

2006 JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY

III B.TECH I SEMESTER SUPPLEMENTARY EXAMINATIONS
OPTIMIZATION TECHNIQUES
 (ELECTRICAL & ELECTRONIC ENGINEERING)

NOVEMBER 2006

TIME - 3 HOUR
 MARK - 80

Answer any FIVE Questions
All Questions carry equal marks

1. (a) Determine the maximum and minimum values of the function: [8] $12x^5 - 45x^4 + 40x^3 + 5$
- (b) A d.c. generator has internal resistance of R ohms and develops an open circuit voltage of ' V ' volts. Find the value of load resistance ' r ' for which the power developed by the generator will be maximum. [10]
2. (a) State and explain the necessary and sufficient conditions for existence of relative optima in case of multivariable optimization with constraints. [10]
- (b) Find the dimensions of a rectangular parallelepiped with largest volume whose sides are parallel to the coordinate planes, to be inscribed in the ellipsoid. 8]
3. (a) State and explain the standard form of LPP. [6]
- (b) Explain the significance of slack, surplus and artificial variables of LPP. [10]
4. Show that the following LPP has unbounded solution [16]
- maximize $Z = 3x_1 + 2x_2$ subject to $x_1 - x_2 \geq 1$ $3x_1 - 2x_2 \leq 6$ $x_1, x_2 \geq 0$
5. (a) If all the sources are emptied and all the destinations are filled, show that $a_i = P$ b_j is a necessary and sufficient condition for the existence of a feasible solution to a transportation problem
- (b) Prove that there are only $m+n-1$ independent equations in a transportation problem, m and n being the no. of origins and destinations and that any one equation can be dropped as the redundant equation. [8+8]
6. Draw the flowchart of Powell's method. Explain about each block. [16]
7. Consider the problem:
 Minimize $f(x_1, x_2) = (x_1 - 1)^2 + (x_2 - 2)^2$ Subject to $2x_1 - x_2 = 0$
 and $x_1 \leq 10$ Construct -K function according to the interior penalty function approach and complete the minimization of -K. [16]
8. Determine the value of u_1, u_2, u_3 so as to maximize $(u_1 \cdot u_2 \cdot u_3)$, Subject to, $u_1 + u_2 + u_3 = 10$ and $u_1, u_2, u_3 \geq 0$ [16]