10
$$




$$
y=x^{2}+3 x+4
$$

11. Evaluate the following definite integral :

$$
\int_{0}^{1} x^{2} \mathrm{~d} x
$$

12. A fair coin is tossed 16 times. Find the mean and variance of the number of heads obtained.
13. Write down any 4 properties of normal curve.
14. If a sample of size 2 is taken from the population $2,3,5$ without replacement, find the mean of the sample means.
15. Name the four properties of a good estimator.
16. Distinguish between assignable causes and chance causes of variation in ANOVA.
17. Control charts for $\bar{X}$ and $R$ charts are maintained on the tensile strength in kg of a certain yarn. The subgroup size is 5 . The values of $\bar{X}$ and $R$ are computed for each subgroup. Sum of Average of 25 subgroup is $\Sigma \overline{\mathrm{X}}=514.8, \Sigma \mathrm{R}=120$. Compute control limits for $\overline{\mathrm{X}}$ chart. [Hint : $\mathrm{A}_{2}=0.577$ ]
18. What are the components of a time series ?
19. From the following data construct Simple Aggregate index number for 2014 taking 2011 as the base :

| Commodities | Price in 2014 | Price in 2011 |
| :--- | :---: | :---: |
| Rice | 32 | 28 |
| Oil | 88 | 75 |
| Sugar | 40 | 35 |
| Wheat | 22 | 18 |



$$
\int_{0}^{1} x^{2} \mathrm{~d} x
$$

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|  | 2014 ¢e விe | 2011 ¢e வile |
| :---: | :---: | :---: |
| ชฺ๐01 | 32 | 28 |
| ๑円冂 | 88 | 75 |
| வツைos | 40 | 35 |
| ¢๐วハை | 22 | 18 |

Answer any 6 questions from 20 to 27. Each carries 4 scores.
20. The following data relate to time spent for exercising daily in minutes $(\mathrm{X})$ and blood pressure (Y) of a group of patients :

|  | $\mathbf{X}$ | $\mathbf{Y}$ |
| :--- | :---: | :---: |
| Mean | 60 | 100 |
| Standard deviation | 20 | 15 |

$$
\mathrm{r}=-0.81
$$

(a) Find the regression line of $Y$ on $X$.
(b) Calculate the blood pressure of a person who exercised 70 minutes daily. (3+1)
21. A random variable $X$ has the following probability distribution :

| X | -1 | 0 | 1 |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{X})$ | 0.4 | 0.3 | 0.3 |

Determine (a) $E(X)$
(b) $\quad \mathrm{V}(\mathrm{X})$
22. For a variable X following Poisson distribution with $\lambda=0.1$, calculate
(1) $\mathrm{P}(\mathrm{X}=2)$
(2) $\mathrm{P}(\mathrm{X}$ is atleast 2$)$
23. In an examination, 600 students have appeared for a paper in Economics. Their average mark is normally distributed with Mean $=40$ and Standard Deviation $=10$. Find the approximate number of students who get marks between 30 and 50 .
24. Explain the concept of statistic and parameter with an example each.
25. The mean weight of a sample of 100 students is 52 kgs . with standard deviation 3 kgs . Can it be considered as a sample taken from a normal population having mean greater than 50 kgs . at $1 \%$ level of significance. $(\mathrm{Z} \alpha=2.33)$
26. The incomplete ANOVA table of a study is given below, complete the fields and interpret the result.

| Source | df | Sum of squares | Mean sum of squares | F |
| :--- | :---: | :---: | :---: | :---: |
| Between samples | 5 | - | 12 | - |
| Within samples | - | 76 | - |  |
| Total | 24 | - |  |  |

$$
\mathrm{F}_{0.01}=4.17
$$

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|  | X | Y |
| :---: | :---: | :---: |
| ®00ృ」 | 60 | 100 |
|  | 20 | 15 |

$$
\mathrm{r}=-0.81
$$






| X | -1 | 0 | 1 |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{X})$ | 0.4 | 0.3 | 0.3 |

（a） $\mathrm{E}(\mathrm{X})$
（b） $\mathrm{V}(\mathrm{X})$
றவ கைஸுகை．

（1） $\mathrm{P}(\mathrm{X}=2)$













| உ๐விS | df | வனిのறலூபூ ढృக |  நைகய゙ロ | F |
| :---: | :---: | :---: | :---: | :---: |
|  | 5 | － | 12 | － |
|  | － | 76 | － |  |
| （ேூ） | 24 | － |  |  |

$$
\mathrm{F}_{0.01}=4.17
$$

27. The following data shows the values of range ( R ) for ten samples of size 5 each. Calculate the values for central line and control limits for range chart. Also draw the control chart and determine whether the process is under control. [ $\mathrm{D}_{3}=0, \mathrm{D}_{4}=2.115$ ]

| Sample No. | Range (R) |
| :---: | :---: |
| 1 | 7 |
| 2 | 4 |
| 3 | 8 |
| 4 | 5 |
| 5 | 7 |
| 6 | 4 |
| 7 | 8 |
| 8 | 4 |
| 9 | 7 |
| 10 | 9 |

Answer any 2 questions from 28 to 30. Each carries 5 scores.
28. Calculate the Karl Pearson's coefficient of correlation for the following :

| X | 5 | 10 | 5 | 11 | 12 | 4 | 3 | 2 | 7 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 1 | 6 | 2 | 8 | 5 | 1 | 4 | 6 | 5 | 2 |

Also comment on the result.
29. (a) A time series is a set of data recorded $\qquad$ .
(i) Geographically
(ii) Chronologically
(iii) Both geographically and chronologically
(iv) None of these
(b) The following data relate to the sale of mobile phones from a shop in the city from 2005 to 2012. Calculate the trend values by 4 yearly moving average.

| Year | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sales | 128 | 265 | 341 | 412 | 485 | 531 | 578 | 620 |$\quad(\mathbf{1}+\mathbf{4})$

30. Using the following data calculate :
(a) Laspeyre's Index Number
(b) Paasche's Index Number
(c) Fisher's Index Number

| Commodities | Base Year |  | Current Year |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Price | Quantity | Price | Quantity |
| A | 9.25 | 5 | 15 | 5 |
| B | 8 | 10 | 12 | 11 |
| C | 4 | 6 | 5 | 6 |
| D | 1 | 4 | 1.25 | 8 |



 $\left[\mathrm{D}_{3}=0, \mathrm{D}_{4}=2.115\right]$

| momiuô mmia | ¢กற91 |
| :---: | :---: |
| 1 | 7 |
| 2 | 4 |
| 3 | 8 |
| 4 | 5 |
| 5 | 7 |
| 6 | 4 |
| 7 | 8 |
| 8 | 4 |
| 9 | 7 |
| 10 | 9 |






| X | 5 | 10 | 5 | 11 | 12 | 4 | 3 | 2 | 7 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 1 | 6 | 2 | 8 | 5 | 1 | 4 | 6 | 5 | 2 |

 $\qquad$




(iv) றのைைmృa잉




| Year | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sales | 128 | 265 | 341 | 412 | 485 | 531 | 578 | 620 |







| Commodities | Base Year |  | Current Year |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Price | Quantity | Price | Quantity |
| A | 9.25 | 5 | 15 | 5 |
| B | 8 | 10 | 12 | 11 |
| C | 4 | 6 | 5 | 6 |
| D | 1 | 4 | 1.25 | 8 |

## Statistical Tables

## Standard Normal Table

| 2 | 0.00 | . 01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.1 | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.1480 | 0.1517 |
| 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.1700 | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| 0.5 | 0.1915 | 0.1950 | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0. | 0.2257 | 0.2291 | 0.2324 | 0.235 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.299 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | 0.3159 | 0.318 | 0.3212 | 0.3238 | 0.32 | 0.3289 | 0.3315 | 0.3340 | 0.3365 | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.1 | 0.3643 | 0.366 | 0.3686 | 0.370 | 0.37 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.420 | 0.4222 | 0.423 | 0.42 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.456 | 0.4573 | 0.458 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.471 | 0.4726 | 0.473 | 0.473 | 0.4744 | 0.4750 | 0.47 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.477 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.1 | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| 2.2 | 0.4861 | 0.486 | 0.4868 | 0.487 | 0.48 | 0.4878 | 0.4881 | 0.488 | 0.4887 | 0.4890 |
| 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.6 | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |
| 3.1 | 0.4990 | 0.4991 | 0.4991 | 0.4991 | 0.4992 | 0.4992 | 0.4992 | 0.4992 | 0.4993 | 0.4993 |
| 3.2 | 0.4993 | 0.4993 | 0.4994 | 0.4994 | 0.4994 | 0.4994 | 0.4994 | 0.4995 | 0.4995 | 0.4995 |
| 3.3 | 0.4995 | 0.4995 | 0.4995 | 0.4996 | 0.4996 | 0.4996 | 0.4996 | 0.4996 | 0.4996 | 0.4997 |
| 3.4 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4998 |
| 3.5 | 0.4998 | 0.4998 | 0.4998 | 0.4998 | 0.4998 | 0.4998 | 0.4998 | 0.4998 | 0.4998 | 0.4998 |
| 3.6 | 0.4998 | 0.4998 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 |
| 3.7 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 |
| 3.8 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 | 0.4999 |
| 3.9 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 |
| 4.0 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 |

