

COMMON QUARTERLY EXAMINATION-2023-24

Time Allowed : 3.00 Hours]

MATHEMATICS

[Max. Marks : 100]

I. Answer all of the following:

SECTION - I

14x1=14

1. If $n(A \times B) = 6$ and $A = \{1, 3\}$ then $n(B)$ is _____.
 - 1
 - 2
 - 3
 - 6
2. If $\{(a, 8), (6, b)\}$ represents an identity function then the value of a and b are respectively
 - (8, 6)
 - (8, 8)
 - (6, 8)
 - (6, 6)
3. $f(x) = (x+1)^3 - (x-1)^3$ represents a function which is _____.
 - Linear
 - Cubic
 - Reciprocal
 - Quadratic
4. If the HCF of 65 and 117 is expressible in the form of $65m - 117$. Then the value of m is _____.
 - 4
 - 2
 - 1
 - 3
5. $7^{44} \equiv \text{_____} \pmod{100}$.
 - 1
 - 2
 - 3
 - 4
6. If $1 + 2 + 3 + \dots + n = k$ then $1^3 + 2^3 + 3^3 + \dots + n^3 = \text{_____}$.
 - K^3
 - K^2
 - $\frac{k(k+1)}{2}$
 - $(k+1)^3$
7. $y^2 + \frac{1}{y^2}$ is not equal to
 - $\frac{y^4 + 1}{y^2}$
 - $\left(y + \frac{1}{y}\right)^2$
 - $\left(y - \frac{1}{y}\right)^2 + 2$
 - $\left(y + \frac{1}{y}\right)^2 - 2$
8. The solution of $(2x - 1)^2 = 9$ is equal to
 - 1
 - 2
 - 1, 2
 - None of these
9. If ΔABC is an isosceles triangle with $\angle C = 90^\circ$ and $AC = 5 \text{ cm}$, then AB is
 - 2.5 cm
 - 5 cm
 - 10 cm
 - $5\sqrt{2} \text{ cm}$
10. If in ΔABC , $DE \parallel BC$, $AB = 3.6 \text{ cm}$, $AC = 2.4 \text{ cm}$ and $AD = 2.1 \text{ cm}$ then the length of AE is
 - 1.4 cm
 - 1.8 cm
 - 1.2 cm
 - 1.05 cm
11. The straight line given by the equation $x = 11$ is
 - Parallel to X axis
 - Parallel to Y axis
 - Passing through the origin
 - Passing through the point $(0, 11)$
12. Slope of line $ax + by + c = 0$ is _____.
 - $\frac{b}{a}$
 - $\frac{a}{b}$
 - $-\frac{b}{a}$
 - $-\frac{a}{b}$
13. $(2, 1)$ is the point of intersection of two lines
 - $x - y - 3 = 0; 3x - y - 7 = 0$
 - $x + y = 3; 3x + y = 7$
 - $3x + y = 3; x + y = 7$
 - $x + 3y - 3 = 0; x - y - 7 = 0$
14. $\tan\theta \operatorname{cosec}^2\theta - \tan^2\theta$ equal to
 - $\sec\theta$
 - $\cot^2\theta$
 - $\sin\theta$
 - $\cot\theta$

SECTION - II

II. Answer any 10 questions. Question No. 28 is compulsory.

10x2=20

15. A Relation R is given by the set $\{(x, y) / y = x+3 \text{ } x \in \{0, 1, 2, 3, 4, 5\}\}$. Determine its domain and range.
16. A function f is defined by $f(x) = 3 - 2x$. Find x such that $[f(x)]^2 = [f(x)]^1$.
17. Let f be a function $f: N \rightarrow N$ be defined by $f(x) = 3x + 2, x \in N$ (i) Find the images of 1 and 2
 ii) Find the pre-images of 29 and 53.

18. If $13824 = 2^a \times 3^b$ then find a and b .

19. Find a_n and a_{14} whose n^{th} term is

$$a_n = \begin{cases} \frac{n^2-1}{n+3}; & n \text{ is even, } n \in N \\ \frac{n^2}{2n+1}; & n \text{ is odd, } n \in N \end{cases}$$

20. Find the sum $3 + 1 + \frac{1}{3} + \dots + \infty$.
21. Find the excluded values of $\frac{x^3 - 27}{x^3 + x^2 - 6x}$.
22. Determine the quadratic equation whose sum and product of -9 and 20.
23. If $\triangle ABC$ is similar to $\triangle DEF$ such that $BC = 3$ cm, $EF = 4$ cm and area of $\triangle ABC = 54$ cm². Find the area of $\triangle DEF$.
24. In $\triangle ABC$, D and E are points on the sides AB and AC respectively such that $DE \parallel BC$. If $\frac{AD}{DB} = \frac{3}{4}$ and $AC = 15$ cm find AE.
25. The line through the points (-2, a) and (9, 3) has slope $-\frac{1}{2}$. Find the value of a.
26. Find the intercepts made by the line $4x - 9y + 36 = 0$ on the co-ordinate axis.
27. Prove that $\sqrt{\frac{1 + \cos\theta}{1 - \cos\theta}} = \operatorname{cosec}\theta + \cot\theta$
28. If the points $(p^2, 0)$, $(0, q^2)$ and $(1, 1)$ are straight line. Then prove that $\frac{1}{p^2} + \frac{1}{q^2} = 1$

SECTION - III

- III. Answer the following any 10 questions. Q.No.42 is compulsory. $10 \times 5 = 50$**
29. Let $A = \{x \in W \mid x < 2\}$, $B = \{x \in N \mid 1 < x \leq 4\}$ and $C = \{3, 5\}$. Verify that $A \times (B \cup C) = (A \times B) \cup (A \times C)$.
30. If the function $f: R \rightarrow R$ is defined by $f(x) = \begin{cases} 2x + 7; & x < -2 \\ x^2 - 2; & -2 \leq x < 3 \\ 3x - 2; & x \geq 3 \end{cases}$ then find the values of
- i) $f(4)$ ii) $f(-2)$ iii) $f(4) + 2f(1)$ iv) $\frac{f(1) - 3f(4)}{f(-3)}$
31. If $f(x) = x-1$, $g(x) = 3x+1$ and $h(x) = x^2$. Prove that $(f \circ g) \circ h = f \circ (g \circ h)$.
32. In an A.P, sum of four consecutive terms is 28 and their sum of their squares is 276. Find the four numbers
33. Find the sum to n terms of $3 + 33 + 333 + \dots$
34. Rekha has 15 square colour papers of sizes 10 cm, 11 cm, 12 cm....24cm. How much area can be decorated with these colour papers?
35. Solve : $x+y+z=5$; $2x-y+z=9$; $x-2y+3z=16$.
36. If $36x^4 - 60x^3 + 61x^2 - mx + n$ is a perfect square, find the values of m and n.
37. Prove that the equation $x^2(p^2 + q^2) + 2x(pr + qs) + r^2 + s^2 = 0$ has no real roots. If $ps = qr$ then show that the roots are real and equal.
38. State and prove Angle bisector theorem.
39. Find the area of the quadrilateral formed by the points (8, 6), (5, 11), (-5, 12) and (-4, 3).
40. Find the equation of perpendicular bisector of line joining the points A (-4, 2) and B (6, -4).
41. If $\frac{\cos\theta}{1 + \sin\theta} = \frac{1}{a}$ then prove that $\frac{a^2 - 1}{a^2 + 1} = \sin\theta$
42. The sum of the reciprocals of $(x+2)$ and $(x-2)$ is equal to 6 times of the reciprocal of $4x+7$. Find the value of x.

SECTION - IV

- IV. Answer the following. $2 \times 8 = 16$**
43. a) A bus is travelling at a uniform speed of 50 km/hr. Draw the distance - time graph and hence find i) the constant of variations ii) how far will it travel in 90 minutes? iii) the time required to cover a distance of 300 km from the graph.
- (OR)
- b) Draw the graph of $xy = 24$, $x, y > 0$ using the graph find (i) y when $x=3$ and (ii) x when $y=6$.
43. a) Construct a triangle similar to a given triangle PQR with its sides equal to $\frac{7}{3}$ of the corresponding sides of the $\triangle PQR$ (scale factor $\frac{7}{3} < 1$)
- (OR)
- b) Construct a $\triangle PQR$ such that $QR = 6.5$ cm, $\angle P = 60^\circ$ and the altitude from P to QR is of length 4.5 cm