

# ANNUAL EVALUATION 2024 - 2025

<b>A</b>	<b>MATHEMATICS EM – ANSWER KEY</b>	<b>E-903</b>
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Qn no.	Key	Score	
<b>Each questions from 1 to 4 carries 2 scores. ( Answer any 3 )</b>			
1	Mean mark = $\frac{70 + 65 + 45 + 54 + 72 + 66 + 58 + 50}{8} = \frac{480}{8} = 60$	2	2
2	Numbers = $\frac{21 + 5}{2}$ , $\frac{21 - 5}{2}$ = 13 , 8	1 1	2
3	$r^2 = \frac{4\pi}{\pi} = 4$ $r = \sqrt{4} = 2 \text{ cm}$	1 1	2
4	Area of the shaded region is $\frac{40 + 50 + 30}{360} = \frac{120}{360} = \frac{1}{3}$ of the total area of the circle. Area of the unshaded region is $\frac{2}{3}$ of the total area of the circle.	1 1	2
<b>Each questions from 5 to 10 carries 3 scores. ( Answer any 4 )</b>			
5	a) $BC = \sqrt{2^2 - 1^2} = \sqrt{3}$ b) Perimeter of the square having side = $4 \times \sqrt{3} = 4 \times 1.73 = 6.92 \text{ m}$	1 2	3
6	a) Base area = $6 \times \frac{\sqrt{3}}{4} \times 8^2 = 96\sqrt{3} \text{ sq.cm}$ [∵ Area of the regular hexagon = $6 \times \frac{\sqrt{3}}{4} \times a^2$ ] b) Volume = $96\sqrt{3} \times 15 = 1440\sqrt{3} \text{ cubic cm.}$ [∵ Volume = Base area × Height ]	2 1	3
7	a) $AB = 2 \times 2 = 4 \text{ cm}$ [∵ $h = \frac{a}{2}\sqrt{3}$ ] b) Area of the triangle ABC = $\frac{\sqrt{3}}{4} \times 4^2 = 4\sqrt{3} \text{ sq.cm}$ [∵ Area of the equilateral triangle = $\frac{\sqrt{3}}{4} \times a^2$ ]	1 2	3
8	a) $\frac{1}{4} \times 12 = 3 \text{ cm}$ [∵ Length of an arc of a circle is proportional to its central angle ] b) $1\frac{1}{2} \times 3 = 4.5 \text{ cm}$ [∵ Lengths of the arcs of same central angle are proportional to the radii of the circles ]	1 2	3
9	For drawing a line of length 13 cm . For dividing this line into three equal parts . For completing the equilateral triangle using one part of above as side.	1 1 1	3

10	a) $2\pi r$ b) Circumference of the circle proportional to the radius. Proportionality constant = $2\pi$	1 1 1	3
<b>Each questions from 11 to 21 carries 4 scores. ( Answer any 8 )</b>			
11	a) If we take radii as $r$ and $2r$ , heights as $4h$ and $3h$ , then Ratio of the lateral surface areas = $2\pi \times r \times 4h : 2\pi \times 2r \times 3h = 4 : 6 = 2 : 3$ b) Lateral surface area of the cylinder = $\frac{30}{2} \times 3 = 45 \text{ sq. cm}$	2 2	4
12	a) $p(0) = 2$ b) $p(1) = 1^2 + 3 \times 1 + 2 = 6$ c) $p(-1) = (-1)^2 + 3 \times (-1) + 2 = 0$ $\frac{p(1) + p(-1)}{p(0)} = \frac{6 + 0}{2} = 3$	1 1 1 1	4
13	a) Radius of the small semicircle = $\frac{4}{2} = 2 \text{ cm}$ b) Area of the large semicircle = $\frac{1}{2} \pi \times 4^2 = 8\pi \text{ sq. cm}$ c) Area of the shaded region = Area of the large semicircle - $2 \times$ Area of the small semicircle = $8\pi - 2 \times \frac{1}{2} \times \pi \times 2^2 = 4\pi \text{ sq. cm}$	1 1 1 1	4
14	a) $x = -2 + 5 = 3$ OR $x = -2 - 5 = -7$ b) $x = \frac{6 + (-2)}{2} = \frac{4}{2} = 2$	2 2	4
15	a) Area of the rectangle = $6 \times 4 = 24 \text{ sq. cm}$ b) Area of the sector = $\frac{90}{360} \times \pi \times 4^2 = 4\pi \text{ sq. cm}$	1 1	

	<p>c) Area of the shaded region = Area of the rectangle – Area of the sector</p> $= 24 - 4\pi \text{ sq. cm}$	1 1	4
16	<p>a) Base perimeter = <math>5 + 12 + 13 = 30 \text{ cm}</math></p> <p>b) Lateral surface area = <math>30 \times 20 = 600 \text{ sq. cm}</math>  [<math>\because</math> Lateral surface area = Base perimeter <math>\times</math> Height ]</p> <p>c) Area of the triangle = <math>\frac{1}{2} \times 5 \times 12 = 30 \text{ sq. cm}</math></p> <p style="text-align: center;"><b>OR</b></p> <p>[ <math>s = \frac{5 + 12 + 13}{2} = 15</math></p> <p style="text-align: center;"><b>Area of the triangle = <math>\sqrt{s(s-a)(s-b)(s-c)} = \sqrt{15 \times 10 \times 3 \times 2}</math></b></p> <p style="text-align: center;"><b>= <math>30 \text{ sq. cm}</math> ]</b></p> <p>Total surface area = <math>2 \times 30 + 30 \times 20 = 660 \text{ sq. cm}</math>  [<math>\because</math> Total surface area = <math>2 \times</math> Base area + Lateral surface area ]</p>	1 1 1 1	4
17	<p>a) If we take length of the rectangle as <math>x</math> and the breadth as <math>y</math>, then</p> $(x-1)(y-1) = 99 \implies xy - x - y + 1 = 99 \implies xy - x - y = 98 \quad (1)$ $(x+1)(y+1) = 143 \implies xy + x + y + 1 = 143 \implies xy + x + y = 142 \quad (2)$ $(1) + (2) \implies xy = \frac{98 + 142}{2} = 120 = \text{Area of the rectangle}$ <p>b) (2) <math>\implies 120 + x + y = 142 \implies x + y = 22 \quad (3)</math></p> $x - y = \sqrt{22^2 - 4 \times 120} = \sqrt{484 - 480} = \sqrt{4} = 2 \quad (4)$ <p>From the equations (3) and (4), we get</p> $x = \frac{22 + 2}{2} = 12, \quad y = \frac{22 - 2}{2} = 10$	1 1 1 1	4
18	<p>a) Central angle of a sector = <math>\frac{4 \times 180}{6} = 120^\circ</math>  [<math>\because</math> Sum of the angles of a regular hexagon = <math>4 \times 180 = 720^\circ</math> ]</p> <p>b) Perimeter of the regular hexagon = <math>6 \times 6 = 36 \text{ cm}</math></p> <p>c) Arc length of a sector = <math>\frac{120}{360} \times 2\pi \times 6 = 2\pi \text{ cm}</math></p> <p>Perimeter of the shaded region</p> $= \text{Perimeter of the regular hexagon} + 6 \times \text{Arc length of a sector}$ $= 36 + 12\pi \text{ cm}$	1 1 1 1	4

19 a)

Length (cm)	Breadth (cm)
10	$\frac{100}{10} = 10$
4	$\frac{100}{4} = 25$

b)  $xy = 100$       OR       $x = \frac{100}{y}$

c)  $x = \frac{100}{y}$       OR       $y = \frac{100}{x}$       OR       $x$  and  $y$  are in inverse proportion.

1  
1  
1  
1

4

20

$x$	-4	-3	-2	-1	0	1	2	3	4
$p(x)$	-6	-5	-4	-3	-2	-1	0	1	2

2

2

4

21

Age	Number of members	Total age
40	8	$40 \times 8 = 320$
45	6	$45 \times 6 = 270$
47	10	$47 \times 10 = 470$
50	7	$50 \times 7 = 350$
55	4	$55 \times 4 = 220$
58	5	$58 \times 5 = 290$
<b>Total</b>	<b>40</b>	<b>1920</b>

a) 40

b) Mean age =  $\frac{1920}{40} = 48$

1

1

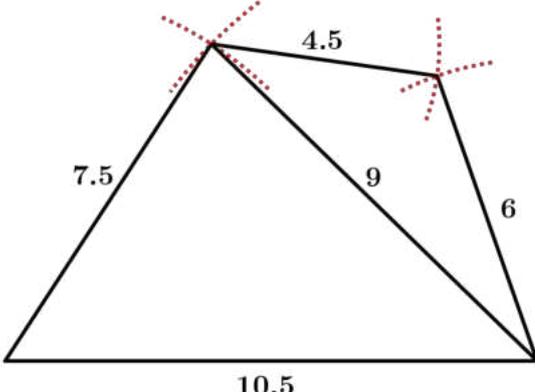
1

1

4

**Each questions from 22 to 29 carries 5 scores. ( Answer any 6 )**

22	<p>a) <math>\angle BAC = 60^\circ</math></p> <p>b) Area of the unshaded sector <math>= \frac{60}{360} \times \pi \times 6^2 = 6\pi \text{ sq. cm}</math></p> <p>c) Area of the equilateral triangle <math>= \frac{\sqrt{3}}{4} \times \pi \times 10^2 = 25\sqrt{3}\pi \text{ sq. cm}</math></p> <p>Area of the shaded region of the triangle</p> $= \text{Area of the equilateral triangle} - \text{Area of the unshaded sector}$ $= 25\sqrt{3} - 6\pi \text{ sq. cm}$ <p>Area of the shaded sector = Area of the circle - Area of the unshaded sector</p> $= \pi \times 6^2 - 6\pi = 30\pi \text{ sq. cm}$ <p style="text-align: center;"><b>OR</b></p> <p>[ Area of the shaded sector <math>= \frac{300}{360} \times \pi \times 6^2 = 30\pi \text{ sq. cm}</math> ]</p> <p>Area of the shaded region</p> $= \text{Area of the shaded sector} + \text{Area of the shaded region of the triangle}$ $= 30\pi + 25\sqrt{3} - 6\pi = 24\pi + 25\sqrt{3} \text{ sq. cm}$	1 1 1 1 1	5
23	<p>a) Radius of the cylinder <math>= \frac{12}{2} = 6 \text{ cm}</math></p> <p>b) Volume of the cylinder <math>= \pi \times 6^2 \times 25 = 900\pi \text{ cubic cm}</math></p> <p>c) Volume of the remaining wax = Volume of the square prism - Volume of the cylinder</p> $= 12^2 \times 25 - 900\pi = 3600 - 900\pi \text{ cubic cm}$ <p>Volume of the cube <math>= 1^3 = 1 \text{ cubic cm}</math></p> <p>Number of the cubes <math>= \frac{\text{Volume of the remaining wax}}{\text{Volume of a cube}} = \frac{3600 - 900\pi}{1}</math></p> $= 3600 - 900 \times 3.14 = 3600 - 2826 = 774$	1 1 1 1 1	5
24	<p>a) <math>p(0) = 4</math> , <math>p(2) = 0</math></p> <p>b) Take <math>p(x) = ax^2 + bx + c</math> , then</p> $p(0) = 4 \implies c = 4$ $p(1) = 0 \implies a \times 1^2 + b \times 1 + c = 0 \implies a + b = -4$ $p(2) = 0 \implies a \times 2^2 + b \times 2 + c = 0 \implies 4a + 2b = -4$ $b = -6 , a = 2$ $p(x) = 2x^2 - 6x + 4$	2 1 1 1	5
25	<p>a) Lateral surface area of a pillar <math>= 4 \times \frac{40}{100} \times 4 = \frac{64}{10} \text{ sq. m}</math></p> <p>b) Total cost <math>= 15 \times \frac{64}{10} \times 90 = 8640 \text{ Rs}</math></p>	2 3	5

26	<p>For calculating the sides as <math>1\frac{1}{2}</math> times of the sides and diagonal of the given quadrilateral</p> <p>For drawing a triangle with sides 10.5 , 7.5 , 9 cm .</p> <p>For drawing another triangle with sides 9 , 4.5 , 6 cm and completing the quadrilateral.</p> 	1 2 2	5																												
27	<p>a) <math>\angle BCQ = 45^\circ</math></p> <p>b) <math>AC = \frac{2}{3} \times 12 = 8 \text{ cm}</math></p> <p>c) <math>CB = 12 - 8 = 4 \text{ cm}</math></p> <p>d) Area of the shaded region = Area of the large sector + Area of the small sector</p> $= \frac{90}{360} \times \pi \times 8^2 + \frac{45}{360} \times \pi \times 4^2$ $= 16\pi + 2\pi = 18\pi \text{ sq. cm}$	1 1 1 1 1	5																												
28	<table border="1" data-bbox="226 1310 1289 1865"> <thead> <tr> <th>Electricity consumption ( Unit )</th> <th>Number of households</th> <th>Class mark</th> <th>Total consumption</th> </tr> </thead> <tbody> <tr> <td>100 – 150</td> <td>4</td> <td><math>\frac{100 + 150}{2} = 125</math></td> <td><math>125 \times 4 = 500</math></td> </tr> <tr> <td>150 – 200</td> <td>2</td> <td><math>\frac{150 + 200}{2} = 175</math></td> <td><math>175 \times 2 = 350</math></td> </tr> <tr> <td>200 – 250</td> <td>5</td> <td><math>\frac{200 + 250}{2} = 225</math></td> <td><math>225 \times 5 = 1125</math></td> </tr> <tr> <td>250 – 300</td> <td>6</td> <td><math>\frac{250 + 300}{2} = 275</math></td> <td><math>275 \times 6 = 1650</math></td> </tr> <tr> <td>300 – 350</td> <td>3</td> <td><math>\frac{300 + 350}{2} = 325</math></td> <td><math>325 \times 3 = 975</math></td> </tr> <tr> <td><b>Total</b></td> <td><b>20</b></td> <td></td> <td><b>4600</b></td> </tr> </tbody> </table> <p>Mean consumption = <math>\frac{4600}{20} = 230 \text{ unit}</math></p>	Electricity consumption ( Unit )	Number of households	Class mark	Total consumption	100 – 150	4	$\frac{100 + 150}{2} = 125$	$125 \times 4 = 500$	150 – 200	2	$\frac{150 + 200}{2} = 175$	$175 \times 2 = 350$	200 – 250	5	$\frac{200 + 250}{2} = 225$	$225 \times 5 = 1125$	250 – 300	6	$\frac{250 + 300}{2} = 275$	$275 \times 6 = 1650$	300 – 350	3	$\frac{300 + 350}{2} = 325$	$325 \times 3 = 975$	<b>Total</b>	<b>20</b>		<b>4600</b>	4 1	5
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29	<p>a) <math>\left(\frac{1}{4} + \frac{1}{5}\right) \div \left(\frac{1}{4} - \frac{1}{5}\right) = 9</math></p> <p>b) 31 <span style="float: right;"><math>\left[\left(\frac{1}{15} + \frac{1}{16}\right) \div \left(\frac{1}{15} - \frac{1}{16}\right) = 31\right]</math></span></p> <p>c) <math>\left(\frac{1}{25} + \frac{1}{26}\right) \div \left(\frac{1}{25} - \frac{1}{26}\right) = 51</math></p> <p>d) <math>P = \frac{1}{30}</math> <span style="float: right;"><math>\left[\left(\frac{1}{29} + \frac{1}{30}\right) \div \left(\frac{1}{29} - \frac{1}{30}\right) = 59\right]</math></span></p> <p>e) <math>n + (n + 1) = 2n + 1</math> <span style="float: right;"><math>\left[\left(\frac{1}{n} + \frac{1}{n+1}\right) \div \left(\frac{1}{n} - \frac{1}{n+1}\right) = 2n+1\right]</math></span></p>	1  1 1 1	5
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