

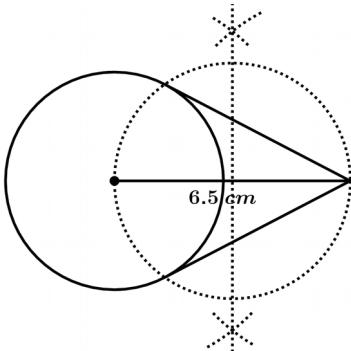
# SECOND TERMINAL EVALUATION 2024 - 2025

**A**

## MATHEMATICS EM – ANSWER KEY

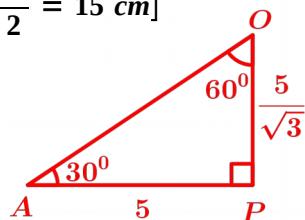
**E-1003**

Qn no.	Key	Score
<b>Each questions from 1 to 4 carries 2 scores. ( Answer any 3 )</b>		
1	a) $x_{10} = 50$ b) 25	1 1
2	a) (6, 0) b) Distance = $5 - 1 = 4$	1 1
3	a) $\angle APB = 40^\circ$ b) $\angle PAB = \frac{180^\circ - 40^\circ}{2} = 70^\circ$ [ $\because PA = PB$ ]	1 1
4	a) 8 b) $\frac{72}{8} = 9 \text{ cm}$	1 1
<b>Each questions from 5 to 10 carries 3 scores. ( Answer any 4 )</b>		
5	Total number of pairs = $5 \times 3 = 15$  a) Probability that both numbers are equal = $\frac{3}{15} = \frac{1}{5}$ [ $\because (1,1), (2,2), (3,3)$ ]  b) Probability that both numbers are prime = $\frac{6}{15} = \frac{2}{5}$ [ $\because (2,2), (2,3), (3,2), (3,3), (5,2), (5,3)$ ]	1 1 1
6	a) $CD = 3 \text{ cm}$  b) $AD = 3\sqrt{3} \text{ cm.}$ , $BD = 3 \text{ cm}$ $AB = 3\sqrt{3} + 3 \text{ cm}$	1 1 1
7	Coordinates of B = $(2 + 5, 3) = (7, 3)$  Coordinates of D = $(2, 3 + 5) = (2, 8)$  Coordinates C = $(7, 8)$	1 1 1
8	For drawing a circle of radius 3 cm and mark a point 6.5 cm away from its centre . For drawing the perpendicular bisector of this 6.5 cm long line and drawing the large circle. For drawing tangents .	1 1 1

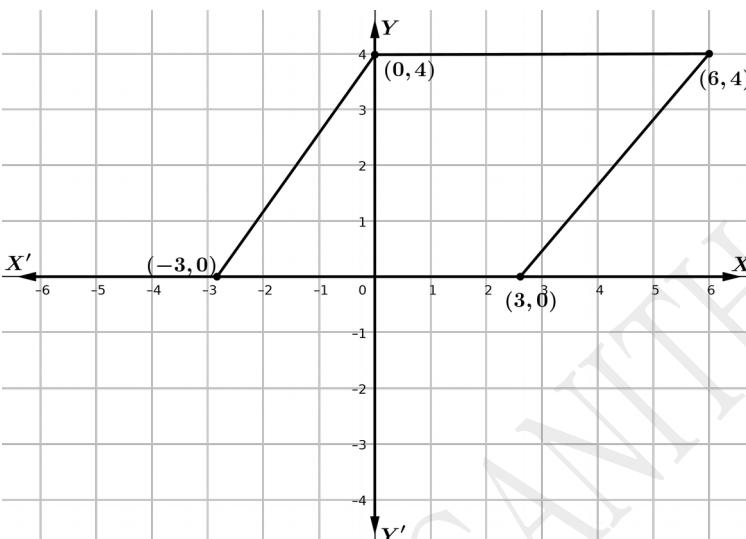
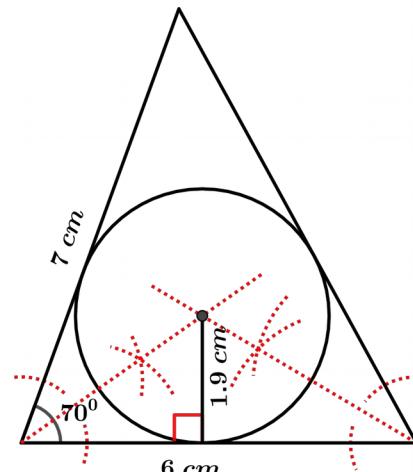


9	a) $h = \sqrt{26^2 - 10^2} = \sqrt{36 \times 16} = 24 \text{ cm}$  b) Volume $= \frac{1}{3} \times 20^2 \times 24 = 3200 \text{ cubic.cm}$	1  2	3
10	a) $PR = \frac{12^2}{8} = 18 \text{ cm}$ $[\because PR \times PS = PQ^2]$  b) $RS = 18 - 8 = 10 \text{ cm}$  c) Radius $= \frac{RS}{2} = 5 \text{ cm}$	1  1  1	3
<b>Each questions from 11 to 21 carries 4 scores. (Answer any 8 )</b>			
11	a) First number $= x \implies$ Next term $= x + 2$  b) $x(x + 2) + 8 = 128 \implies x^2 + 2x + 8 = 128$  c) $x^2 + 2x + 1 = 121 \implies x^2 + 2x + 1^2 = 121 \implies (x + 1)^2 = 11^2$  $x + 1 = 11 \implies x = 10 \implies$ Numbers $= 10, 12$	1  1  1  1	4
12	a) $\angle ADC = 90^\circ$ $[\because \text{Angle in a semicircle}]$  b) $\angle AOB = 140^\circ$ $[\because OA = OB, \angle OAB = \angle OBA]$  c) $\angle ADB = \frac{140^\circ}{2} = 70^\circ$ $[\because \text{Angle on the alternate arc of an arc is half its central angle}]$  d) $\angle ACD = 70^\circ$ $[\because \angle ADB = \angle ABD, \angle ACD = \angle ABD]$ .	1  1  1  1	4
13	a) $\angle A = 180^\circ - (40^\circ + 75^\circ) = 65^\circ$  b) Diameter of the circumcircle $= \frac{7}{\sin 65^\circ} = \frac{7}{0.91} \text{ cm}$  c) $AB = \frac{7}{0.91} \times 0.97 \text{ cm}$ $[\because \frac{AB}{\sin 75^\circ} = 2r]$  d) $AC = \frac{7}{0.91} \times 0.64 \text{ cm}$ $[\because \frac{AC}{\sin 40^\circ} = 2r]$	1  1  1  1	4
14	a) $AB = 7 - (-1) = 8$  $BC = \sqrt{(3-7)^2 + (5-2)^2} = \sqrt{25} = 5$  $AC = \sqrt{[3 - (-1)]^2 + (5 - 2)^2} = \sqrt{25} = 5$  b) Isosceles triangle	1  1  1  1	4
15	For drawing a circle of radius 3 cm.  For drawing supplementary angles of the angles of the triangle at the centre of the circle  For drawing tangents to complete the triangle	1  1  2	4

16	<p>a) Slant height = 18 cm</p> <p>b) <math>\frac{140}{360} = \frac{r}{18}</math></p> $r = \frac{140 \times 18}{360} = 7 \text{ cm}$ <p>c) Curved surface area = <math>\pi \times 7 \times 18 = 126\pi \text{ sq.cm}</math></p> <p>[ OR , Curved surface area of the cone = Area of the sector</p> $= \frac{140}{360} \times \pi \times 18^2 = 126\pi \text{ sq.cm } ]$	1 1 1 1	4
17	<p>a) <math>AC = \frac{13}{5} \times 5 = 13 \text{ cm}</math> <math>[\because \sin A = \frac{BC}{AC}]</math></p> <p>b) <math>AB = \sqrt{13^2 - 5^2} = \sqrt{18 \times 8} = 12 \text{ cm}</math></p> <p>c) <math>\tan A = \frac{5}{12}</math> <math>[\because \tan A = \frac{BC}{AB}]</math></p> <p>d) <math>\tan A \times \tan C = \frac{5}{12} \times \frac{12}{5} = 1</math></p>	1 1 1 1	4
18	<p>a) <math>r = \sqrt{(3 - 0)^2 + (4 - 0)^2} = \sqrt{25} = 5</math></p> <p>b) <math>(5, 0), (-5, 0)</math></p> <p>c) <math>\sqrt{(-1 - 0)^2 + (-5 - 0)^2} = \sqrt{26}</math></p> <p>Outside the circle.</p>	1 1 1 1	4
19	<p>a) <math>\angle C = 60^\circ</math> <math>[\because \angle C + \angle BOC = 180^\circ]</math></p> <p>b) <math>\angle A = 60^\circ \implies \triangle ABC \text{ is an equilateral triangle.}</math></p> <p>Perimeter = <math>3 \times 10 = 30 \text{ cm}</math> <math>[\because AB = AP + PB]</math></p> <p>c) <math>r = \frac{5}{\sqrt{3}} \text{ cm}</math> <math>[\because r = \frac{A}{S}, A = \frac{\sqrt{3} \times 10^2}{4} \text{ sq.cm}, S = \frac{30}{2} = 15 \text{ cm}]</math></p> <p>[ OR , In right triangle OPA , <math>r = OP = \frac{5}{\sqrt{3}} \text{ cm}</math></p>	1 1 1 1	4



20	<p>a) <math>AP = \frac{10}{2} = 5 \text{ cm}</math></p> <p>b) <math>PB = 5 \times 0.83 = 4.15 \text{ cm}</math> <math>[\because \tan 40^\circ = \frac{PB}{PA}]</math></p> <p>c) <math>BD = 2 \times 4.15 = 8.3 \text{ cm}</math></p> <p>Area <math>= \frac{1}{2} \times 10 \times 8.3 = 41.5 \text{ sq.cm}</math></p>	1 1 1 1	4
21	<p>a) <math>\frac{4}{3} \pi r^3 = 4 \pi r^2 \implies r = 3</math></p> <p>b) Volume of the sphere <math>= \frac{4}{3} \times \pi \times 3^3 = \frac{4}{3} \times 27\pi</math></p> <p>Volume of a hemisphere <math>= \frac{2}{3} \times \pi \times 1^3 = \frac{4}{3} \times \pi</math></p> <p>Number of hemispheres <math>= \frac{\text{Volume of the sphere}}{\text{Volume of a hemisphere}} = \frac{\frac{4}{3} \times 27\pi}{\frac{2}{3} \times \pi} = 54</math></p>	1 1 1 1	4
<b>Each questions from 22 to 29 carries 5 scores. (Answer any 6 )</b>			
22	<p>a) <math>x_1 = 4 + 1 = 5</math></p> <p>b) <math>x_{21} = 4 \times 21 + 1 = 85</math></p> <p>c) Sum <math>= \frac{21}{2} \times (5 + 85) = \frac{21}{2} \times 90 = 945</math> <math>[\because \text{Sum} = \frac{n}{2} (x_1 + x_n)]</math></p> <p style="color: red;">[ OR, Sum <math>= 21 \times \text{Middle term} = 21 \times x_{11} = 21 \times 45 = 945 ]</math></p> <p>d) <math>945 + 21 = 966</math></p>	1 1 2 1	5
23	<p>a) Volume of the vessel <math>= \pi \times 20^2 \times 30 = 12000\pi \text{ cubic.m}.</math></p> $= \frac{12000\pi}{1000} = 12\pi \text{ m}.$ <p>b) Volume of the water flowing out = Volume of the sphere</p> $= \frac{4}{3} \times \pi \times 15^3 = 4500\pi \text{ cubic.cm}$ $= \frac{4500\pi}{1000} = 4.500\pi \text{ litres}$ <p>Volume of the water remain in the vessel <math>= 12\pi - 4.500\pi = 7.500\pi \text{ litres}</math></p>	1 1 1 1 1	5
24	<p>a)</p> <p>Height of the building = AB</p> <p>Height of the tower = CD</p>	1	

	b) $AB = 40 \times \tan 50^\circ = 40 \times 1.19 = 47.6 \text{ m}$ $[\because \text{In right triangle } ABC, \tan 50^\circ = \frac{AB}{40}]$ c) $DE = 40 \times \tan 35^\circ = 40 \times 0.70 = 28 \text{ m}$ $[\because \text{In right triangle } AED, \tan 35^\circ = \frac{DE}{40}]$ Height of the tower = $CD = CE + DE = 47.6 + 28 = 75.6 \text{ m}$	2 1 1	5
25	a)		
	 <p>b) Area of the quadrilateral = <math>6 \times 4 = 24 \text{ sq.cm}</math>  <math>[\because \text{This quadrilateral is a parallelogram}]</math></p>	1	4 5
26	a) $\angle BAC = 180^\circ - (65^\circ + 55^\circ) = 60^\circ$ b) $\angle ABP = 55^\circ$ $[\because PA = PB]$ c) $\angle P = 180^\circ - (55^\circ + 55^\circ) = 70^\circ$ $\angle R = 180^\circ - (65^\circ + 65^\circ) = 50^\circ$ $[\because RA = RC]$ $\angle Q = 180^\circ - (70^\circ + 50^\circ) = 60^\circ$ $[\because \angle P + \angle Q + \angle R = 180^\circ]$	1 1 1 1 1	5
27			5 5

28	<p>a) <math>a = \frac{96}{4} = 24 \text{ cm.}</math></p> <p>b) <math>l = \sqrt{12^2 + 9^2} = \sqrt{225} = 15 \text{ cm}</math></p> <p>c) Surface area of a toy <math>= a^2 + 2al = 24^2 + 2 \times 24 \times 15</math>  <math>= 1296 \text{ sq.cm}</math>  <math>= \frac{1296}{10000} \text{ sq.cm}</math></p> <p>Total cost <math>= 100 \times \frac{1296}{10000} \times 50 = 648 \text{ Rs}</math></p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>	<p>5</p>
29	<p>a) <math>1^3 + 2^3 + 3^3 + 4^3 = 10^2 = 100</math></p> <p>b) <math>1 + 2 + 3 + 4 + 5 = \frac{5 \times 6}{2} = 15</math></p> <p>c) <math>\left(\frac{6 \times 7}{2}\right)^2 = 21^2 = 441</math></p> <p>d) <math>\left(\frac{10 \times 11}{2}\right)^2 = 55^2</math></p> <p>e) <math>\left(\frac{n(n+1)}{2}\right)^2</math></p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>	<p>5</p>